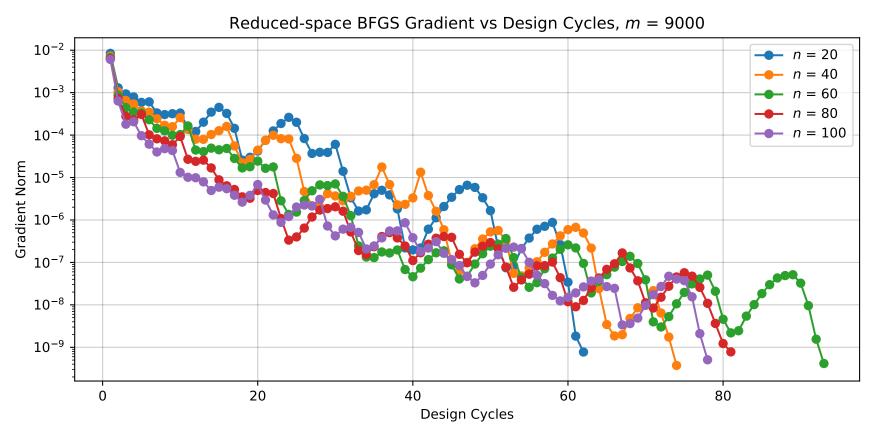
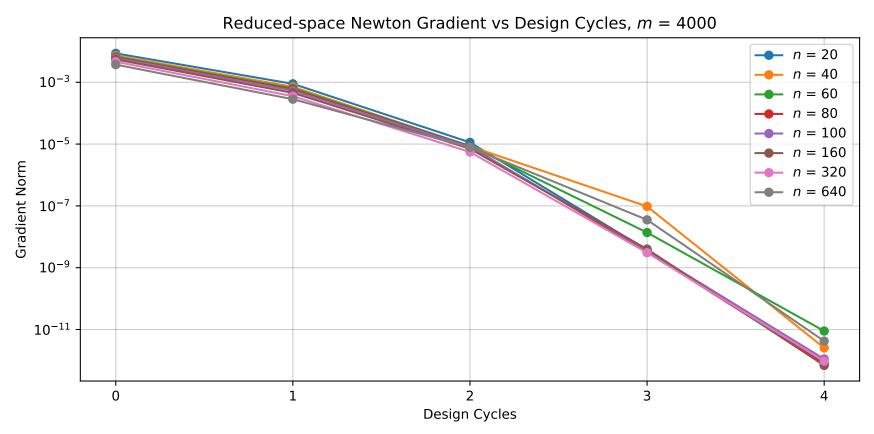
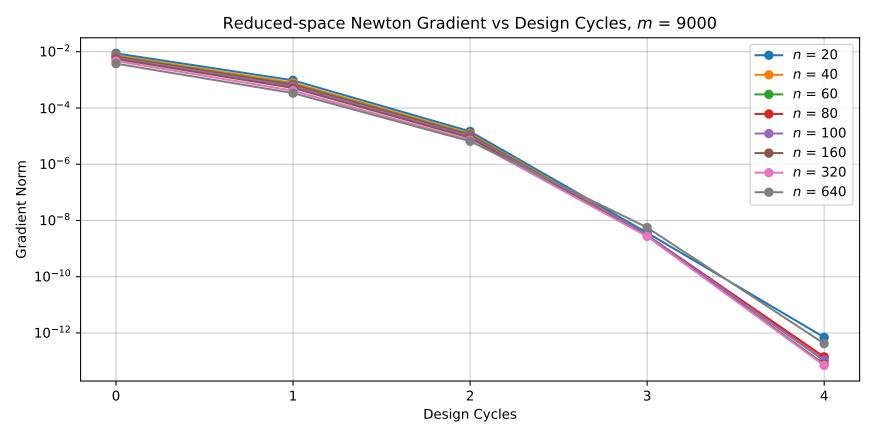
Reduced-space BFGS Gradient vs Design Cycles, m = 4000--- n = 20- n = 40 $10^{-3}$ - n = 60- n = 80n = 100Gradient Norm 10<sup>-5</sup>  $10^{-5}$  $10^{-9}$ 20 60 40 80

