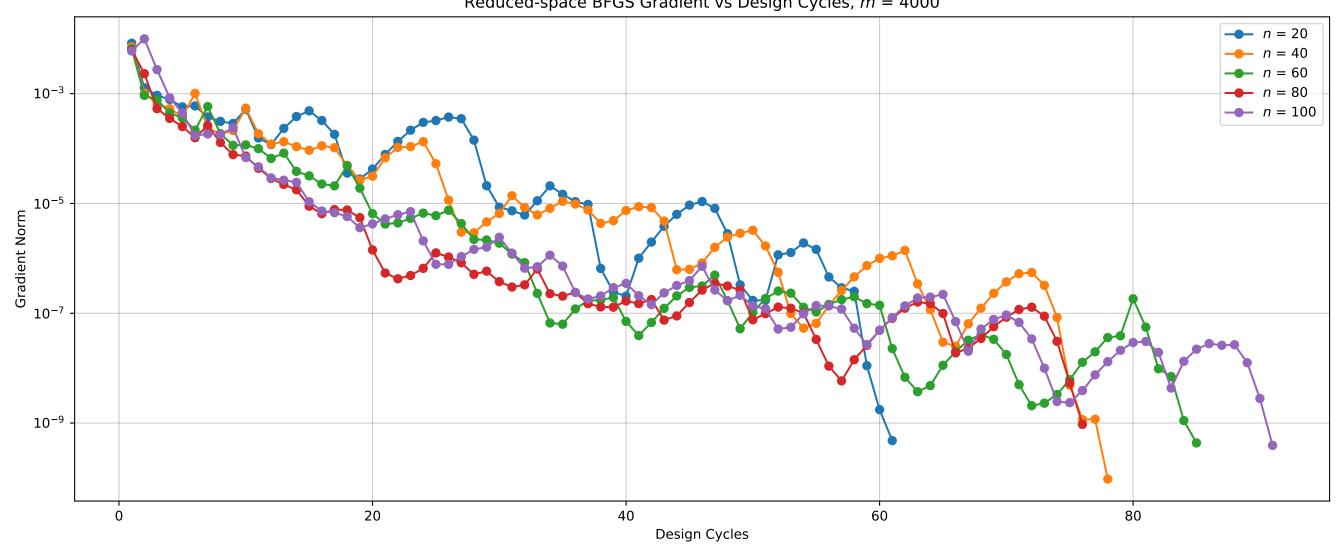
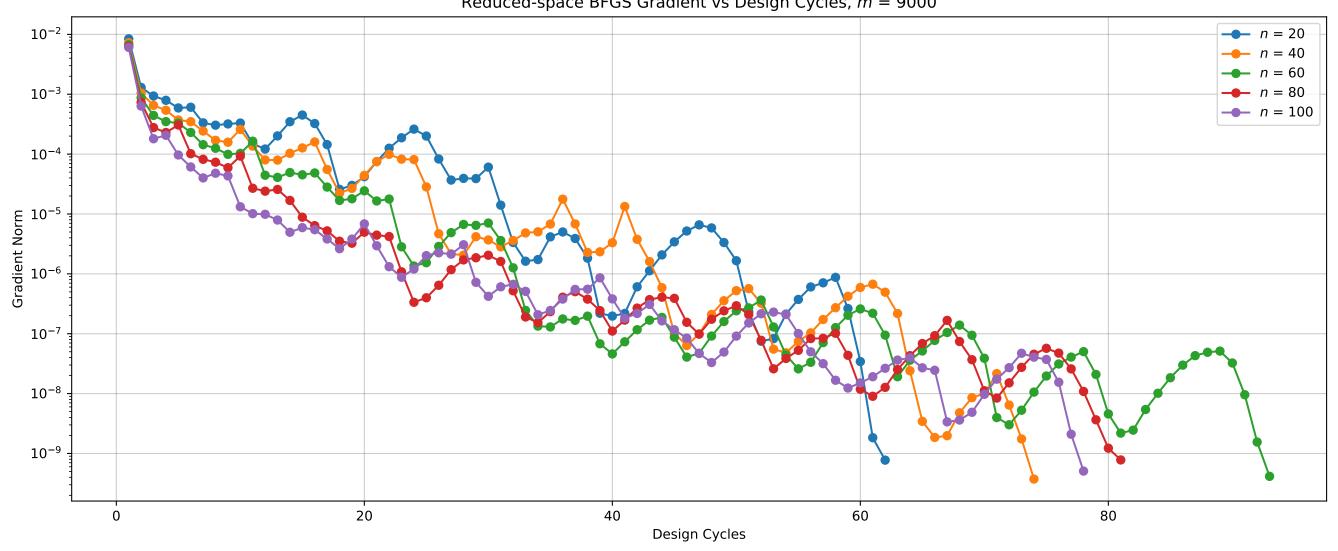
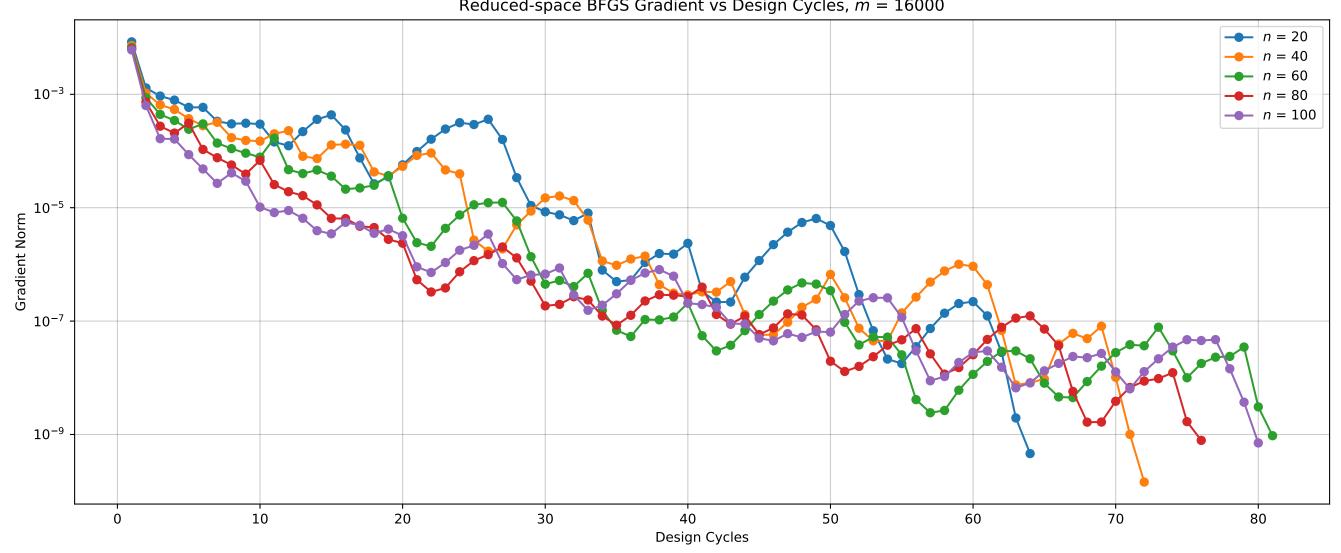
Reduced-space BFGS Gradient vs Design Cycles, m = 4000



