

# LINFO1104

## Concepts, paradigms, and semantics of programming languages

### Lecture 10-11

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## Overview of lectures 10-11

- Limitation of deterministic dataflow
  - Some applications cannot be written in deterministic dataflow!  
We explain why not.
- Message-passing concurrency  
(multi-agent actor programming)
  - We overcome the limitation by adding one new concept, **ports**, to deterministic dataflow
  - We define **port objects** and **active objects** and show how to write message protocols and multi-agent actor programs
  - We show another approach using ports, namely use **deterministic dataflow by default and add ports** but only when necessary



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## Limitation of deterministic dataflow



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## Limitation of deterministic dataflow



- In lectures 8-9 we saw deterministic dataflow, which makes concurrent programming very easy
  - It allows “Concurrency for Dummies”: threads can be added to the program at will without changing the result
- But unfortunately it cannot be used all the time!
  - It has a strong limitation: it cannot be used to write programs when the nondeterminism must be visible
  - But why must nondeterminism sometimes be visible? Let’s see an example: a client/server application.

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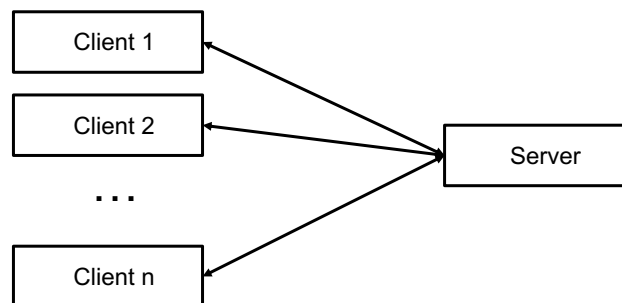
## Client/server application (1)



- A client/server application consists of a set of clients all communicating to one server
  - The clients and the server are concurrent agents
  - Each client sends messages to the server and receives replies
- Client/server applications are ubiquitous on the Internet
  - For example, all Web stores are client/servers: the users are clients and the store is the server
  - When shopping at Amazon, your Web browser sends messages and receives replies from the Amazon server
- Client/server cannot be written in deterministic dataflow!
  - Why not? Let's try and see what goes wrong! Try it yourself!

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## Client/server application (2)



- Each client has a link to the server and can send messages to the server at any time
- The server receives each message, does a local computation, and then replies immediately

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## Client/server: first attempt



- Let's try to write a client/server in deterministic dataflow
  - Assume that there are two clients, each with an output stream, and the server receives both
- Here is the server code:

```
proc {Server S1 S2}
  case S1|S2 of (M1|T1)|S2 then
    (handle M1) {Server T1 S2}
  [] S1|(M2|T2) then
    (handle M2) {Server S1 T2}
  end
end
```

This doesn't work!  
Why not?

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## Client/server: second attempt



- The first attempt does not work if Client 2 sends a message and Client 1 sends nothing
- We can try doing it the other way around:

```
proc {Server S1 S2}
  case S1|S2 of S1|(M2|T2) then
    (handle M1) {Server S1 T2}
  [] (M1|T1)|S2 then
    (handle M2) {Server T1 S2}
  end
end
```

- This doesn't work if Client 1 sends a message and Client 2 sends nothing!

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## Client/server: third attempt



- Maybe the server has to receive from both clients:

```
proc {Server S1 S2}
  case S1|S2 of (M1|T1)|(M2|T2) then
    (handle M1)
    (handle M2)
    {Server T1 T2}
  end
end
```

- This does not work either! (Why not?)

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## What is the problem?



- The **case** statement waits on **a single pattern**
  - This is because of determinism: with the same input, the **case** statement must give the same result
- But the server must wait on **two patterns**
  - Either M1 from Client 1 or M2 from Client 2
  - Either pattern is possible, it depends on when each client sends the message and on how long the message takes to reach the server
    - The decision is made **outside the program**
  - This means exactly that execution is nondeterministic!

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## Understanding nondeterminism



- Nondeterminism means that a choice is made **outside of the program's control**
  - This is exactly what is happening here: the choice is the arrival order of the client messages, which depends on the human clients and on the message travel time
- The nondeterminism is inherently part of the client/server execution, it cannot be avoided
  - The nondeterminism is a consequence of the initial requirement: "The server receives each message, does a local computation, and then replies immediately"
  - This means that the reply cannot be delayed while the server waits for another message

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## Overcoming the limitation



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## Overcoming the limitation



- Deterministic dataflow cannot express an application that requires nondeterminism
- To do this, we need to extend the kernel language with a new concept
- The new concept must be able to wait on several events nondeterministically
  - The new language is no longer deterministic!
- We will show two possible solutions

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## Solution 1: WaitTwo



- We introduce the function:  
    {WaitTwo X Y}  
    with the following semantics:
  - {WaitTwo X Y} can return 1 if X is bound
  - {WaitTwo X Y} can return 2 if Y is bound
  - If either X or Y is bound, {WaitTwo X Y} will return
- If both X and Y are unbound, it just waits
- If both X and Y are bound, it can return either 1 or 2, both are possible (nondeterminism!)

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## Client/Server with WaitTwo



- Here is the client/server with WaitTwo:

```
proc {Server S1 S2}
  C={WaitTwo S1 S2}
in
  case C|S1|S2 of 1|(M1|T1)|S2 then
    (handle M1) {Server T1 S2}
  [] 2|S1|(M2|T2) then
    (handle M2) {Server S1 T2}
  end
end
```

- If Client 1 sends a message, C=1 and it is handled
- If Client 2 sends a message, C=2 and it is handled
- What happens if both Client 1 and Client 2 send messages?