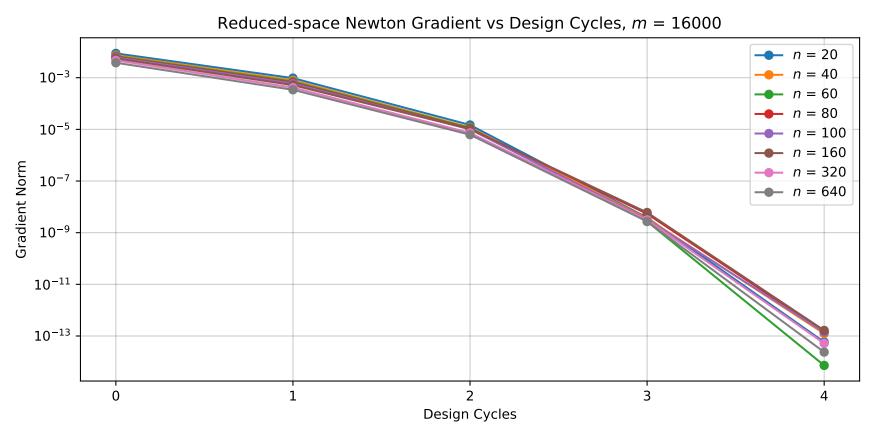
**Design Cycles** 

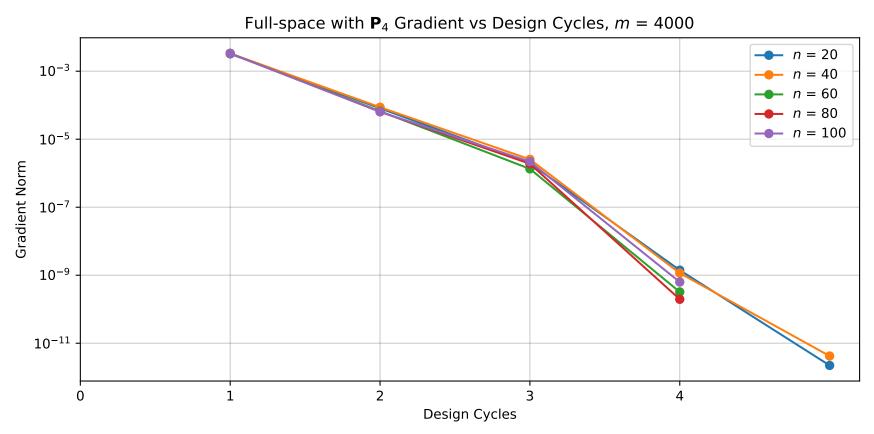


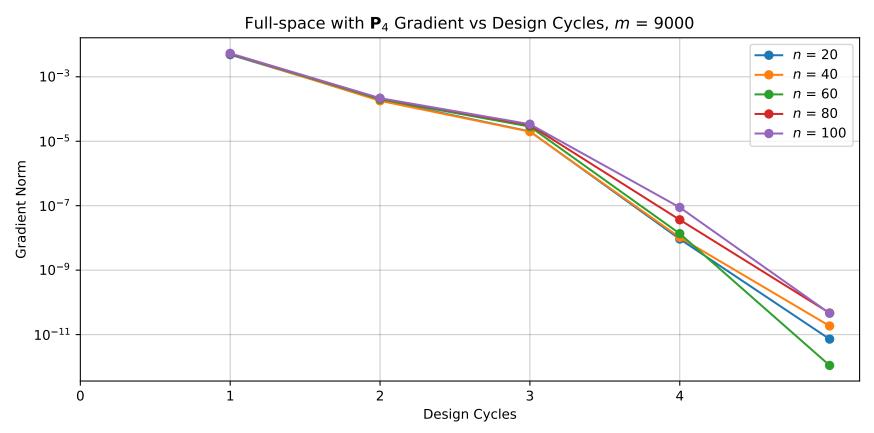
Reduced-space BFGS Gradient vs Design Cycles, m = 16000- n = 20- n = 40 $10^{-3}$ - n = 60n = 80n = 100Gradient Norm 10<sup>-2</sup>  $10^{-5}$  $10^{-9}$ 20 30 50 60 70 80 10 40 **Design Cycles** 

