

# Logic Operations on Binaries

## Intro to MIPS

**CS 64: Computer Organization and Design Logic**

**Lecture #3**

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***Why do CPU programmers celebrate  
Christmas and Halloween  
on the same day?***

**Because Oct-31 = Dec-25 !!!**

# Administrative Stuff

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- Assignment 1 is due on Tuesday on Gradescope
  - How was lab on Thursday?
- Assignment 2 will be issued soon
- Reminder: No class next week Monday (Uni. Holiday)

# Any Questions From Last Lecture?

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# Practice on Binary Addition, etc...

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*See board...*

- Addition
- Subtraction
- Carry Out (C)
- Overflow (V)

# Binary Logic Refresher

## NOT, AND, OR

X	NOT X $\overline{X}$
0	1
1	0

X	Y	X AND Y X && Y X.Y
0	0	0
0	1	0
1	0	0
1	1	1

X	Y	X OR Y X    Y X + Y
0	0	0
0	1	1
1	0	1
1	1	1

# Binary Logic Refresher

## Exclusive-OR (XOR)

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The output is “1” only if the inputs are opposite

X	Y	X XOR Y $X \oplus Y$
0	0	0
0	1	1
1	0	1
1	1	0

# Bitwise NOT

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- Similar to logical NOT (!), except it works on a bit-by-bit manner
- In C/C++, it's denoted by a tilde: ~

$$\sim(1001) = 0110$$



# Exercises

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- Remember: hexadecimal numbers are often written in the **0xhh** notation, so for example:

The hex 3B would be written as **0x3B**

- What is  $\sim(0x04)$ ?
  - Ans: 0xFB
- What is  $\sim(0xE7)$ ?
  - Ans: 0x18

# Bitwise AND

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- Similar to logical AND (&&), except it works on a bit-by-bit manner
- In C/C++, it's denoted by a single ampersand: &

$$\begin{array}{rcll} (1001 & \& & 0101) & = & 1 & 0 & 0 & 1 \\ & & & & & \& & 0 & 1 & 0 & 1 \\ & & & & & & & & & & \\ & & & & & = & 0 & 0 & 0 & 1 \end{array}$$

# Exercises

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- What is  $(0xFF) \& (0x56)$ ?
  - Ans: 0x56
- What is  $(0x0F) \& (0x56)$ ?
  - Ans: 0x06
- What is  $(0x11) \& (0x56)$ ?
  - Ans: 0x10
- Note how  $\&$  can be used as a “masking” function
  - Masking?! What’s being “masked”???

# Bitwise OR

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- Similar to logical OR (`||`), except it works on a bit-by-bit manner
- In C/C++, it's denoted by a single pipe: `|`

$$\begin{array}{rcl} (1001 & | & 0101) \\ & & = 1 \ 0 \ 0 \ 1 \\ & & | \ 0 \ 1 \ 0 \ 1 \\ & & = 1 \ 1 \ 0 \ 1 \end{array}$$

# Exercises

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- What is  $(0xFF) \mid (0x92)$ ?
  - Ans:  $0xFF$
- What is  $(0xAA) \mid (0x55)$ ?
  - Ans:  $0xFF$
- What is  $(0xA5) \mid (0x92)$ ?
  - Ans:  $0xB7$

# Bitwise XOR

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- Works on a bit-by-bit manner
- In C/C++, it's denoted by a single carat: ^

$$\begin{array}{rcl} (1001 \text{ } ^\wedge \text{ } 0101) & = & 1 \ 0 \ 0 \ 1 \\ & & ^\wedge \quad 0 \ 1 \ 0 \ 1 \\ & & \\ & = & 1 \ 1 \ 0 \ 0 \end{array}$$

# Exercises

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- What is  $(0xA1) \wedge (0x13)$ ?
  - Ans: 0xB2
- What is  $(0xFF) \wedge (0x13)$ ?
  - Ans: 0xEC
- Note how  $(1 \wedge b)$  is always the inverse of  $b$  ( $\sim b$ )  
and how  $(0 \wedge b)$  is always just  $b$

## Bit Shift *Left*

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- Move all the bits N positions to the left
- What do you do the positions now empty?
  - You put in N number of 0s
- Example: Shift “1001” 2 positions to the left  
$$1001 \ll 2 = \mathbf{100100}$$
- Why is this useful as a form of multiplication?



