

# **Theory Meets Experiments 2025:**

## **Direct Detection across Dark Matter mass ranges**

### **Wave Dark Matter Experiments**

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(UC Berkeley and LBNL)

# Lecture 2: searches for low-mass axions

- Review + moved from yesterday:
  - dark matter signal
  - dark matter detection regimes
- Low mass motivation and background
- Lumped-element detection
- SRF cavity detection

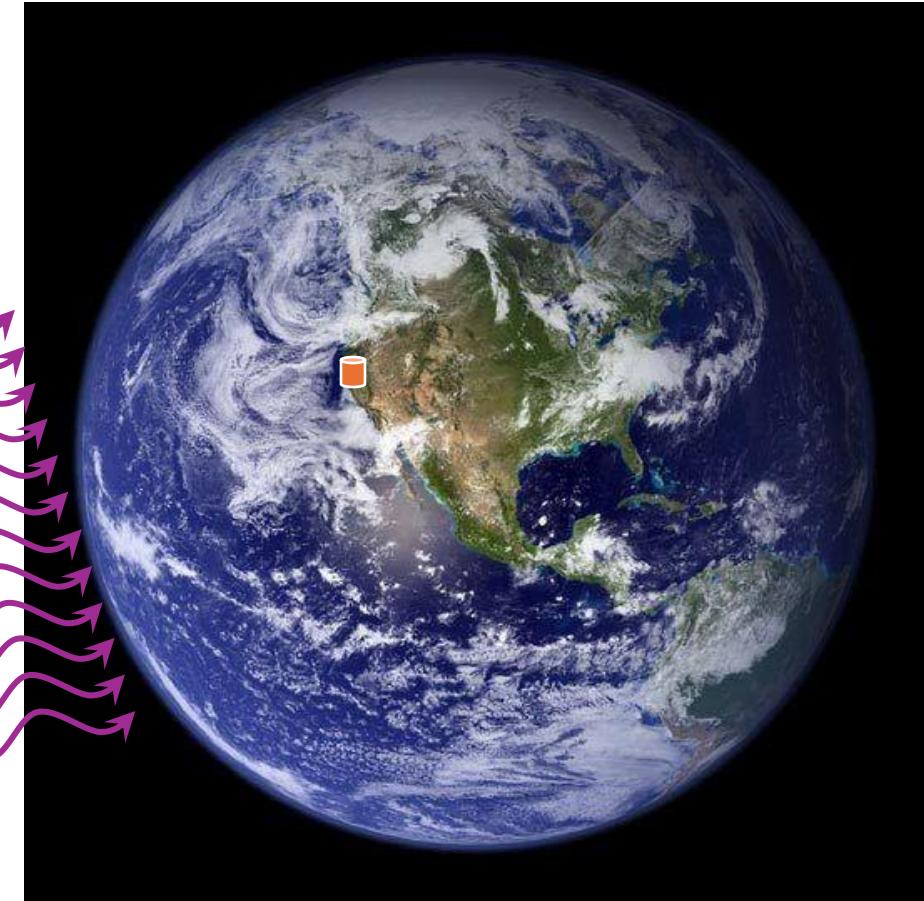
# Axion-photon experiment ingredients

1. Strong magnetic field (axion-to-photon converter)
2. Coupling system (couple photons/EM signal into detector)
3. Very sensitive detector (amplify a tiny signal)

$$\mathbf{J}_{\text{eff}} = g_{a\gamma\gamma} \sqrt{2\rho_{DM}} \cos(m_a t) \mathbf{B}$$

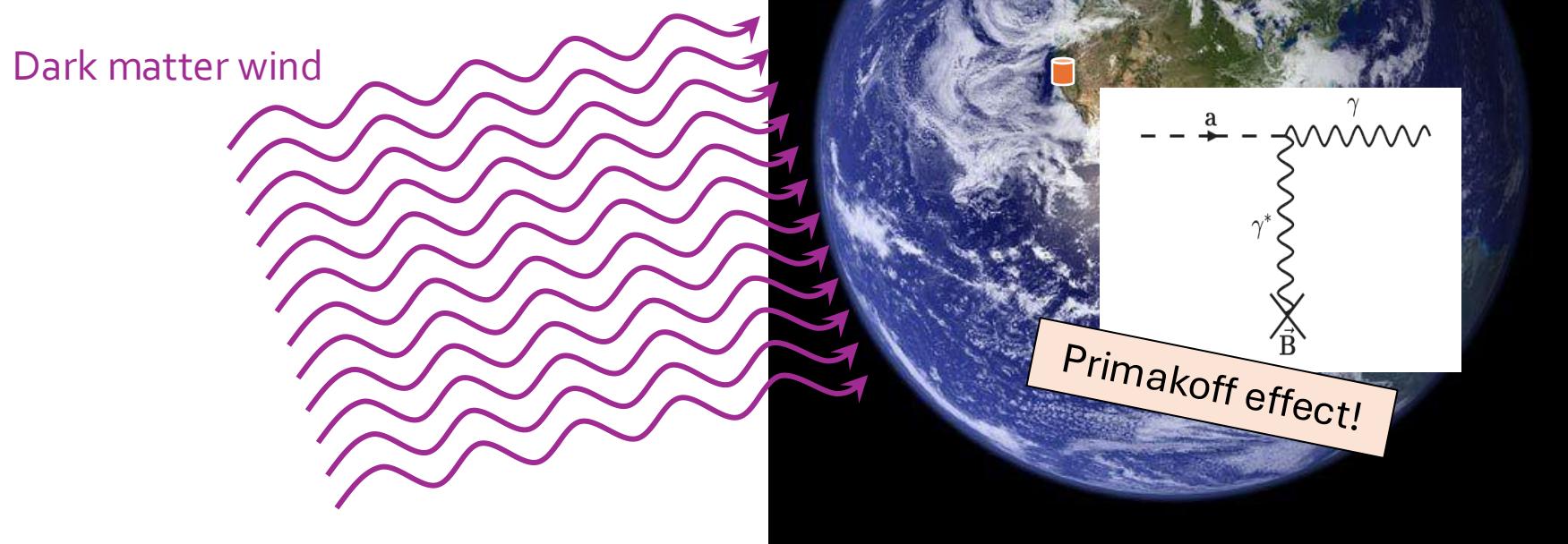
# Sources of axions: dark matter

“Haloscopes”



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# What does the dark matter signal look like?

- Approximately monochromatic sinusoidal signal

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Why only  
“approximately”?

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- Virialized dark matter halo → distribution of velocities

$$\Delta v \sim 10^{-3} \quad \leftarrow 220 \text{ km/s (velocity dispersion)}$$

$$v_{\text{obs}} \sim 10^{-3} \quad \leftarrow 232 \text{ km/s (sun's orbital velocity)}$$

$$v_{\text{DM, max}} = v_{\text{esc}} \quad \leftarrow 550 \text{ km/s}$$

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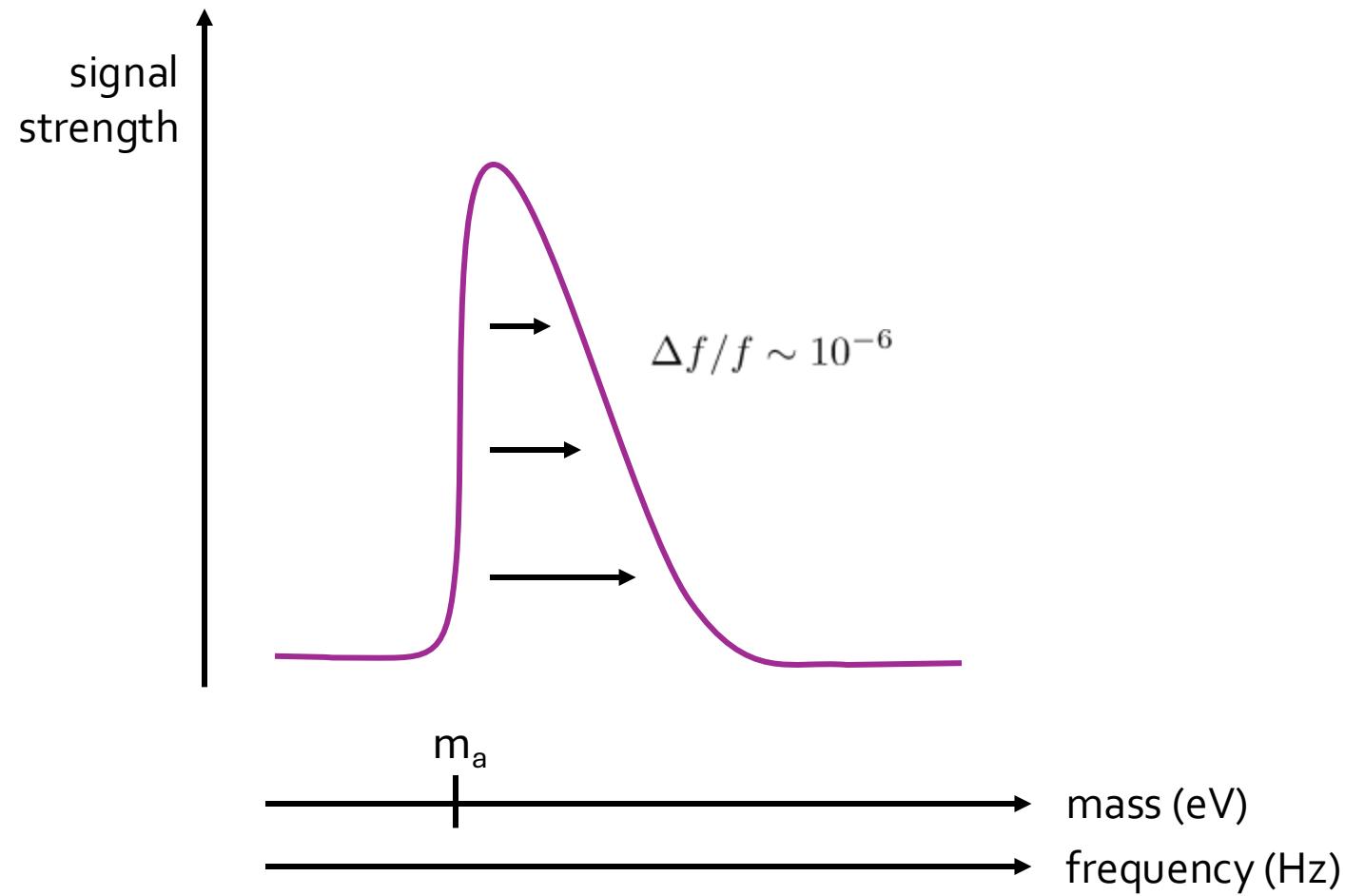


this low dispersion implies the axion field is coherent over:

$$\tau \sim 10^6 \times \frac{2\pi}{m_a}$$

# How do we read out the dark matter signal?

- Take time series
- Fourier transform
- Search in frequency space for persistent signal

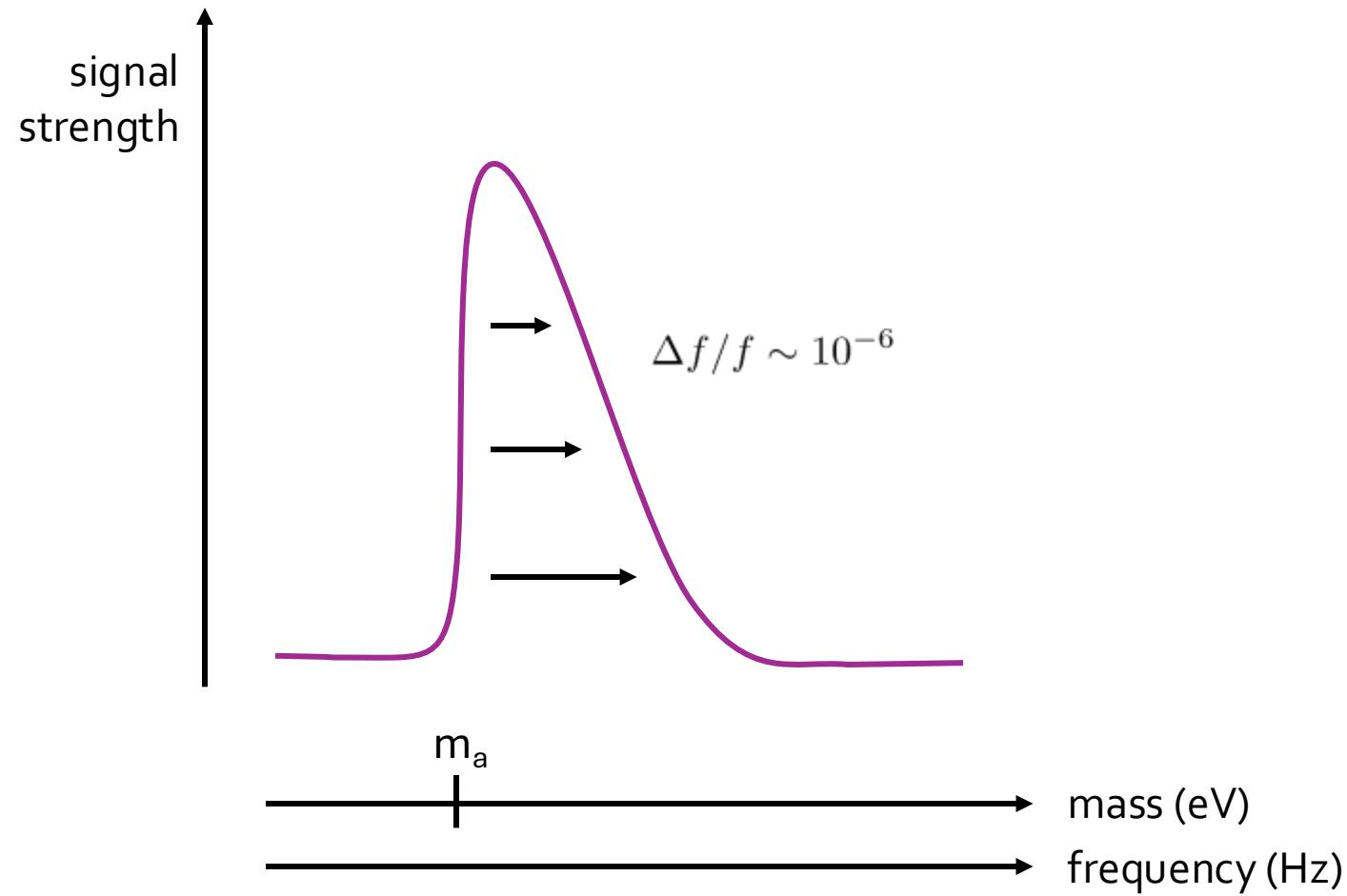


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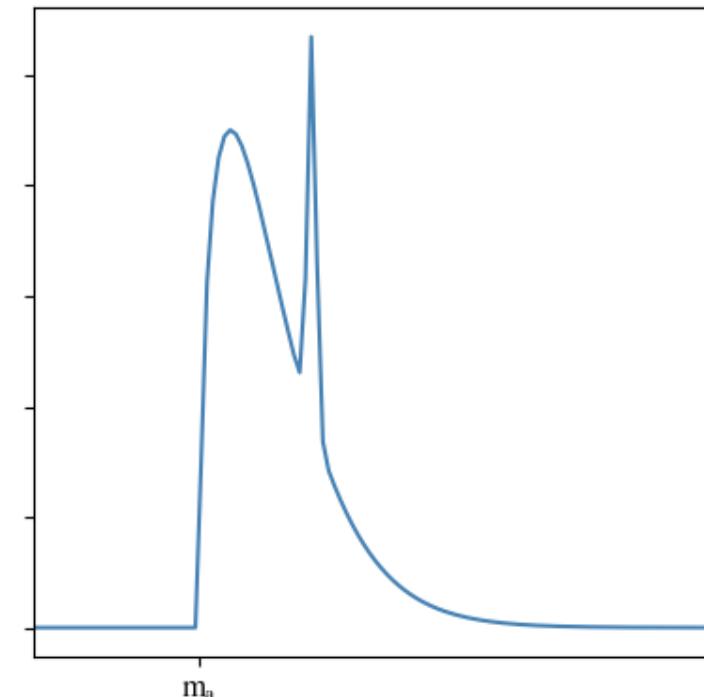
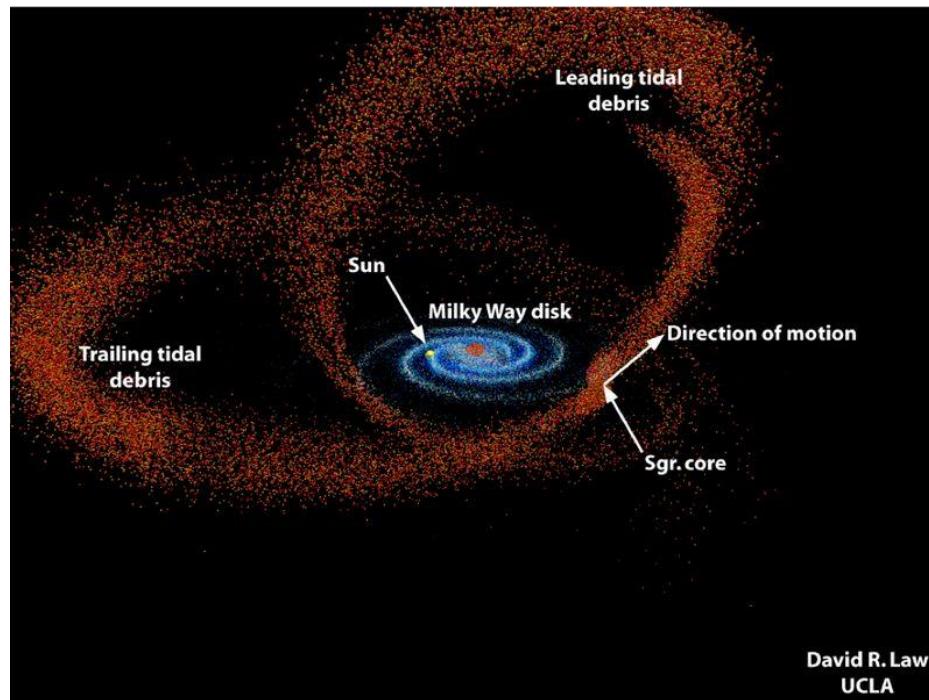


persistence assumption breaks down if axions are clumped



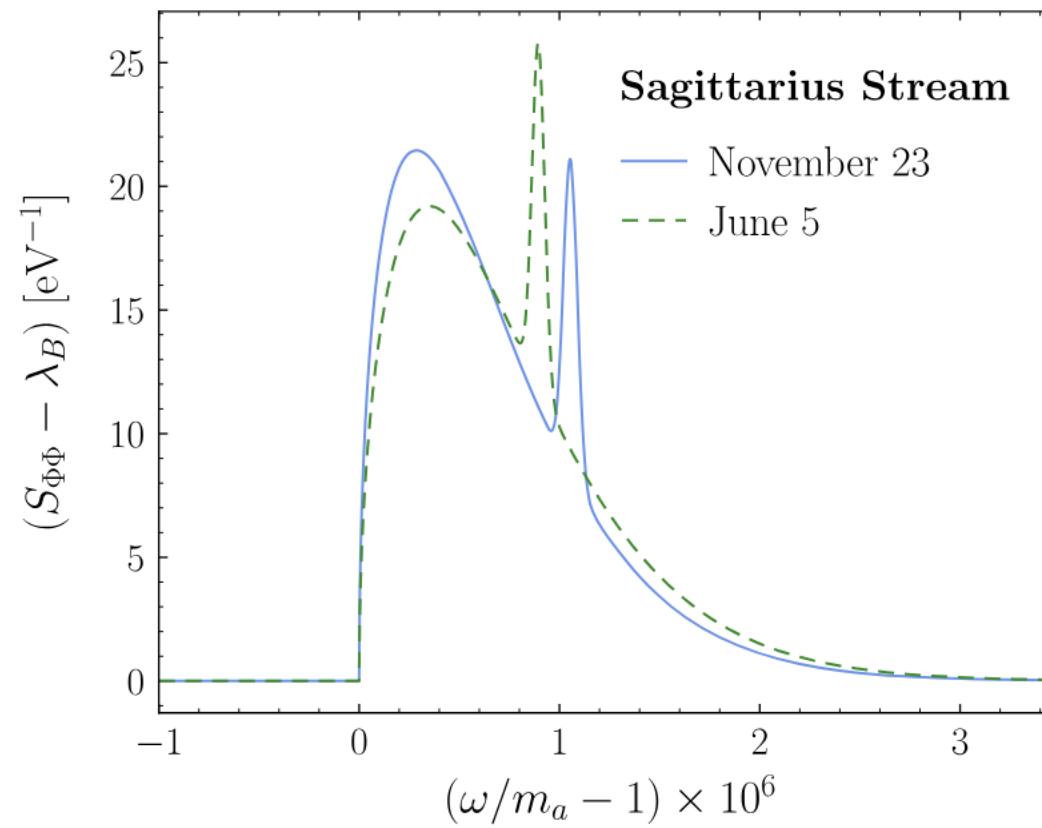
# Variations to the Standard Halo Model

- Dark matter isn't all virialized
- May have a more intense signal from dark matter streams
  - Lower velocity dispersion