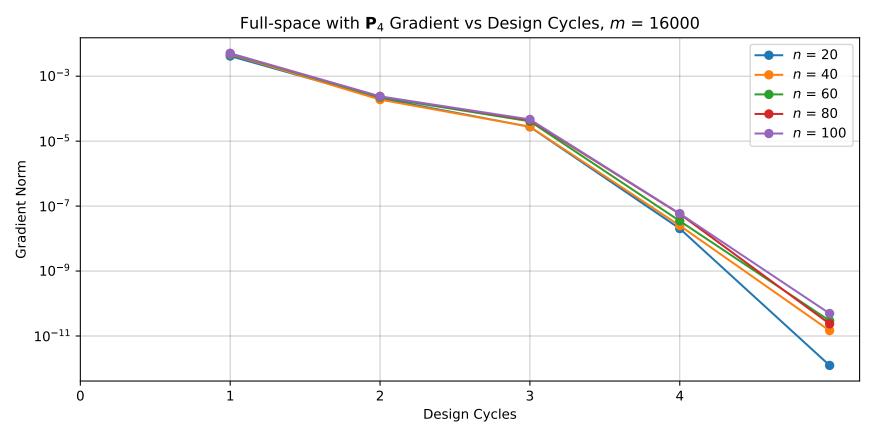




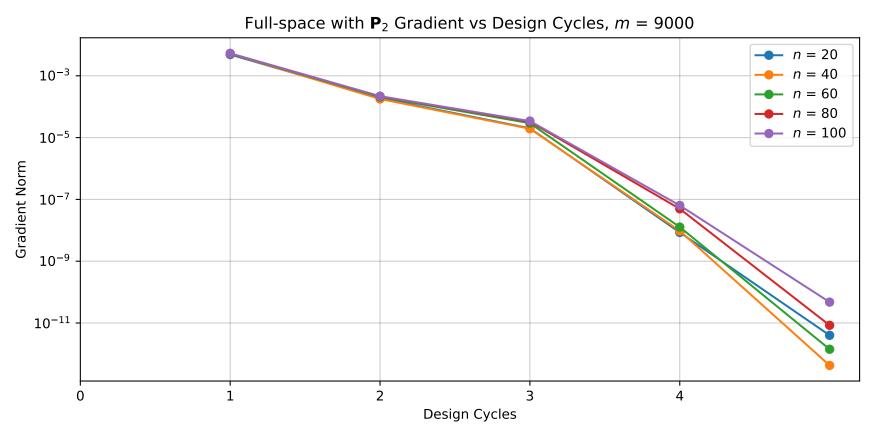


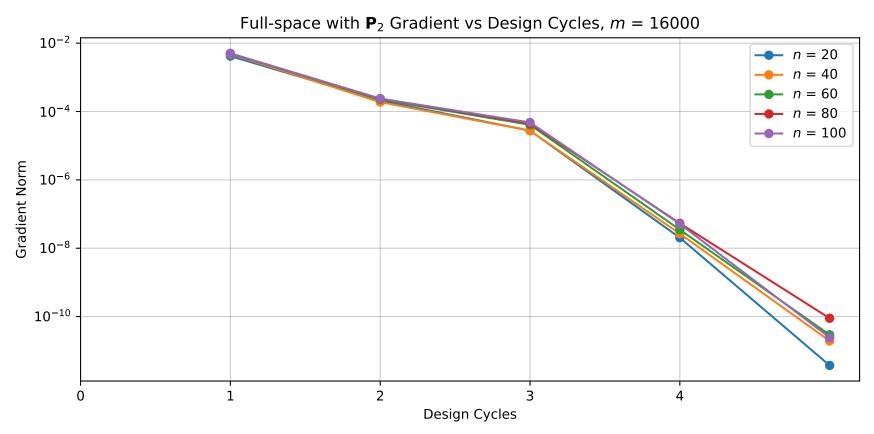


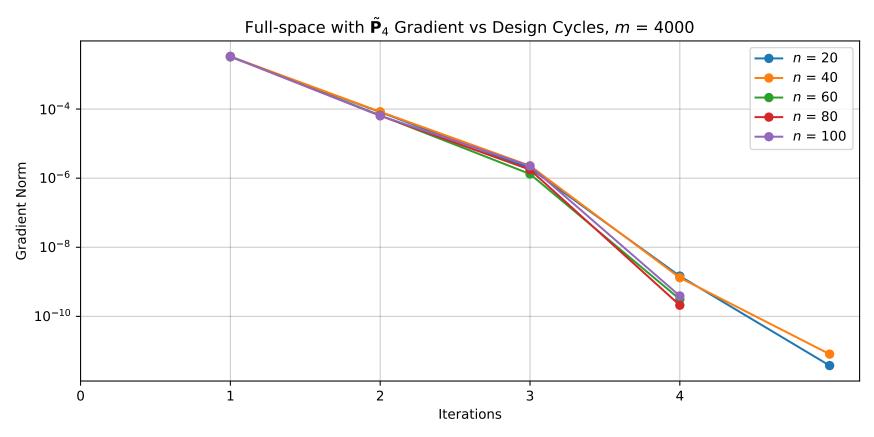


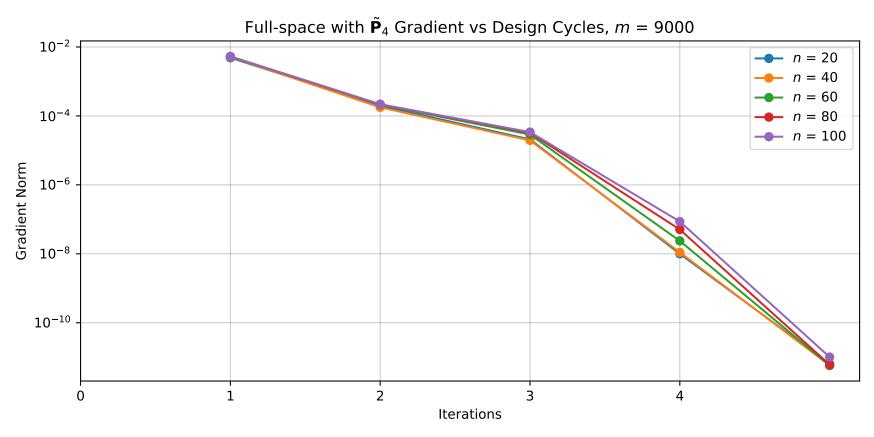


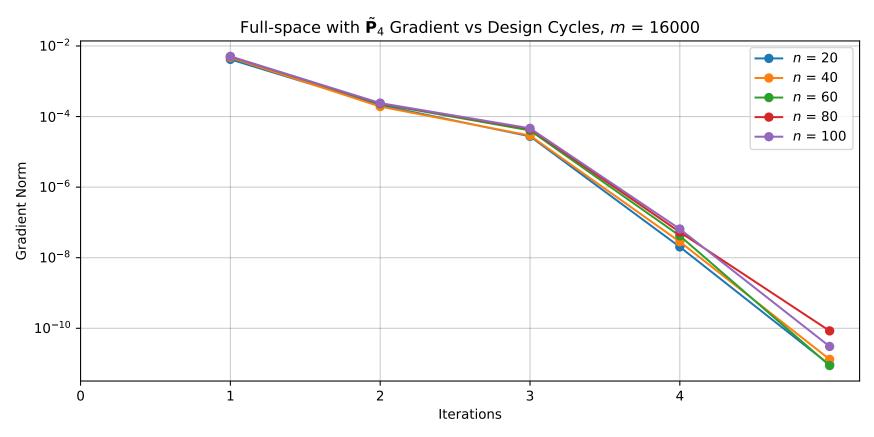
Full-space with  $P_2$  Gradient vs Design Cycles, m = 4000--- n = 2010<sup>-3</sup> --- n = 40--- n = 60--- n = 80--- n = 100 $10^{-5}$ **Gradient Norm**  $10^{-7}$  $10^{-9}$  $10^{-11}$ **Design Cycles** 

