Biostatistics Refresher

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Topics

- Core Ideas: Prevalence & Incidence
- Types of Studies
- Measures of Risk
- Statistical Inference
- Measures for Screening and Diagnostic Tests

Notes

- Biostatistics & Epidemiology are big topics
- The measures and approaches discussed here are the core ideas
- Many studies use more sophisticated techniques and/or adjustments
- Trying to reproduce results from a paper?
 - Sophisticated techniques or adjustments might prevent this
 - Rounding might make numbers 'a little' off
- Proportions vs. Percentages
 - Proportions are more suitable for calculations; between 0 and 1
 - Percentages are often reported; between 0% and 100%

Incidence and Prevalence

• Prevalence: the proportion of a population with the disease (overall)

$$Prevalence = \frac{Number of subjects with the disease}{Total number of subjects in the population}$$

- **Incidence**: measures new cases of a disease in a population in a specific time period
 - Reported as incidence rate or incidence proportion (also called incidence risk or cumulative incidence)

Incidence Proportion =
$$\frac{\text{number of new cases of disease over time}}{\text{population without disease at baseline}}$$

Incidence Rate =
$$\frac{\text{number of new cases of disease over time}}{\text{person-time at risk}}$$

Example 2.3 Investigators seek to determine the incidence of influenza among nurses at three local hospitals. They identify 500 nurses who do not have influenza as of December 1, 2010, and follow them for the development of influenza over the next 3 months. They find that ten of the study nurses develop influenza during follow-up. What is the incidence proportion of influenza?

Detour: Instead of all 500 nurses, consider these 6.

What is the incidence rate for these 6 individuals?

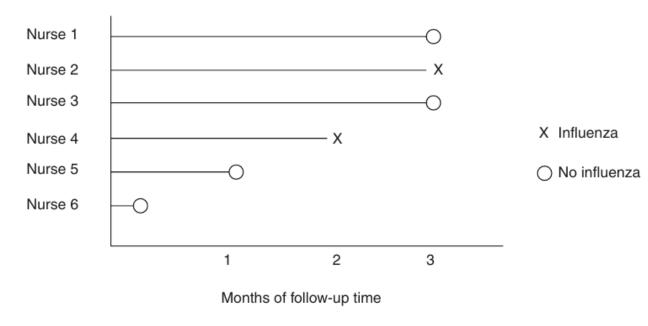


Fig. 2.1 Diagram of individual risk times and disease status

Table 2.1 List of individual risk times and disease status

	Develops influenza	Person-time	Reason for discontinuation
Nurse 1	No	3 months	Study ended
Nurse 2	Yes	3 months	Developed influenza
Nurse 3	No	3 months	Study ended
Nurse 4	Yes	2 months	Developed influenza
Nurse 5	No	1.25 months	Dropped out
Nurse 6	No	0.25 months	Dropped out
Total	2 cases	12.5 months	

Example 2.3 Investigators seek to determine the incidence of influenza among nurses at three local hospitals. They identify 500 nurses who do not have influenza as of December 1, 2010, and follow them for the development of influenza over the next 3 months. They find that ten of the study nurses develop influenza during follow-up.

What is the incidence rate of influenza?

Need to know person-time at risk. Suppose it is 1200 months.

- Incidence proportions: more interpretable
- Incidence rates: used for comparisons of disease among different groups

• Incidence rate is often multiplied by a factor (e.g. 10 or 1000) to make it more easily interpretable.

Morbidity and Mortality

- Morbidity refers to *illness* not death
- Mortality refers to death

Prevalence measures morbidity in a population Mortality rate measures deaths in the population

Types of Studies: Overview

- Case Reports
- Cross-Sectional Studies
- Cohort Studies
- Case-Control Studies
- Randomized Trials

Types of Studies: Case Reports

- Observational study
- Describes experiences of individuals with a disease or condition

- Good for: new diseases, generating hypotheses, raising awareness
- Limitations:
 - Cannot calculate incidence
 - No comparison group
 - Often describe individuals that are not typical
 - Often small sample sizes lots of variability

Types of Studies: Cross-Sectional

 Measure the outcome of interest and exposures/factors at the same time from a group of interest.