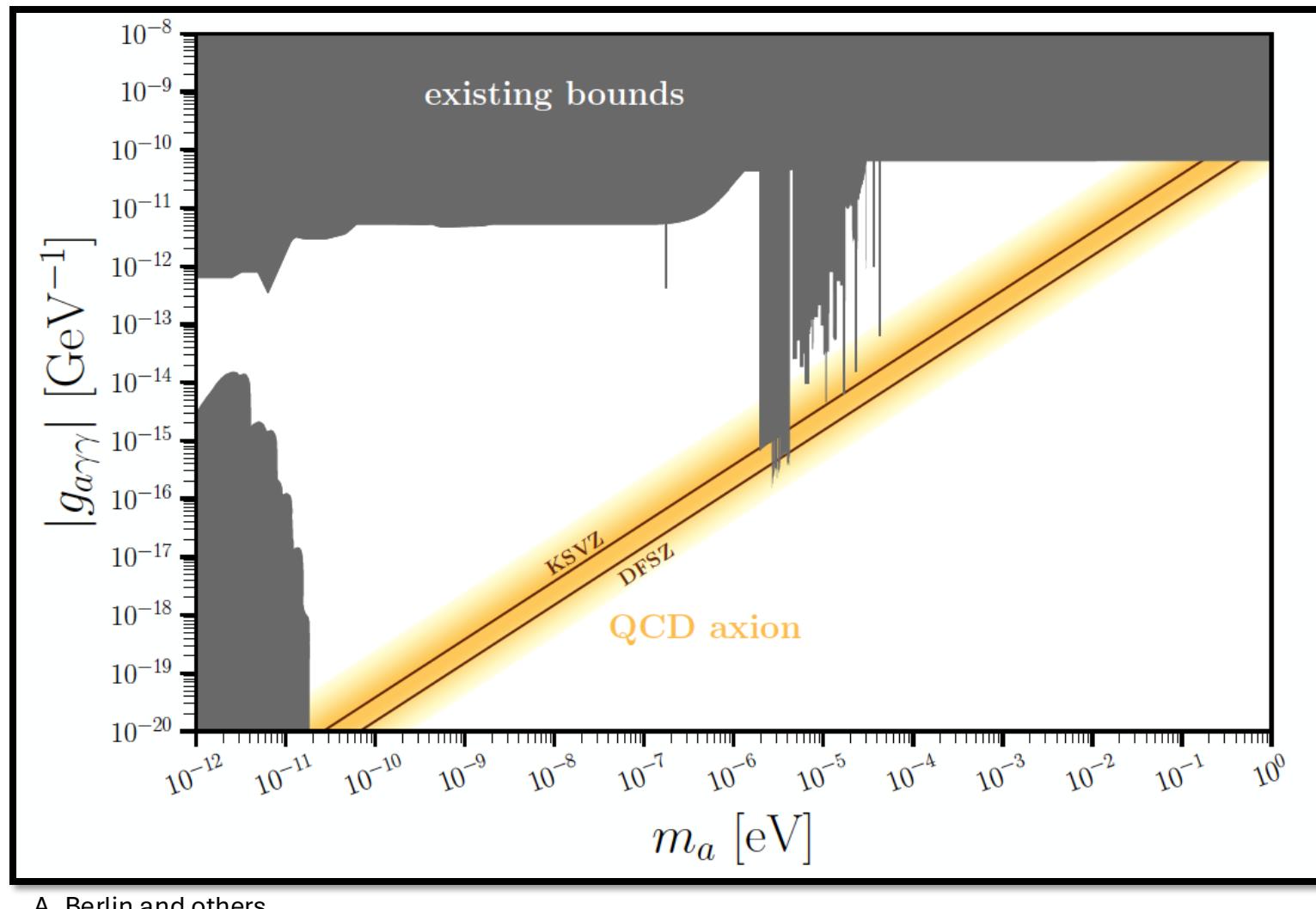


# Time variation of signal

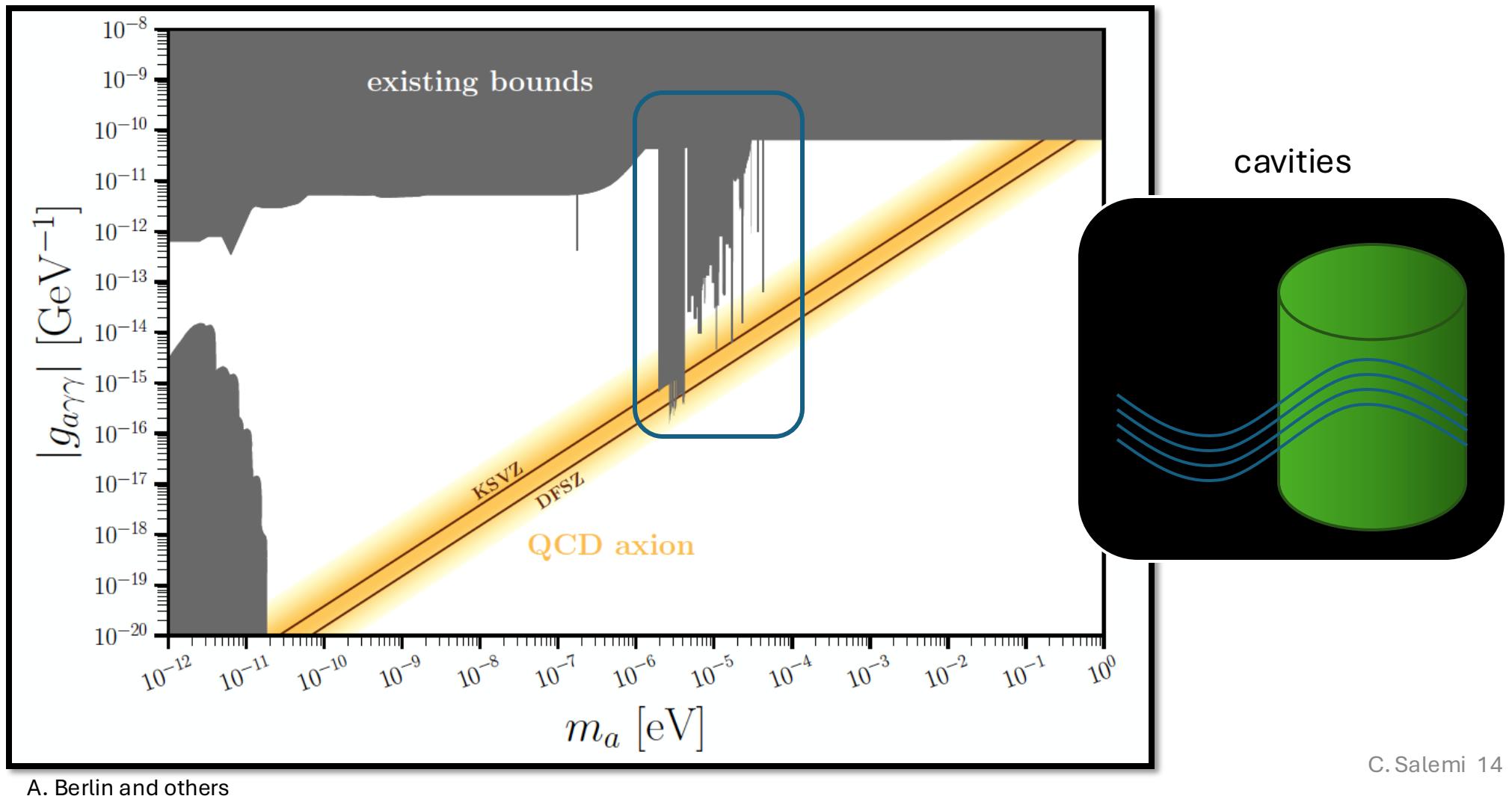
Daily and annual modulation expected



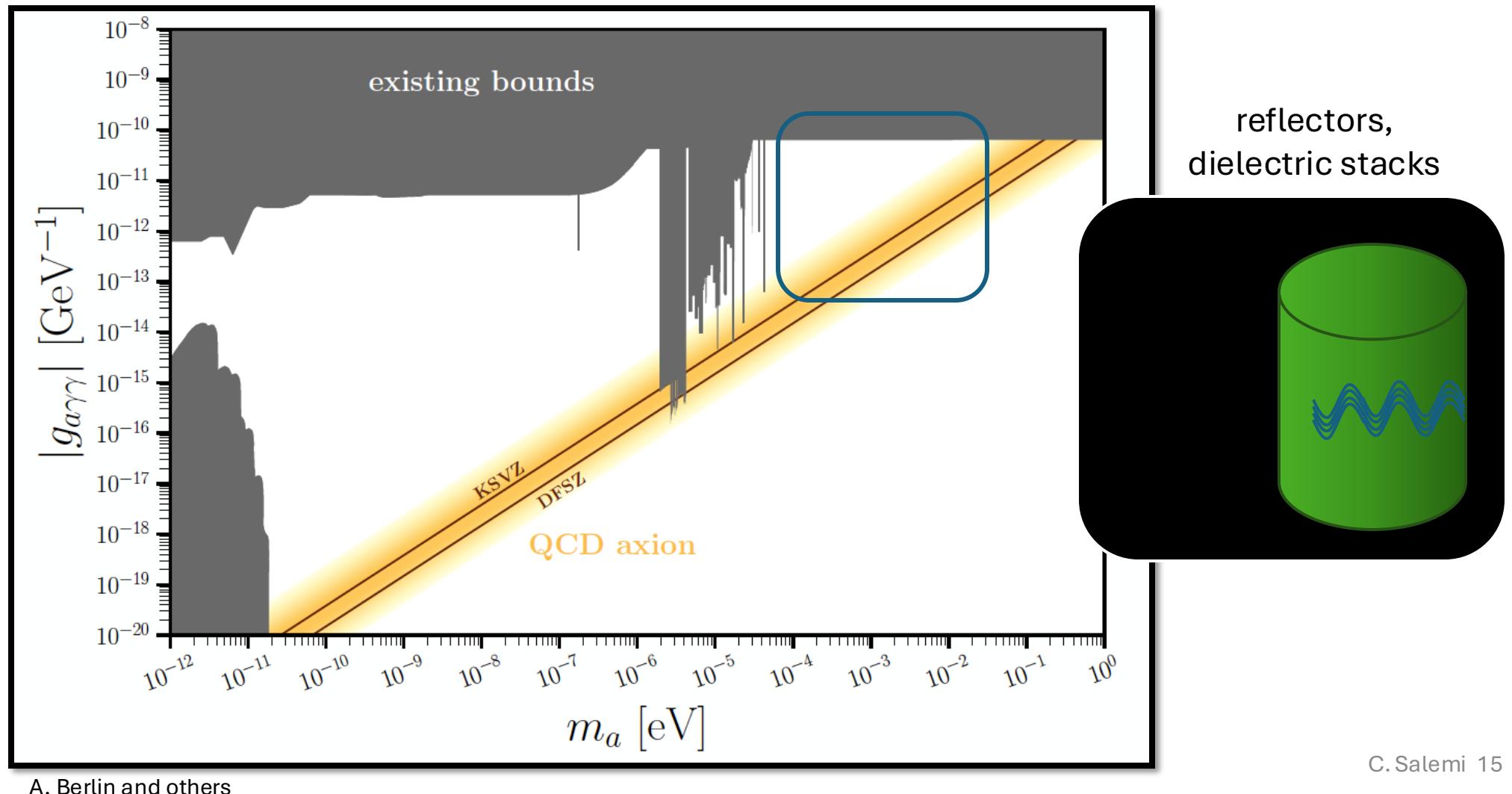
# Different wavy regimes



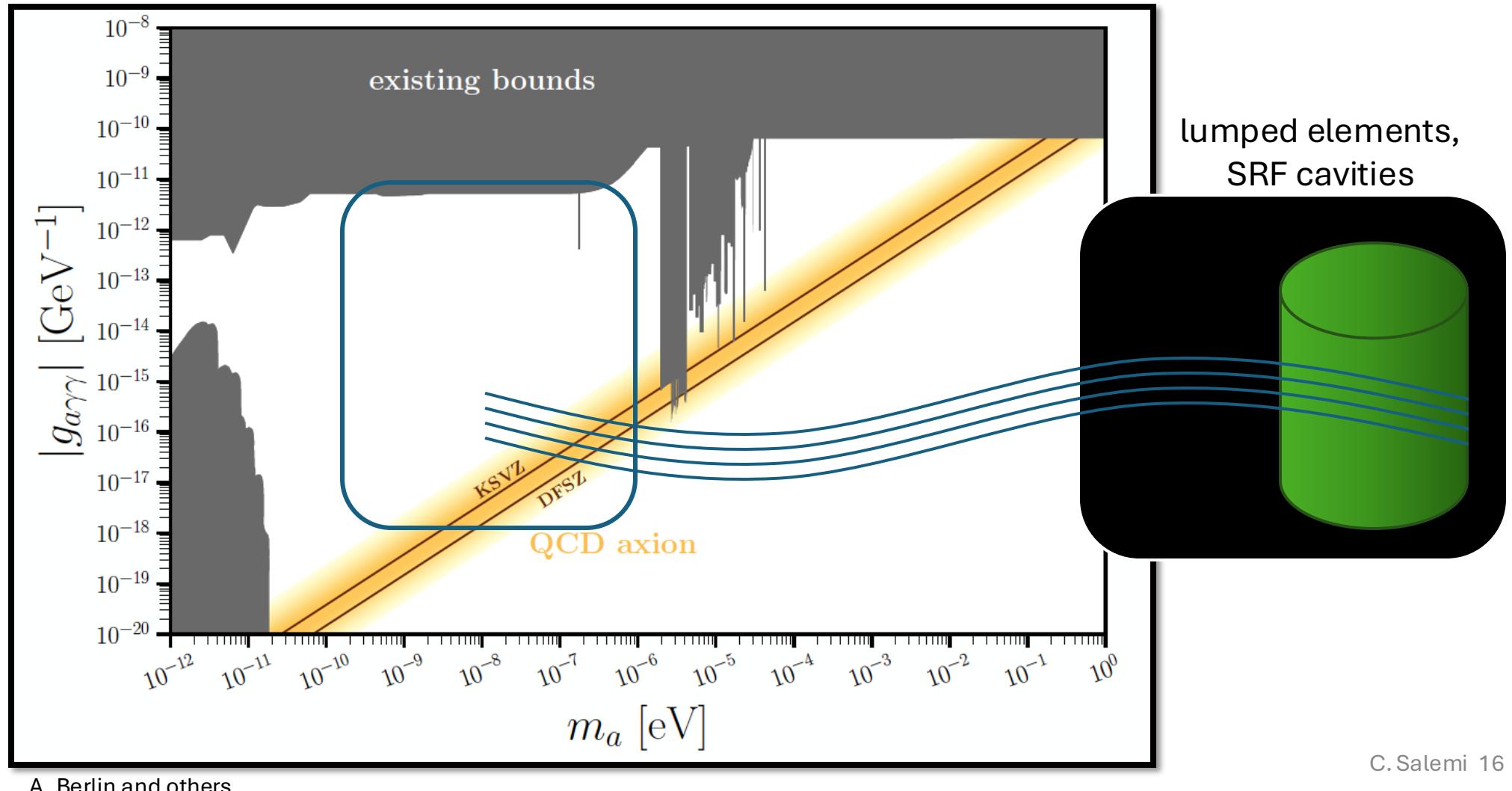
# Different wavy regimes: middle masses



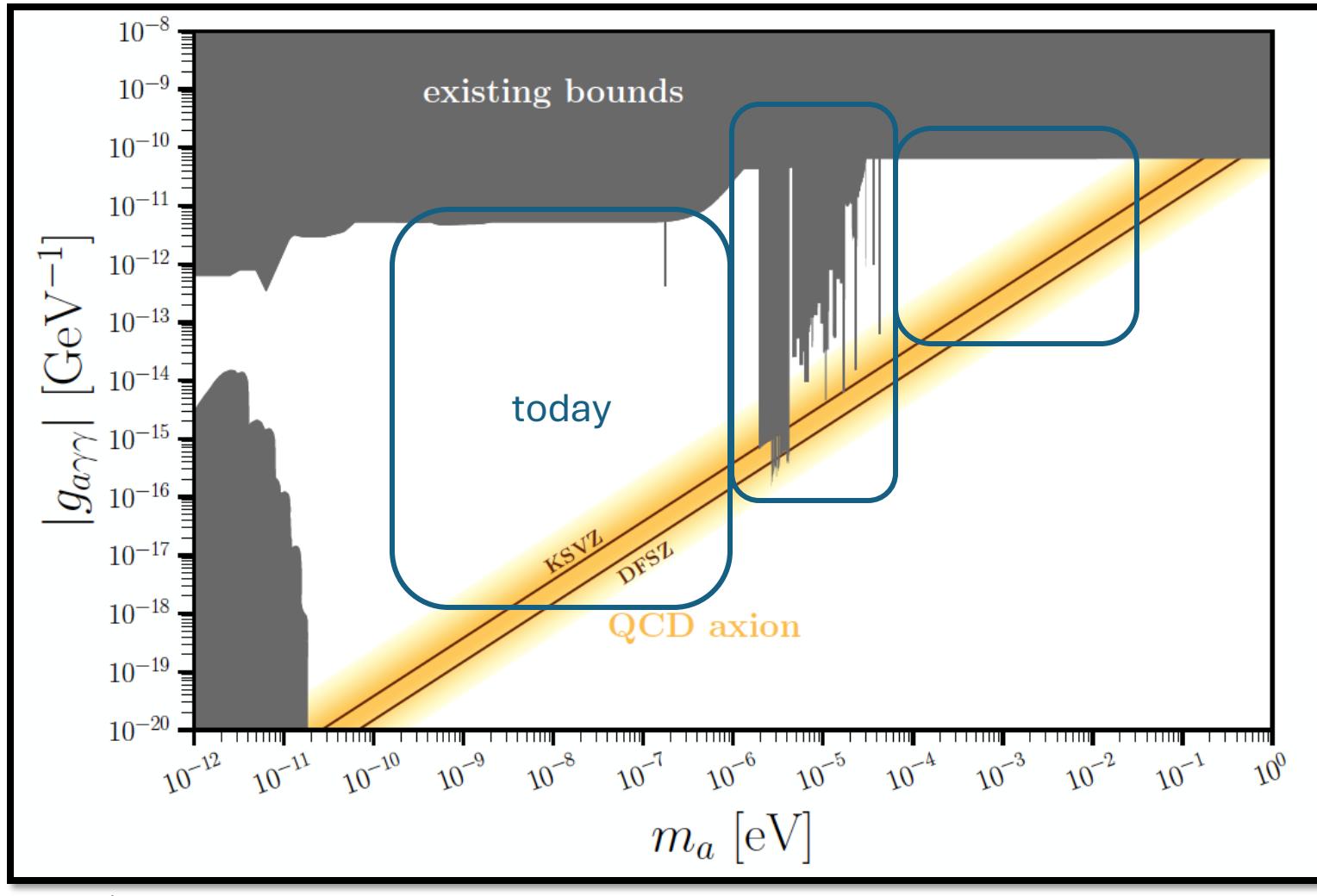
# Different wavy regimes: high masses



# Different wavy regimes: low masses



# You will hear about all of these this week!



# Other considerations for dark matter searches: Broadband vs. resonant

- **Broadband readout:**
  - Read out a wide range of frequencies all at once

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  - Axion signal rings up a resonator in narrow frequency band
  - Huge signal boost by quality factor of resonator

# Other considerations for dark matter searches: Broadband vs. resonant

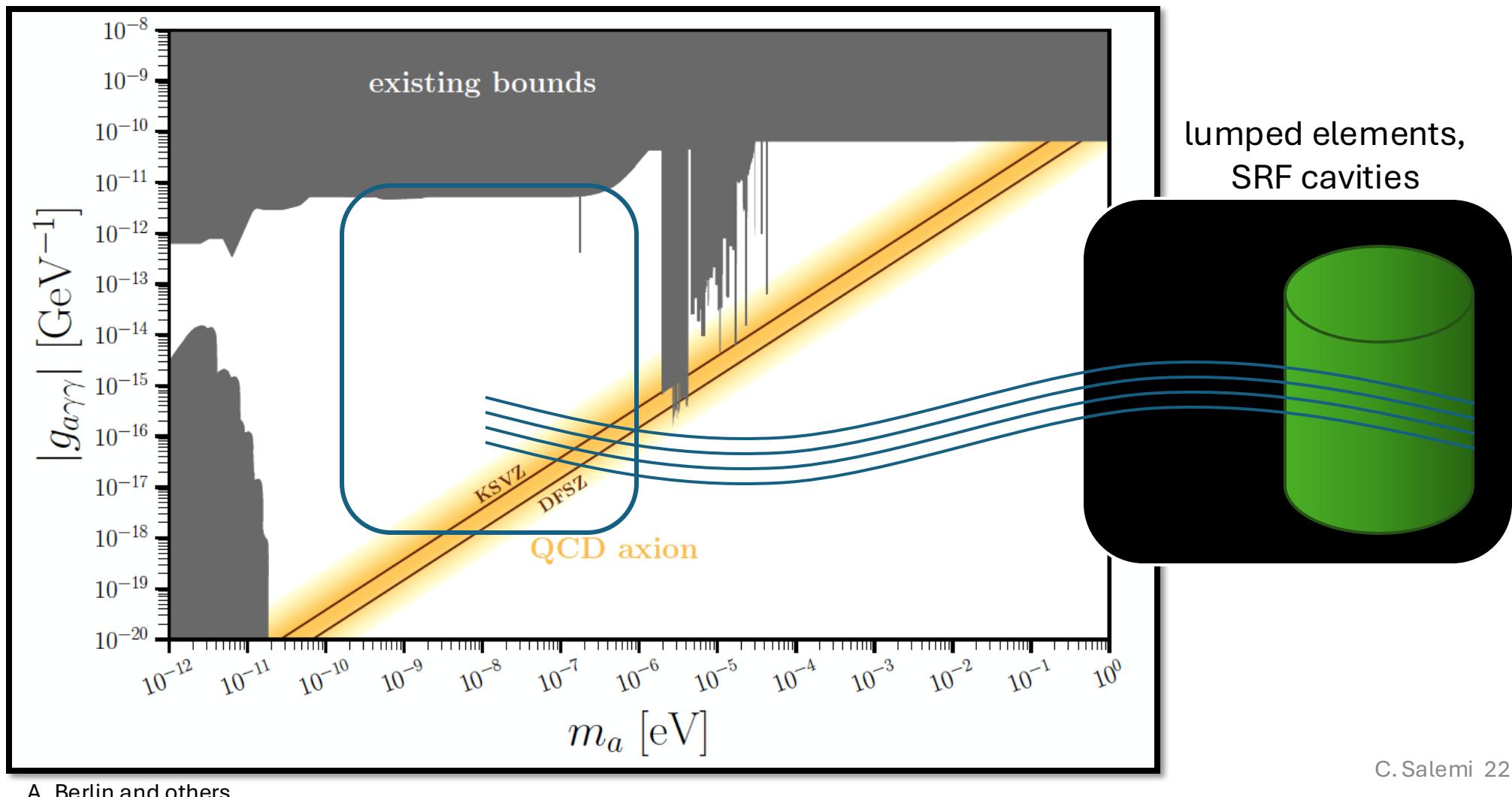
- **Broadband readout:**
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$$Q = 2\pi \frac{\text{energy stored}}{\text{energy dissipated per cycle}}$$
 $\xleftarrow{\text{equivalent}}$ 
$$Q = \frac{f}{\Delta f}$$

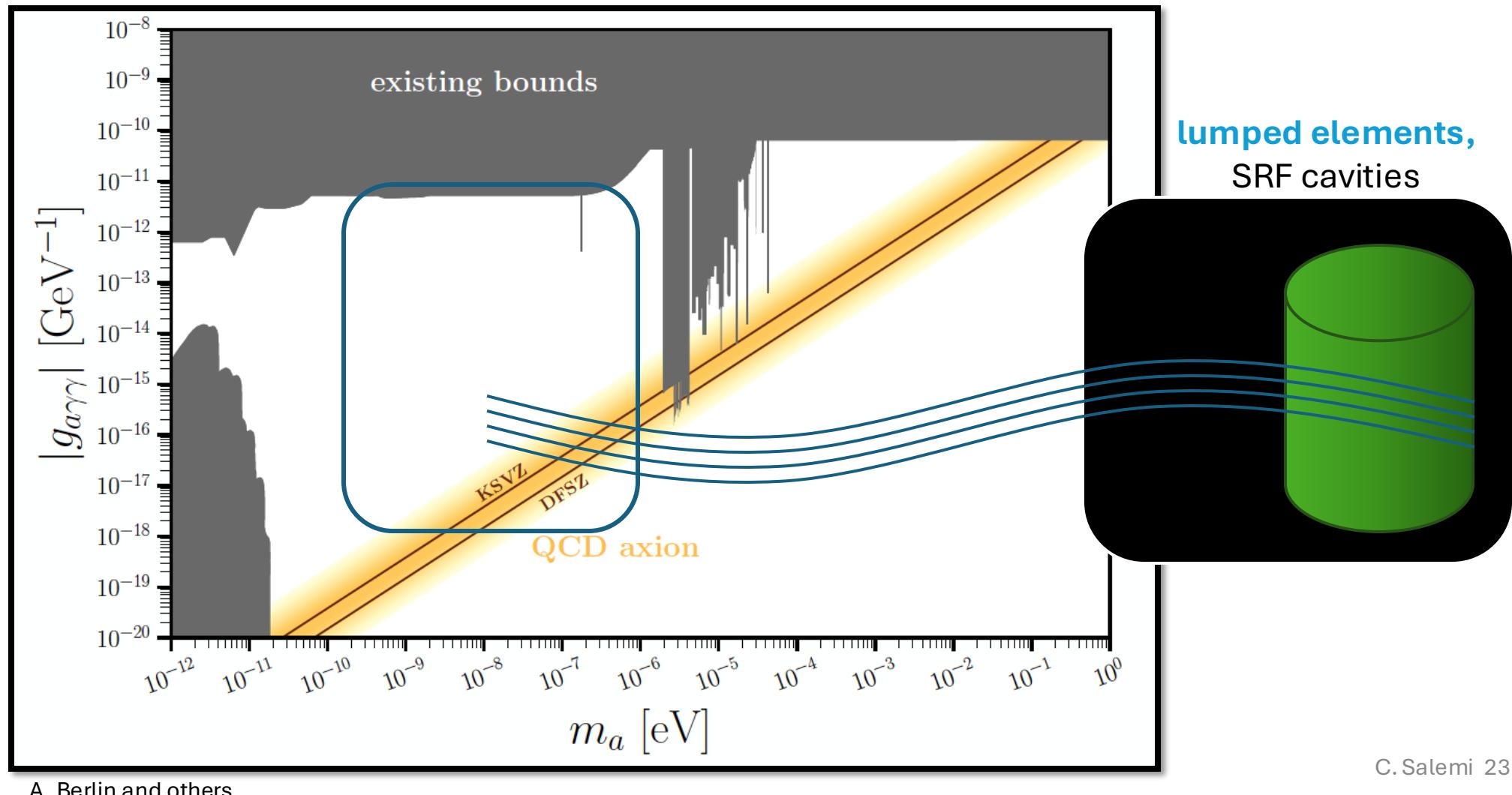
# Which to pick—deep or broad?