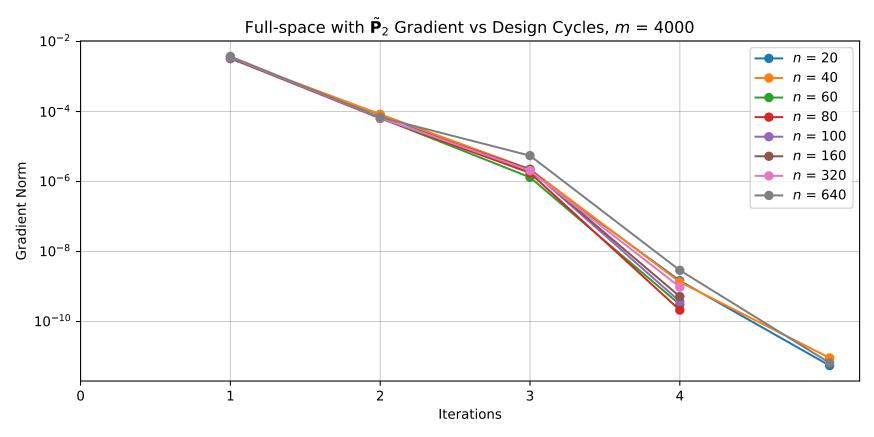


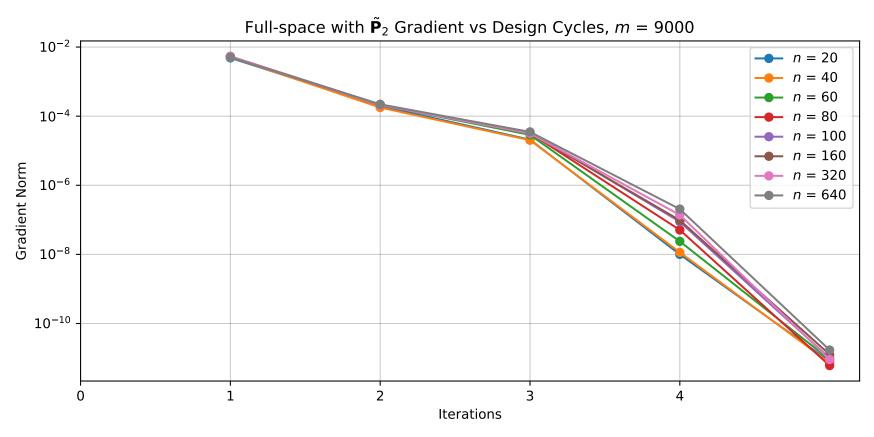


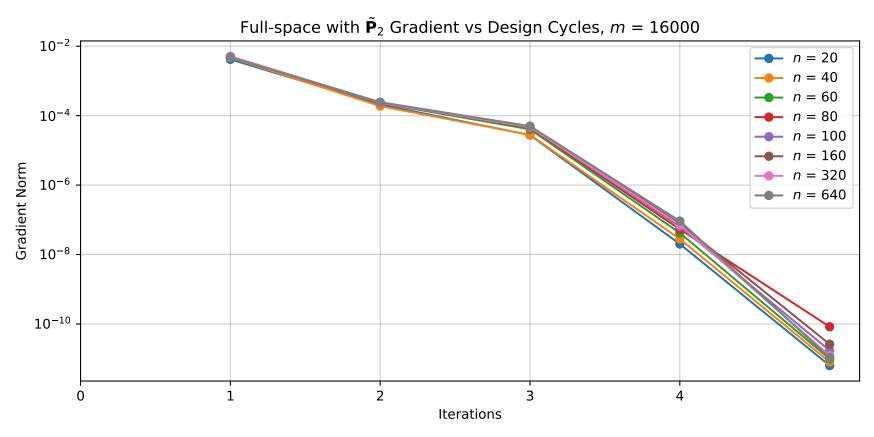




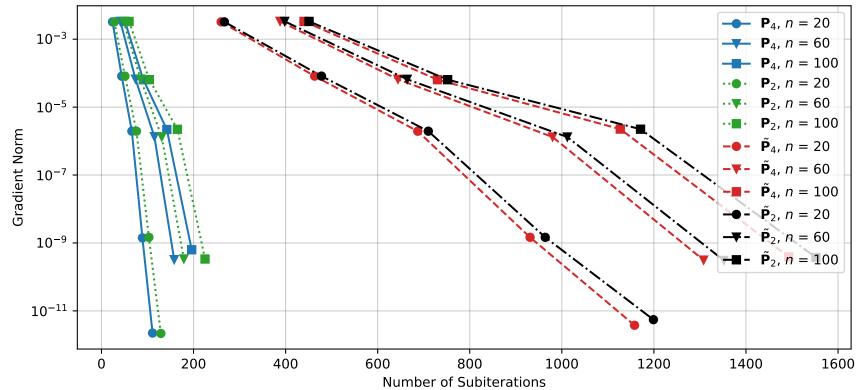




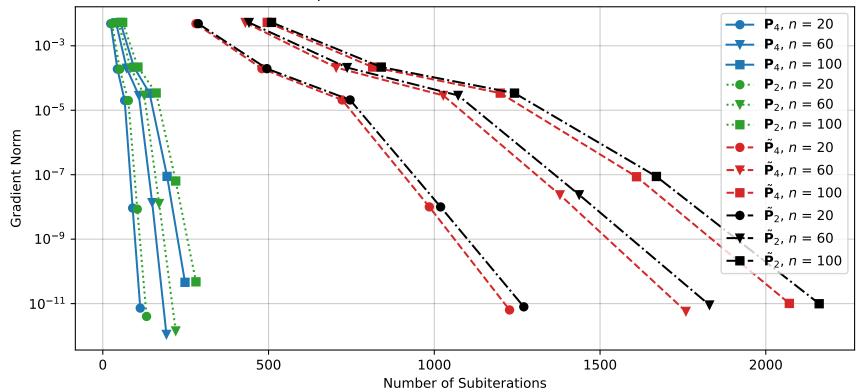




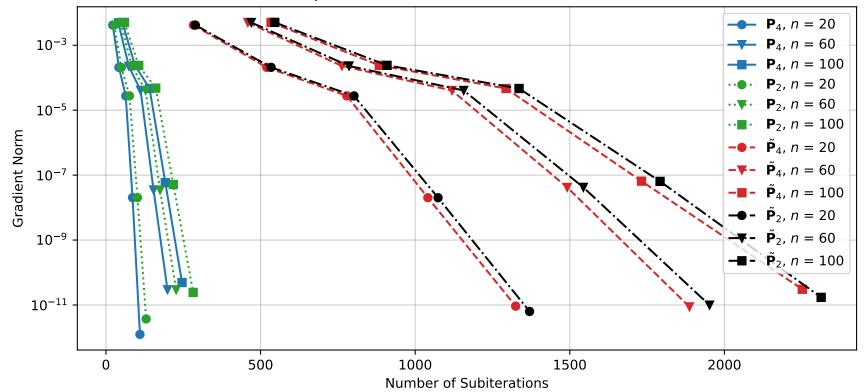
Full-space Gradient vs Subiterations, m = 4000