Good for: establishing associations between exposures/factors and disease prevalence

Limitations: cannot establish a temporal link (though if only one direction of a link is plausible you may still be able to justify a temporal link)

Types of Studies: Cohort

Observational study that follows a group over time:

- 1. Exclude individuals with the disease
- 2. Define cohorts by measuring exposures
- 3. Follow over time to determine incidence

Good for:

- Temporal relationships
- Studying multiple outcomes

• Limitations:

- Confounding & bias
- Not always efficient (rare or long latency)

Analysis:

- Relative risk
- Attributable risk, population attributable risk

Types of Studies: Case-Control

Observational study that compares groups of individuals

- 1. Identify individuals **with** the condition of interest
- 2. Separately, identify another group of individuals **without** the condition of interest.
- 3. Work backward to determine what factors may be influencing having the condition of interest.

Good for:

- Studying rare diseases
- Efficiency (using few participants)
- Multiple risk factors

• Limitations:

- Confounding & bias
- Retrospective
- Cannot calculate incidence

Analysis:

- Cannot use Relative Risk
- Odds Ratio

Types of Studies: Randomized Trials

- Experimental, prospective study to compare treatments with controls
- Participants are *assigned* to an experimental condition (contrast with observational studies)

Good for:

• Establishing cause and effect (e.g. does a treatment perform better than control?)

• Limitations:

 External validity issues (realism, monitored clinical environment, many exclusion criteria)

Risk

- Risk
- Absolute Risk Reduction (ARR)
- Number Needed to Treat (NNT)
- Number Needed to Harm (NNH)
- Relative Risk (RR)
- Relative Risk Reduction (RRR)
- Odds Ratio (OR)

		Event	
		Occurred	
		Yes	No
Group	Treatment	а	b
	Control	С	d

These labels are arbitrary. Often exposed/unexposed is used. There is no firm rule about which variable is *rows* and which is *columns*. A description of the data and study design is key.

Risk

- Risk means the *proportion* of people for which an event occurs during the study.
 - This is sometimes called the *incidence* proportion (different from the *incidence rate*).
- The proportion in each group for which the Event did occur (Yes):

$$p_{\text{Treatment}} = \frac{a}{a+b}$$

$$p_{\text{Control}} = \frac{c}{c+d}$$

		Event	
		Occurred	
		Yes	No
Group	Treatment	а	b
	Control	С	d

Risk and Study Design

- Note that the study design is deeply connected to the types of analyses that can be done with a 2x2 table.
- Example: In a **Cohort Study**, the **Exposed** group and **Unexposed** group belong to a single cohort. The cohort is followed to determine **Status**.

		Status	
		Disease Not	
Group	Exposed	а	b
	Unexposed	С	d

- Note these sums have meanings:
 - a + b is the number of people in the Exposed group with the Disease
 - a + c is the number of people in the <u>Cohort</u> with the <u>Disease</u>

These values can be used to estimate the prevalence of the *Disease*,

$$\frac{a+c}{a+c+b+d}$$

Risk and Study Design

- Note that the study design is deeply connected to the types of analyses that can be done with a 2x2 table.
- Example: In a **Case Control Study**, participants are recruited because they have the *Disease* and or because they do *Not* it.

	Status	
	Disease Not	
Exposed	а	b
Unexposed	С	d

- Note these sums have meanings:
 - a + c is the number of people in the study with the *Disease* (i.e. selected in the *Disease* group)
 - a + b is <u>NOT</u> the number of people in the Exposed group... there wasn't an exposure group!

Because the participants were selected based on outcome (*Disease* then *Not*), we **cannot** get an estimate of the prevalence.