- Most experiments opt for resonant
  - QCD axion band is reallllly low in coupling
- A boost for broadband experiments
  - In ALP space, we don't have a strong theoretical prior to go “deep”
  - Tuning is technically challenging
  - Clumpy dark matter is only accessible with a broadband experiment unless you get VERY lucky

# Rest of today: long wavelength detection



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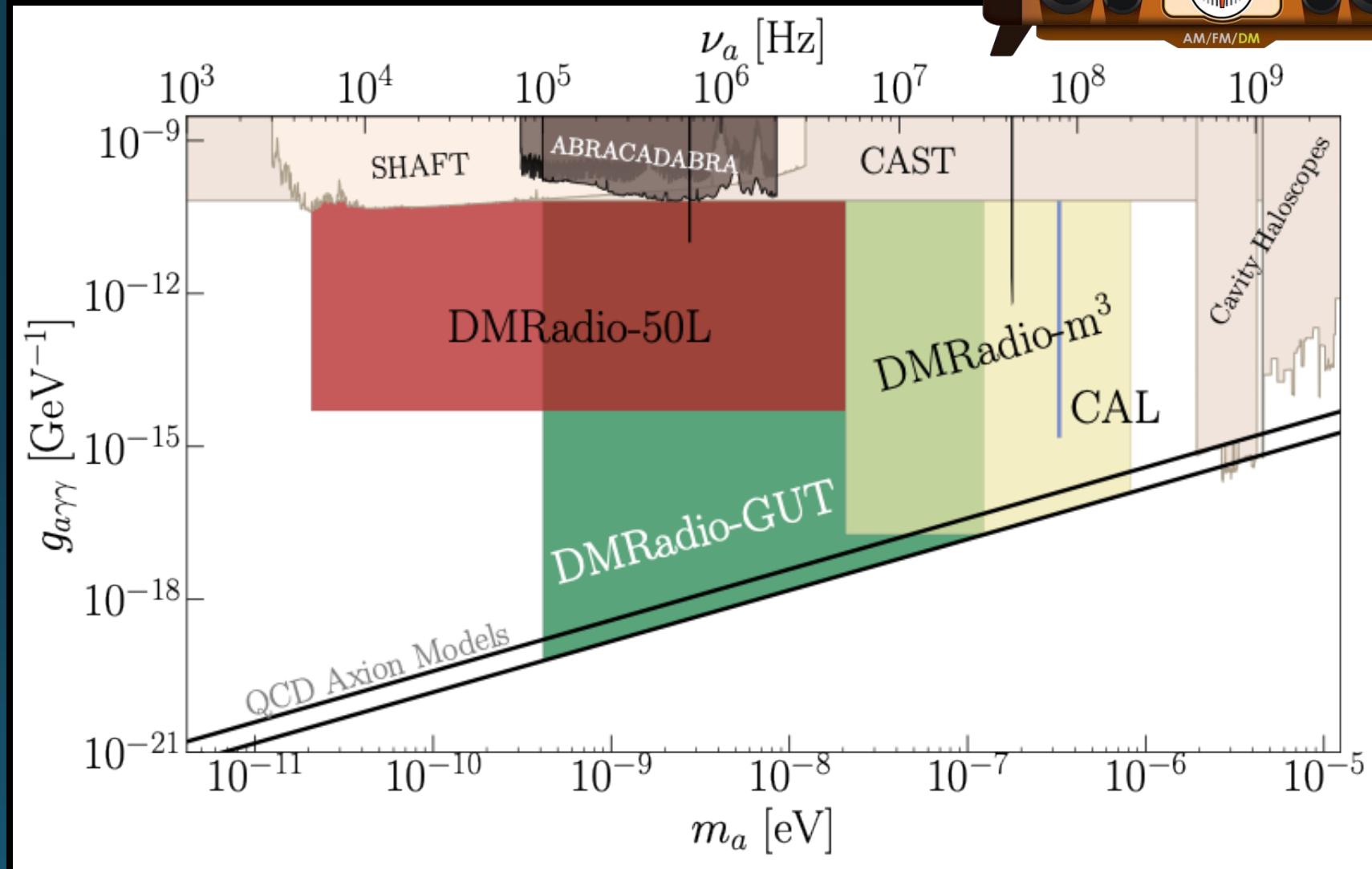


# Low-mass axions are highly motivated

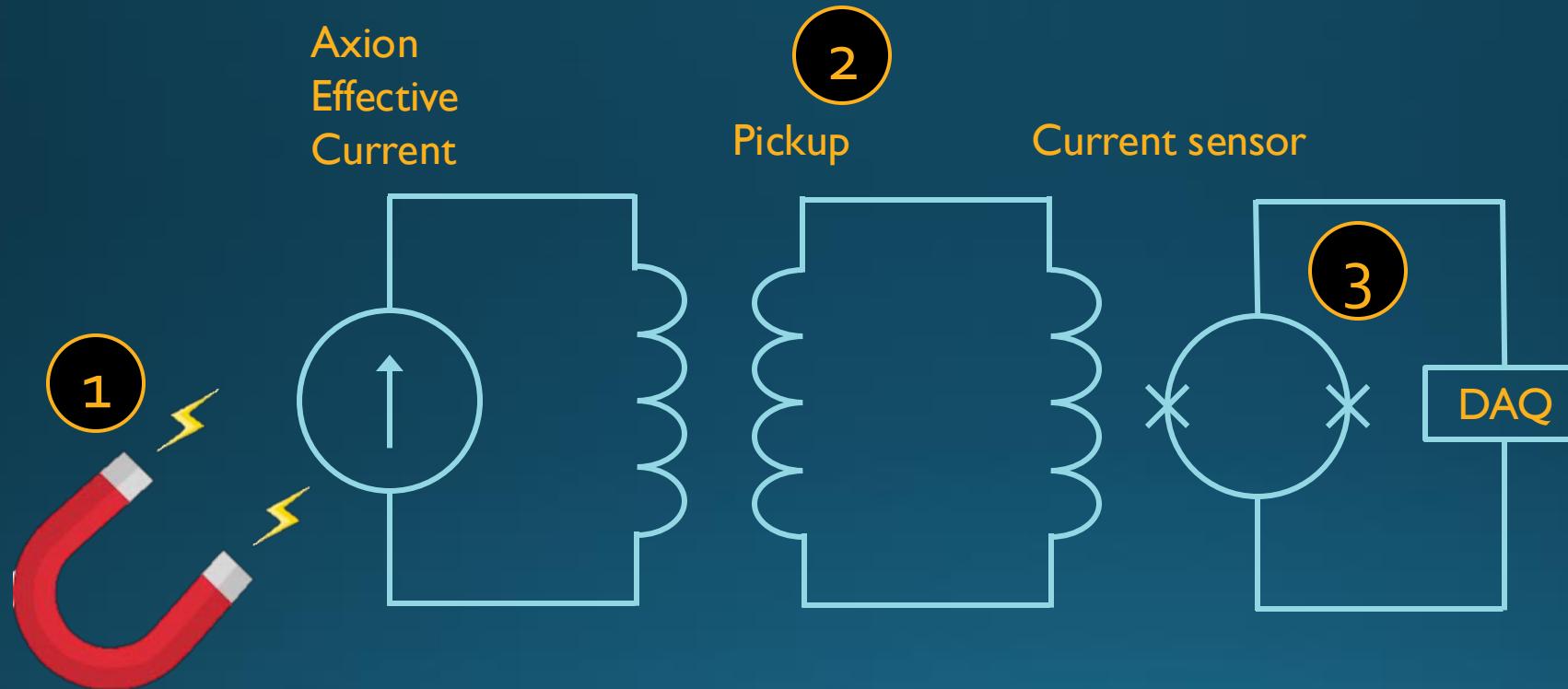
- **Field theory:** if you put  $f_a$  at the GUT scale, get  $\sim$ neV axion
- **String theory:** universally predicts (one or more) low-mass axions
  - Model-independent axion  $\sim 0.5$  neV
  - Low-mass axion experiments can constrain string models
- **Cosmology:** can naturally get correct dark matter abundance with a variety of inflation models (pre-inflationary PQ symmetry breaking)

M. Dine and W. Fischler, Phys. Lett. 120B, 137 (1983)  
J. Preskill, M. Wise, and F. Wilczek, Phys. Lett. 120B, 127 (1983)  
L. F. Abbott and P. Sikivie, Phys. Lett. 120B, 133 (1983)  
M. Tegmark, A. Aguirre, M. Rees, and F. Wilczek, Phys. Rev. D 73, 023505 (2006).  
M. P. Hertzberg, M. Tegmark, and F. Wilczek, Phys. Rev. D 78, 083507 (2008).  
R. T. Co, F. D'Eramo, and L. J. Hall, Phys. Rev. D 94, 075001 (2016).  
P. W. Graham and A. Scherlis, Phys. Rev. D 98, 035017 (2018)  
F. Takahashi, W. Yin, and A. H. Guth, Phys. Rev. D 98, 015042 (2018)  
J. Benabou, K. Fraser, M. Reig, B. Safdi, arxiv: 2505.15884  
and many more!

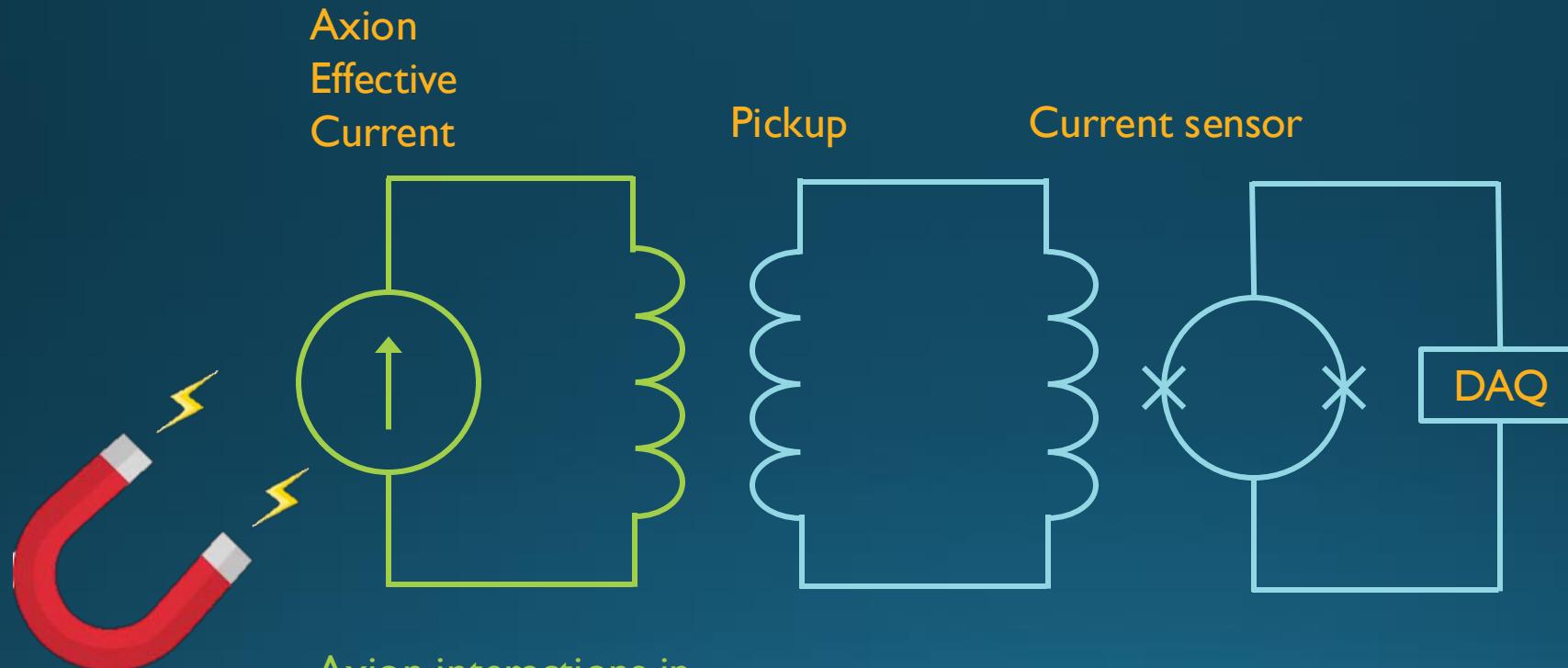
• ABRACADABRA ➔



# Schematic of lumped-element detection

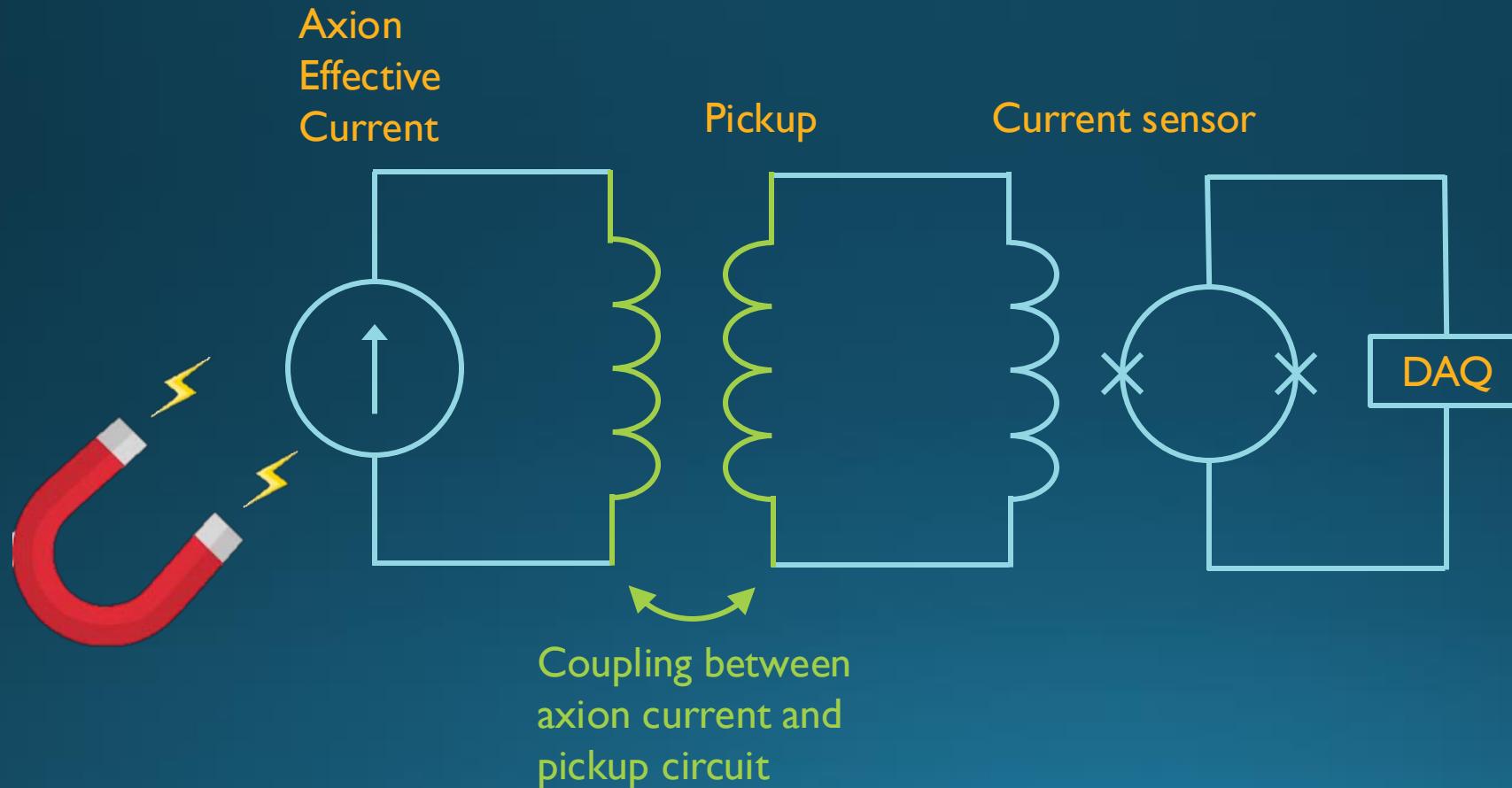


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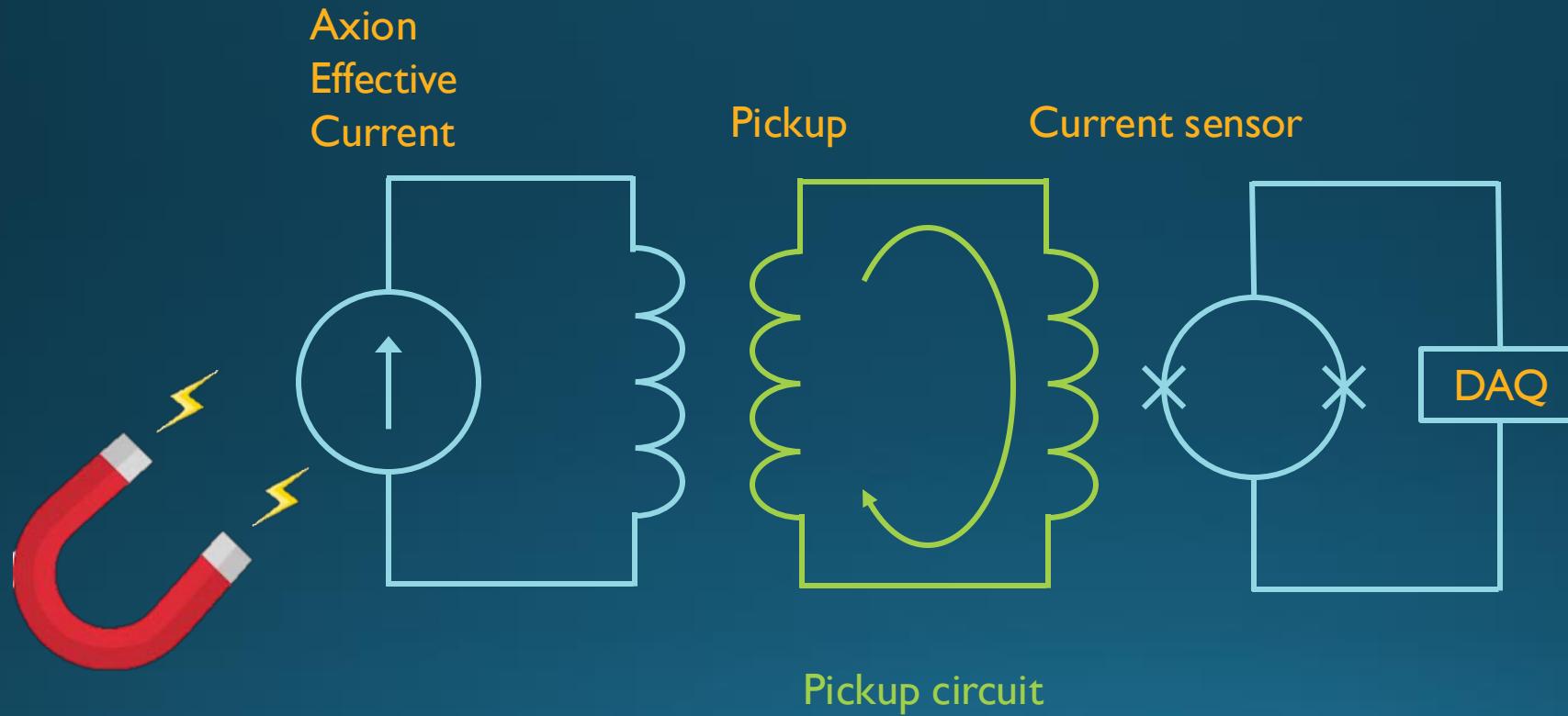


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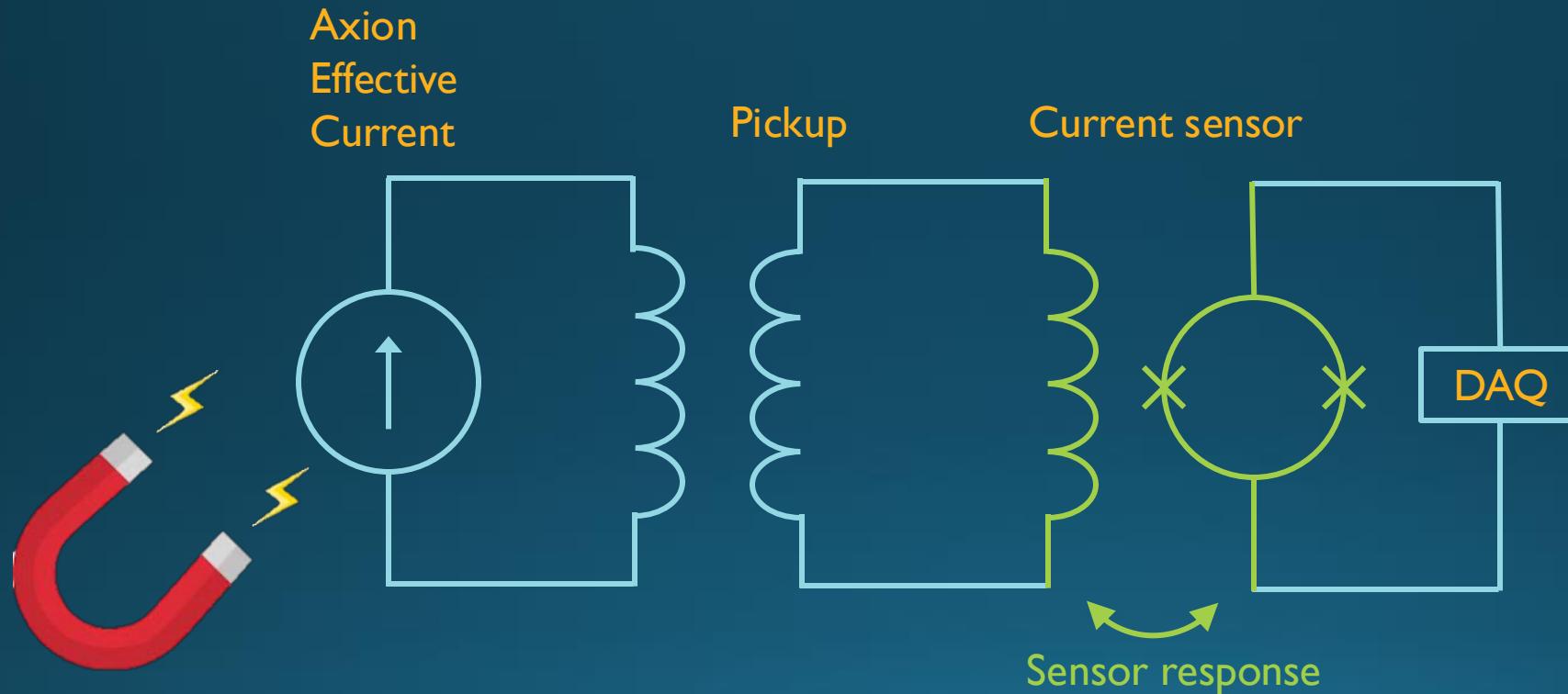
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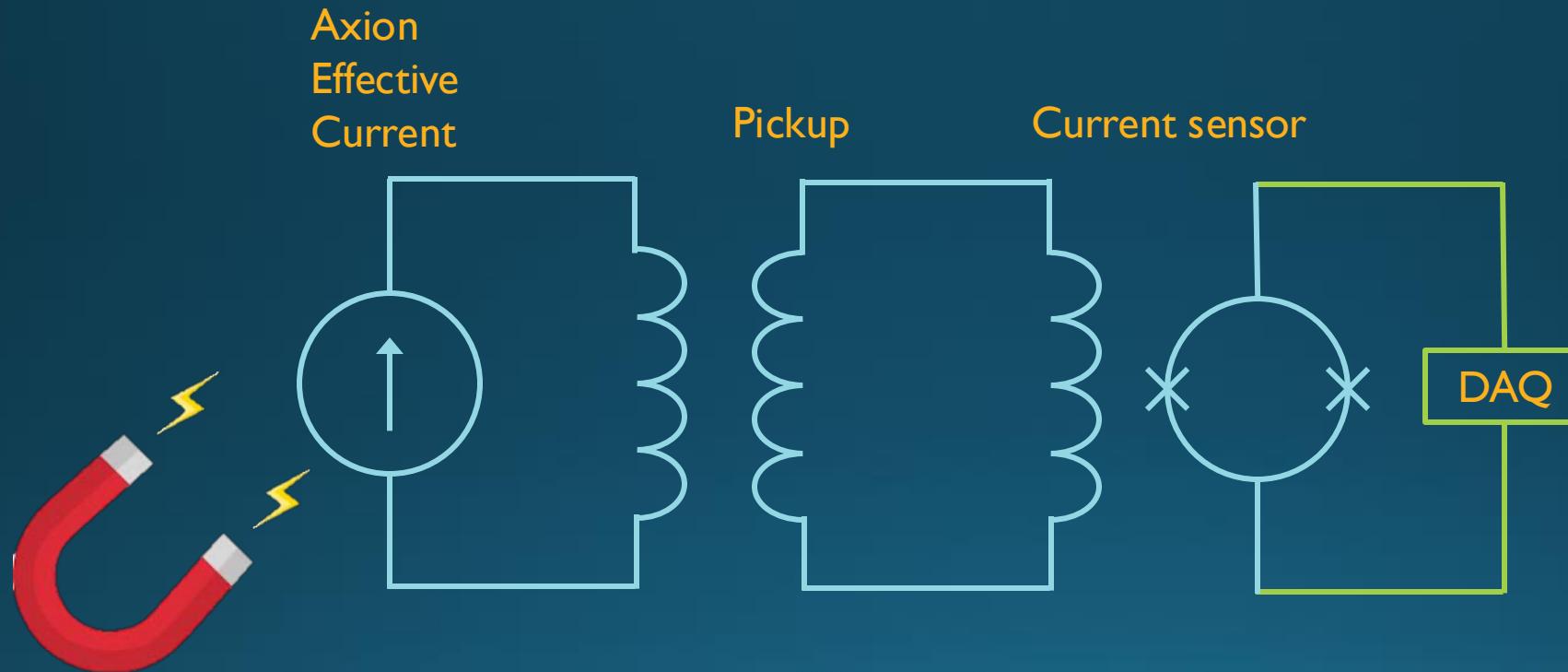
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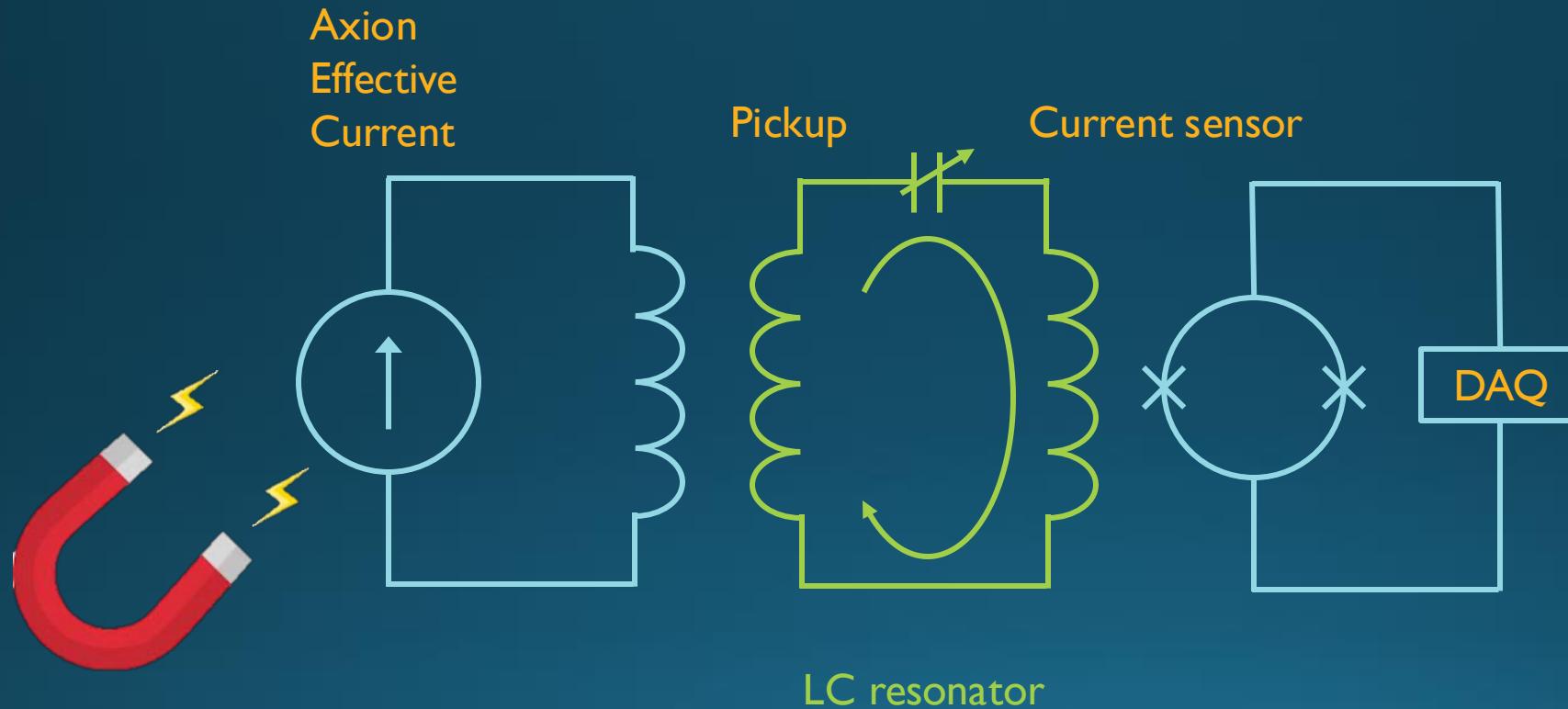