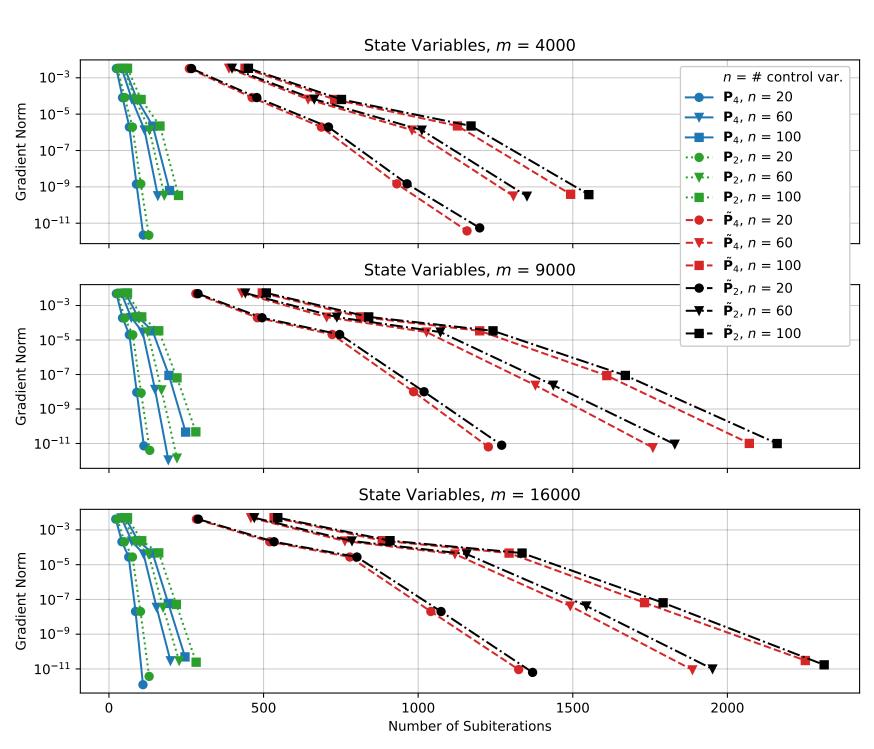


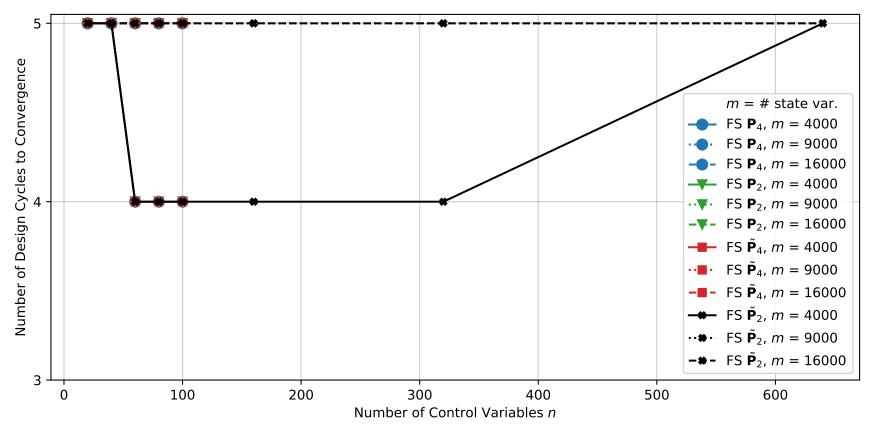
Full-space Gradient vs Subiterations, m = 9000