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## WaitTwo is not scalable



- What happens if we have millions of clients?
  - WaitTwo solves the problem for two clients
  - How can we wait on millions of clients?
- One possibility is to “merge” all client streams into a single stream:

```
fun {Merge S1 S2}
  C={WaitTwo S1 S2}
in
  case C|S1|S2 of 1|(M1|T1)|S2 then M1|{Merge T1 S2}
  [] 2|S1|(M2|T2) then M2|{Merge S1 T2}
  end
end
```

- With Merge we build a huge tree of stream mergers. It must expand and contract if new clients arrive or old clients leave. Not very nice!

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## Solution 2: Ports



- A better solution is to add ports (named streams)
- Ports have two operations:  

```
P={NewPort S} % Create port P with stream S
{Send P X}      % Add X to end of port P's stream
```
- How does this solve our problem?
  - With a million clients  $C_1$  to  $C_{1000000}$ :  
Each client  $C_i$  does {Send  $M_i$  P} for each message it sends
  - The server reads the stream S, which contains all messages from all clients in some nondeterministic order

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## Port example operations



- We create a port and do sends:  

```
P={NewPort S}
{Browse S} % Displays _
{Send P a} % Displays a|_
{Send P b} % Displays a|b|_
```
- What happens if we do:  

```
thread {Send P c} end
thread {Send P d} end
```
- What are the possible results of these two sends for all choices of the scheduler?

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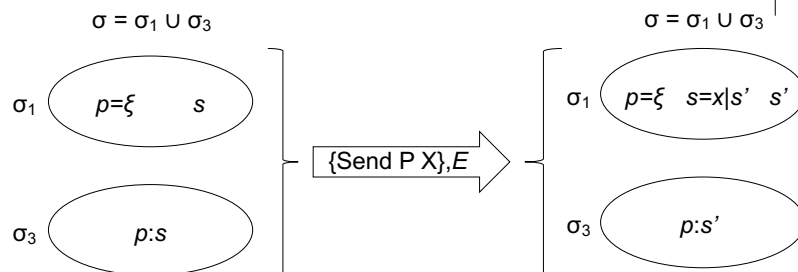
## Port semantics (1)



- Assume single-assignment store  $\sigma_1$  with variables
- Assume a port store  $\sigma_3$  that contains pairs of variables
  - (Remember  $\sigma_2$  was the cell store we introduced before)
- $P = \{\text{NewPort } S\}, \{P \xrightarrow{\text{environment}} p, S \rightarrow s\}$ 
  - Assume unbound variables  $p, s \in \sigma_1$
  - Create fresh name  $\xi$ , bind  $p = \xi$ , add pair  $p:s$  to  $\sigma_2$
- $\{\text{Send } P \ X\}, \{P \rightarrow p, X \rightarrow x\}$ 
  - Assume  $p = \xi$ , unbound variable  $s \in \sigma_1, p:s \in \sigma_2$
  - Create fresh unbound variable  $s'$ , bind  $s = x|s'$ , update pair to  $p:s'$

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## Port semantics (2)



- $\{\text{Send } X \ P\}$  adds  $x$  to the end of the port's stream and updates the new end of stream
  - The send operation is **atomic**, which means the scheduler is guaranteed never to stop in the middle, so it happens as if it is **one indivisible step**
- We assume that environment  $E = \{P \rightarrow p, X \rightarrow x\}$

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## Client/server with ports



- Assume port  $P = \{\text{NewPort } S\}$
- Client code: (any number of clients!)
  - Do  $\{\text{Send } P \ M\}$  to send message to server
- Server code:

```
proc {Server S}
  case S of M|T then
    (handle M)
    {Server T}
  end
end
```

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## Message-passing concurrency



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## Message-passing concurrency



- Message-passing concurrency is a new paradigm for concurrent programming
  - It consists of deterministic dataflow with ports
  - It is also called **multi-agent actor programming**
- We will show how to write concurrent programs in this new paradigm
  - We will define **port objects** and **active objects**
  - We show how to do **message protocols**
  - We show how to combine **deterministic dataflow with ports**, leading to the best all-round paradigm for concurrent programming

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## Stateless port objects (stateless agents)



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## Stateless port objects



- A **stateless port object** is a combination of a port, a thread, and a recursive list function
  - We also call it a **stateless agent**
- Each agent is defined in terms of how it replies to messages
- Each agent has its own thread, so there are no problems with concurrency
- Agents are a very useful concept!

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## A math agent



- Here is a simple procedure to do arithmetic:

```
proc {Math M}
  case M
  of add(N M A) then A=N+M
  [] mul(N M A) then A=N*M
  ...
end
end
```

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## Making it a port object



- We add a port, a thread, and a recursive procedure:

```
MP={NewPort S}  
proc {MathProcess Ms}  
  case Ms of M|Mr then  
    {Math M} {MathProcess Mr}  
  end  
end  
thread {MathProcess S} end
```

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## Using ForAll



- We replace MathProcess by ForAll:

```
proc {ForAll Xs P}  
  case Xs of nil then skip  
  [] X|Xr then {P X} {ForAll Xr P}  
  end  
end
```

- Using ForAll, we get:

```
proc {MathProcess Ms} {ForAll Ms Math} end
```

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## Defining new port objects (1)



- A generic way to build stateless port objects:

```
fun {NewPortObject0 Process}
  Port Stream
in
  Port={NewPort Stream}
  thread {ForAll Stream Process} end
Port
end
```

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## Defining new port objects (2)



- A generic way to build stateless port objects:

```
fun {NewPortObject0 Process}
  Port Stream
in
  Port={NewPort Stream}
  thread for M in Stream do {Process M} end end
Port
end
```

Using syntax  
of **for** loops

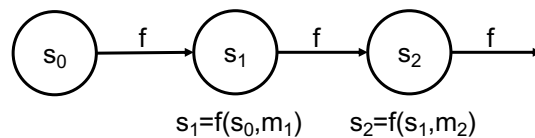
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# Stateful port objects (stateful agents)