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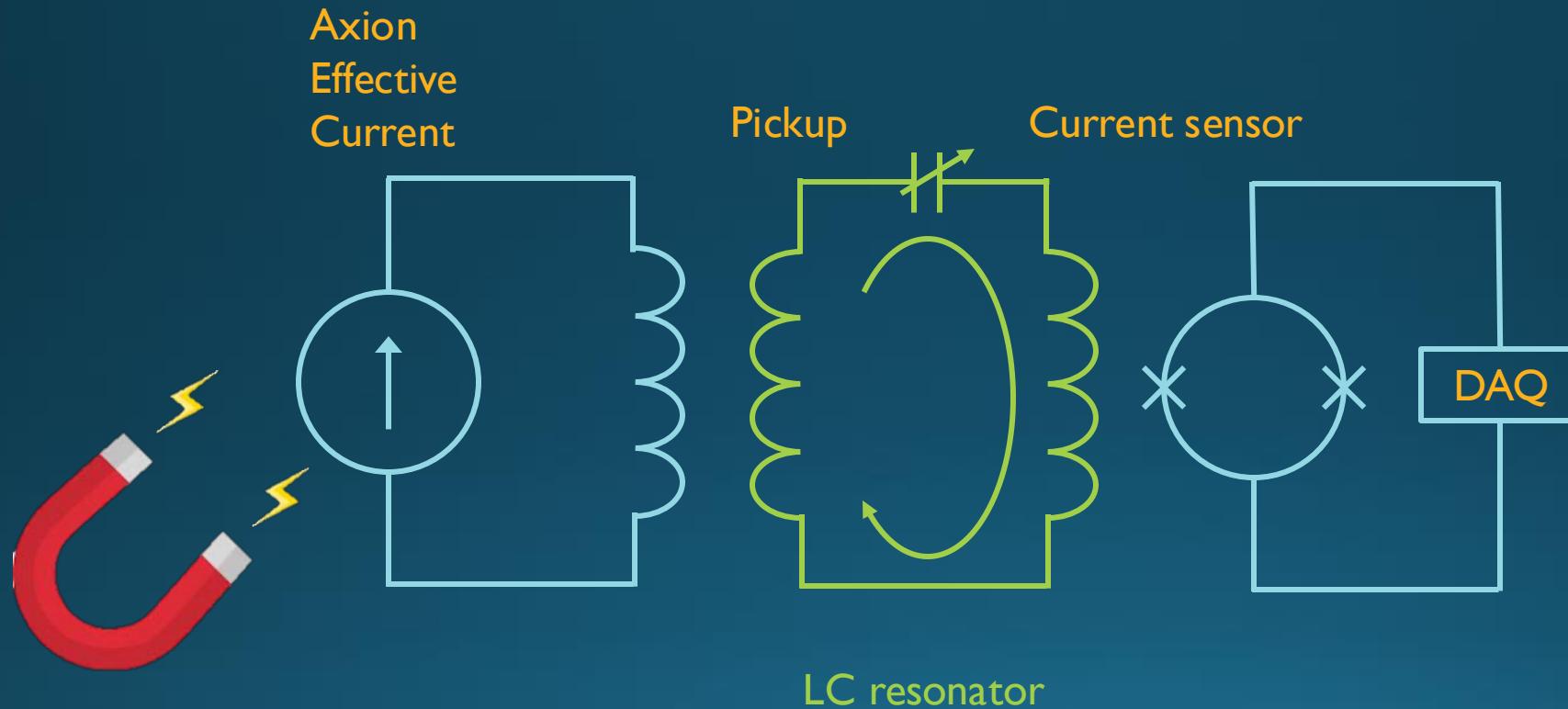
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## Resonant readout



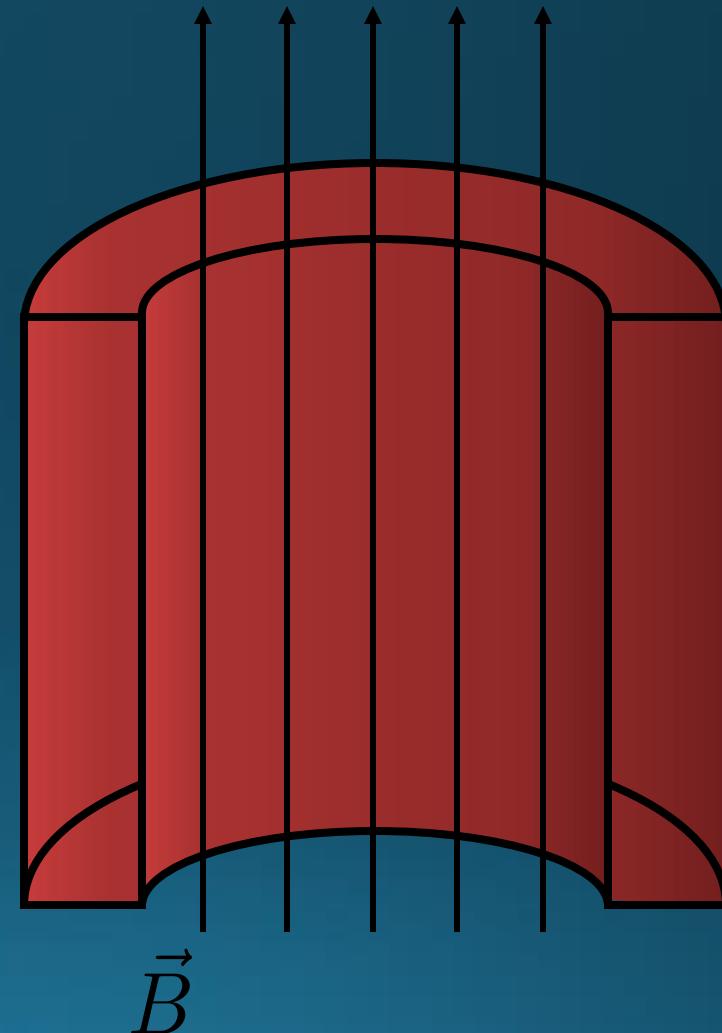
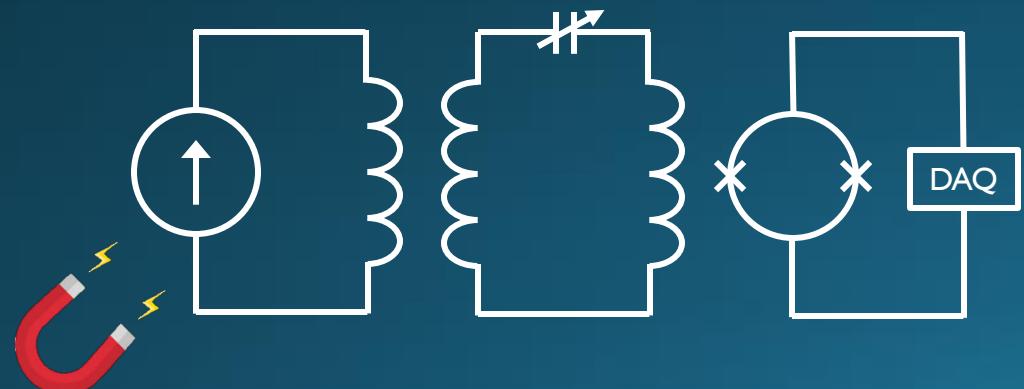
# Schematic of lumped-element detection

## Resonant readout



# The CAL detector

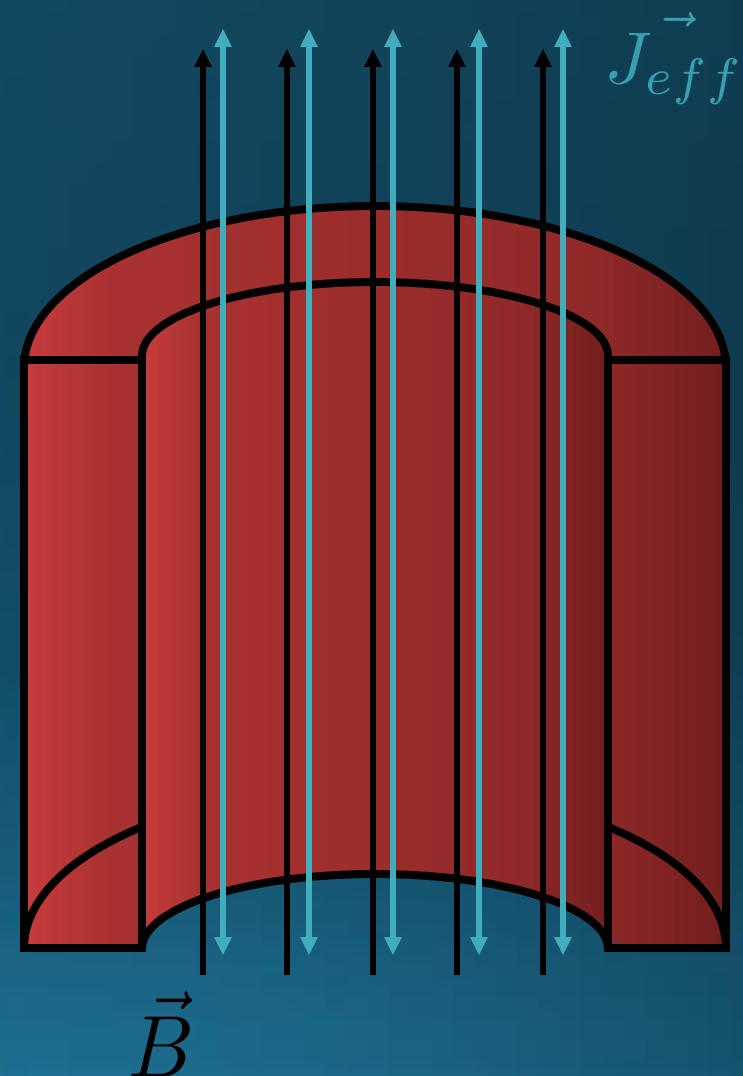
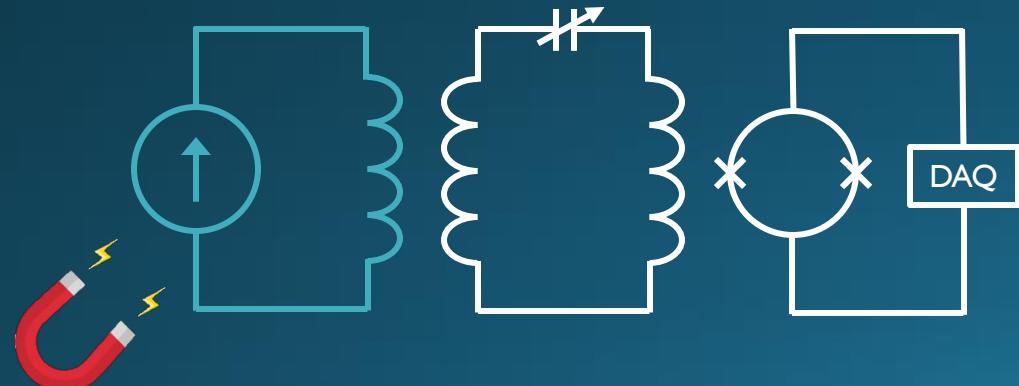
Solenoidal superconducting magnet  
with fixed field,  $B_0$



# The CAL detector

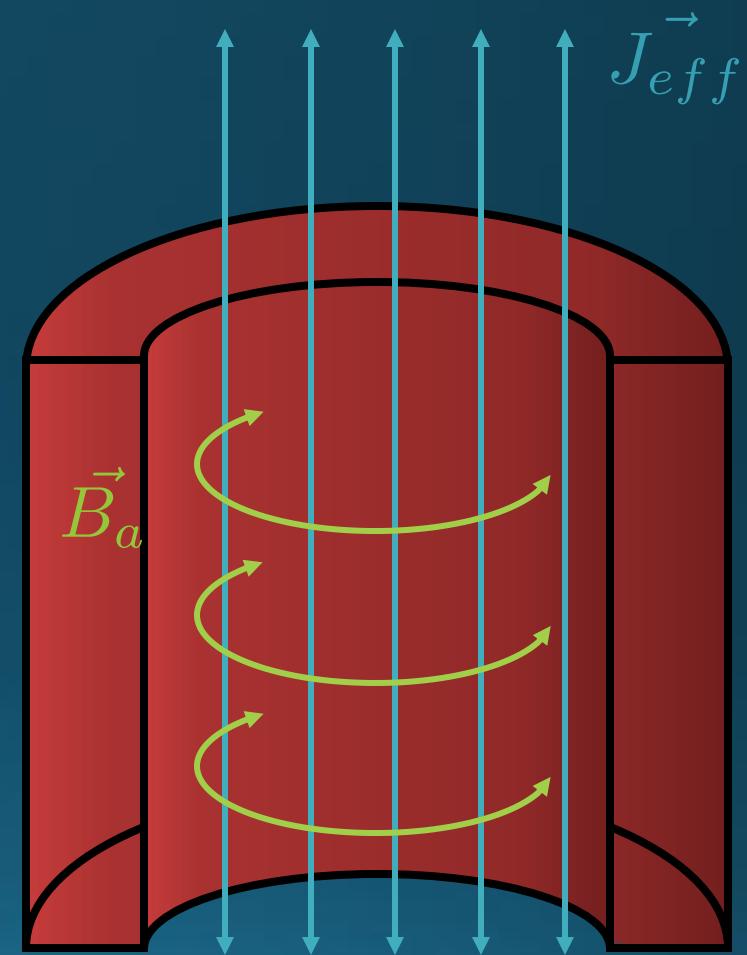
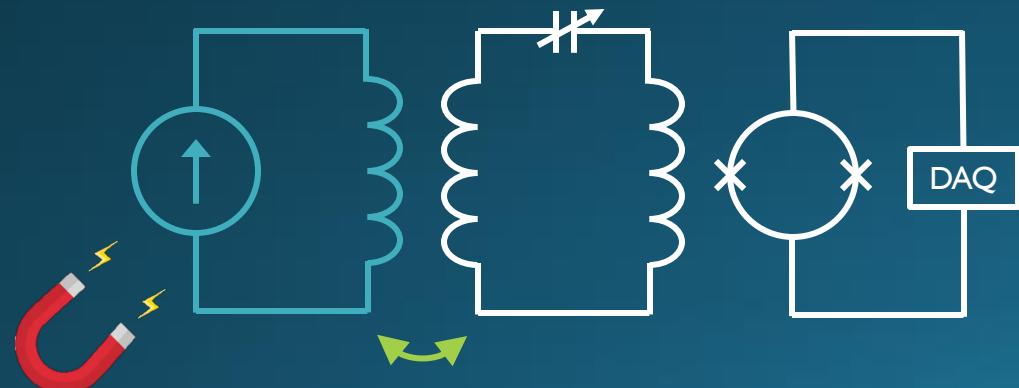
Axion dark matter generates parallel oscillating effective current,  $\vec{J}_{\text{eff}}$

$$\vec{J}_{\text{eff}} = g_{a\gamma\gamma} \sqrt{2\rho_{\text{DM}}} \cos(m_a t) \vec{B}_0$$



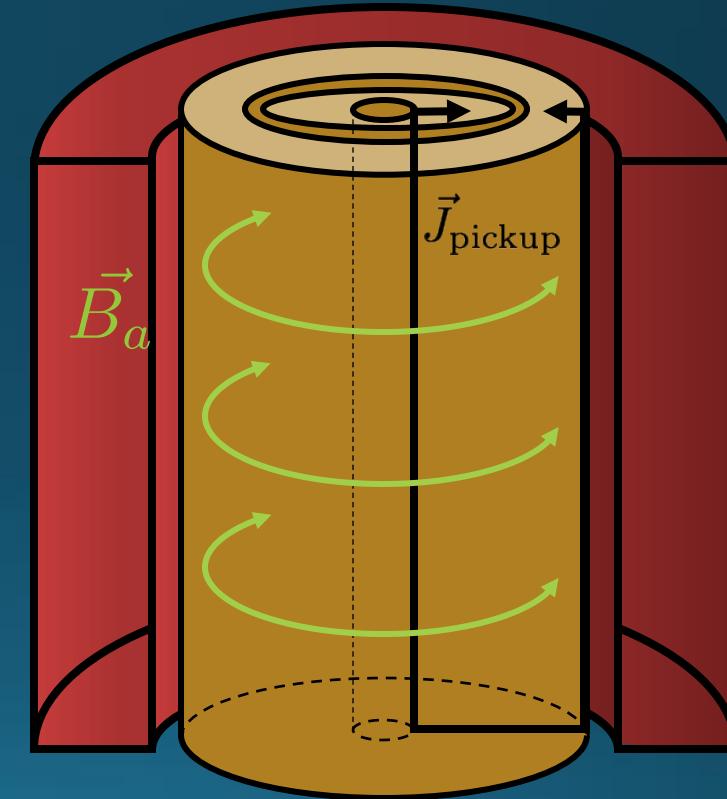
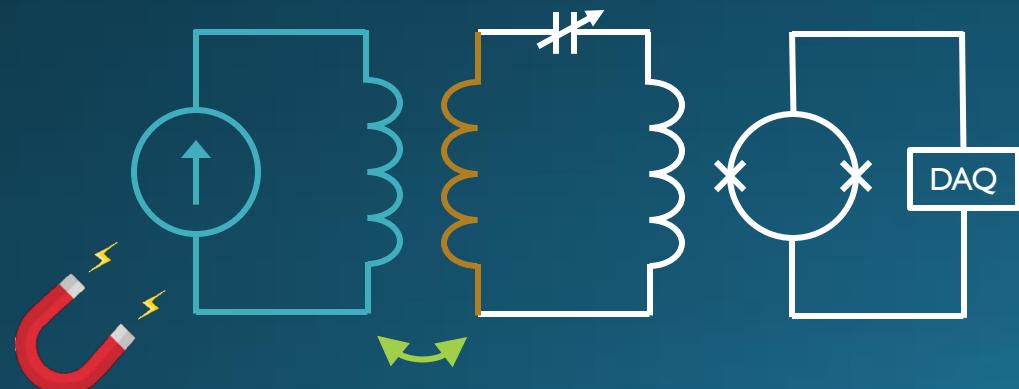
# The CAL detector

Axion dark matter generates parallel oscillating effective current,  $\vec{J}_{eff}$ , which generates an oscillating magnetic field