Risk Difference

- Also known as:
 - Attributable Risk
 - Absolute Risk Increase (ARI)
 - Absolute Risk Reduction (ARR) (context)

		Event	
		Occurred	
		Yes	No
Group	Treatment	а	b
	Control	С	d

Compare the risks using subtraction

Attributable $Risk = Risk_{Control} - Risk_{Treatment}$

Risk Difference = $p_{Control} - p_{Treatment}$

 Be careful with order and context – usually structured so that the value is positive

Number Needed to Treat (NNT)

- Also known as Number Needed to Harm (NNH), depending on context
- Estimates the number of people who need to receive the treatment/intervention to prevent or cause one instance of the outcome
- Note the value should be positive and is usually rounded

$$NNT = \frac{1}{\text{Attributable Risk}} = \frac{1}{\text{Risk}_{\text{Control}} - \text{Risk}_{\text{Treatment}}}$$

$$NNT = \frac{1}{p_{\text{Control}} - p_{\text{Treatment}}}$$

The **relative risk (RR)** is an *incidence ratio*.

$$RR = \frac{\text{Risk for Treatment Group}}{\text{Risk for Control Group}}$$

$$RR = \frac{"Yes" proportion for Treatment Group}{"Yes" proportion for Control Group}$$

$$RR = \frac{a/(a+b)}{c/(c+d)}$$

		Event	
		Occurred	
		Yes	No
Group	Treatment	а	b
	Control	С	d

Possible values for RR and their meaning:

RR > 1: The Treatment group has a *higher* risk than the Control group

RR = 1: The Treatment group has the same risk as the Control group

RR < 1: The Treatment group has a *lower* risk than the Control group

Cannot be calculated from case-control studies

A study of patients presenting GeoSentinel clinics following rabies exposure for rabies post-exposure provalaxis (RPEP) examined the relationship between receiving rabies immunoglobin (RIG) and where RPEP was started (in country of exposure or not). (Gautret et al., 2018)

		RIG given in country of exposure	
		Yes No	
Country of	Thailand	43	44
Exposure	Other	78	139

		RIG given in country of exposure	
		Yes	No
Country of	Indonesia	5	82
Exposure	Other	42	175

		RIG given in country of exposure	
		Yes	No
Country of Exposure	Thailand	43	44
	Other	78	139

The relative risk for receiving RIG in the country of exposure for Thailand is 1.38. Reasonable interpretations of 1.38 include:

- Exposure to rabies in Thailand is associated with 1.38 times greater chance of receiving RIG compared with exposure in other countries.
- Exposure to rabies in Thailand is associated with a 38% greater chance of receiving RIG compared with exposure in other countries.

		RIG given in country of exposure	
		Yes	No
Country of	Indonesia	5	82
Exposure	Other	42	175

The relative risk for receiving RIG in the country of exposure for Indonesia is 0.30. Reasonable interpretations of 0.30 include:

- Exposure to rabies in Indonesia is associated with a 70% lower chance of receiving RIG compared with exposure in other countries.
- Exposure to rabies in a country *other than* Indonesia is associated with a 3.33 times greater chance of receiving RIG compared with exposure in Indonesia.

Relative Risk Reduction (RRR)

- This measure is a blend of two:
 - Relative Risk
 - Risk Difference (Attributable Risk)
- The risk difference is compared to the risk for the control group using division:

$$RRR = \frac{\text{Attributable Risk}}{\text{Risk for Control Group}}$$

$$RRR = \frac{\text{Risk}_{\text{Control}} - \text{Risk}_{\text{Treated}}}{\text{Risk}_{\text{Control}}} = \frac{p_{\text{Control}} - p_{\text{Treatment}}}{p_{\text{Control}}}$$

Odds Ratio

The **odds ratio (OR)** compares *odds* for two groups.

Odds is a technical term for $\frac{p_{success}}{p_{failure}}$ and NOT a synonym for "probability."