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## Stateful port objects (Section 5.2)



- A stateful port object, also called stateful agent, has an internal memory  $s_i$  called its **state**
- The state is updated with each message received, which gives a **state transition function**:  
 $F: \text{State} \times \text{Msg} \mapsto \text{State}$

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## Creating stateful port objects



- We define a generic function for stateful port objects:

```
fun {NewPortObject Init F}  
  proc {Loop S State}  
    case S of M|T then {Loop T {F State M}} end  
  end  
  P  
in  
  thread S in P={NewPort S} {Loop S Init} end  
  P  
end
```

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## Structure of Loop



- Does the Loop function ring a bell?

```
proc {Loop S State}  
  case S of M|T then {Loop T {F State M}} end  
end
```

- Loop starts from an initial state
- Loop successively applies F to the previous state and a message
- The function F is a binary operation
- ...

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## Structure of Loop



- Does the Loop function ring a bell?

```
proc {Loop S State}  
  case S of M|T then {Loop T {F State M}} end  
end
```

- Loop starts from an initial state
- Loop successively applies F to the previous state and a message
- The function F is a binary operation
- Of course! It is a Fold operation!

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## FoldL operation



- FoldL is an important higher-order operation:

```
fun {FoldL S F U}  
  case S  
  of nil then U  
  [] H|T then {FoldL T F {F U H}}  
  end  
end
```

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## Fold is the heart of the agent



- We replace:  
`thread S in P={NewPort S} {Loop S Init} end`
- by:  
`thread S in P={NewPort S} {FoldL S F Init} end`
- Oops! There is a small bug...

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## Updated NewPortObject



- We define a generic function for stateful port objects:  

```
fun {NewPortObject Init F}  
  P Out  
in  
  thread S in P={NewPort S} Out={FoldL S F Init} end  
  P  
end
```
- Out is the final state when the agent terminates
  - It never terminates here, but in another definition it might

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## Example Cell agent



- This agent behaves like a cell!

```
fun {CellProcess S M}  
  case M  
  of assign(New) then New  
  [] access(Old) then Old=S S  
  end  
end
```

- Cells and ports are equivalent in expressiveness
  - Even though they look very different

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## Uniform interfaces (1)



- We can create and use a cell agent:

```
declare Cell  
Cell={NewPortObject CellProcess 0}  
{Send Cell assign(1)}  
local X in {Send Cell access(X)} {Browse X} end
```

- We want to have the same interface as objects:

```
{Cell assign(1)}  
local X in {Cell access(X)} {Browse X} end
```

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## Uniform interfaces (2)



- We change the output to be a procedure:

```
fun {NewPortObject Init F}  
  P Out  
in  
  thread S in P={NewPort S} Out={FoldL S F Init} end  
  proc {$ M} {Send P M} end  
end
```

- P is hidden inside the procedure by lexical scoping
- This makes it easier to use port objects or standard objects as we saw before

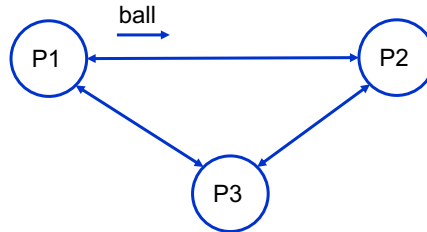
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## Play ball example



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## Play ball example



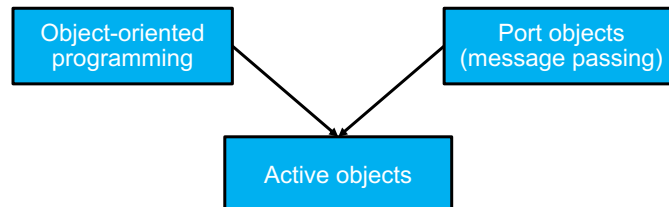
- This is a simple multi-agent program using stateful port objects
  - Three players stand in a circle. There is one ball. A player who receives the ball will send it to one of the other two, chosen randomly.
  - Each player counts the number of times it has received the ball, and it responds to a query asking for this count
- See the live lecture for the code!

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## Active objects

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## Active objects (Section 7.8)



- An active object is a port object whose behavior is defined by a class
- Active objects combine the abilities of object-oriented programming (including polymorphism and inheritance) and message-passing concurrency
- To explain active objects, we refresh your memory on object-oriented programming and we introduce classes in Oz

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## Classes and objects in Oz



- We saw objects in the course
- We now complete this explanation by introducing classes and their Oz syntax

```
class Counter
  attr i
  meth init(X)
    i := X
  end
  meth inc(X)
    i := @i + X
  end
  meth get(X)
    X=@i
  end
end
```

- Create an object:

```
Ctr={New Counter init(0)}
```

- Call the object:

```
{Ctr inc(10)}
{Ctr inc(5)}
local X in
  {Ctr get(X)}
  {Browse X}
end
```

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## Defining active objects



- Active objects are defined by combining classes and port objects
- We use the uniform interface to make them look like standard Oz objects

```
fun {NewActive Class Init}
  Obj={New Class Init}
  P
in
  thread S in
    {NewPort S P}
    for M in S do {Obj M} end
  end
  proc {$ M} {Send P M} end
end
```

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## Passive objects and active objects

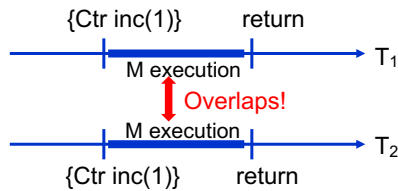


- We make a distinction between passive objects and active objects
- Standard objects in Oz (and many other languages, such as Java and Python) are now called **passive objects**
  - This is because they execute in the thread of their caller; they do not have their own thread
- This is in contrast to **active objects**, which have their own thread
- Let us compare passive and active objects!