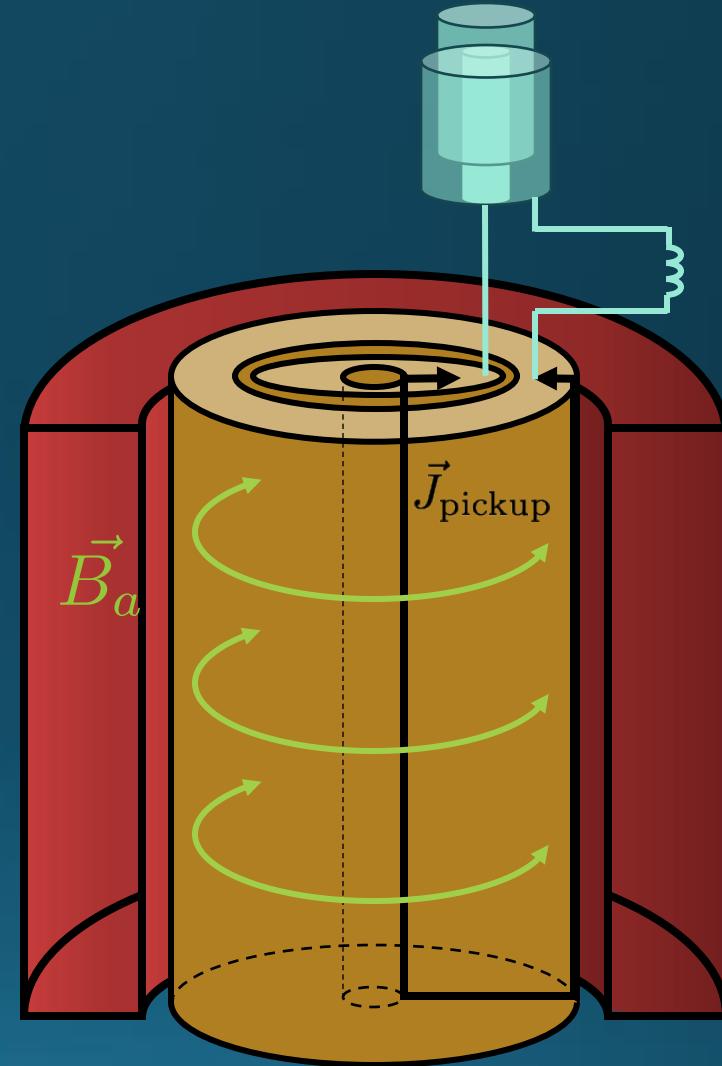
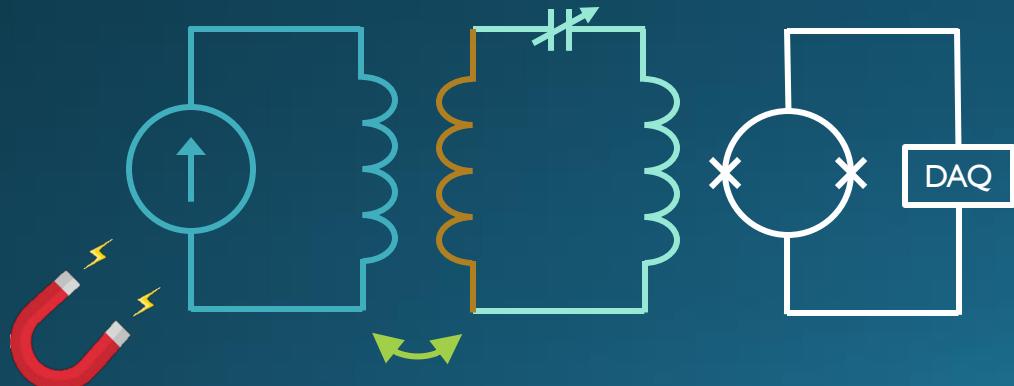
# The CAL detector

...inducing currents on the pickup coax



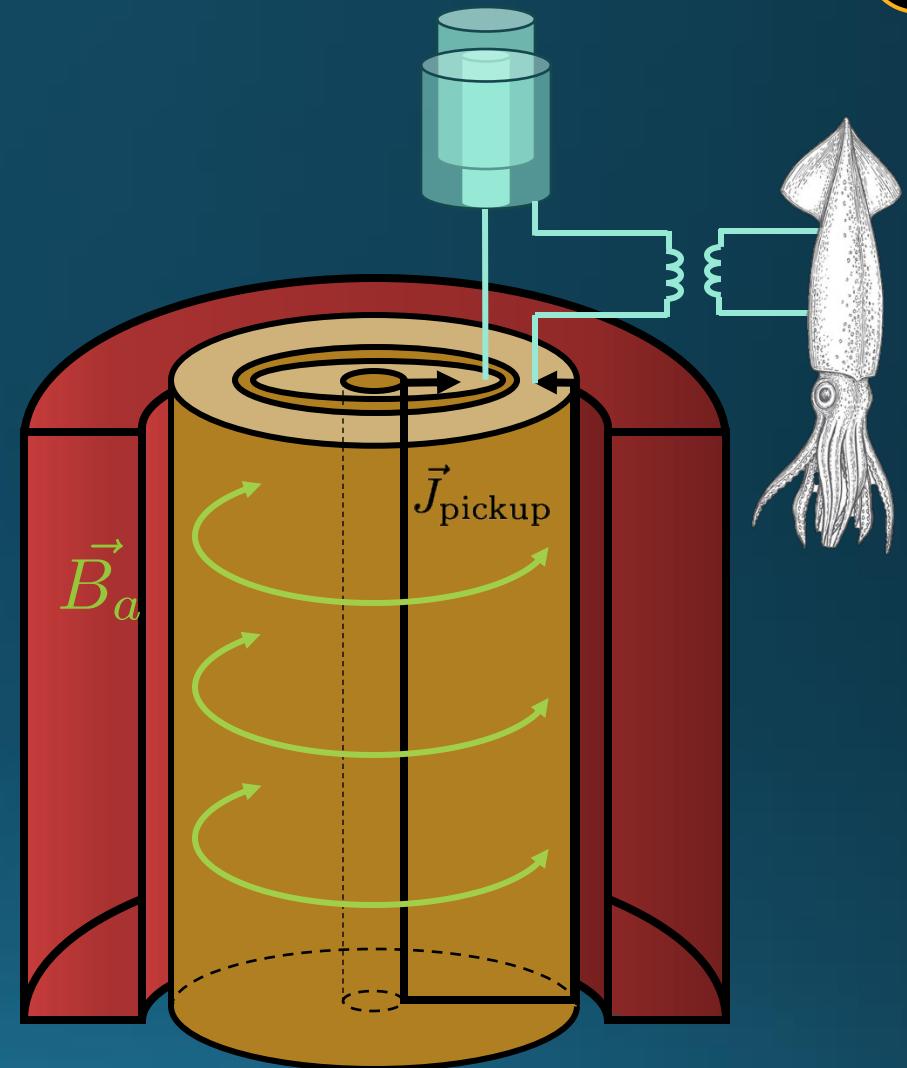
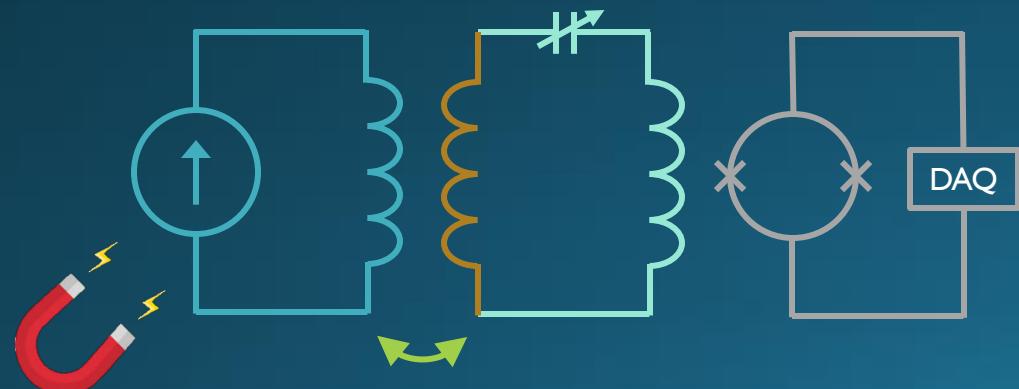
# The CAL detector

...inducing currents on the pickup coax and ringing up the tunable LC resonator

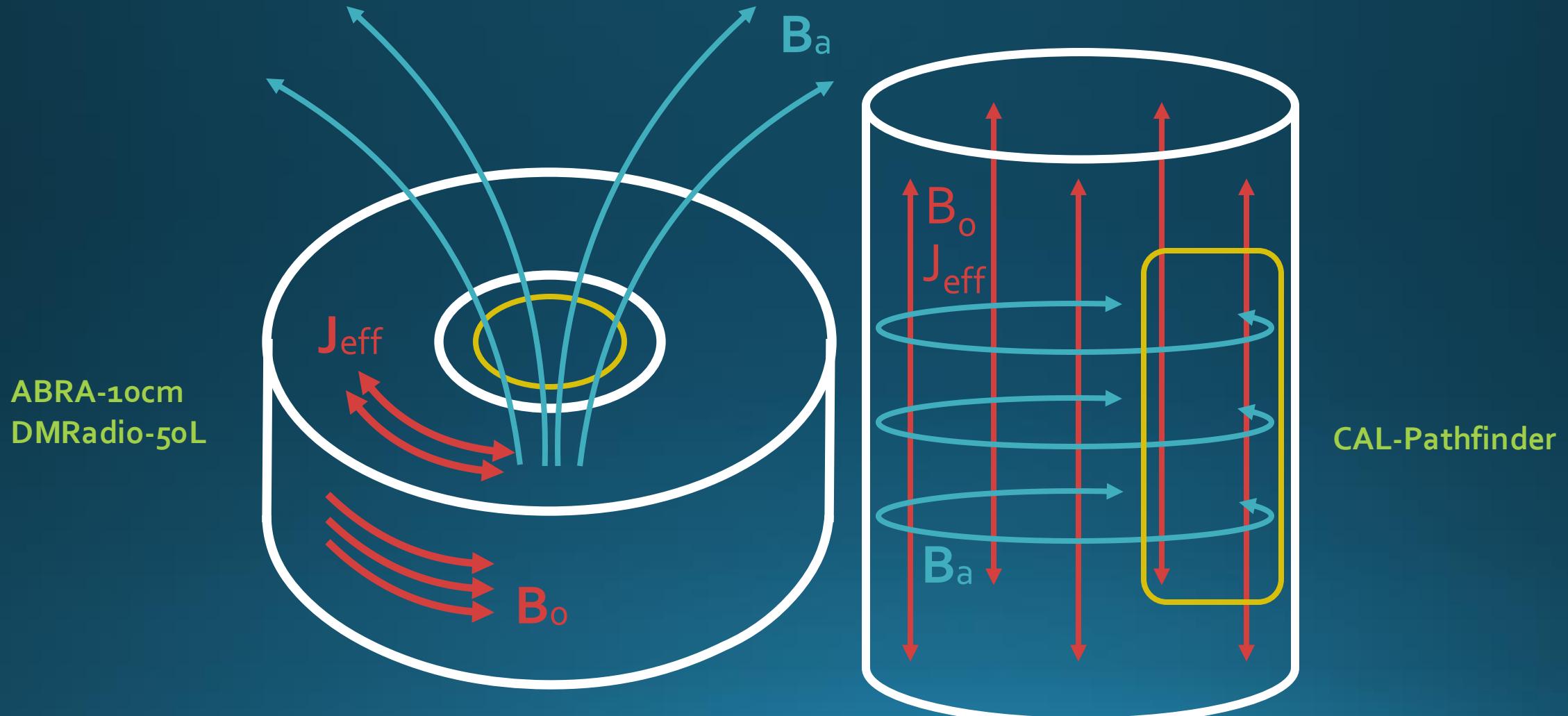


# The CAL detector

This signal is read out and amplified using a SQUID current sensor



# Detector geometry: toroid vs solenoid



# Design considerations for different geometries

	Toroid	Solenoid
High quality factor	<ul style="list-style-type: none"><li>• Superconducting sheath shields lossy magnet materials</li><li>• Pickup in field-free region: can use low <math>T_c</math> superconductors for resonator</li></ul>	<ul style="list-style-type: none"><li>• Current contained in coaxial pickup so naturally no access to lossy magnet materials</li><li>• Pickup in high-field region: use high purity copper or high <math>T_c</math> superconductors</li></ul>

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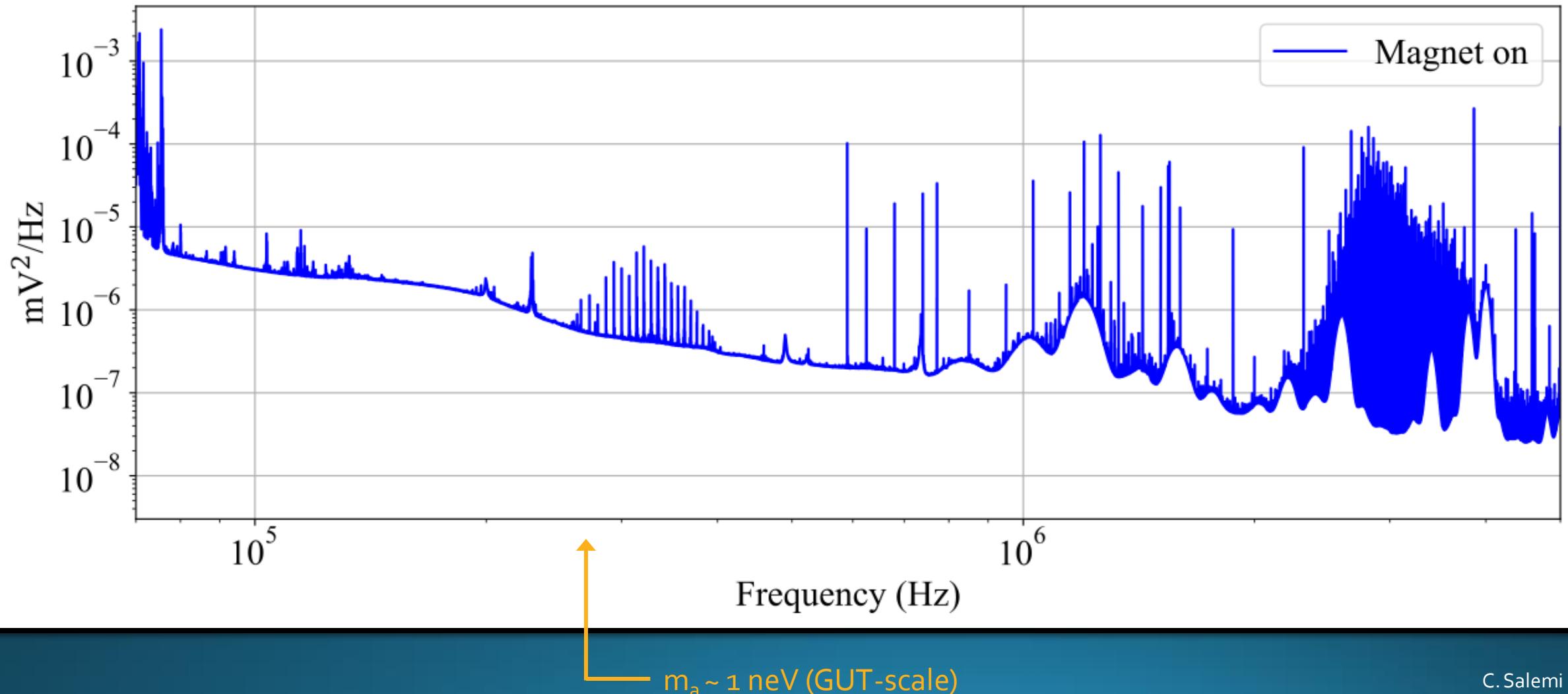
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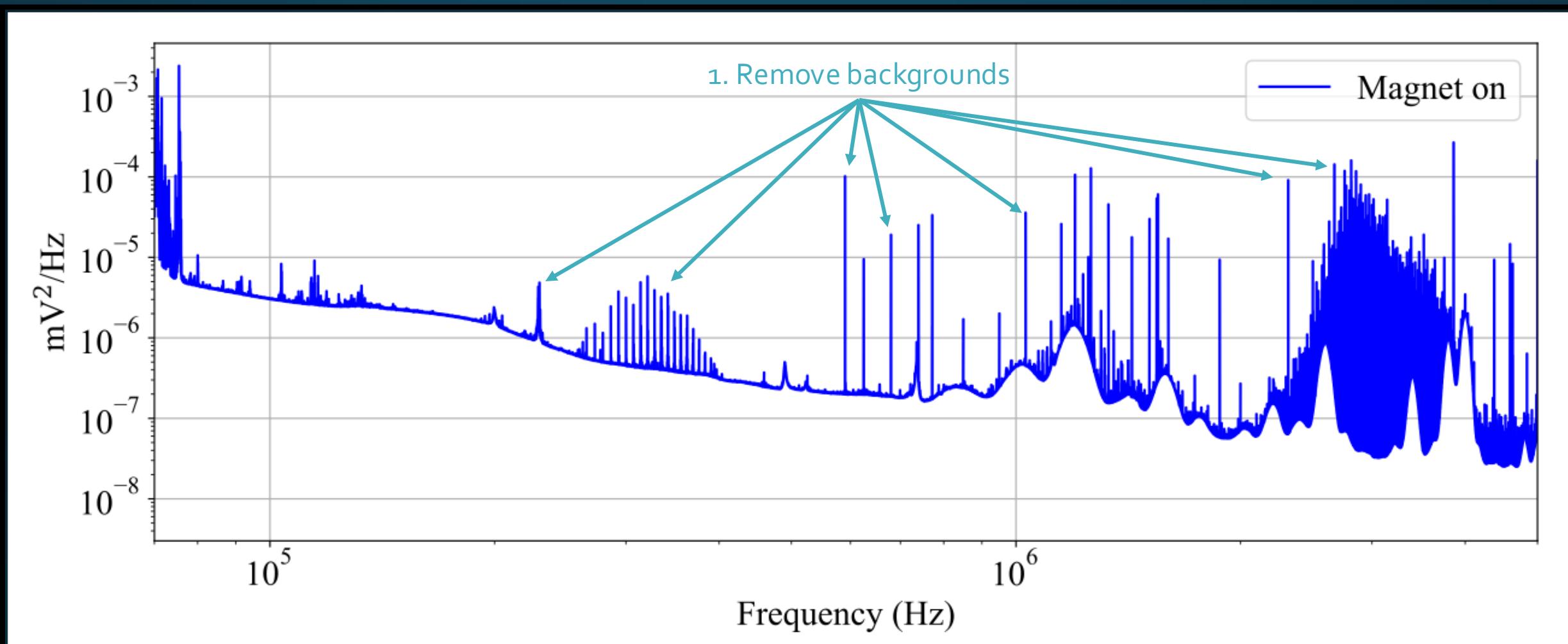
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Can both of these geometries also be used to detect dark photons?

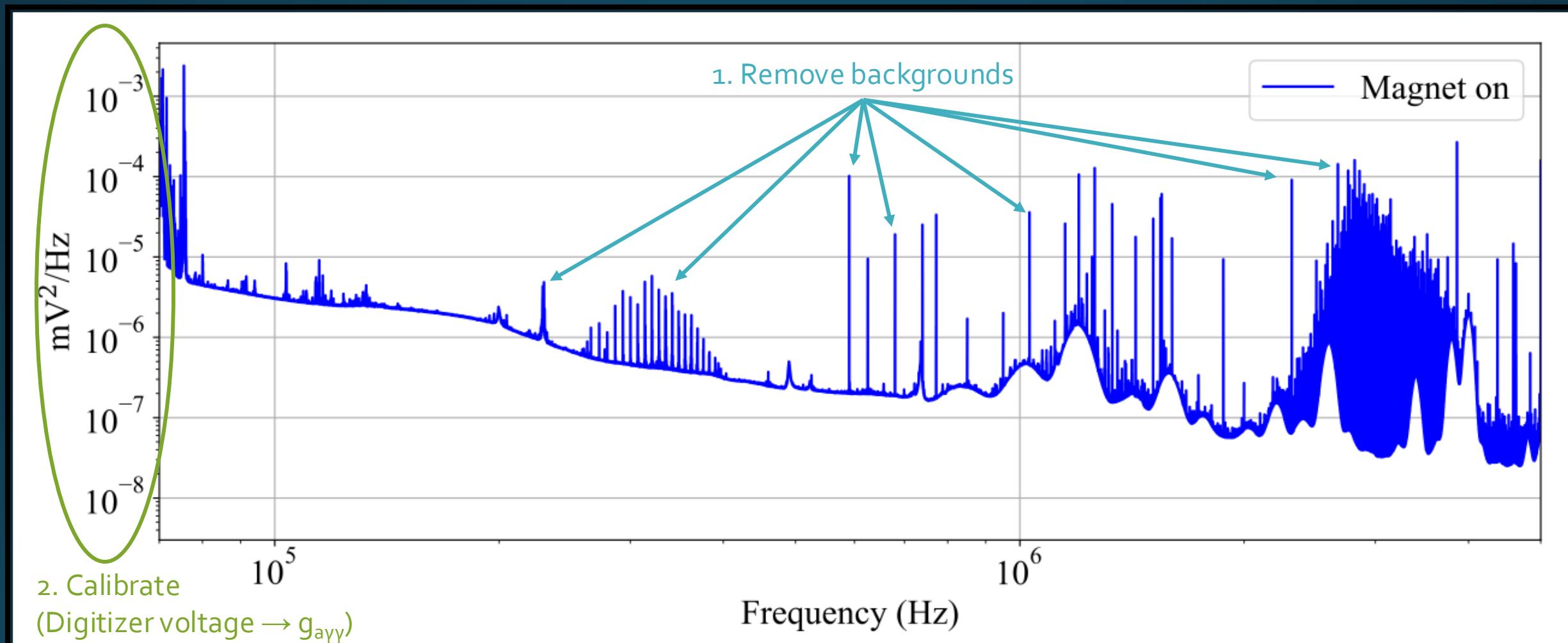
# Example data: ABRA-10cm



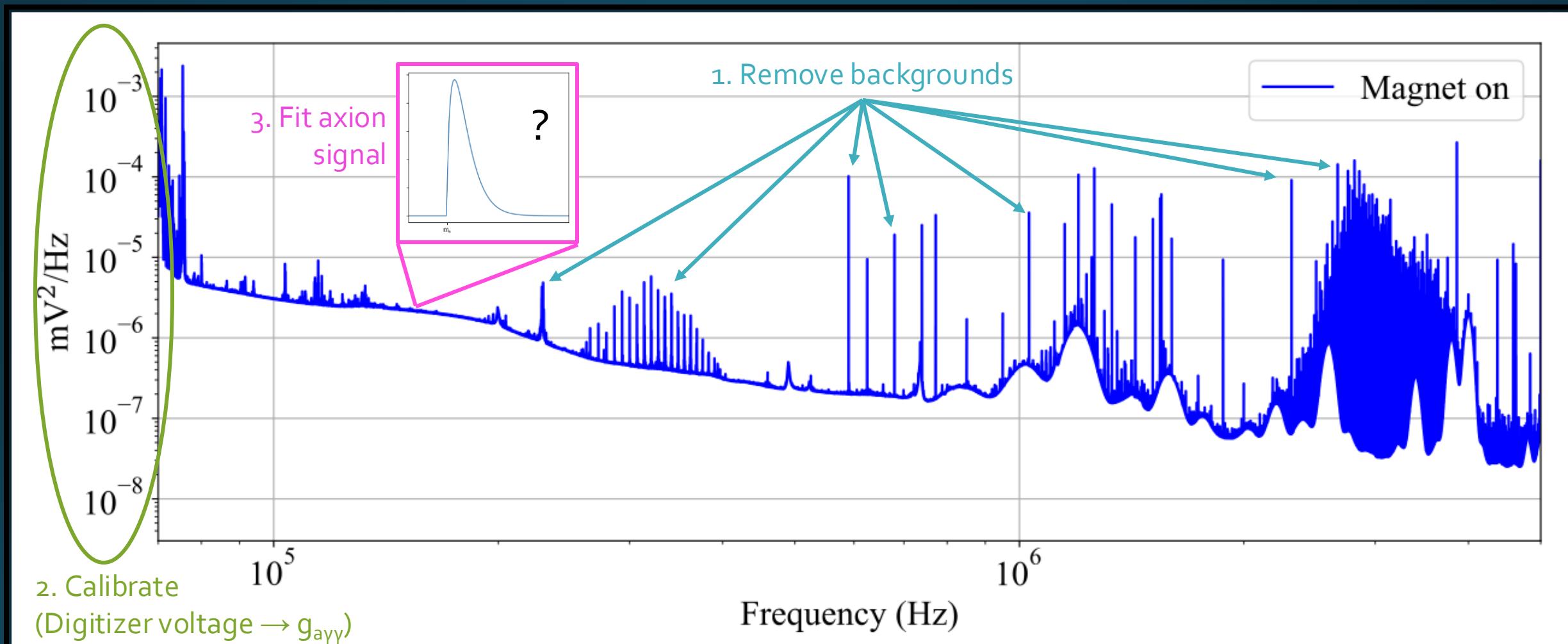
# ABRA-10cm data processing



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# ABRA-10cm data processing



# Calibrating lumped-element detectors

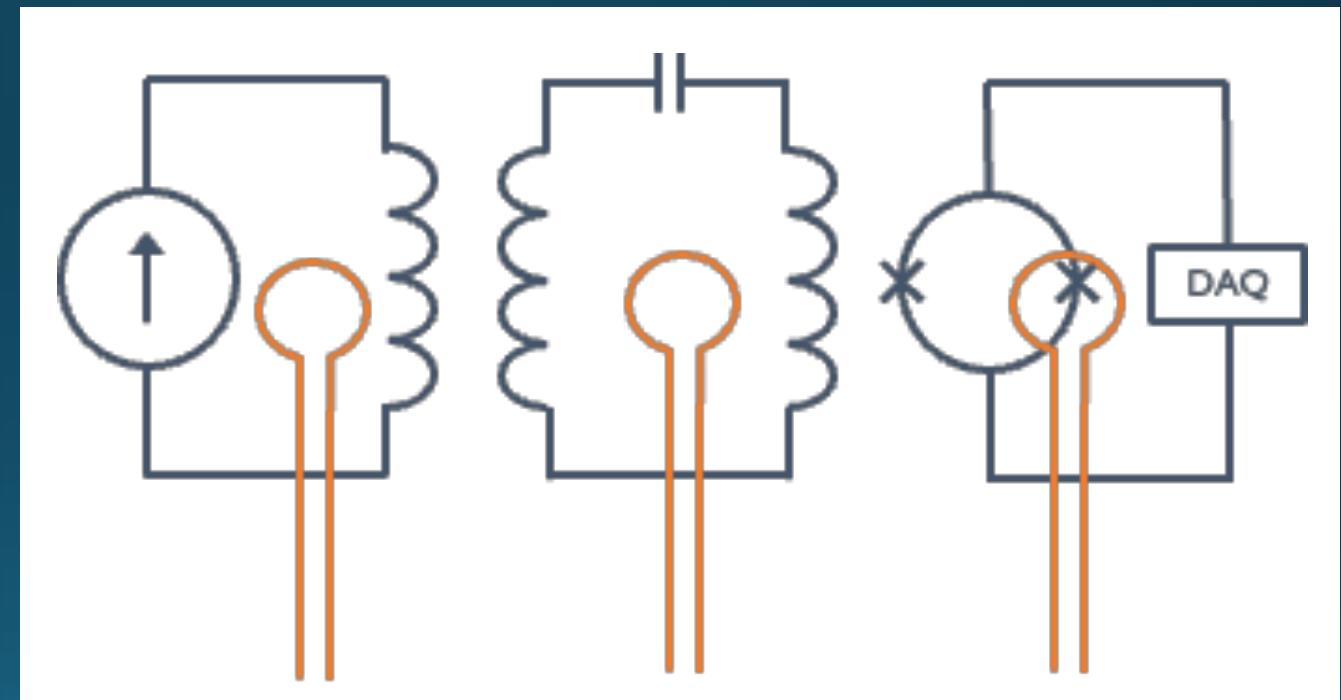
- Info we need:
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  - Resonance frequency
  - Q
  - System gain
  - Readout gain