The odds ratio is more difficult to interpret then the relative risk.

$$OR = \frac{a/b}{c/d} = \frac{ad}{bc}$$

Can be calculated from case-control studies... often a good estimate for relative risk.

$$OR = RR \times \left(\frac{1 - p_{\text{Treatment}}}{1 - p_{\text{Control}}}\right)$$

		Event	
		Occurred	
		Yes	No
Group	Treatment	а	b
	Control	С	d

Possible values for RR and their meaning:

OR > 1: The Treatment group has a *higher* odds than the Control group

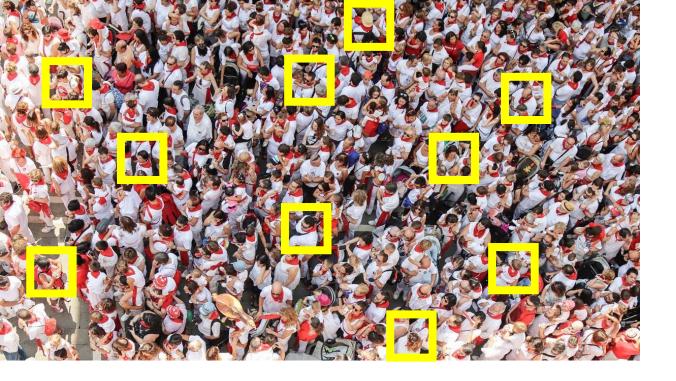
OR = 1: The Treatment group has the same odds as the Control group

OR < 1: The Treatment group has a *lower* odds than the Control group

Can be calculated from case-control studies

Relative Risk and Odds Ratio

- OR is more difficult to interpret... but we often want to (and can) interpret it *like* a RR
- Note that for both measures the reciprocal is also a valid value.
- That is, $\frac{1}{RR}$ is a relative risk, and $\frac{1}{OR}$ is an odds ratio.
- The relationship (less than, greater than) 1 will change.
- This might make the value easier or harder to interpret.
- Neither RR nor OR are symmetric about 1 (e.g. 1.5 vs. 0.67)
- Exposed group usually in the numerator (convention).



Statistical Inference



Statistical Inference

Use data from a small group (sample) ...

... to draw conclusions about a larger group (population).



Statistical Inference

Two major approaches:

- Hypothesis testing (p-values)
 - "Which of two descriptions of the population is better-supported by the data?"
- Confidence Intervals (CIs)
 - "Based on the data, what are plausible values for an unknown population value?"

• Underlying logic of statistical inference is *sophisticated and subtle* – be careful when reporting/documenting statistics (see NHST)

- Null hypothesis (H_0) : usually "no effect" (or equivalent)
- Alternative hypothesis (H_A) : usually "there is some effect"

• Critical idea:

- We assume that the null hypothesis is true and collect evidence against it.
- If we collect enough evidence against the null hypothesis to think it is wrong...
- Then we think the alternative hypothesis is a better description of reality.
- We do <u>NOT</u> accept or prove the null hypothesis true.
- At best we "fail to reject" the null hypothesis.

A p-value quantifies the strength of the evidence against the null hypothesis.

A p-value answers this question:

- If the null hypothesis is true,
- what is the probability
- we would observe a test statistic as extreme
- (or more extreme)
- than the test statistic we actually did observe?

A p-value quantifies the strength of the evidence against the null hypothesis.

A p-value answers this question:

• If the null hypothesis is true, what is the probability we would observe a test statistic as extreme (or more extreme) than the test statistic we actually did observe?

A small p-value is strong evidence against the null hypothesis.

A BIG p-value is weak evidence against the null hypothesis.

• Caution: This feels counterintuitive to many people at first.

• Cut-offs/guidelines for p-values depend on the context, but one set you might consider is

p-value	Strength of Evidence	
p-value > 0.10	Almost no evidence for H_A	
$0.05 < p-value \le 0.10$	Weak evidence for H_A	
$0.01 < p-value \le 0.05$	Good evidence for H_A	
p−value ≤ 0.01	Very good evidence for H_A	

• Note that these cutoffs reflect a continuum of evidence against the null hypothesis, H_0 .

 A study compared healthcare costs for patients prescribed a High Dose of gabapentin to those prescribed a Low Dose. (Fleet et al., 2018)

Table 5. Average per person adjusted cost in 30-day follow-up period.

All Patients	Gabapentin	Emergency Visit
High Dose	\$64.75	\$103.70
Low Dose	\$33.53	\$90.30
Average Cost Differential	\$31.22	\$13.41
P-value	< 0.0001	< 0.0001

• If there was really no difference in average cost for Emergency Visits, the probability we would see an average difference of \$13.41 (or greater) is less than 0.0001.

