

```

64     for pos_i in range(len(state.lattice)):
65         for pos_j in range(len(state.lattice)):
66             interaction_energy +=
                -state.J*state.lattice[pos_i,pos_j]*(state.lattice[pos_i,(pos_j+1)%state.N]
                + state.lattice[(pos_i-1)%state.N,pos_j] +
                state.lattice[(pos_i+1)%state.N,pos_j] +
                state.lattice[pos_i,(pos_j-1)%state.N])
67     interaction_energy *= 0.5 # avoid double counting
68
69     magnetisation_energy = -state.H*calculate_magnetisation(state)
70
71     return interaction_energy+magnetisation_energy
72
73
74 # In[ ]:
75
76
77 # Function to normalize data by number of lattice sites
78 def normalize_data(data, N):
79     return data/(N**2)
80
81
82 # In[ ]:
83
84
85 # Metropolis algorithm
86 def Metropolis_algorithm(N_range, J, H, T_range, no_of_sweeps):
87     # arrays to store magnetisation and energy time series
88     M = np.zeros((len(N_range),len(T_range),no_of_sweeps))
89     E = np.zeros((len(N_range),len(T_range),no_of_sweeps))
90     M_normalized = np.zeros((len(N_range),len(T_range),no_of_sweeps))
91     E_normalized = np.zeros((len(N_range),len(T_range),no_of_sweeps))
92     run_time = np.zeros((len(N_range),len(T_range)))
93
94     # Monte Carlo sweeps
95     for N_index in range(len(N_range)):
96         for T_index in range(len(T_range)):
97             state = Ising(N_range[N_index],J,H)
98
99             t0 = time.time()
100            for sweep in range(no_of_sweeps): # run!
101                monte_carlo_sweep(state,T_range[T_index])
102
103                M[N_index,T_index,sweep] = calculate_magnetisation(state)
104                E[N_index,T_index,sweep] = calculate_energy(state)
105                M_normalized[N_index,T_index,sweep] =
                    normalize_data(M[N_index,T_index,sweep],state.N)
106                E_normalized[N_index,T_index,sweep] =
                    normalize_data(E[N_index,T_index,sweep],state.N)
107
108                if sweep%1000 == 0: # output checkpoints
109                    print('N = {0}, T = {1}, sweep =
                        {2}'.format(N_range[N_index],T_range[T_index],sweep))
110                t1 = time.time()
111                run_time[N_index,T_index] = t1-t0
112
113            return M, E, M_normalized, E_normalized, run_time
114
115
116 # In[ ]:
117
118
119 # Function to plot evolution of data over time
120 def plot_time_series(data, N_range, N_index_range, T_range, T_index_range, start_point,
stop_point, xname, yname):
121     for N_index in N_index_range:
122         for T_index in T_index_range:

```