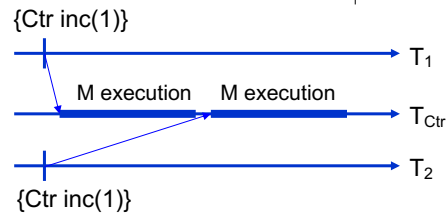
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## Concurrency comparison



- Passive objects cannot be safely called from more than one thread
- The method executions can overlap, which leads to concurrency bugs



- Active objects are completely safe when called from more than one thread
- The method executions are executed sequentially in the active object's own thread

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## Passive objects are not concurrency-safe!

- The following code is buggy:

```

Ctr={New Counter init(0)}
thread {Ctr inc(1)} end
thread {Ctr inc(1)} end
local X in
  {Ctr get(X)}
  {Browse X}
end
    
```

- This can display 1! Why?
  - Look at the instruction `i := @i + 1`
  - If the scheduler puts T1 to sleep after `@i` and before `i:=`, executes T2 fully, and then resumes T1

- The following code is correct:

```

Ctr={NewActive Counter init(0)}
thread {Ctr inc(1)} end
thread {Ctr inc(1)} end
local X in
  {Ctr get(X)}
  {Browse X}
end
    
```

- This will always display 2
  - Because the two methods are executed sequentially by Ctr's thread

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# Message protocols



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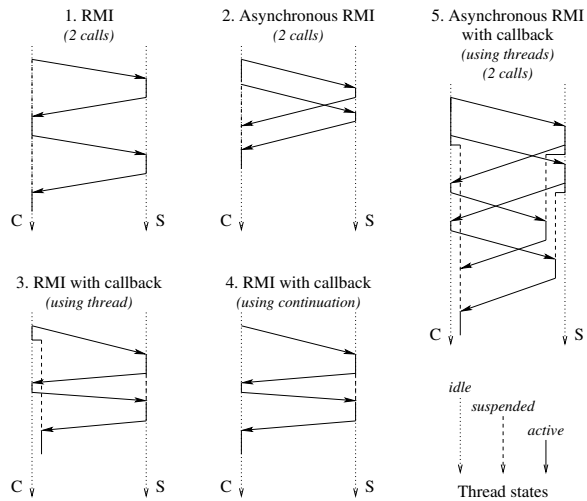
## Message protocols (1)



- A message protocol is a sequence of messages between two or more parties that can be understood at a higher level of abstraction than individual messages
- Using port objects, let us investigate some important message protocols
- We will see the protocols using examples that are coded live
  - Explained in Section 5.3 of the course textbook

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## Message protocols (2)



- We start with a simple RMI
- We then make it asynchronous and add callbacks
- The most complicated protocol is asynchronous RMI with callback

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## Memory management and garbage collection



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## Memory management



- We give another example of using the semantics to understand program execution
  - We will explain the concept of **memory management** using the abstract machine
  - Memory management is important for all paradigms
- Managing program memory during execution
  - We have already explained the advantages of **last call optimization** using the abstract machine
  - Now we will explain automatic memory management, which is also known as **garbage collection**

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## Example of memory management



- Consider the following simple program:

```
proc {Loop10 I}  
  if I==10 then skip  
    {Browse I}  
    {Loop10 I+1}  
  end  
end
```

- Calling {Loop10 0} displays integers 0 up to 9

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## Execution of {Loop10 0} (1)

- We show part of the execution states:
 
$$\begin{aligned}
 & \langle [\{ \text{Loop10 0} \}, E_0], \sigma \rangle \rightarrow \\
 & \langle [\{ \text{Browse l}, \{ l \mapsto i_0 \} \}, \{ \text{Loop10 l+1}, \{ l \mapsto i_0 \} \}], \sigma \cup \{ i_0 = 0 \} \rangle \rightarrow \\
 & \langle [\{ \text{Loop10 l+1}, \{ l \mapsto i_0 \} \}], \sigma \cup \{ i_0 = 0 \} \rangle \rightarrow \\
 & \langle [\{ \text{Browse l}, \{ l \mapsto i_1 \} \}, \{ \text{Loop10 l+1}, \{ l \mapsto i_1 \} \}], \sigma \cup \{ i_0 = 0, i_1 = 1 \} \rangle \rightarrow \\
 & \langle [\{ \text{Loop10 l+1}, \{ l \mapsto i_1 \} \}], \sigma \cup \{ i_0 = 0, i_1 = 0 \} \rangle \rightarrow \\
 & \dots \\
 & \langle [\{ \text{Browse l}, \{ l \mapsto i_9 \} \}, \{ \text{Loop10 l+1}, \{ l \mapsto i_9 \} \}], \sigma \cup \{ i_0 = 0, i_1 = 1, \dots, i_9 = 9 \} \rangle \rightarrow \\
 & \dots
 \end{aligned}$$
- You can observe two things:
  - The **stack size is constant** (last call optimization)
  - The **memory size keeps growing**
    - But most of the variables are only used briefly and then no longer needed!
  - We will see how to remove the unneeded variables

$\{i_0, \dots, i_9\}$  not needed!  
Only  $i_1$  is needed (from stack)

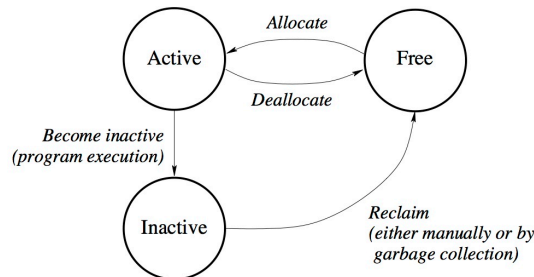
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## Data representation in memory

- Programs execute in main memory, which consists of a **set of memory words**
  - In today's personal computers, a memory word has a 64-bit size (in older computers they have 32-bit size)
  - Memory words are used to represent the semantic stack and the memory (variables and cells)
- When the operating system starts a process, it gives the process an **initial set of memory words** for its execution
  - This set can be increased or reduced in size by system calls
  - During program execution, the set of words is managed by the process, i.e., by the executing program

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## Life cycle of a memory word



- A memory word can have three states: **active**, **inactive**, and **free**
- When execution starts, all words are in the free pool
- When the program needs a word, it allocates one from the free pool
- It may happen that a program no longer needs a word:
  - If it **knows** that it no longer needs it, it deallocates it (puts it back on the free pool)
  - If it **does not know**, then the word becomes inactive (a kind of limbo state!)