Reduced-space BFGS Gradient vs Design Cycles, m = 9000



Reduced-space BFGS Gradient vs Design Cycles, m = 16000

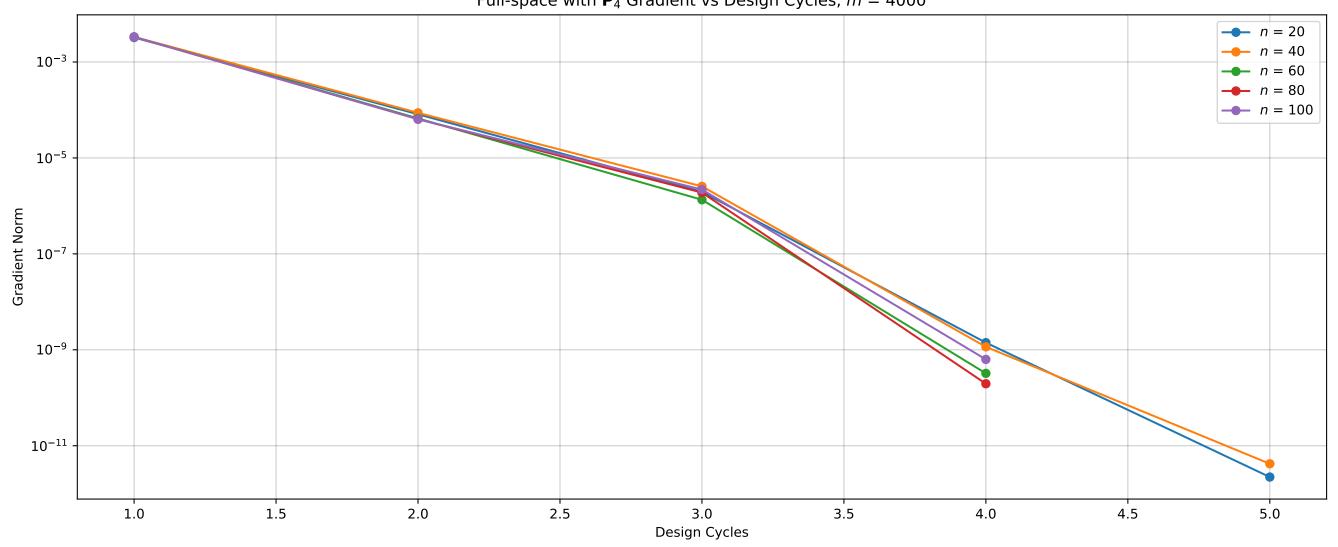


Reduced-space Newton Gradient vs Design Cycles, m = 4000--- n = 20--- n = 40--- n = 6010⁻³ --- n = 80--- n = 100--- n = 160--- n = 320 10^{-5} --- n = 640**Gradient Norm** 10^{-7} 10^{-9} 10^{-11} 0.0 0.5 1.0 1.5 2.0 2.5 3.0 3.5 4.0 Design Cycles

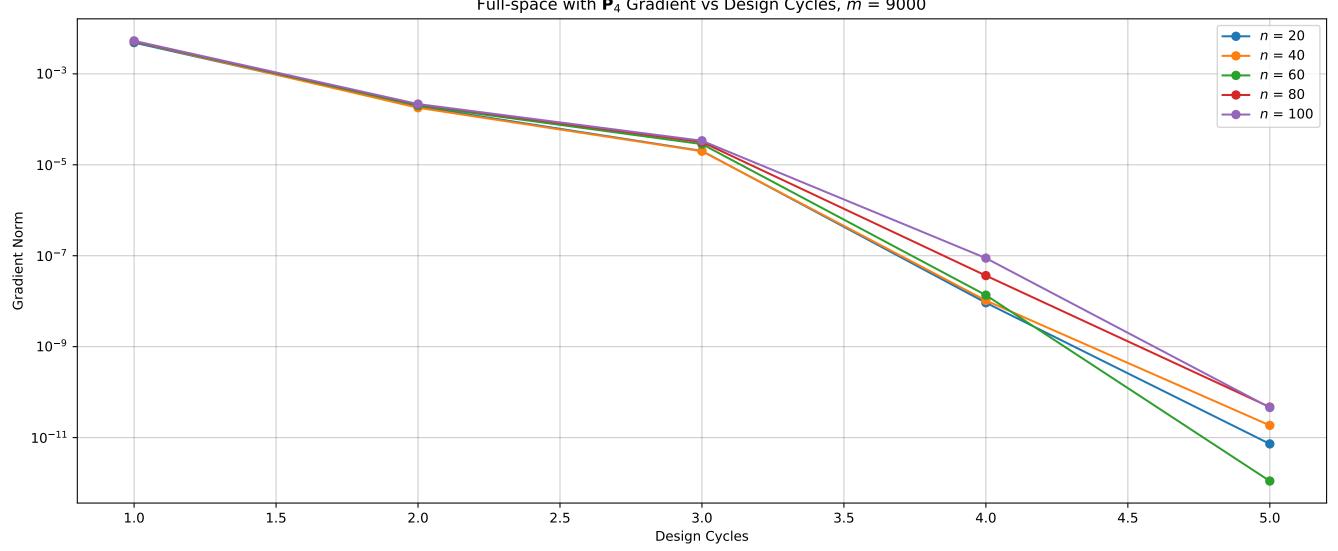
Reduced-space Newton Gradient vs Design Cycles, m = 9000--- n = 20 10^{-2} --- n = 40--- n = 60--- n = 80--- n = 100 10^{-4} --- n = 160--- n = 320--- n = 640 10^{-6} **Gradient Norm** 10^{-8} 10^{-10} 10^{-12} -0.0 0.5 1.0 1.5 2.0 2.5 3.0 3.5 4.0 Design Cycles

Reduced-space Newton Gradient vs Design Cycles, m = 16000--- n = 20--- n = 4010⁻³ --- n = 60--- n = 80--- n = 100--- n = 160 10^{-5} --- n = 320--- n = 640E 10⁻⁹ 10^{-11} 10^{-13} 0.0 0.5 1.0 1.5 2.0 2.5 3.0 3.5 4.0 Design Cycles