# Calibrating lumped-element detectors

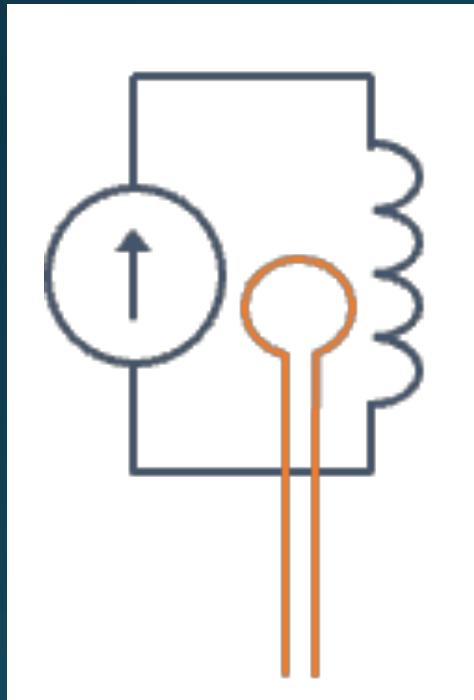
- Info we need:
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- Consider:
  - Where to inject calibration signal
  - What frequency(ies) to inject at
  - What 'shape' signal to inject

# Where to inject calibration signals

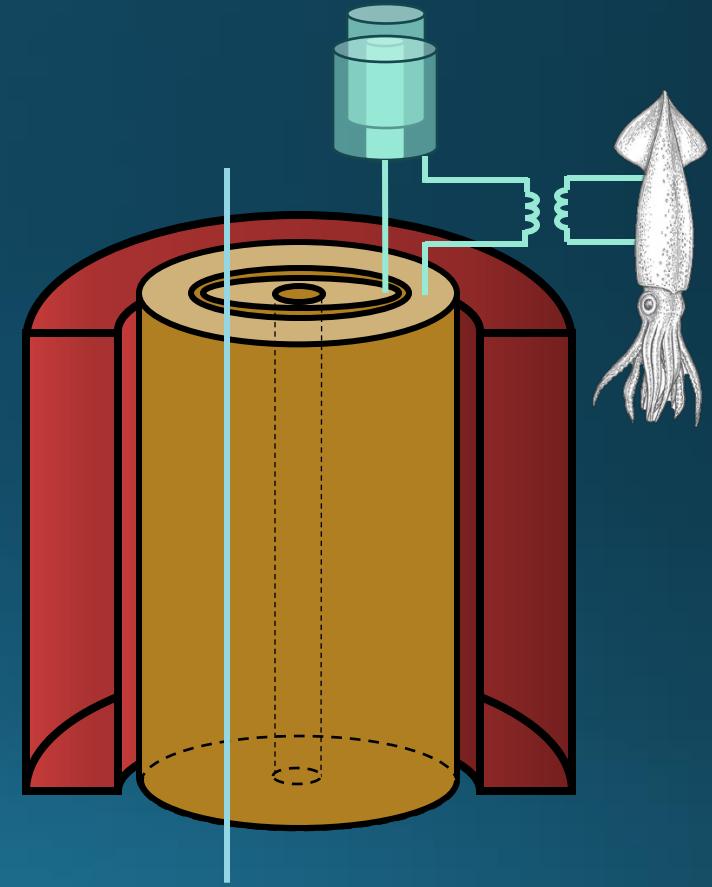
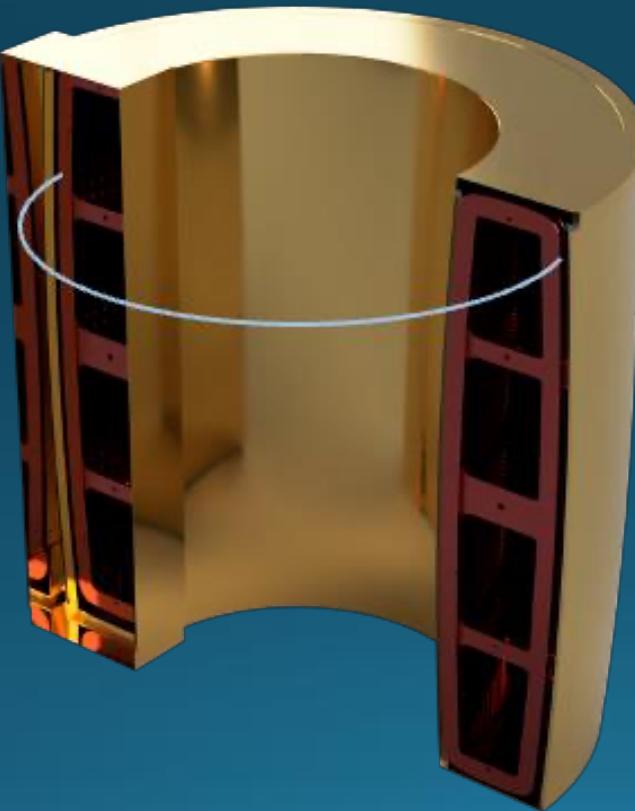
- Mimetic axion loop
- Loop into resonator
- Directly into SQUID



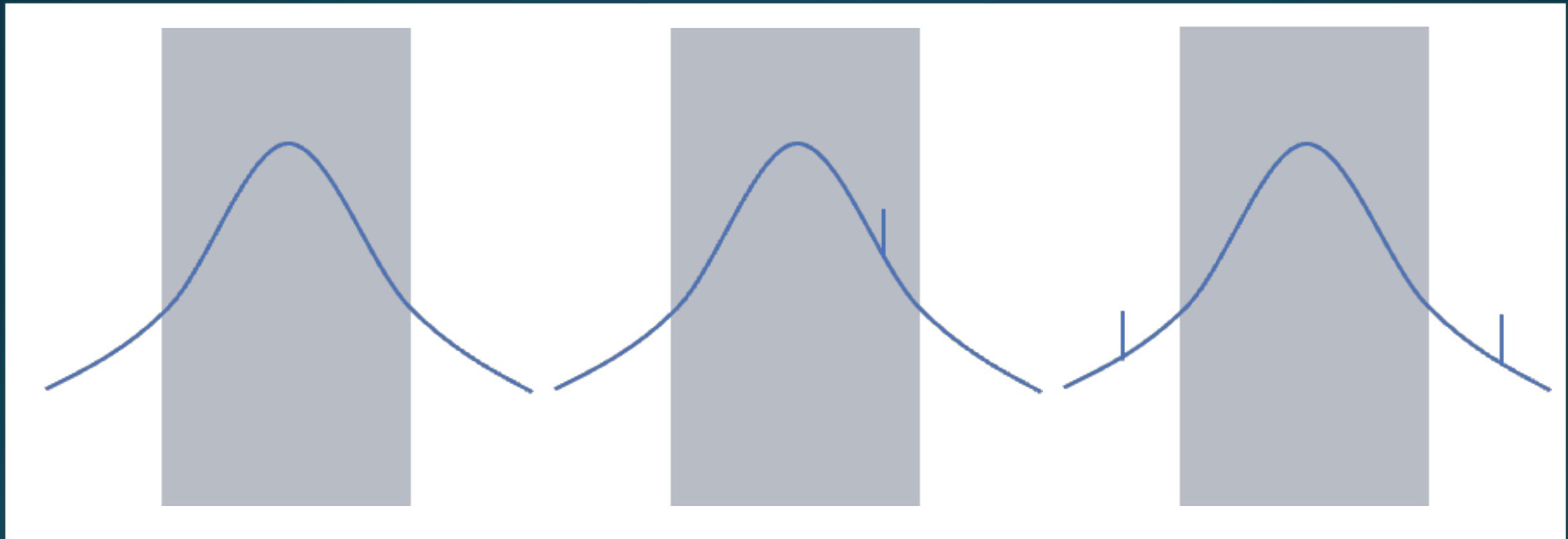
# Where to inject calibration signals



Mimetic axion



# What frequencies to inject



no injection;  
read out noise only

in-band injection

sideband injection

# What signature to inject

- Monochromatic tones:
  - Scan across resonance
  - Sidebands
- Ringdown:
  - Single monochromatic injection over time  $\Delta t$  near resonance
  - Measure resonator decay over  $\Delta t'$
- Synthetic axion signal:
  - Non-trivial frequency distribution (more useful for blinding)

# A brief note on background rejection

- Axion signal...

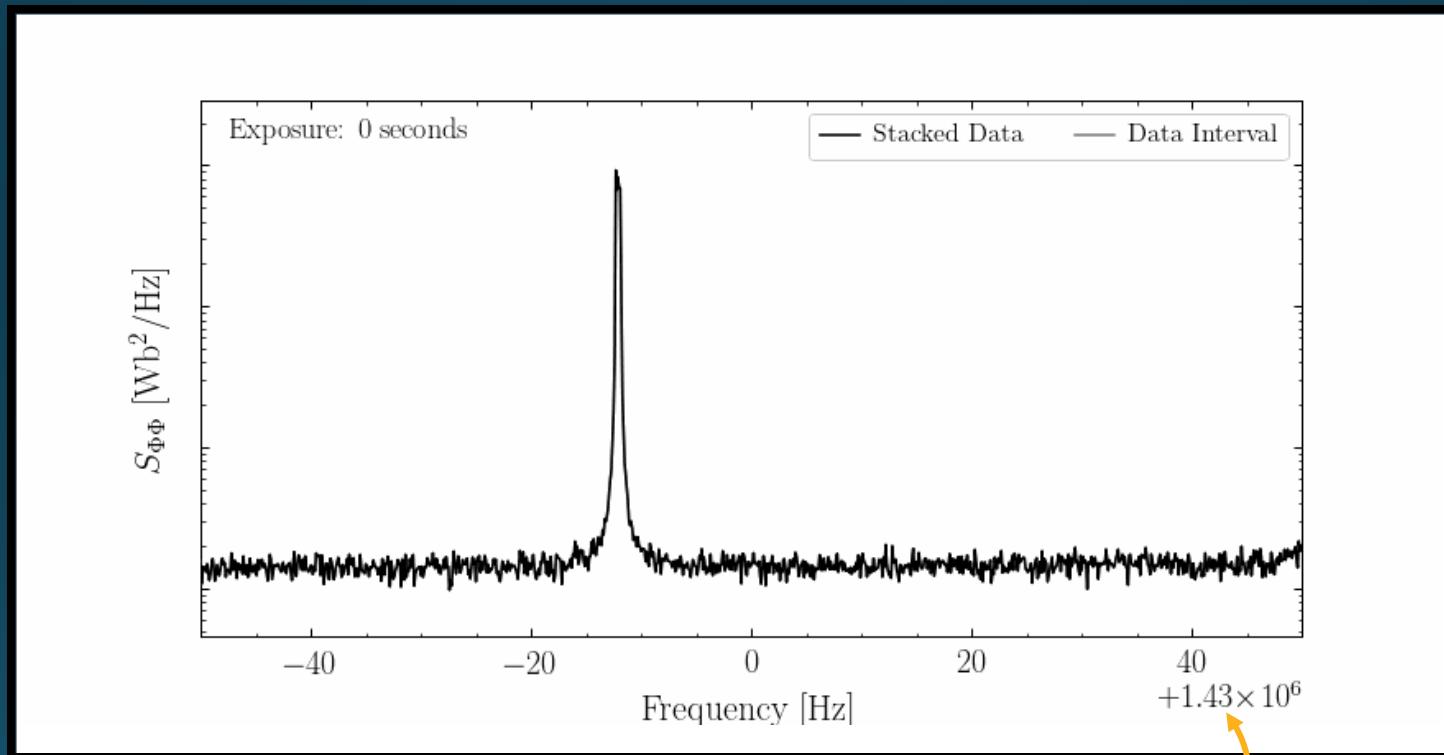
What is different about the  
axion signal from  
background sources?

# A brief note on background rejection

- Axion signal...
  - has an expected lineshape
  - is persistent over time in amplitude and frequency, even on a rescan
  - rolls off with the resonance
  - scales with B field strength
  - modulates daily and annually

hard to think of any backgrounds that obey all of these criteria

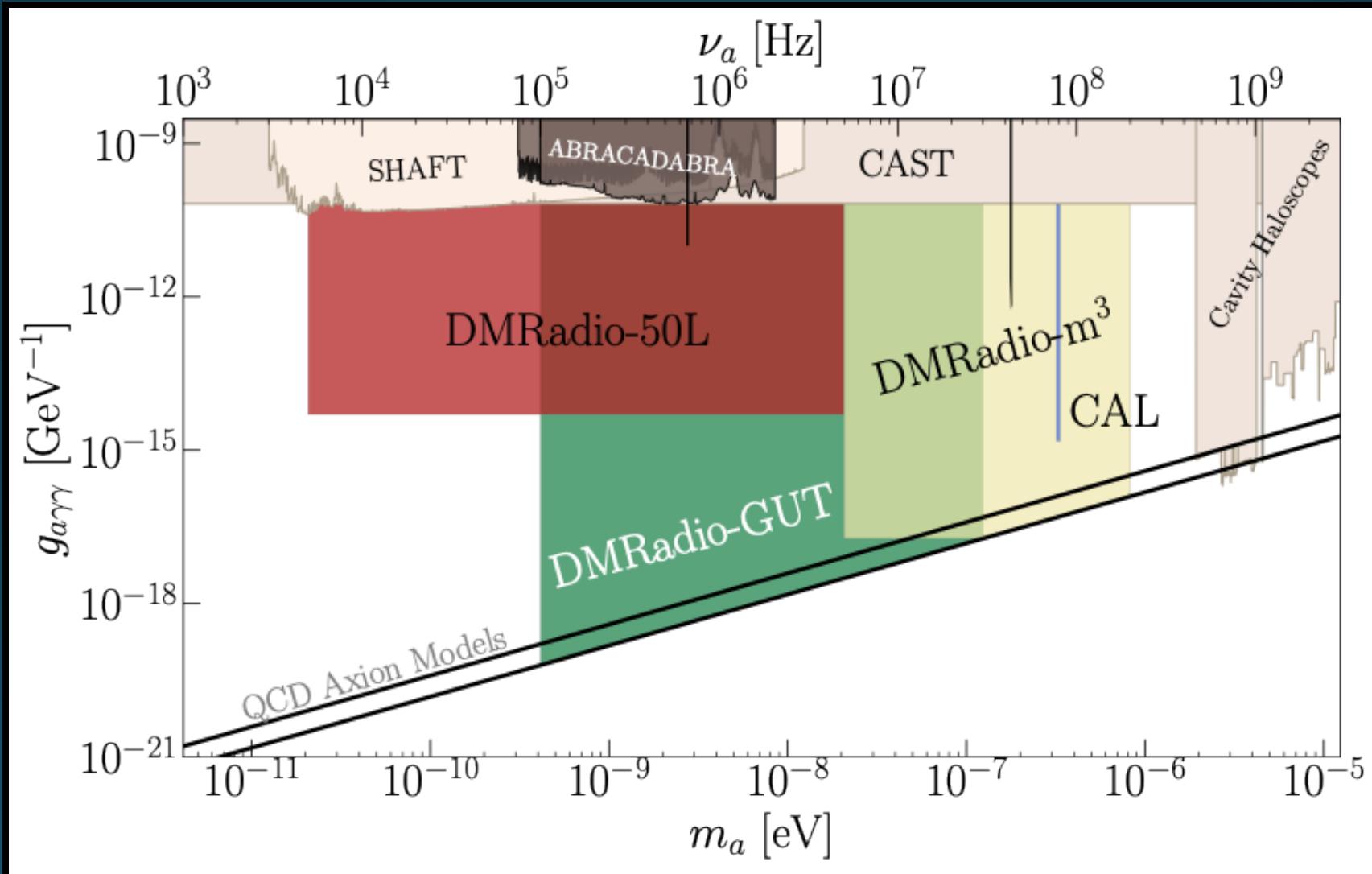
# My favorite ABRA-10cm background



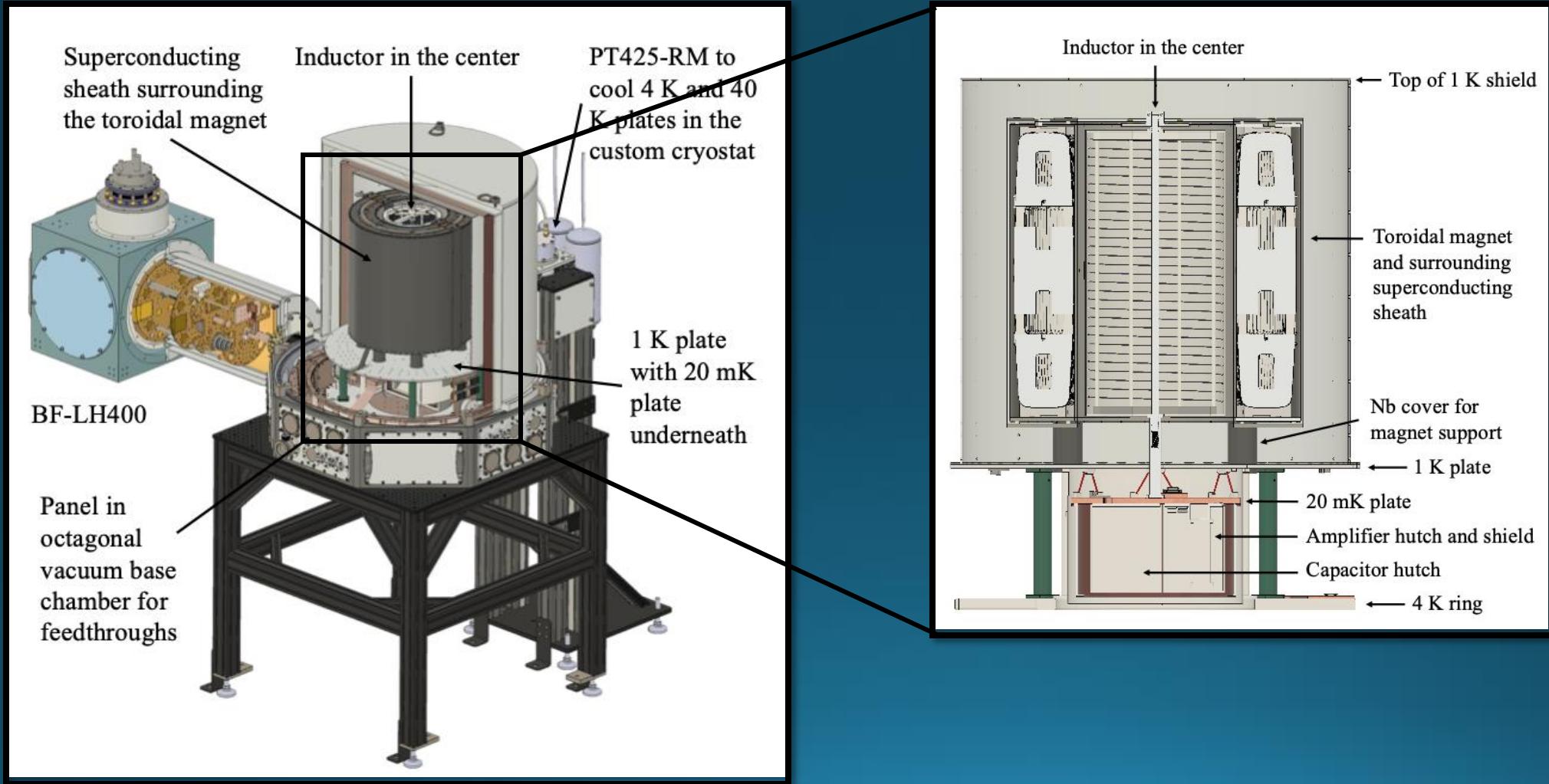
J. Foster



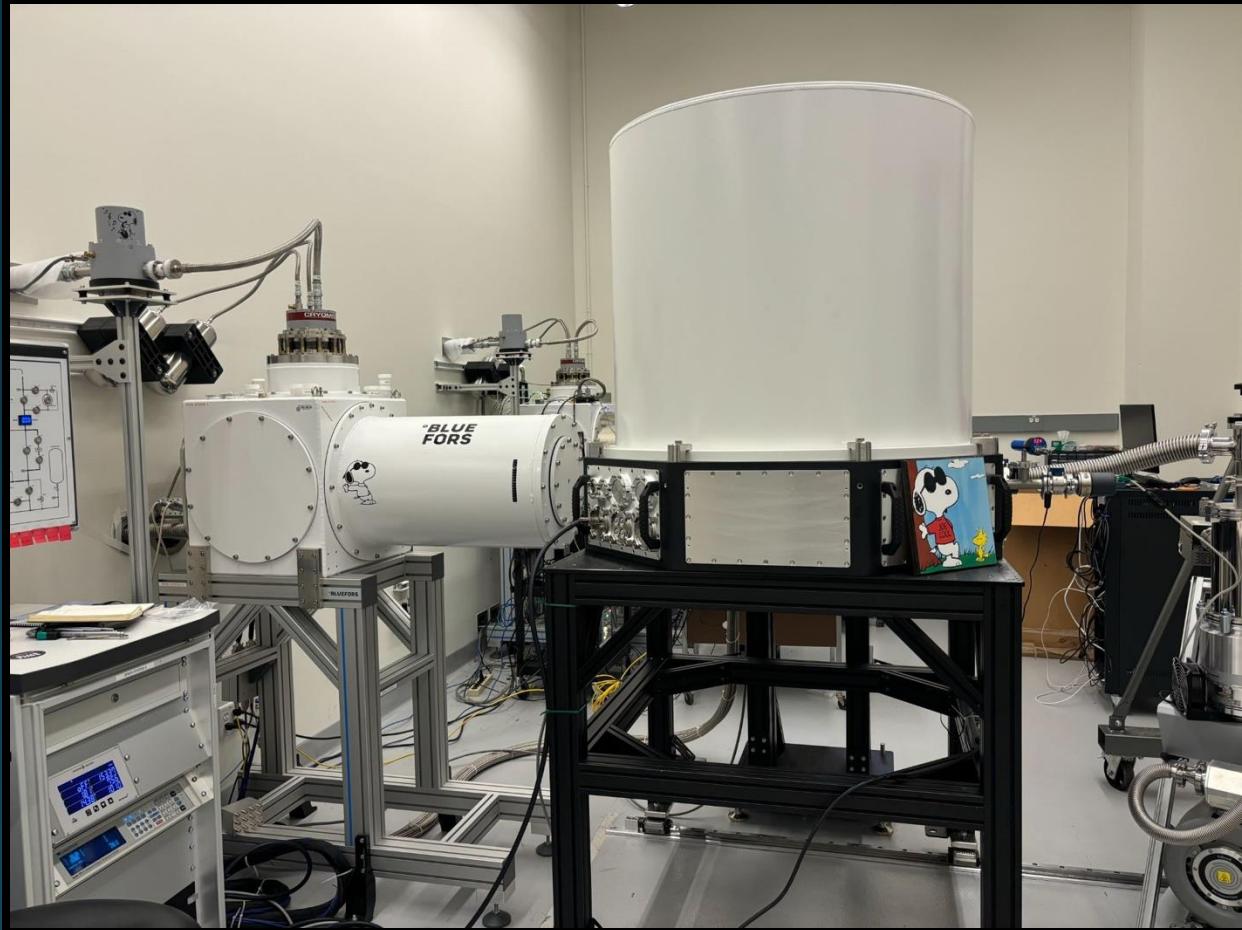
# Why so many experiments?