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## When reclaiming goes wrong



- Inactive memory blocks must eventually be put back in the free pool ("reclaimed")
- Two kinds of problems can occur if this is done wrong:
  - **Dangling reference**: when a word is reclaimed even though it is still reachable. The system thinks the word is inactive, but it is still active.
  - **Memory leak**: when a word is never reclaimed even though it is not reachable. Too many memory leaks can cause the process to crash or exhaust the computer's resources.
- Reclaiming can be done manually (by the programmer) or by an algorithm (garbage collection)
  - **Manual reclaiming** is quite tricky and not recommended!
  - **Garbage collection** is much more reliable, if the garbage collection algorithm is correctly implemented. We will see how this works!

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## Execution of {Loop10 0} (2)



- We show part of the execution states:  

$$\langle [(\{\text{Loop10 0}\}, E_0)], \sigma \rangle \rightarrow$$

$$\langle [(\{\text{Browse l}\}, \{l \rightarrow i_0\}), (\{\text{Loop10 l+1}\}, \{l \rightarrow i_0\})], \sigma \cup \{i_0=0\} \rangle \rightarrow$$

$$\langle [(\{\text{Loop10 l+1}\}, \{l \rightarrow i_0\})], \sigma \cup \{i_0=0\} \rangle \rightarrow$$

$$\langle [(\{\text{Browse l}\}, \{l \rightarrow i_1\}), (\{\text{Loop10 l+1}\}, \{l \rightarrow i_1\})], \sigma \cup \{i_0=0, i_1=1\} \rangle \rightarrow$$

$$\langle [(\{\text{Loop10 l+1}\}, \{l \rightarrow i_1\})], \sigma \cup \{i_0=0, i_1=0\} \rangle \rightarrow$$

$$\dots$$

$$\langle [(\{\text{Browse l}\}, \{l \rightarrow i_9\}), (\{\text{Loop10 l+1}\}, \{l \rightarrow i_9\})], \sigma \cup \{i_0=0, i_1=1, \dots, i_9=9\} \rangle \rightarrow$$

$$\dots$$
- We can observe the life cycle of these words:
  - When the stack shrinks, its words can be immediately deallocated (become free)
  - The memory  $\sigma_1$  never shrinks: we only add new variables
    - The same thing happens to the cell store  $\sigma_2$ : we only add new cells
  - All **unneeded variables and cells become inactive**: can we find out which ones?

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## When is a word inactive?



- A word becomes inactive when it is **unreachable from the stack**
- Consider an example execution state:  

$$\langle [(\{\text{Browse l}\}, \{l \rightarrow i_9\}), (\{\text{Loop10 l+1}\}, \{l \rightarrow i_9\})], \sigma \cup \{i_0=0, i_1=1, \dots, i_9=9\} \rangle$$
- The words used to represent **variables  $i_0$  up to  $i_8$  are inactive**
- Consider another example execution state:  

$$\langle [(\{\text{Browse l}\}, \{l \rightarrow k_1\})], \{k_2=b|k_1, k_1=c|k_0, b=5, c=6, k_0=\text{nil}\} \rangle$$
- The browse refers to list 6|nil stored in memory (variables  $k_1, c, k_0$ )
  - The stack contains  $k_1$ , which refers **indirectly** to  $c$  and  $k_0$ . They are all reachable!
- The words used to represent **variables  $k_2$  and  $b$  are inactive**
- Is there a way to detect the inactive variables and make them free?

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## Finding inactive words



- Program execution is **determined by the stack**
  - All words used to represent variables and cells reachable from the stack (directly or indirectly) are active
- To make words free, we need to find the variables and cells that are **unreachable from the stack**
  - This is not a simple algorithm
  - Technically, the algorithm does transitive closure of the one-step reachability relation
  - We give a formal definition of reachability
- All variables and cells that are reachable are active
  - All the others (unreachable!) are inactive and can be made free

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## Reachability relation

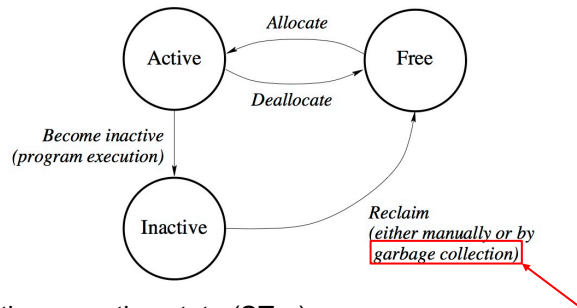


- We define an algorithm to compute the reachability of all variables
  - Given an execution state  $(ST, \sigma)$  where  $ST$  is the stack and  $\sigma = \sigma_1 \cup \sigma_2$  where  $\sigma_1$  is the variable store and  $\sigma_2$  is the cell store
  - Denote by  $V_\sigma$  and  $V_{ST}$  the set of all variables in  $\sigma$  and  $ST$ , respectively
- We first define the **one-step reachability relation** as follows:
  - $x \mapsto y$  : if  $x = r(\dots f; y \dots) \in \sigma_1$  (record in the variable store)
  - $x \mapsto y$  : if  $x; y \in \sigma_2$  (cell in the cell store)
- We say that a variable  $x \in V$  is **reachable** if there exists a path  $x_0 \mapsto x_1 \mapsto x_2 \mapsto \dots \mapsto x_{n-1} \mapsto x$  (of any length  $\geq 0$ ) such that:
  - $x_0 \in V_{ST}$
  - $1 \leq \forall i < n : x_{i-1} \mapsto x_i$  holds
- All reachable variables are represented by active words. All variables that are not reachable are represented by inactive words and can be made free.