# Multiplication by Bit Left Shifting

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- Veeeery useful in CPU (ALU) design
  - Why?
- Because you don't have to design a “multiplier” function
- You just have to design a way for the bits to shift (which is a relatively easier design)

## Bit Shift *Right*

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- Move all the bits N positions to the ***right***, subbing-in either N number of 0s or N 1s on the left
- Takes on two different forms
- Example: Shift “1001” 2 positions to the right  
 $1001 \gg 2 = \text{either } \mathbf{0010} \text{ or } \mathbf{1110}$
- The information carried in the last 2 bits is lost.
- If Shift Left does *multiplication*, what does Shift Right do?
  - It divides, **but** it truncates the result

# Two Forms of Shift Right

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- Subbing-in 0s makes sense (esp. if the number is unsigned)
- BUT! When should we sub-in the leftmost bits with 1s?
  - ANS: When the number is signed and negative
- So what if it's a signed number that's positive?
  - ANS: You should sub-in the leftmost bits with 0s!
- This is called “*arithmetic*” shift right:
  - $1100 \text{ (arithmetic)} \gg 1 = 1110$
  - $0101 \text{ (arithmetic)} \gg 1 = 0010$

# Two Forms of Shift Right

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- If the number is unsigned (and thus always positive), we can use “**logical**” shift right
  - Never use this type of shift right on signed numbers...
- **Arithmetic** shift preserves sign bit
- **Logical** shift cannot/does not preserve sign bit

# Exercise Using Logic Ops

- Given an argument that's a 32-bit integer number **i**, write a function in C++ that can isolate the bit in **position 5** of that integer and print it.

- Example: **i** = 1266

- In 32-bits of binary, that's:

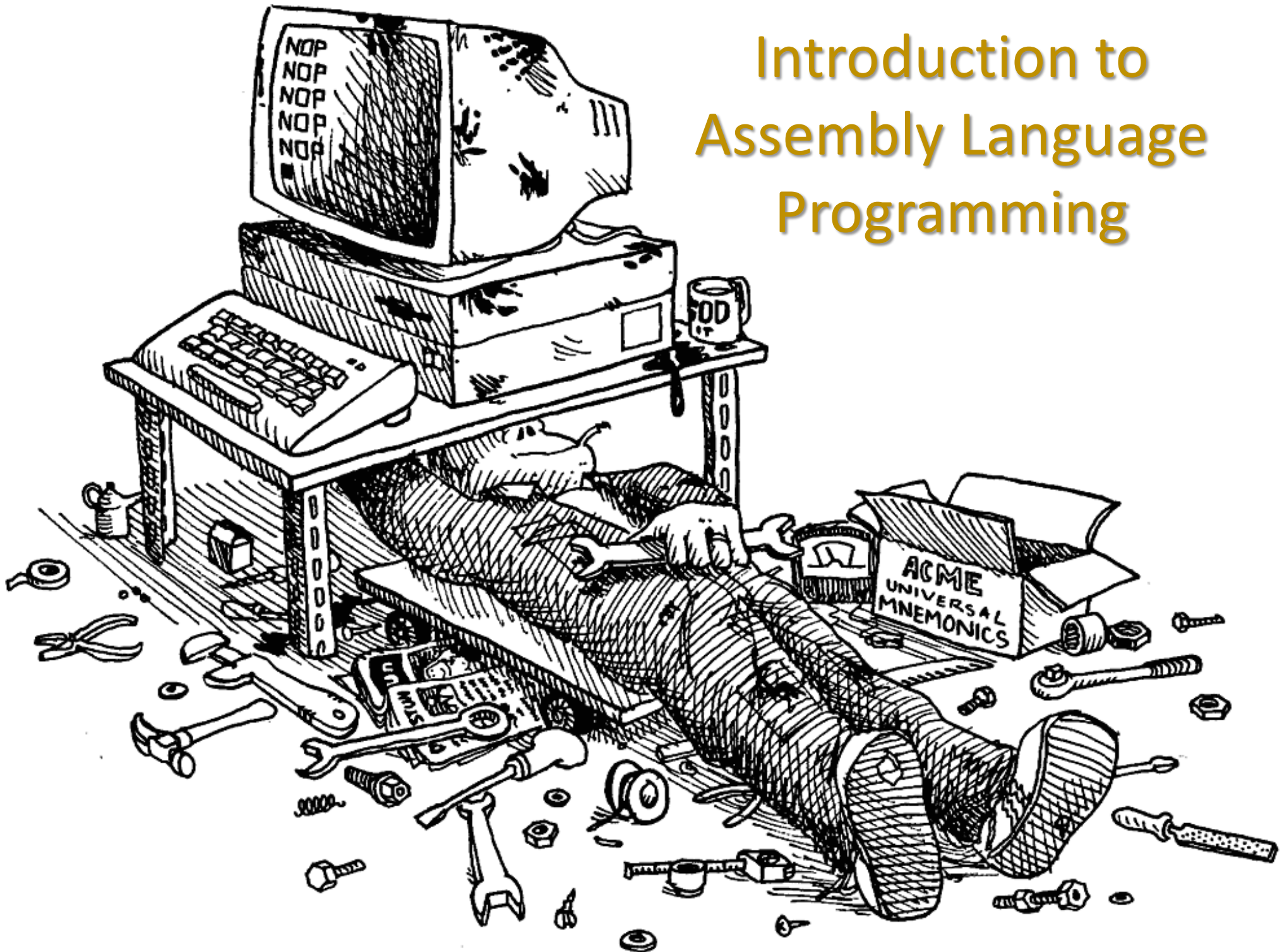
**0000 0000 0000 0000 0000 0100 1111 0010**