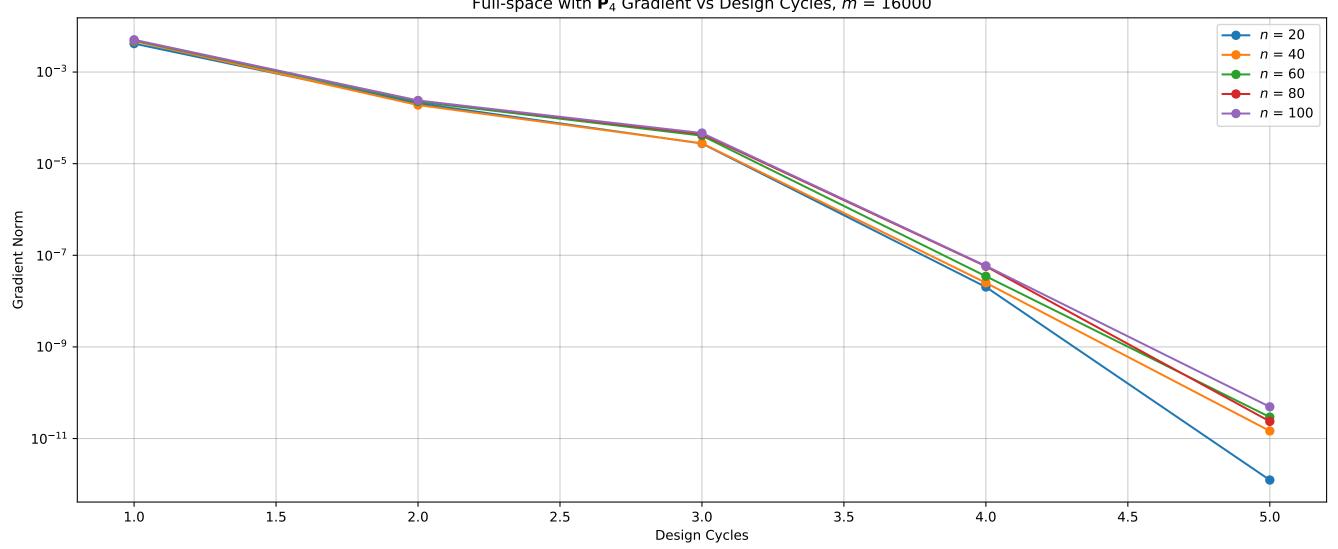
Full-space with \mathbf{P}_4 Gradient vs Design Cycles, m = 4000



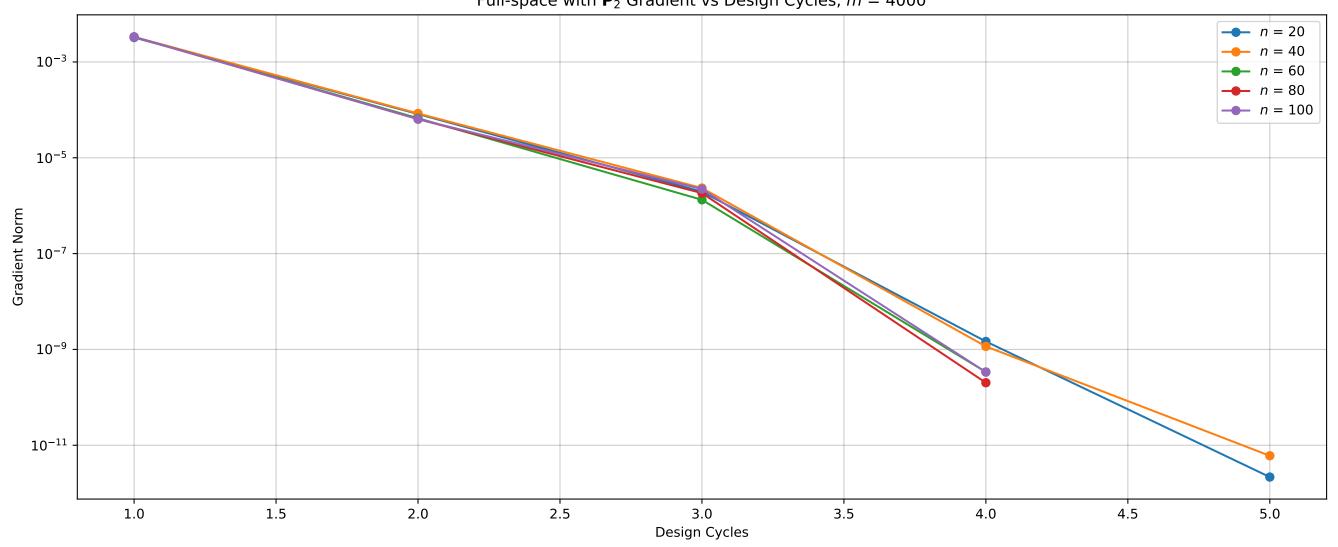
Full-space with \mathbf{P}_4 Gradient vs Design Cycles, m = 9000



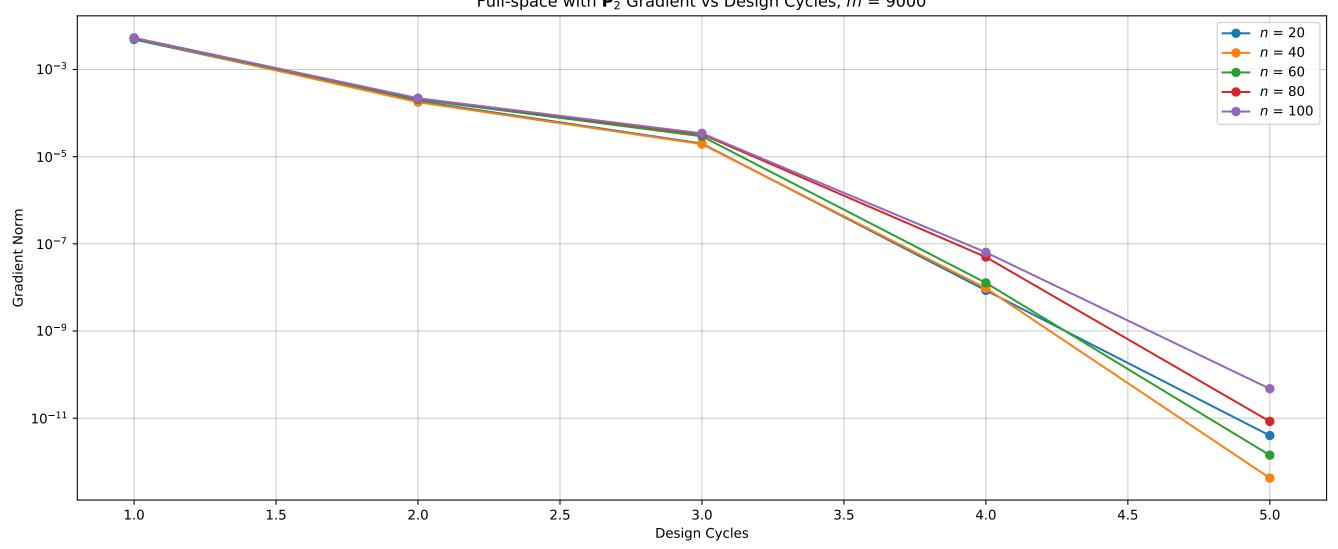
Full-space with P_4 Gradient vs Design Cycles, m = 16000