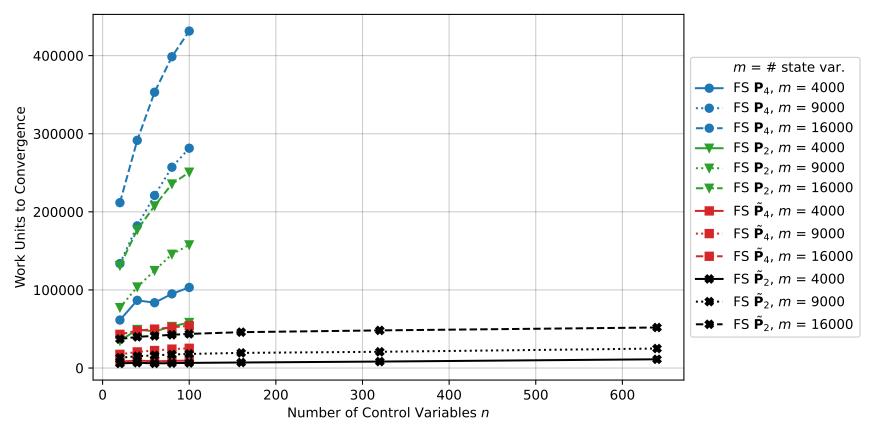


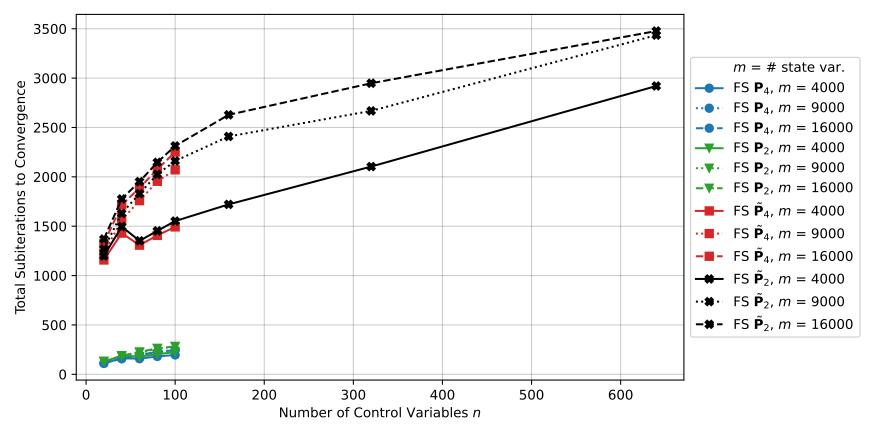
Full-space Gradient vs Subiterations, m = 16000