- So, the bit in position 5 is the highlighted one (it's **1**)
- So your code should print out **"1"**

- Answer:

```
void print5(int i):  
{  
    i >> 5;  
    i = i & 1;  
    cout << i;  
}
```

# Introduction to Assembly Language Programming



# The Simple Language of a CPU

- We have: variables, integers, floating points, arithmetic ops, and assignment ops
- Restrictions:
  - Can only assign **integers** directly to variables
  - Can only do arithmetic on (e.g. add) variables, always **two at a time** (no more)

EXAMPLE:

**$z = 5 + 7;$**  has to be simplified to:

**$x = 5;$**

**$y = 7;$**

**$z = x + y;$**

**What func is needed to implement this?**



*An adder: but how many bits?*

# Core Components

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What we need in a CPU is:

- Some place to hold the statements (instructions to the CPU) as we operate on them
- Some *place* to tell us *which statement* is next
- Some *place* to hold the *variables*
- Some *way* to do arithmetic on *numbers*

**That's ALL that Processors Do!!**

*Processors just read a series of statements (instructions) forever.  
No magic!*



# Core Components

What we need in a CPU is:

- Some place to **hold the statements** (instructions to the CPU) as we operate on them → **MEMORY**
- Some *place* to tell us *which statement* is **next** → **PROGRAM COUNTER (PC)**
- Some *place* to **hold the variables** → **REGISTERS**
- Some *way* to **do arithmetic on numbers** → **ARITHMETIC LOGIC UNIT (ALU)**

...And one more thing:

- Some place to tell us which statement is **currently** being executed → **INSTRUCTION REGISTER (IR)**

# Basic Interaction

- Copy instruction from **memory** at wherever the **program counter (PC)** says into the **instruction register (IR)**
- Execute it, possibly involving registers and the **arithmetic logic unit (ALU)**
- Update the **PC** to point to the next instruction
- Repeat

```
Initialize();  
while (true) {  
    instruc_reg = GetFromMem[prog_countr];  
    executeInstruc(instruc_reg);  
    prog_countr++;  
}
```

pseudocode

## Instruction Register

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?

## Registers

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x: ?

y: ?

z: ?

## Program Counter

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?