Full-space with \mathbf{P}_2 Gradient vs Design Cycles, m = 4000



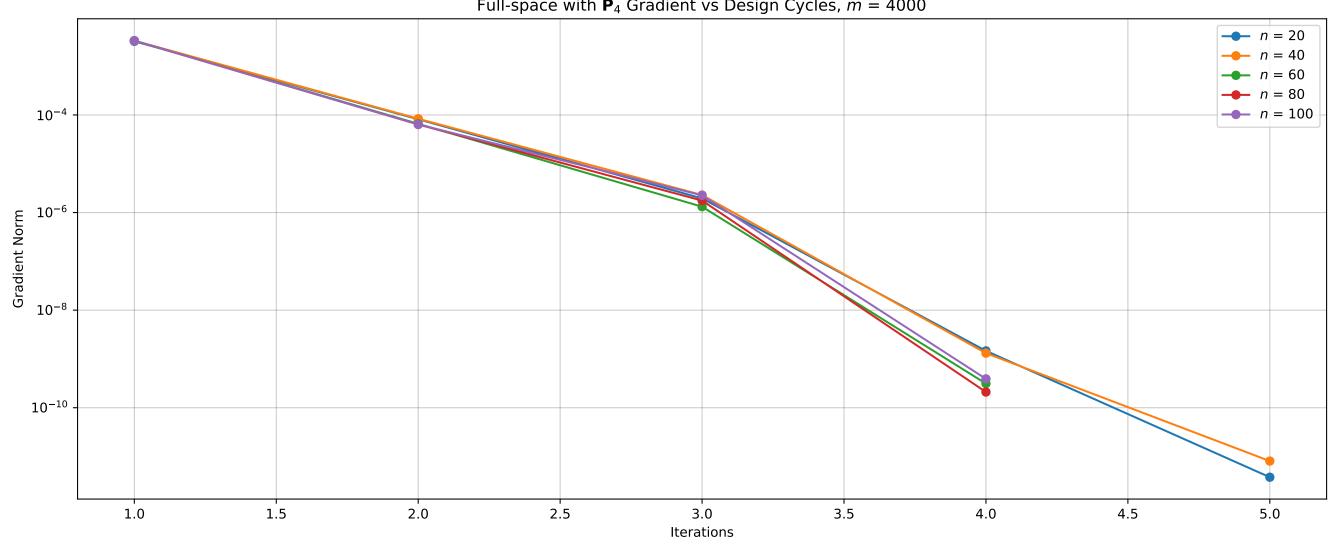
Full-space with \mathbf{P}_2 Gradient vs Design Cycles, m = 9000



Full-space with P_2 Gradient vs Design Cycles, m = 16000 10^{-2} --- n = 20-- n = 40--- n = 60--- n = 100 10^{-4} 10^{-6} **Gradient Norm** 10^{-8} 10^{-10} 1.0 1.5 2.0 2.5 3.0 3.5 5.0 4.0 4.5

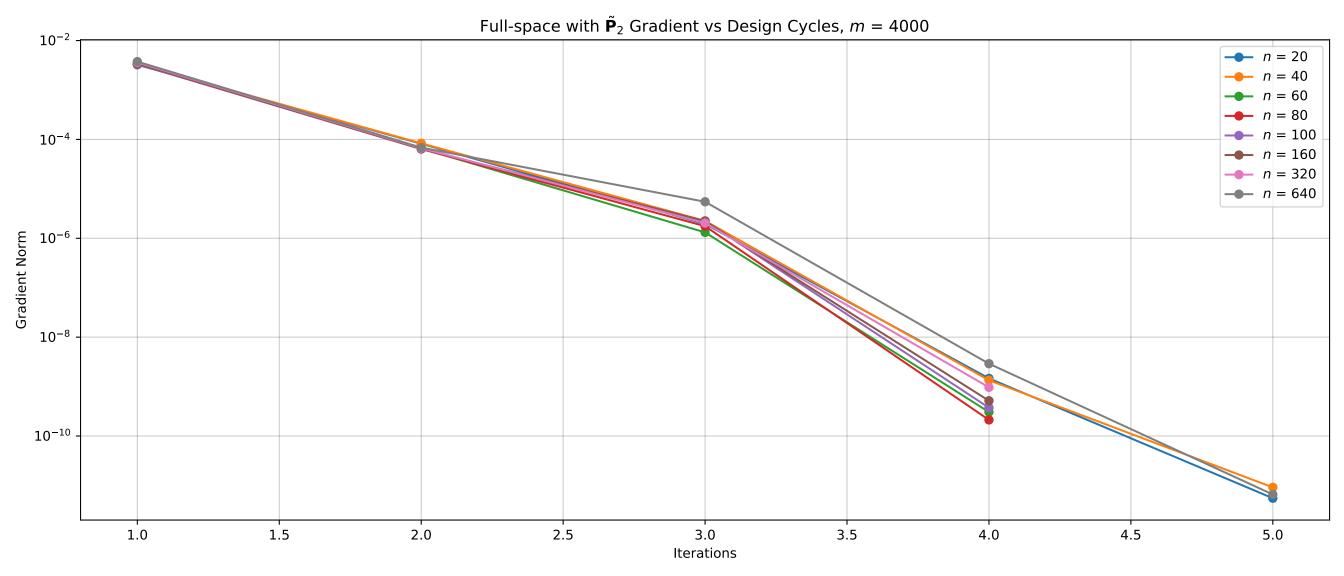
Design Cycles

Full-space with $\tilde{\mathbf{P}}_4$ Gradient vs Design Cycles, m=4000



Full-space with $\tilde{\mathbf{P}}_4$ Gradient vs Design Cycles, m=9000 10^{-2} --- n = 20--- n = 100 10^{-4} **Gradient Norm** 10^{-6} 10^{-8} 10^{-10} 2.0 1.0 1.5 2.5 3.0 3.5 4.0 4.5 5.0 Iterations

Full-space with $\tilde{\mathbf{P}}_4$ Gradient vs Design Cycles, m=16000 10^{-2} --- n = 20--- n = 100 10^{-4} **Gradient Norm** 10^{-6} 10⁻⁸ 10^{-10} 2.0 1.0 1.5 2.5 3.0 3.5 4.0 4.5 5.0 Iterations