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## Garbage collection



- Given the execution state  $(ST, \sigma)$ 
  - A word becomes inactive when it is directly or indirectly unreachable from the stack
  - An executing program does not immediately know when a word becomes inactive
- Garbage collection determines which variables and cells are inactive
  - All words used to represent inactive variables and cells can be made free
  - The algorithm is complex and time-consuming: deciding when to execute the algorithm is a difficult task, because it should not hinder normal execution while at the same time allow efficient memory management

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## Execution of {Loop10 0} (3)

- We show part of the execution states:
 
$$\begin{aligned}
 & ([(\{\text{Loop10 0}\}, E_0)], \sigma) \rightarrow \\
 & ([(\{\text{Browse } l\}, \{l \rightarrow i_0\}), (\{\text{Loop10 } l+1\}, \{l \rightarrow i_0\})], \sigma \cup \{i_0=0\}) \rightarrow \\
 & ([(\{\text{Loop10 } l+1\}, \{l \rightarrow i_0\})], \sigma \cup \{i_0=0\}) \rightarrow \\
 & ([(\{\text{Browse } l\}, \{l \rightarrow i_1\}), (\{\text{Loop10 } l+1\}, \{l \rightarrow i_1\})], \sigma \cup \{i_0=0, i_1=1\}) \rightarrow \\
 & ([(\{\text{Loop10 } l+1\}, \{l \rightarrow i_1\})], \sigma \cup \{i_0=0, i_1=0\}) \rightarrow \\
 & \dots \\
 & ([(\{\text{Browse } l\}, \{l \rightarrow i_9\}), (\{\text{Loop10 } l+1\}, \{l \rightarrow i_9\})], \sigma \cup \{i_0=0, i_1=1, \dots, i_9=9\}) \\
 & \xrightarrow{\text{GC}} \\
 & ([(\{\text{Browse } l\}, \{l \rightarrow i_9\}), (\{\text{Loop10 } l+1\}, \{l \rightarrow i_9\})], \sigma \cup \{i_9=9\})
 \end{aligned}$$
- Let us run garbage collection on the final execution state
  - The garbage collection algorithm does  $(ST, \sigma) \rightarrow_{GC} (ST', \sigma')$
  - Garbage collection removes variables  $\{i_0, \dots, i_8\}$  and their bindings
  - Garbage collection has no influence on program execution: the program will give the same results with or without garbage collection.

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## Garbage collection today



- Many modern programming languages do garbage collection
  - Java, Python, Erlang, Oz, Haskell, Scheme, ...
- A few low-level languages that allow direct access to the processor do not do garbage collection
  - Assembly language, C, C++
  - For some low-level tasks, such as writing device drivers, it is important to do only manual memory management
  - Even so, there exist “conservative GC” algorithms for C and C++

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## Active memory versus memory consumption



Garbage collection

- **Active memory** is how many words the program needs at any time
  - An **in-memory database** has a large active memory (= the size of the database) but a small memory consumption (= little memory is needed to calculate the result of a query)
- **Memory consumption** is the number of words allocated per time unit
  - A **simulation of molecules moving in a box** has a large memory consumption (= each particle position is recalculated at every time step according to a complex computation that needs much temporary data) but a small active memory (= little memory is needed to store positions and velocities of all particles)

Intuition: Your **active size** is how much you weigh (in kg); your **food consumption** is how much you eat (in kg/day)

- The food you eat is used by your metabolism but only a small part (or none) becomes part of your body! Even if you eat 2 kg/day you won't weigh 200 kg after 100 days.

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# Deterministic dataflow with ports



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## The best way (as far as I know)



- Writing general concurrent programs is difficult!
  - But deterministic dataflow is easy (“Concurrency for Dummies”)
  - Can this help with general programs?
- This leads to the best way to write concurrent programs
  - Start with **deterministic dataflow** as the default
  - Add **ports** where they are needed, but as few as possible
  - This differs from message passing (multi-agent actors) in that we don’t use port objects or active objects directly
- We give some example designs using this approach
  - Concurrent composition (static and dynamic)
  - Eliminating sequential dependencies

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## Concurrent composition (fixed number of threads)



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## Concurrent composition (Section 4.4.3)



- The **thread** statement creates a thread that executes independently of the original thread

```
thread <s>1 end
thread <s>2 end
% Two new threads with <s>1 and <s>2, original thread continues
```
- Sometimes the new threads have to be subordinate to the original
  - The original thread waits until the new threads have terminated
- This operation is called **concurrent composition**

```
(<s>1 || <s>2) % Create two threads and wait until both are terminated
<s>3           % Executes only after both are done
```

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## Implementation



- We implement  $\langle s \rangle_1 \parallel \langle s \rangle_2$  using dataflow variables
  - We use the constant **unit** when the value does not matter

```
local X1 X2 in
  thread <s>_1 X1=unit end
  thread <s>_2 X2=unit end
  {Wait X1}
  {Wait X2}
end
```

