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## Problem 1.2

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### Problem 1.2

0.0/2.0 points (ungraded)

Let  $\varepsilon$  be arbitrary  $n$ -th root of unity (distinct from 1). Prove the following equality.

$$1 + 2\varepsilon + 3\varepsilon^2 + \dots + n\varepsilon^{n-1} = \frac{n}{\varepsilon - 1}$$

In order to prove it, compute this sum in the closed form. To this end, notice that the summed series can be obtained by differentiation of a more usual geometric series. What is the result?

$$1 + 2\varepsilon + 3\varepsilon^2 + \dots + n\varepsilon^{n-1} = \frac{(n(\boxed{\phantom{000}}) - 1)\varepsilon^{\boxed{\phantom{000}}}}{(\boxed{\phantom{000}})^{\boxed{\phantom{000}}}}$$

	$\varepsilon - 1$	$\varepsilon + 1$	$n$	2	1		
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Notice that from this result the statment of the problem follows immediately.

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