# The 50L detector (next physics data) from design...



# The 50L detector (next physics data) from design... to reality



# A note on the challenge of low frequencies

- Lowest nominal DMRadio-GUT frequency: 100 kHz
  - $10^6$  cycles at 100 kHz is 10 s
  - Bandwidth for Q =  $10^6$  at 100 kHz is 0.1 Hz
  - Scan rate is then  $0.1 \text{ Hz}/10 \text{ s} = 10^{-2} \text{ Hz/s}$
- Highest nominal DMRadio-GUT frequency: ~10 MHz
  - $10^6$  cycles at 10 MHz is 0.1 s
  - Bandwidth for Q =  $10^6$  at 10 MHz is 10 Hz
  - Scan rate is then  $10 \text{ Hz}/0.1 \text{ s} = 10^2 \text{ Hz/s}$
- Total scan time is dominated by scanning lowest frequencies

# Scanning and dead time

- At low frequencies, it takes a long time to ring up the resonator
- At high frequencies, scan time can begin to be dominated by tuning and calibration in between frequency steps

# Lumped-element scan rate

$$\frac{d\nu}{dt} \approx \frac{1}{\text{SNR}^2} \left( g_{a\gamma\gamma}^4 \rho_{\text{DM}}^2 Q_a \nu \right) \left( c_{\text{PU}}^4 \frac{Q B_0^4 V^{10/3}}{k_B T \eta} \right)$$

axion physics
detector

*V* : resonator frequency

$Q_a$  : axion quality factor

$Q$  : resonator quality factor

# CPU : pickup coupling

$B_0$  : peak magnetic field

**V** : pickup volume

$T$  : system effective temperature

$\eta$  : amplifier noise

# Funny exponents

$$\frac{d\nu}{dt} \propto c_{\text{PU}}^4 \frac{Q B_0^{4/3} V^{10/3}}{k_B T \eta}$$

$(B_0^2 V \cdot V^{2/3})^2$

magnet inductor  
stored area:  $L \propto A$   
energy

# Lots of pieces to work on

$$\frac{d\nu}{dt} \propto \frac{c_{\text{PU}}^4}{T} \frac{Q \left( \frac{B_0^2 V}{k_B T \eta} \cdot V^{2/3} \right)^2}{\text{maximize magnet stored energy}}$$

reduce resonator loss

maximize axion-coupled inductance

get as cold as possible

beyond SQL amplifiers

efficient axion-detector and internal transformer couplings

# Technology o: Cryogenics

$$\frac{d\nu}{dt} \propto c_{\text{PU}}^4 \frac{Q (B_0^2 V \cdot V^{2/3})^2}{k_B T \eta}$$

get as cold as  
possible

# Low temperatures are required

- Superconductors must be cooled below their transition temperature
  - Needed for low loss
  - Nb ~ 9K, Al ~ 1K
  - Generally want to cool well below this point

# Low temperatures are required

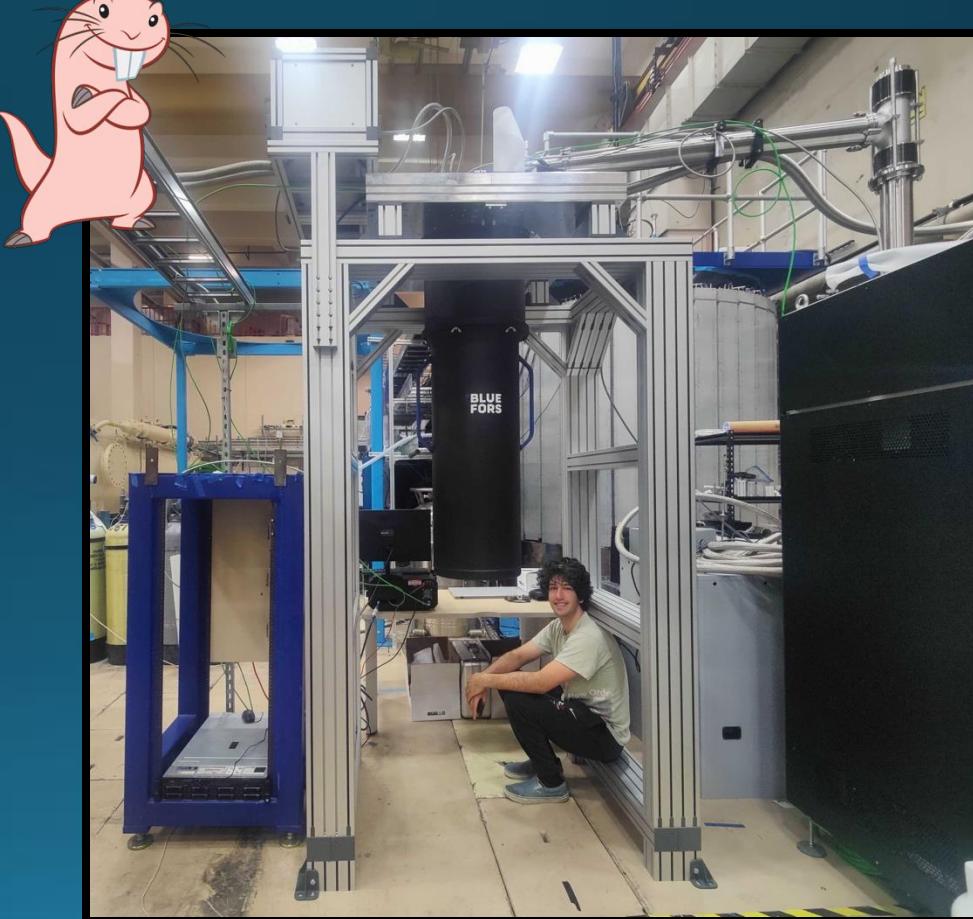
- Superconductors must be cooled below their transition temperature
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Why is this true?

# Low temperatures are required

- Superconductors must be cooled below their transition temperature
  - Needed for low loss
  - Nb ~ 9K, Al ~ 1K
  - Generally want to cool well below this point
- Thermal noise is the fundamental limitation at low frequencies\*
  - Cool as low as possible!

# Achieve mK temperatures with dilution refrigerators



# Technology 1: Magnets

maximize magnet  
stored energy

$$\frac{d\nu}{dt} \propto c_{\text{PU}}^4 \frac{Q \left( \overline{B_0^2 V} \cdot V^{2/3} \right)^2}{k_B T \eta}$$

What do we want  
from our magnets?

# Magnet requirements

- High field
- High volume
- Stable, known field pattern
- Toroid or solenoid
- Low-field region for superconducting sensors

# Magnet considerations

- Forces
  - GUT magnet:  $B^2V/(2\mu_0) \approx 1 \text{ GJ}$  (almost a quarter of a ton of TNT)
- Quench protection
- How strong/large you can reach is material-dependent
  - Critical temperature:  $T_c$
  - Critical field:  $H_{c1}$
  - Critical current density
- Cost: magnet often is ~half the price of an axion experiment

# Magnet materials (Iron)

- low saturation ( $\sim 1\text{-}2\text{T}$ )
- permanent (or semi-permanent with a coil)
- too much mass to cool down effectively, so must be larger to accommodate cryostat infrastructure inside

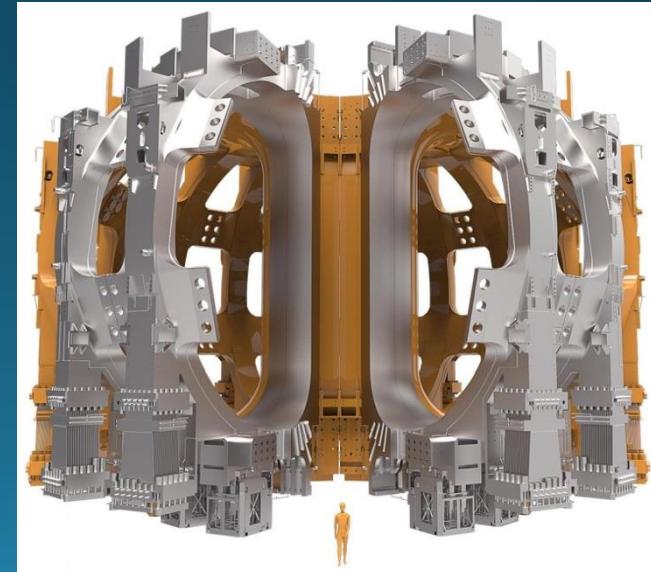
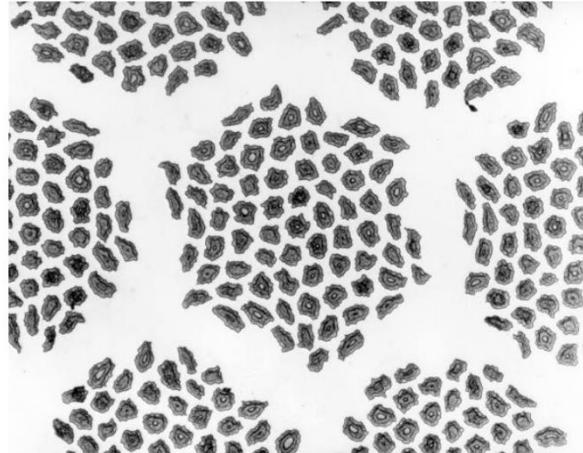
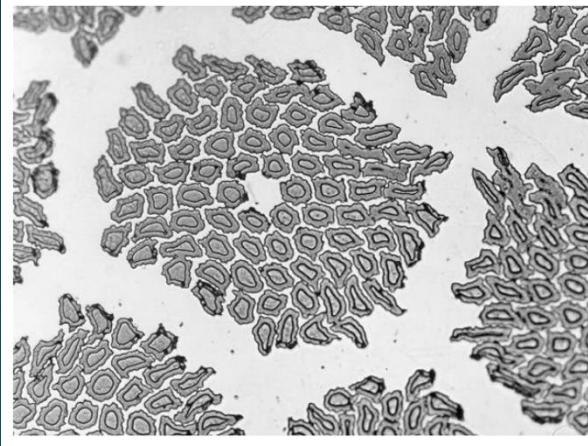
# Magnet materials (NbTi)

- traditional superconducting magnet wire material
- easy to make into flexible cabling for winding
- typically have multiple strands of NbTi in a copper matrix for thermalization and quench protection
- critical field ~ 15T; in practice magnets max field ~9-10T
- most existing axion experiments



# Magnet materials ( $\text{Nb}_3\text{Sn}$ )

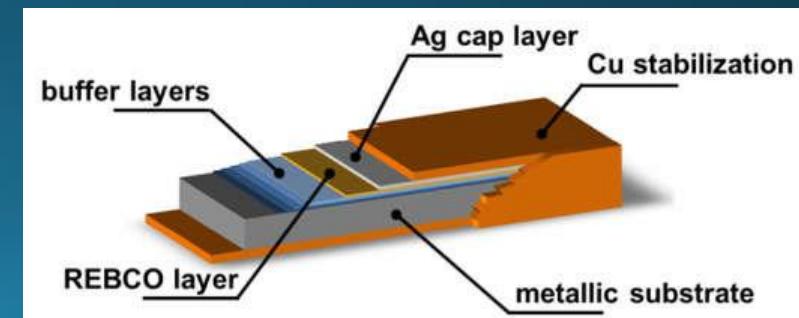
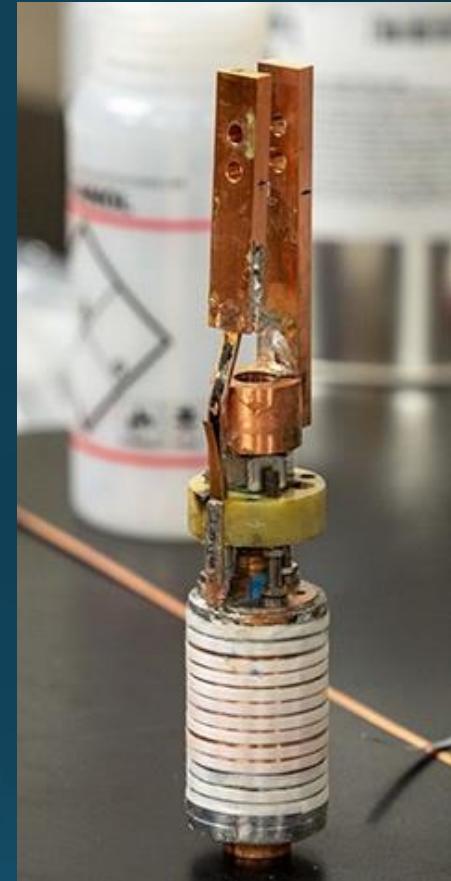
- can reach higher fields (critical field  $\sim 30\text{T}$ , max practical  $\sim 16\text{-}20\text{T}$ )
- very brittle – challenging to work with and cannot pull into wires
- how to form?
  - make composite wire of Nb filaments in Cu+Sn (bronze) matrix
  - wind your magnet
  - bake @  $650\text{-}700\text{C}$  to react Nb + Sn



ITER tokomak  
uses  $\text{Nb}_3\text{Sn}$

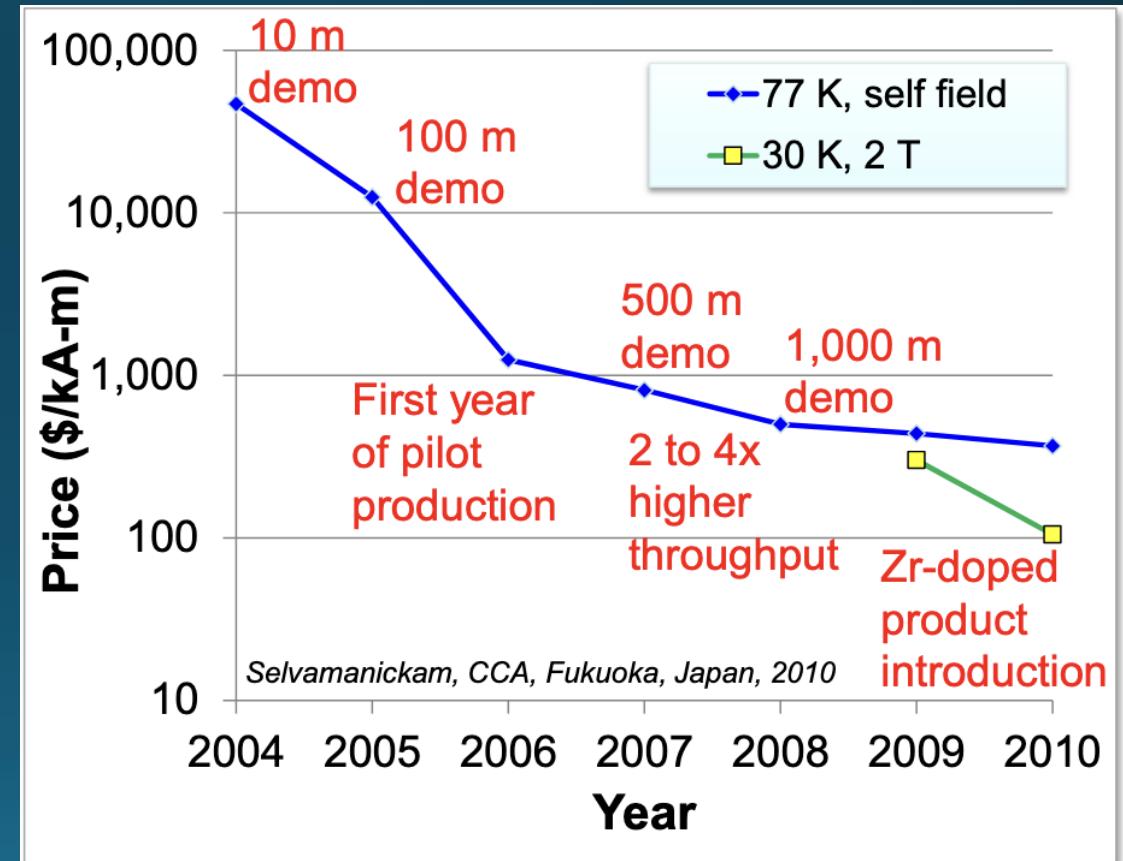
# Magnet materials (HTS)

- Rare Earth Barium Copper Oxide
  - e.g. BSCCO, YBCO
- can reach much higher fields (record: 48.7 T from Florida Mag Lab)
- can also operate at higher temperatures (e.g. operate with LN<sub>2</sub>)
  - can cool more to have higher current densities
- exist as tapes rather than wires – need different winding methods
- quenches are less well understood
- \$\$\$ (although prices are dropping!)



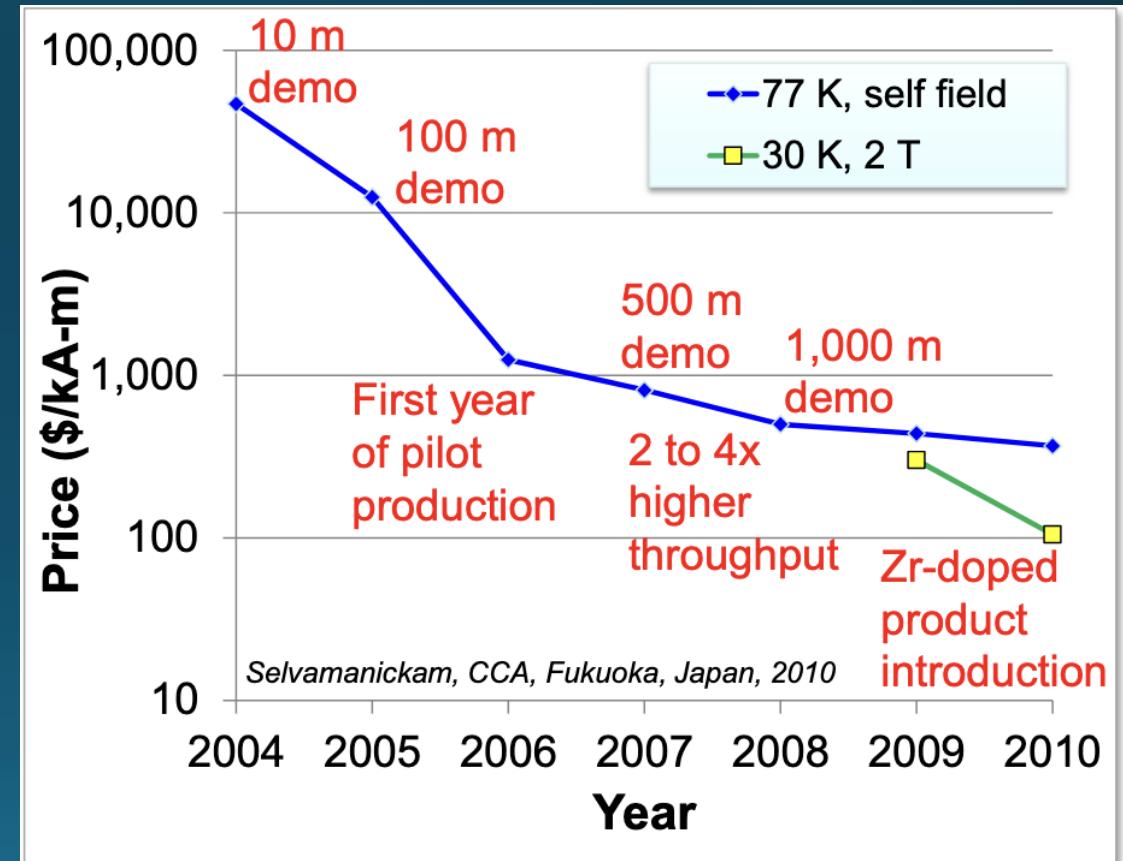
# Cost comparison...