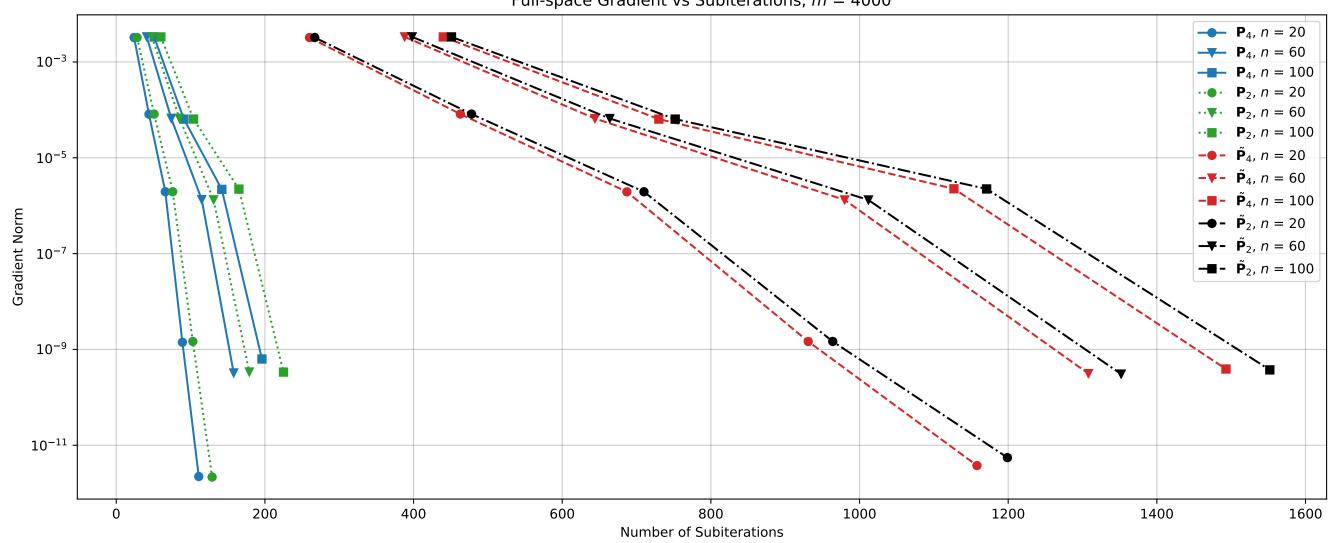


Full-space with $\tilde{\mathbf{P}}_2$ Gradient vs Design Cycles, m=9000 10^{-2} --- n = 20--- n = 80--- n = 100 10^{-4} --- n = 160--- n = 320--- n = 640**Gradient Norm** 10^{-6} 10^{-8} 10^{-10} 1.0 1.5 2.0 2.5 3.0 3.5 5.0 4.0 4.5 Iterations

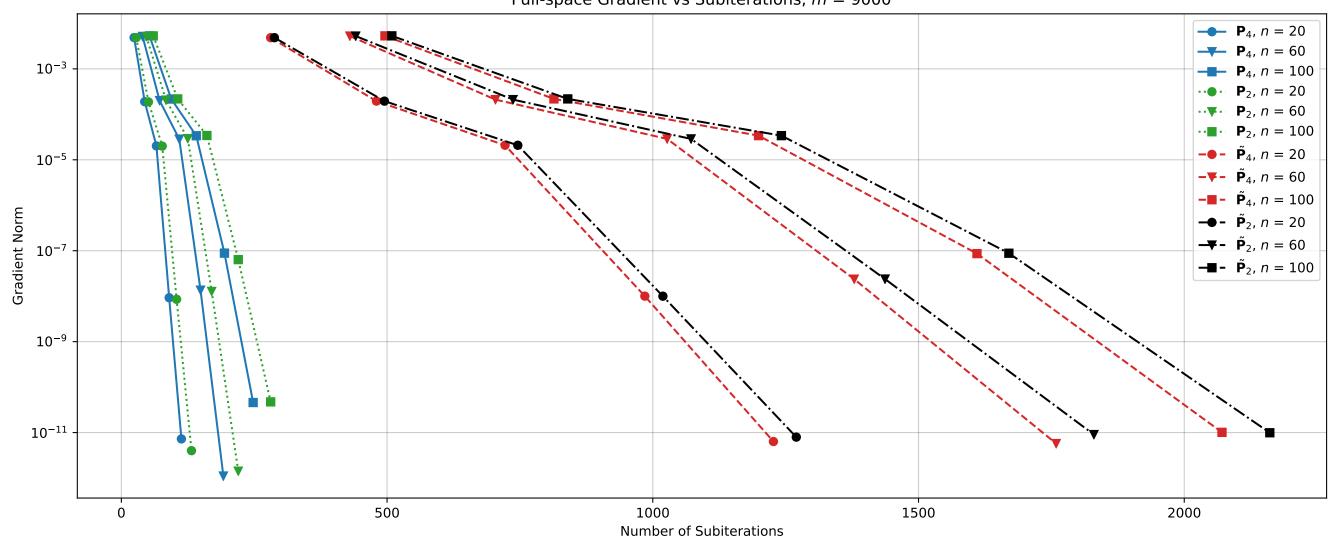
Full-space with $\tilde{\mathbf{P}}_2$ Gradient vs Design Cycles, m=16000 10^{-2} --- n = 20--- n = 100 10^{-4} --- n = 160--- n = 320--- n = 640**Gradient Norm** 10^{-6} 10^{-8} 10^{-10} 2.0 1.0 1.5 2.5 3.0 3.5 5.0 4.0 4.5

Iterations

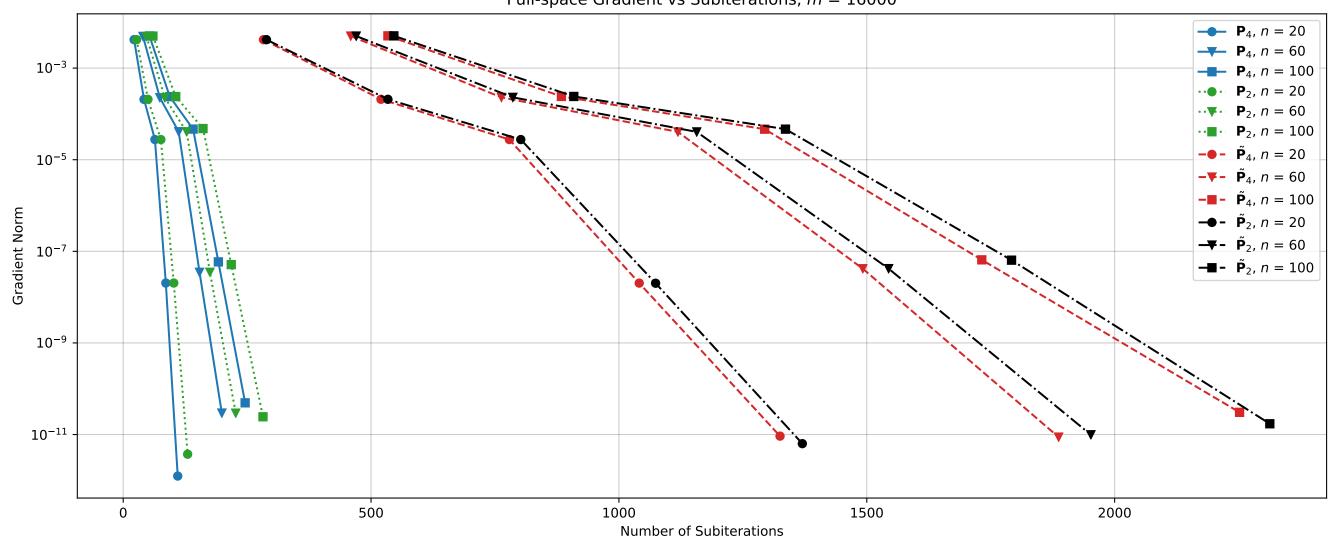
Full-space Gradient vs Subiterations, m = 4000