## Memory

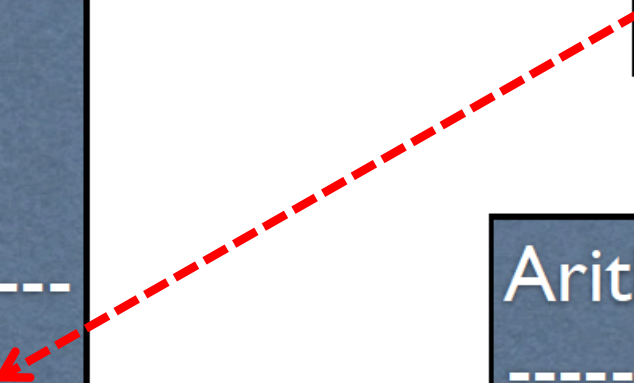
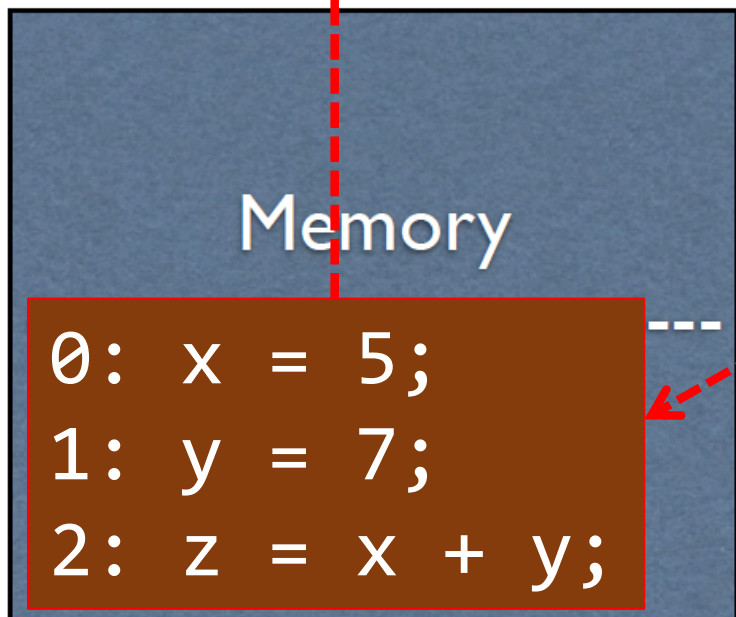
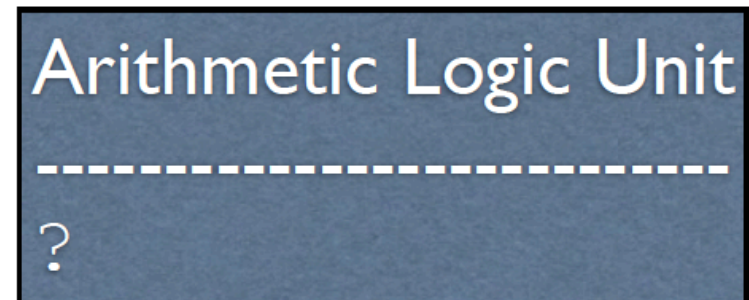
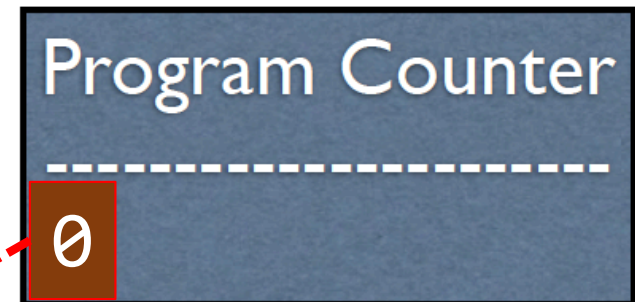
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?

## Arithmetic Logic Unit

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?



Instruction Register

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x = 5;

Registers

---

x: 5  
y: 7  
z: ?