- It does not matter in which order we wait

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## Higher-order abstraction



- Using higher-order programming, we implement the general form:  
 $\langle s \rangle_1 \parallel \langle s \rangle_2 \parallel \dots \parallel \langle s \rangle_n$
- The instruction  $\langle s \rangle_1$  is written as **proc**  $\{\$ \}$   $\langle s \rangle_1$  **end**
- We define the procedure {Barrier Ps} with list of statements Ps:  

```
proc {Barrier Ps}
  Xs={Map Ps fun { $ P } X in thread {P} X=unit end X end}
in
  for X in Xs do {Wait X} end
end
```
- Note that Barrier can be defined using deterministic dataflow only
  - No ports needed; we will add one port later when we make it dynamic

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## Example

- What does the following code print:

```
{Barrier
  [proc {$} {Delay 500}
    {Barrier
      [proc {$} {Delay 200} {Browse c} end
      proc {$} {Delay 400} {Browse d} end]}
    {Browse e}
  end
  proc {$} {Delay 600} {Browse e} end}}
```

- Remember the precise meaning of {Delay N}: “The current thread is suspended for **at least N milliseconds**”
  - It cannot be “exactly N milliseconds” because the scheduler cannot guarantee when the thread will be chosen to run again

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## Linguistic abstraction

- If your language allows defining new syntax, you can define a **linguistic abstraction** for concurrent composition:

```
conc <s>1 || <s>2 || ... || <s>n end
```

- This translates into:

```
{Barrier [proc {$} <s>1 end
  proc {$} <s>2 end
  ...
  proc {$} <s>n end ]}
```

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## Concurrent composition (variable number of threads)



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## Dynamic concurrent composition (Section 5.6.3)



- Concurrent composition (barrier synchronization) requires that the number of threads be known in advance
- What can we do when the number of threads is not known?
  - Assume we do a computation that can **create new threads dynamically**
  - We need to synchronize on the termination of all the created threads
  - This is hard because new threads can themselves create new threads!
    - It is like the thread statement: in **thread** `<s>` **end**, the `<s>` can also create threads
- This abstraction **cannot be written in deterministic dataflow**
  - Because it is nondeterministic: the order of thread creation is not known
  - We will define it using one port!
    - It is an interesting fact that only one port is needed, unlike message passing in which each port object has a port. Here, the abstraction is mostly deterministic dataflow, with just one added port for doing one specific nondeterministic thing.

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## Specifying the abstraction

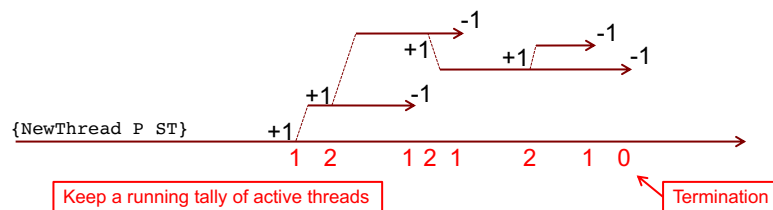
- The main thread waits until all subordinate threads are terminated
- We can define this abstraction as follows:

```
{NewThread proc {$} <s> end SubThread}
{SubThread proc {$} <s> end}
```

- NewThread creates a new computation with <s> in the main thread and outputs the procedure SubThread
  - NewThread terminates only after all subordinate threads are terminated
- SubThread creates a subordinate thread with <s>
  - Both <s> are allowed to call SubThread, and so on recursively, so the tree of threads can be arbitrarily deep

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## Algorithm



- We use a port to count the number of active threads
- Each new thread sends +1 to the port when it is created and -1 to the port when it terminates
  - This is trickier than it seems: send +1 *just before* creation and -1 *inside the thread* just before termination (we need to make a proof)
  - When the running total on the stream is 0 then all threads are terminated

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## Implementation



- The implementation can look something like this:

```
proc {NewThread P SubThread} % SubThread is an output
  S Pt={NewPort S}
in
  proc {SubThread P}
    {Send Pt 1}
    thread
      {P} {Send Pt ~1} % Minus sign in Oz is tilde
    end
  end
  {SubThread P} % Main computation
  {ZeroExit 0 S} % Keep running sum on S and stop when 0
end
```

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## Proof of correctness: this program is subtle!



- What about this implementation?

```
proc {NewThread P SubThread} % SubThread is an output
  S Pt={NewPort S}
in
  proc {SubThread P}
    thread
      {Send Pt 1} {P} {Send Pt ~1}
    end
  end
  {SubThread P} % Main computation
  {ZeroExit 0 S} % Keep running sum on S and stop when 0
end
```

Done inside the new thread

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## Proof of correctness: buggy version!



- What about this implementation? **It is buggy! Do you see why?**

```
proc {NewThread P SubThread}
  S Pt={NewPort S}
in
  proc {SubThread P}
    thread
      {Send Pt 1} {P} {Send Pt ~1}
    end
  end
  {SubThread P} % Main computation
  {ZeroExit 0 S} % Keep running sum on S and stop when 0
end
```

**We need a proof!**

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## Proof of correctness: invariant assertion



- We can prove correctness by using **an invariant assertion**
- Consider the following assertion:
  - **(the sum of the elements on S)  $\geq$  (the number of active threads)**
  - When the sum is zero, it implies the number of active threads is zero
- We use induction on execution steps to show that this is always true
  - **Base case:** True at the call to NewThread since both numbers are zero
  - **Inductive case:** there are four relevant actions (see next slide!)
- The invariant assertion is just a safety property, what about liveness?
  - The first call to SubThread sends 1 to S, so we have to wait until the first created thread terminates