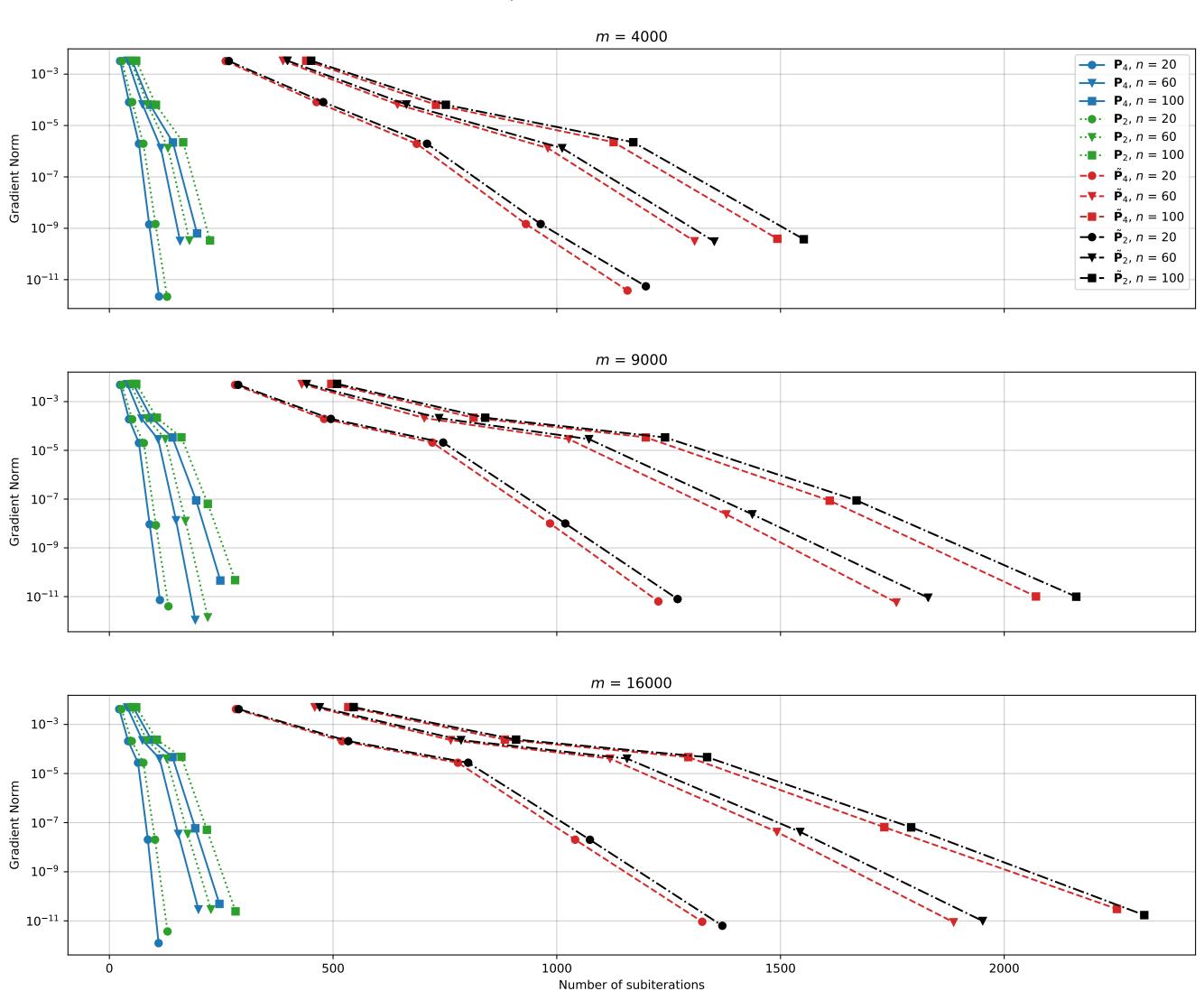


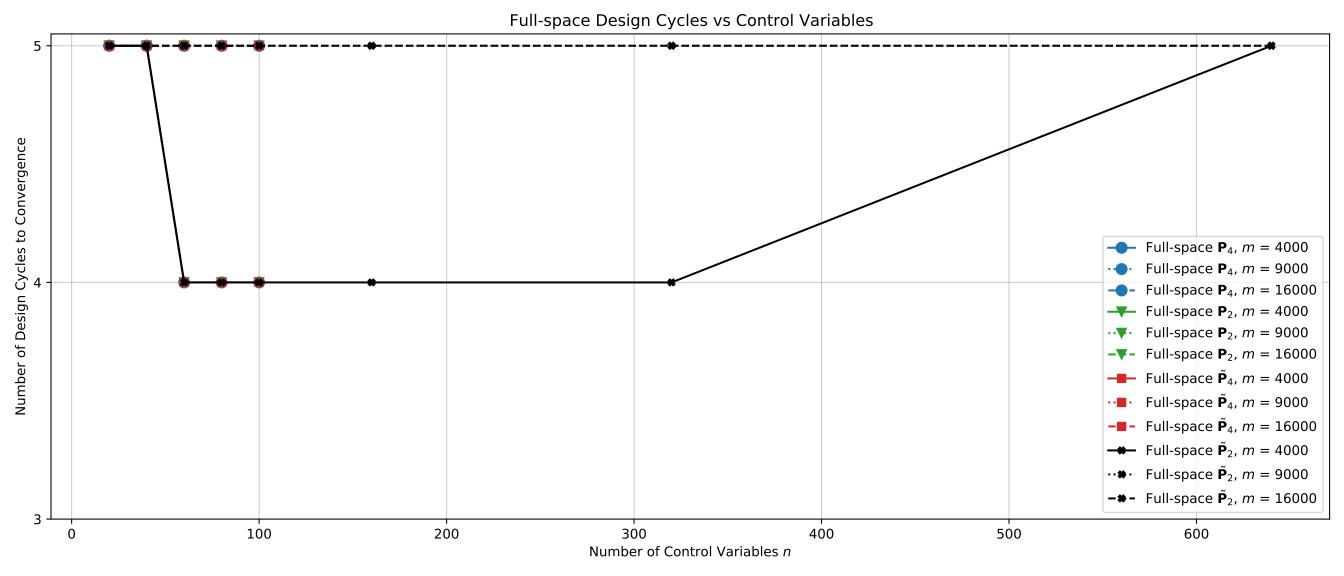
Full-space Gradient vs Subiterations, m = 9000