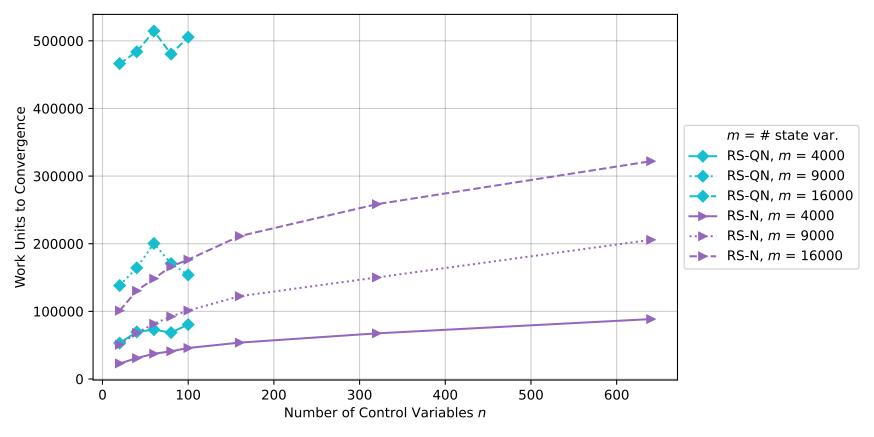


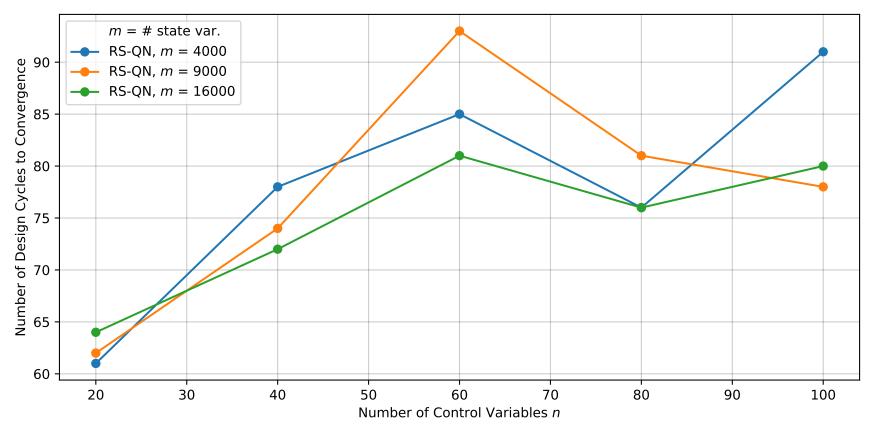


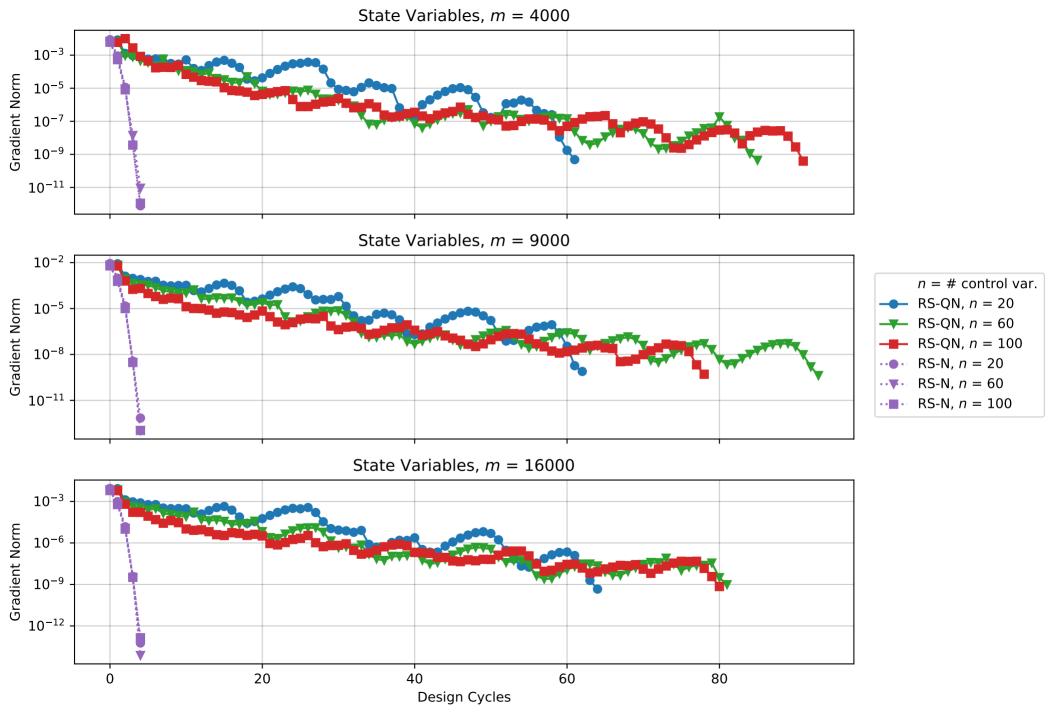


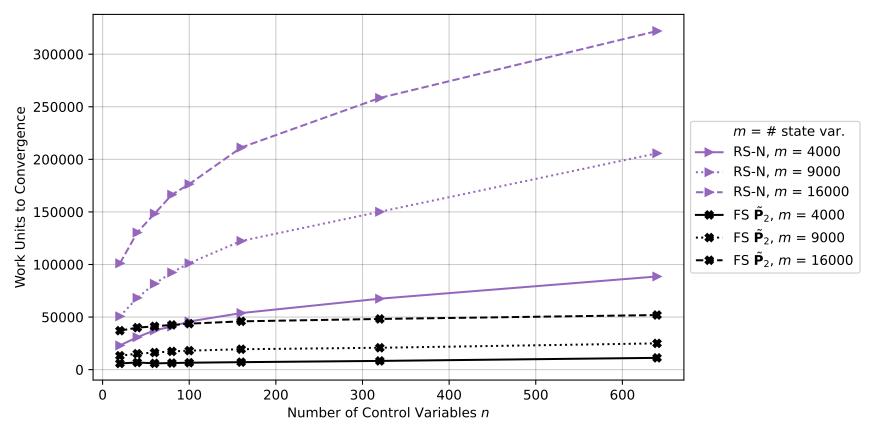


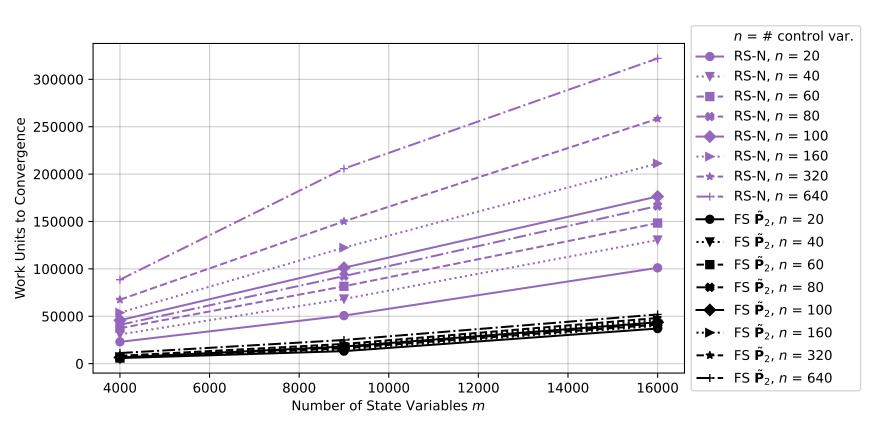












Gradient Norm vs Design Cycles m = 4000- RS-QN, n = 20- RS-QN, n = 60 $10^{-3}$ - RS-QN, n = 100 $\cdot \cdot \bullet \cdot \mid RS-N, n = 20$ RS-N, n = 60 $10^{-5}$ RS-N, n = 100**Gradient Norm** --- FS  $\tilde{\bf P}_2$ , n = 20**-**▼- FS  $\tilde{\mathbf{P}}_2$ , n = 60 $10^{-7}$ FS  $\tilde{\mathbf{P}}_2$ , n = 100 $10^{-9}$  $10^{-11}$ 60 20 40 80 **Design Cycles**