Hypothesis Testing

• Consider this excerpt of Table 3 from the rabies study earlier (Gautret et al., 2018)

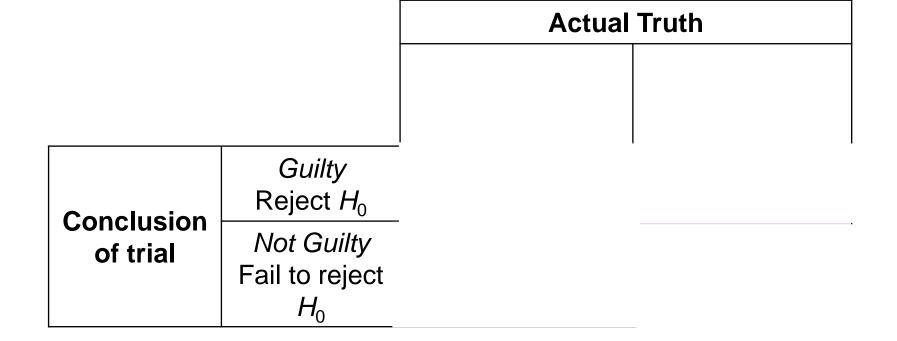
Characteristic		RIG given in country of exposure (N = 87)	RIG not given in country of exposure (N = 217)	Relative risk of receiving RIG in the country of exposure (95% CI)	P value
Countries of exposure n (%)	Thailand	43 (49.4)	78 (39.5)	1.38 (1.0-1.8)	0.02
	Indonesia	5 (5.8)	42 (19.4)	0.30 (0.1-0.7)	0.01
	India	3 (3.4)	13 (6.0)	0.58 (0.2–2.0)	0.38
	China	1 (1.2)	12 (5.5)	0.21 (0.0–1.6)	0.13
	Algeria	6 (6.9)	7 (3.2)	2.14 (0.7-6.2)	0.16
	Philippines	8 (9.2)	1 (0.5)	19.95 (2.5–157.2)	0.01
	Sri Lanka	8 (9.2)	5 (2.3)	3.99 (1.3–11.9)	0.013

• For which countries have a RR significantly different from 1?

- If we reject H_0 when H_0 is true, we have committed a **Type I error**.
- If we fail to reject H_0 when H_0 is false, we have committed a **Type II** error.

		Truth about the population	
		H_0 true	H_0 false (H_a true)
Conclusion based on sample	Reject H ₀	Type I error	Correct conclusion
	Fail to reject H_0	Correct conclusion	Type II error

- If we reject H_0 when H_0 is true, we have committed a **Type I error**.
- If we fail to reject H_0 when H_0 is false, we have committed a **Type II** error.



- How can we reduce the chances that we *send an innocent person to jail*?
 - How can we lower the chances of a **Type I Error**?
- What are the consequences of this?

		Actual Truth	
		<i>Innocent</i> <i>H</i> ₀ true	Committed Crime H_0 false (H_a true)
Conclusion	<i>Guilty</i> Reject <i>H</i> ₀	Type I error	Correct conclusion
Conclusion of trial	Not Guilty Fail to reject H ₀	Correct conclusion	Type II error

- How can we reduce the chances that we let a guilty person go free?
 - How can we lower the chances of a **Type II Error**?
- What are the consequences of this?

		Actual Truth	
		<i>Innocent</i> <i>H</i> ₀ true	Committed Crime H_0 false $(H_a \text{ true})$
Conclusion of trial	<i>Guilty</i> Reject <i>H</i> ₀	Type I error	Correct conclusion
	Not Guilty Fail to reject H ₀	Correct conclusion	Type II error

- Replication studies and meta-analyses are important
- Importance of Type I & Type II Errors strongly depend on context
- Need to know statistical hypotheses (may not be explicitly written, but usually standard – consult references)
- **Power** is the ability to correctly reject the null hypothesis Power = $1 P(Type\ II\ Error)$