Full-space Gradient vs Subiterations, m = 16000



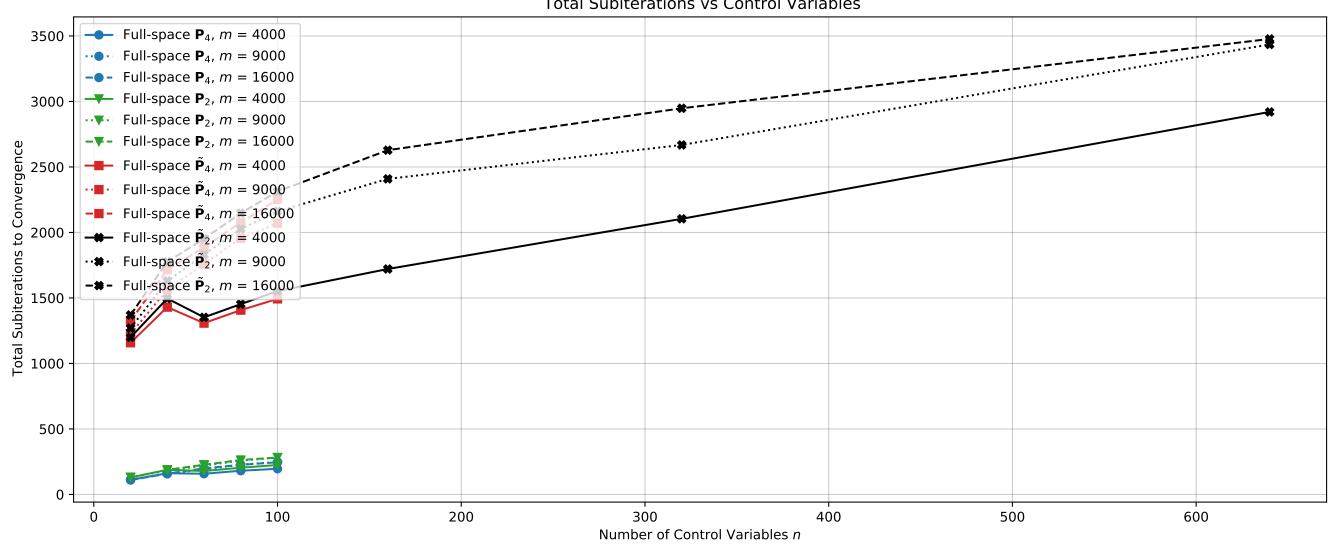




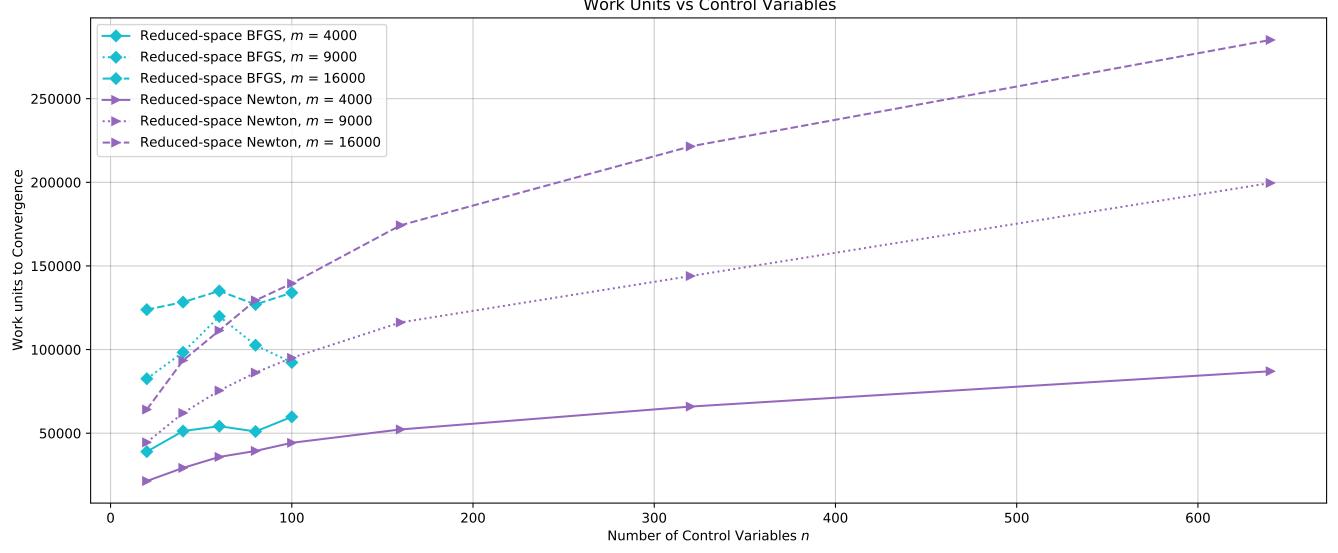
Work Units vs Control Variables --- Full-space P_4 , m = 4000400000 ••• Full-space \mathbf{P}_4 , m = 9000**---** Full-space P_4 , m = 16000Full-space \mathbf{P}_2 , m = 4000350000 ••• Full-space \mathbf{P}_2 , m = 9000**-**▼- Full-space P_2 , m = 16000300000 Full-space $\tilde{\mathbf{P}}_4$, m = 4000Full-space $\tilde{\mathbf{P}}_4$, m = 9000250000 **-**■- Full-space $\tilde{\mathbf{P}}_4$, m = 16000 \longrightarrow Full-space $\tilde{\mathbf{P}}_2$, m = 4000•• Full-space $\tilde{\mathbf{P}}_2$, m = 9000₽ 200000 Work Units 120000 **-*-** Full-space $\tilde{\mathbf{P}}_2$, m = 16000100000 50000 0 · 100 200 300 400 500 600