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## Inductive case



- During any execution, there are four possible execution steps that can change the truth of the assertion:
  - **Sending 1** : clearly keeps the assertion true
  - **Starting a thread** : keeps the assertion true since it follows a send of 1, and the assertion was true just before the send
  - **Sending ~1** : we can assume without loss of generality that thread termination occurs just before sending ~1, since the thread no longer does any work after the send
  - **Terminating a thread** : clearly keeps the assertion true
- You see why the {Send Pt 1} must be done **outside** of the new thread!
  - {Send Pt 1} must be done **before** creating the new thread

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## ZeroExit procedure



- The procedure {ZeroExit N S} keeps a running sum of elements from S and exits when the sum equals 0

```
proc {ZeroExit N S}
  case S of X|S2 then
    if N+X==0 then skip
    else {ZeroExit N+X S2} end
  end
end
```

Always read at least one element

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# Eliminating sequential dependencies



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## Eliminating sequential dependencies (Section 5.6.4)



- A sequential program **orders all instructions**
  - This is a sequential dependency, by definition!
- But sometimes these dependencies are useless and may cause the program to block unnecessary
  - Can we get rid of these dependencies?
- The solution is to add threads to remove useless dependencies, but without changing the result
  - In deterministic dataflow, we can add threads wherever we want, if the computation in the thread is purely functional
  - In our example, we will need **one port** to collect the elements computed in each thread: this adds nondeterminism only in one place, so we can easily check that it is ok

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## Example: The Filter function



- The function {Filter L F} takes a list L and a one-argument boolean function F and outputs the list of elements where the function is true:  

```
fun {Filter L F}  
  case L of nil then nil  
  [] X|L2 then  
    if {F X} then X|{Filter L2 F} else {Filter L2 F} end  
  end  
end
```
- This is efficient, but it introduces sequential dependencies! The call:  

```
{Filter [A 5 1 B 4 0 6] fun {$ X} X>2 end}
```

  
blocks right away on A, even though we know that 5, 4, and 6 will eventually be in the output. Waiting for A stops everything!

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## Filter without sequential dependencies



- Let us write a new version of Filter that avoids these dependencies
  - It will construct its output incrementally, as input information arrives
- We can write ConcFilter using two building blocks:
  - **Concurrent composition** (as seen before): {Barrier Ps}
  - **Asynchronous channel** (port with a Close operation)
- ConcFilter removes dependencies but is **nondeterministic**:  

```
{ConcFilter [A 5 1 B 4 0 6] fun {$ X} X>2 end}
```

  - This returns right away with 5|4|6|... and will eliminate 1 and 0
  - But it can return the elements in **any order**, 6|5|4|... for example
- **We have traded off dependencies for nondeterminism**

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## Ports with a Close operation



- We need a port that can be closed (ending the stream with nil)
- We define {NewPortClose S Send Close}
  - S is the port's stream
  - {Send M} sends message M to the port
  - {Close} closes the port, i.e., binds the tail to nil and no more send is allowed
- Definition: (defined with a cell!)

```
proc {NewPortClose S Send Close}
  PC={NewCell S}
in
  proc {Send M} S in {Exchange PC M|S S} end
  proc {Close} nil=@PC end
end
```
- The cell PC is like an object attribute: it allows reading and writing
  - The Exchange operation does both read and write atomically
  - Exchange is needed to make the Send concurrency-safe (see passive objects!)

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## ConcFilter idea



- The original {Filter L F} computes all {F X} in the same thread
- The new {ConcFilter L F} computes **each {F X} in a separate thread**
  - If {F X} returns true, then send X to the port
  - The port's stream is the function's output
- When all threads terminate, the port is closed
  - This makes the stream into a list
  - We use {Barrier Ps} to detect when all threads terminate
- Creating the procedure arguments to Barrier
  - For each X in L, we need to execute **if {F X} then {Send X} end**
  - So we create the procedure **proc {\$} if {F X} then {Send X} end end**

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## Defining ConcFilter



- ConcFilter uses Map to build the arguments to Barrier:

```
proc {ConcFilter L F L2}
  Send Close
in
  {NewPortClose L2 Send Close}
  {Barrier
    {Map L % For each X of the input list, build procedure
      fun {$ X}
        proc {$} if {F X} then {Send X} end end
      end}}
  {Close}
end
```

Procedure input to Barrier

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## Conclusion



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## Conclusion: how to build concurrent programs



- We have seen three good ways to build concurrent programs
- **Deterministic dataflow (including lazy)**: best, but has limitations
  - Cannot express programs that need nondeterminism, like client/server
  - Is widely used in cloud analytics tools (e.g., Apache Flink, Spark)
- **Message passing (multi-agent actor)**: fully general, but harder
  - Stateful agents that communicate with asynchronous messages
  - **Erlang** is a successful industrial example of this approach
- **Deterministic dataflow with ports**: best all-round approach
  - Write most of the program as deterministic dataflow
  - Add ports only where they are needed; usually very few are needed
  - This is a novel approach that will likely appear more in the future

We will see Erlang next week!

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## Introduction to Erlang



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## Introduction to Erlang (Section 5.7)



- The Erlang language was originally developed by Ericsson for telecommunications applications in 1986 (Java was developed in 1991)
  - It is released as OTP (Open Telecom Platform) with a full set of libraries
  - It is supported by Ericsson, the Erlang Ecosystem Foundation, and a large user community ([www.erlang.org](http://www.erlang.org))
- Erlang programs consist of “processes”, which are **port objects** and communicate using **asynchronous FIFO message passing**
  - Erlang processes **share nothing**: all data is copied between them
  - Erlang processes receive messages through a mailbox that is accessed by **pattern matching**. Messages can be **received out of order** if they match.
- Erlang supports building reliable long-lived distributed systems
  - Successful “let it crash” philosophy using failure linking and supervisor trees
  - Ericsson AXD 301 ATM switch with 1.7 million lines of Erlang claims 99.9999999% availability (one may doubt the number of 9’s, but the system is extremely available!)