Program Counter

---

1

Memory

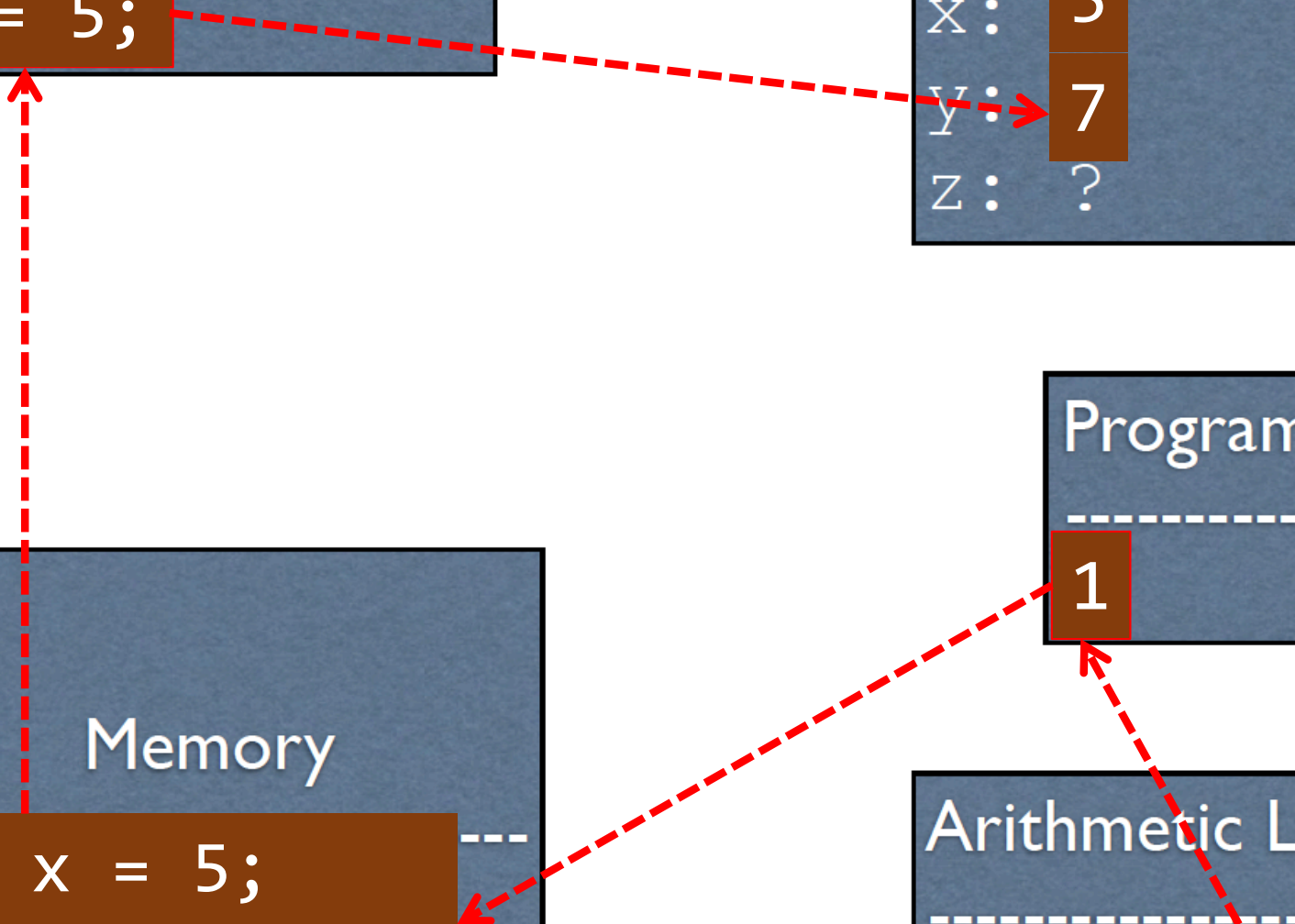
---

0: x = 5;  
1: y = 7;  
2: z = x + y;

Arithmetic Logic Unit

---

0 + 1 = 1





## Instruction Register

$z = x + y;$

## Registers

x: 5

y: 7

z: ?

## Program Counter

2

## Memory

0:  $x = 5;$

1:  $y = 7;$

2:  $z = x + y;$

## Arithmetic Logic Unit

$1 + 1 = 2$

## Instruction Register

$z = x + y;$

## Memory

0:  $x = 5;$

1:  $y = 7;$

2:  $z = x + y;$

## Registers

x: 5

y: 7

z: 12

## Program Counter

2

## Arithmetic Logic Unit

$5 + 7 = 12$

# Why MIPS?

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- MIPS:
  - a **r**educed **i**nstruction **S**et **C**omputer (RISC) architecture developed by a company called MIPS Technologies (1981)
- Relevant in *embedded systems*
  - An area of CS/CE
- All modern commercial processors share the same core concepts as MIPS, just with extra stuff
  - Some modern CPUs include Intel, ARM, AMD
- ...but most importantly...



# MIPS is Simpler...

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... than other instruction sets for CPUs

So it's a great learning tool!

- Dozens of instructions (as opposed to hundreds)
- Lack of redundant instructions or special cases
- 5 stage pipeline versus 12 stages (Intel i7 processors)

# YOUR TO-DOs

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- Readings! Do Them!
  - Consult syllabus...
- Finish Assignment #1
  - You have to submit it as a **PDF** using *Gradescope*
  - Due on **Tuesday 1/14, by 11:59:59 PM**

**</LECTURE>**