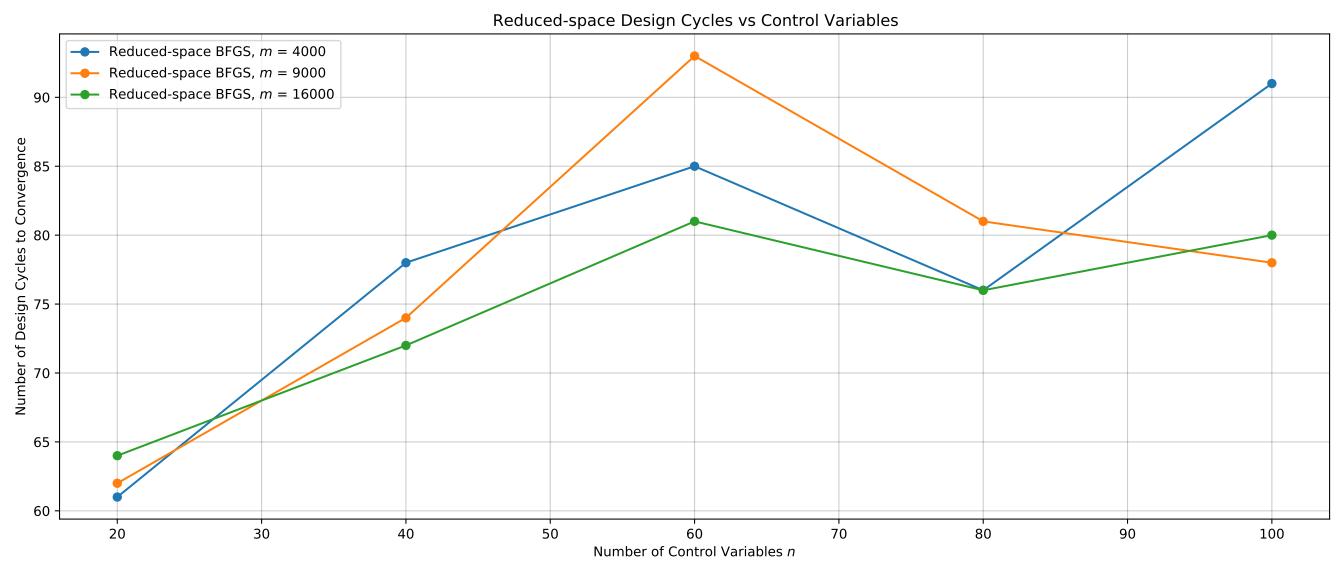
Number of Control Variables n

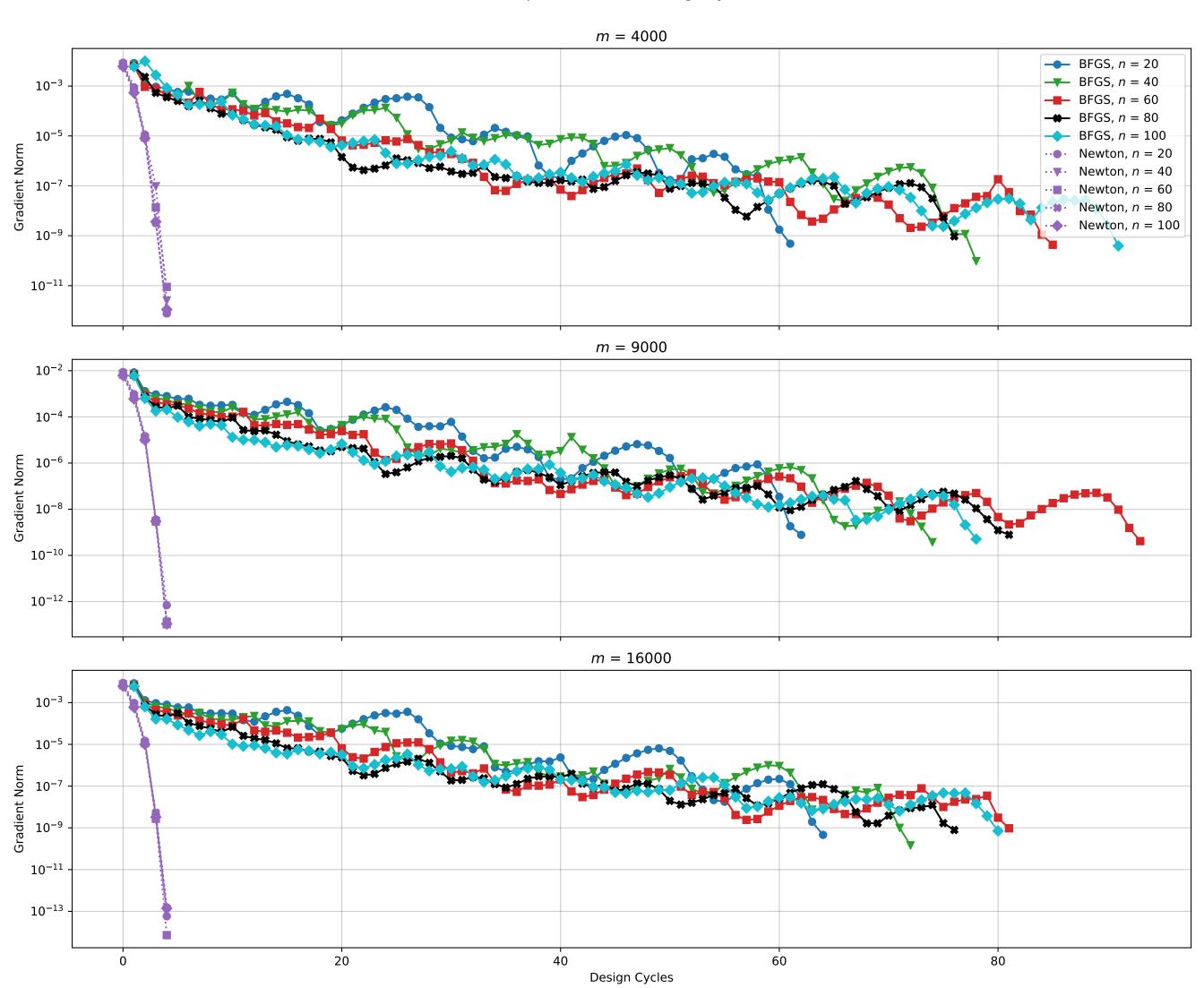




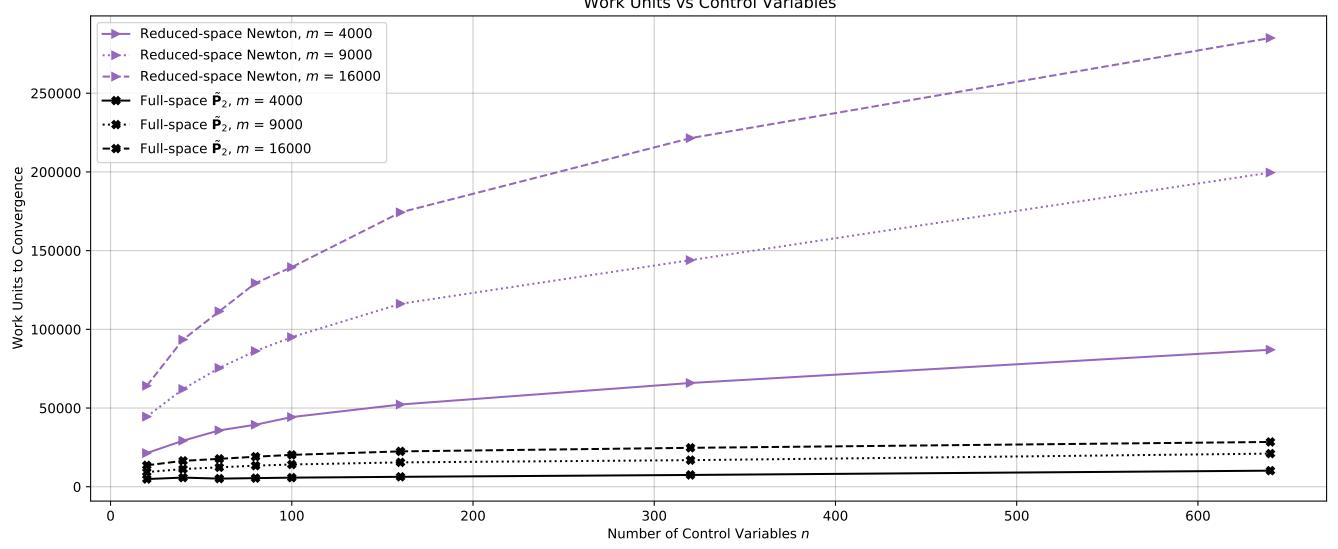
Work Units vs Control Variables







Work Units vs Control Variables



Work Units vs State Variables