Confidence Intervals

- Provide an interval of values that are all plausible for a true, unknown population value based on the data
- A confidence level is specified (often 95%)
- Want to be more confident (e.g. 95% -> 99%)?
- Interval gets w i d e r.
- Want a narrower (more precise) interval?
- Lower confidence level (e.g. 95% -> 90%)

Confidence Intervals

- The confidence level (e.g. 95%) is a statement about the confidence in the method and <u>not</u> a statement of confidence about the specific interval calculated!
- That is, if you commit to making 95% confidence intervals over and over, about 95% of them will contain the true (unknown) value you want to identify.
- And therefore about 5% will *not* contain the true (unknown) value you want to identify. (That is, they will be wrong.)
- No way of knowing which are right and which are wrong.
- (Confidence in the *method!*)

Confidence Intervals

- Confidence Intervals can be used in a way analogous to Hypothesis Testing.
- In Hypothesis Testing, there is often a single value in the null hypothesis.
 - Difference in values? Usually null hypothesis is "0"
 - Ratio of values? Usually null hypothesis is "1"
- Examine the CI:
 - if this value is *in* the CI, then it is plausible...
 - if it is plausible, that is *not* evidence against the null hypothesis...
 - "fail to reject" the null hypothesis
- If the value is *not* in the CI, it is not plausible, go with the alternative hypothesis

Hypothesis Testing

• Consider this excerpt of Table 3 from the rabies study earlier (Gautret et al., 2018)

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• For which countries have a RR significantly different from 1?

Sensitivity and Specificity

- Screening diseases need a gold standard
- "Accuracy" of a test is not good enough
- The sensitivity of a test is its ability to correctly identify patients who have the condition being tested for
 - Correct positives
- The specificity of a test is its ability to correctly identify patients who do not have the condition being tested for
 - Correct negatives

Sensitivity and Specificity

TP = True Positive TN = True Negative FN = False Negative FP = False Positive

True Disease Status

No

Yes

Screening	Positive	TP	FP
Result	Negative	FN	TN

Sensitivity =
$$\frac{\text{True Positives}}{\text{All Yes Disease}} = \frac{\text{TP}}{\text{TP} + \text{FN}}$$

Specificity =
$$\frac{\text{True Negatives}}{\text{All No Disease}} = \frac{\text{TN}}{\text{TN} + \text{FP}}$$

False Positive Error Rate = $\frac{\text{False Positives}}{\text{All No Disease}} = \frac{\text{FP}}{\text{TN} + \text{FP}}$

The rate at which true No disease patients are incorrectly flagged Positive.

False Negative Error Rate = $\frac{\text{False Negatives}}{\text{All Yes Disease}} = \frac{\text{FN}}{\text{TP} + \text{FN}}$

The rate at which true Yes disease patients are incorrectly flagged Negative.

Sensitivity and Specificity

TP = True Positive TN = True Negative FN = False Negative FP = False Positive

True	Disease
St	tatus

No

Screening	Positive	TP	FP
Result	Negative	FN	TN

Positive Predictive Value(PPV) =
$$\frac{\text{True Positives}}{\text{All Positives}} = \frac{\text{TP}}{\text{TP} + \text{FP}}$$

The proportion of patients with *Positive* results who *Yes* had the disease

Yes

Negative Predictive Value(NPV) =
$$\frac{\text{True Negatives}}{\text{All Negatives}} = \frac{\text{TN}}{\text{TN} + \text{FN}}$$

The proportion of patients with *Negative* results who *No*, did not have the disease

Likelihood Ratio Positive (LR+) =
$$\frac{\text{Sensitivity}}{1 - \text{Specificity}}$$

The higher this value is, the better a test is. (Should be much larger than 1.)

Likelihood Ratio Negative (LR-) =
$$\frac{1 - \text{Sensitivity}}{\text{Specificity}}$$

The lower this value is, the better a test is. (Should be as close to 0 as possible.)

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Resources

- The Little Handbook of Statistical Practice
 - StatisticalPractice.com redirects to http://www.jerrydallal.com/lhsp/lhsp.htm
 - Old but good