- Cost given as USD/kA\*m
- Analysis from 1998
- 4K materials:
  - NbTi: \$1/(kA\*m)
  - Nb<sub>3</sub>Sn: \$8/(kA\*m)
- HTS:
  - ~\$800-1200/(kA\*m)
  - This analysis says that costs need to drop to ~\$10/(kA\*m) to be widely adopted



# Cost comparison...

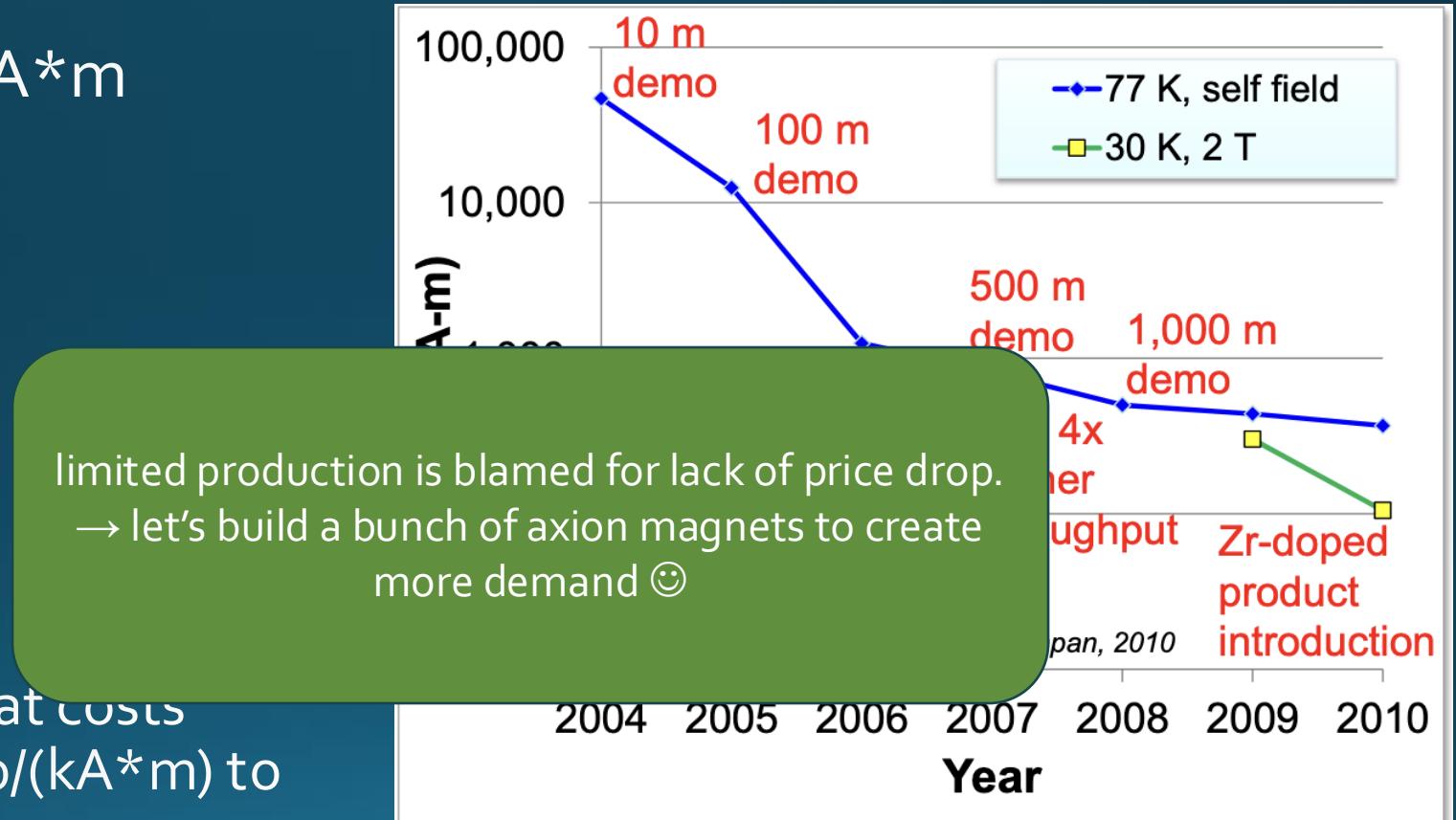
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2010 prediction for 2021: \$35/(kA\*m)  
actual 2021: \$200/(kA\*m)

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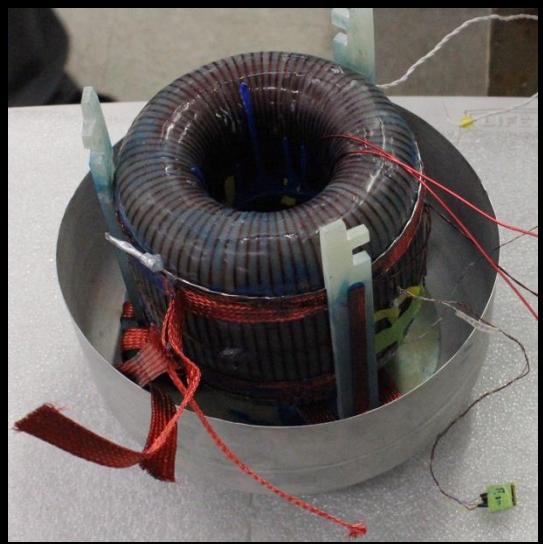


2010 prediction for 2021: \$35/(kA\*m)  
actual 2021: \$200/(kA\*m)

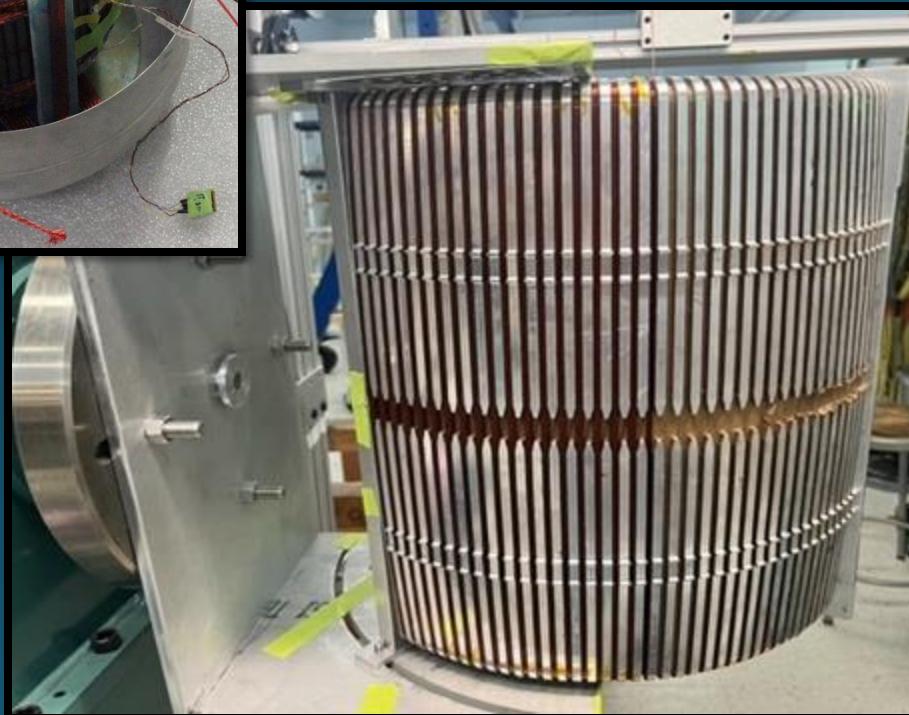
# DMRadio program NbTi magnets

ABRA-10cm

1T, 0.5 L toroid

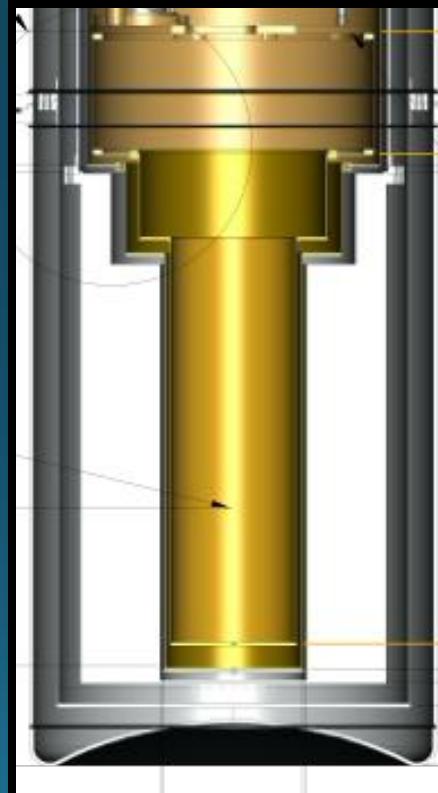


DMRadio-50L  
1T, 50 L toroid



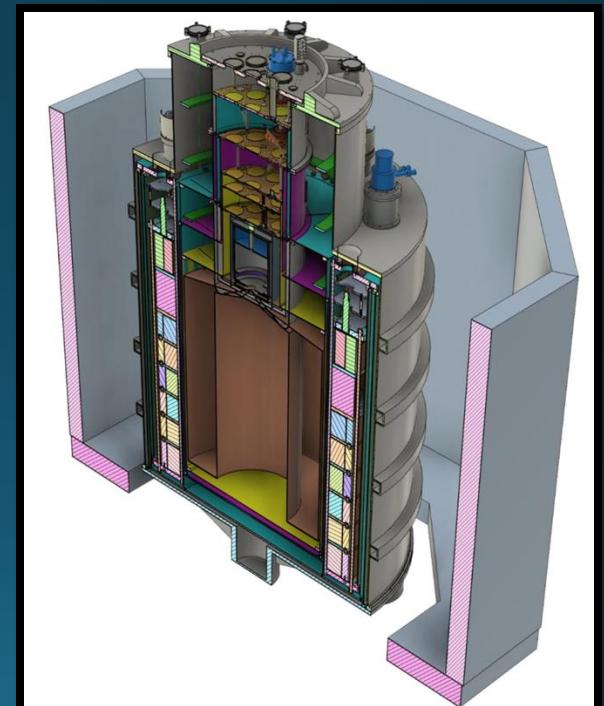
CAL

9T, 10 L solenoid



DMRadio-m<sup>3</sup>

~5T, 1000 L solenoid



# DMRadio-GUT magnet needs

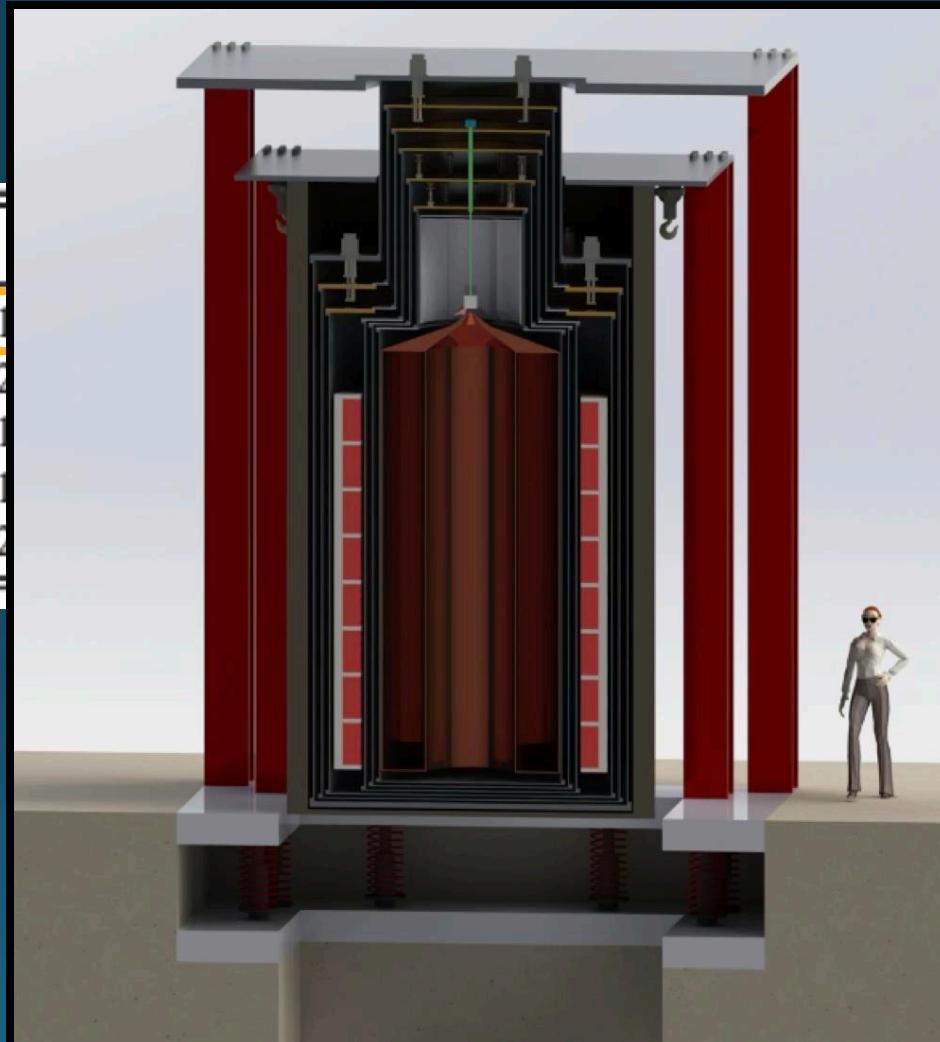
Scenario	$B_0$	$V$	$c_{PU}$	$Q$	$\eta_A$	$T$	Scan time
Baseline	16 T*	$10 \text{ m}^3$	0.1	$20 \times 10^6$	-20 dB	10 mK	6.2 years
Stronger magnet + higher noise	29 T	$10 \text{ m}^3$	0.1	$20 \times 10^6$	-5 dB	10 mK	3.2 years
Lower noise + lower volume	16 T	$8 \text{ m}^3$	0.1	$20 \times 10^6$	-25 dB	10 mK	7.3 years
Higher volume + lower $Q$	16 T	$17 \text{ m}^3$	0.1	$2 \times 10^6$	-20 dB	10 mK	10.6 years
Stronger magnet + lower $Q$	26 T	$10 \text{ m}^3$	0.1	$2 \times 10^6$	-20 dB	10 mK	8.9 years

Brouwer et al. Phys.Rev.D, 2022b

\*16 T peak/12 T RMS

# DMRadio-GUT magnet needs

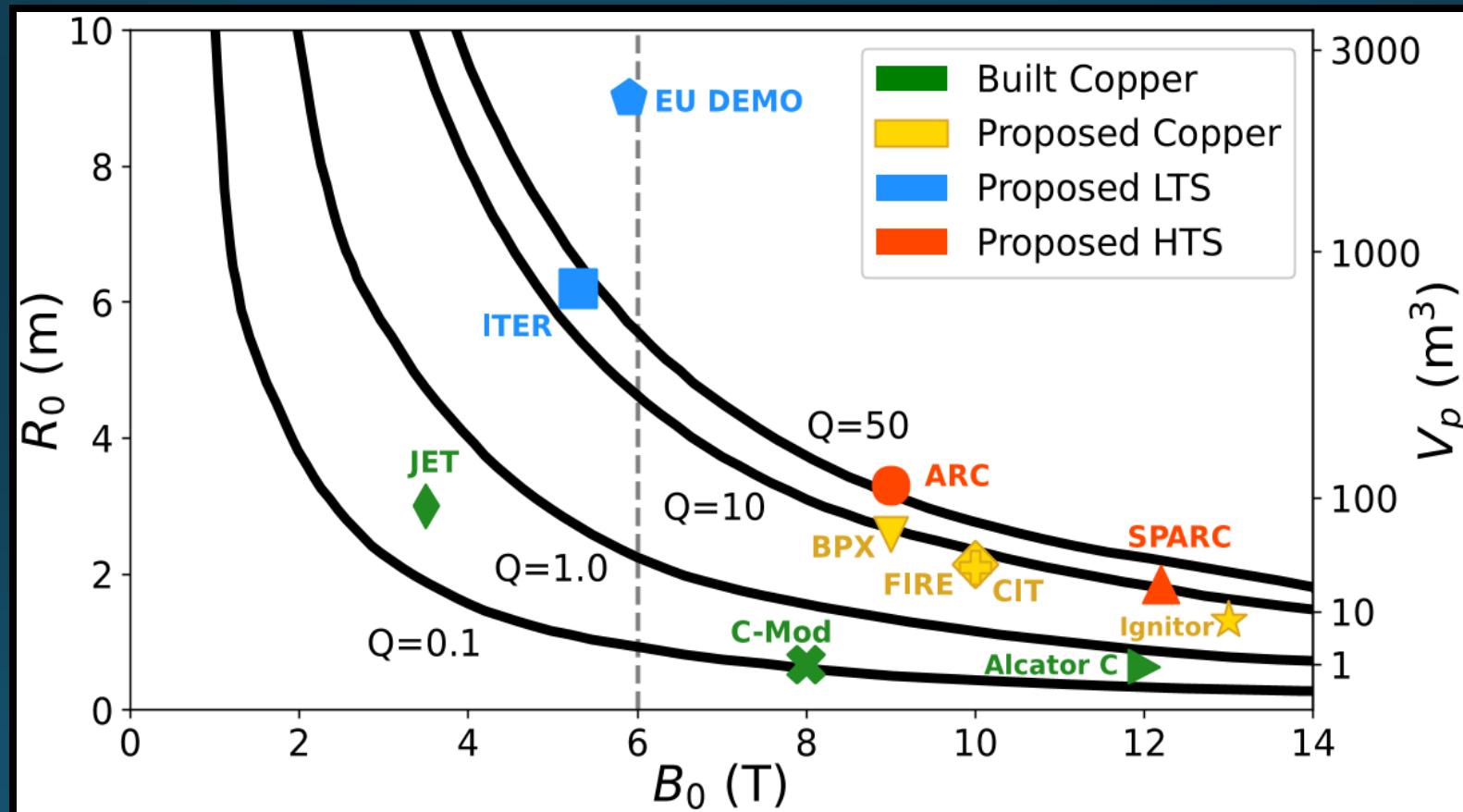
Scenario	
Baseline	1
Stronger magnet + higher noise	2
Lower noise + lower volume	1
Higher volume + lower $Q$	1
Stronger magnet + lower $Q$	2



$\eta_A$	$T$	Scan time
-20 dB	10 mK	6.2 years
-5 dB	10 mK	3.2 years
-25 dB	10 mK	7.3 years
-20 dB	10 mK	10.6 years
-20 dB	10 mK	8.9 years

Brouwer et al. Phys.Rev.D, 2022b

# R&D for large scale magnets is synergistic with fusion



Comparison to fusion magnets  
Creely et al. (SPARC)

# Technology 2: Tunable low-frequency resonators

$$\frac{d\nu}{dt} \propto c_{\text{PU}}^4 \frac{\cancel{Q} \left( B_0^2 V \cdot \cancel{V^{2/3}} \right)^2}{k_B T \eta}$$

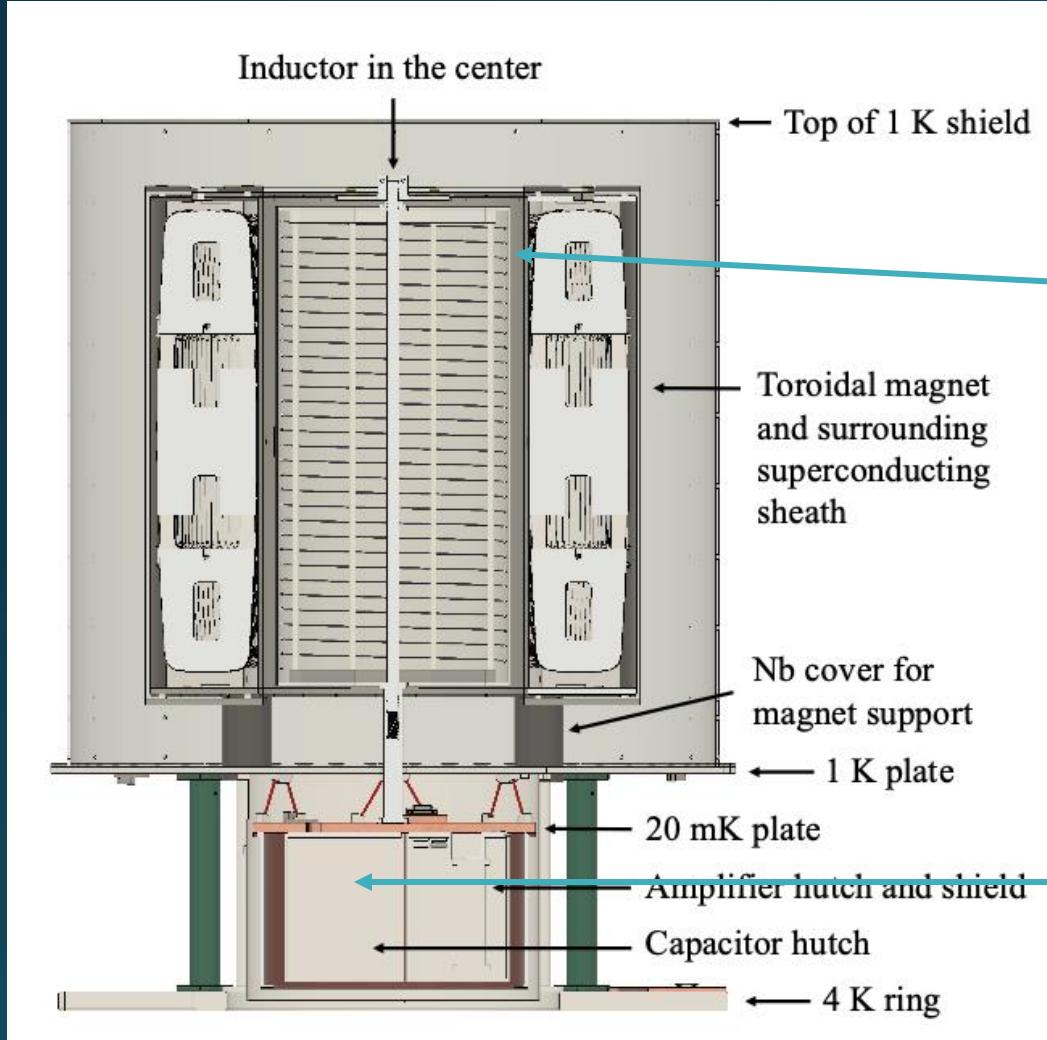
reduce resonator loss  
maximize axion-coupled inductance  
efficient axion-detector and internal transformer couplings

# Resonator needs

- Low loss/high Q
  - Best = superconducting (but unhappy\* in B fields)
  - Requires fastidious separation from outside environment
- Tunable
  - We need orders of magnitude in frequency—require multiple resonators and/or tuning elements
  - Different geometry for pickup and tuning elements depending on magnet geometry

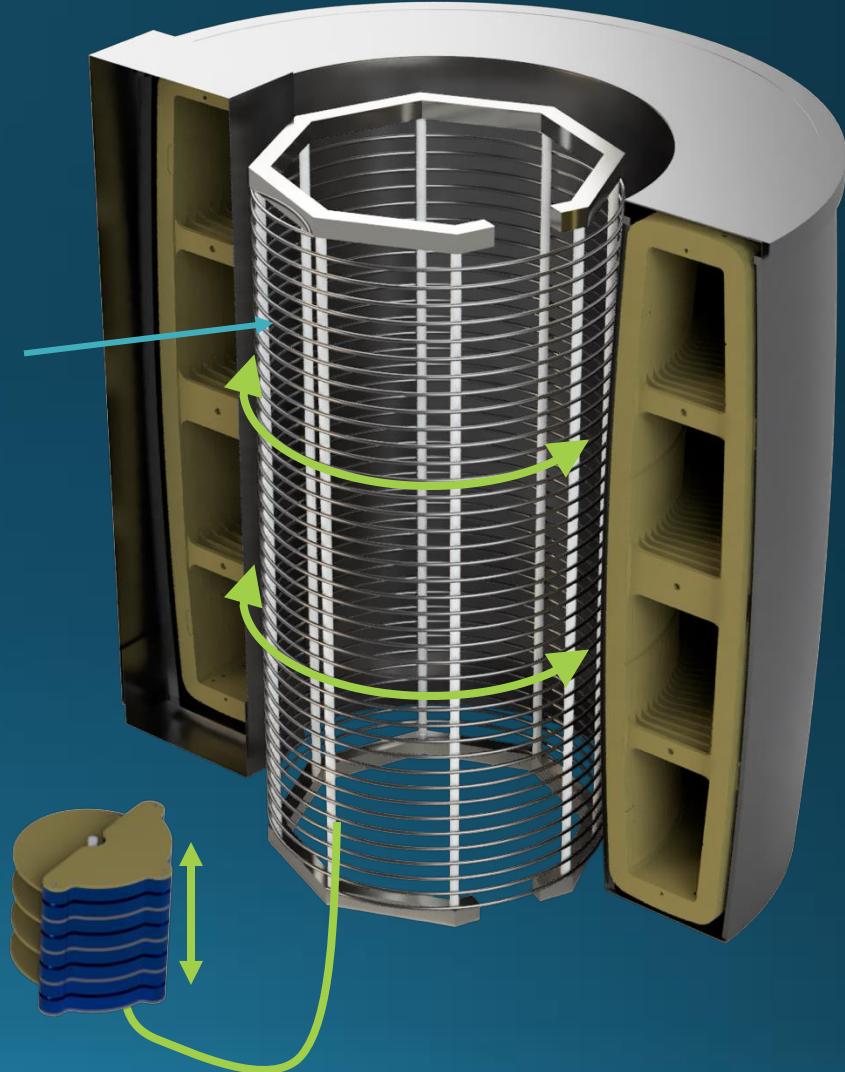
\*strength of tolerable B field depends on material

# Resonator for toroid



NbTi wound-wire inductor

tunable butterfly capacitor



# Challenge: reducing thermal load while maintaining high Q

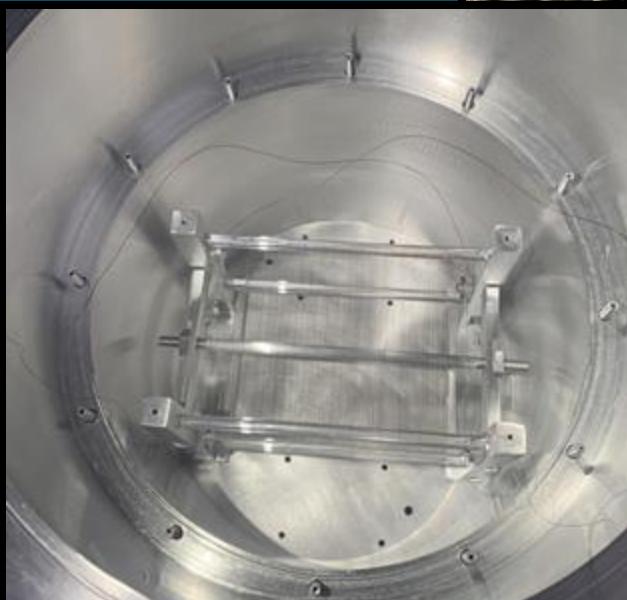
- Materials
  - Low  $\tan(\delta)$  dielectrics: sapphire  $\sim 2e-5$ , alumina  $\sim 1e-4$
  - Low participation
  - Eliminate wire insulation where possible
- Connections
  - Screw terminals for better superconducting connections
  - Reduce connections where possible
- Cool well below  $T_c$  to avoid quasiparticles
  - Indium at aluminum-sapphire interfaces for better thermalization
- Motion
  - Reduce friction at interfaces (materials choices, ball bearings)

# Very high-Q fixed-frequency resonator demonstration

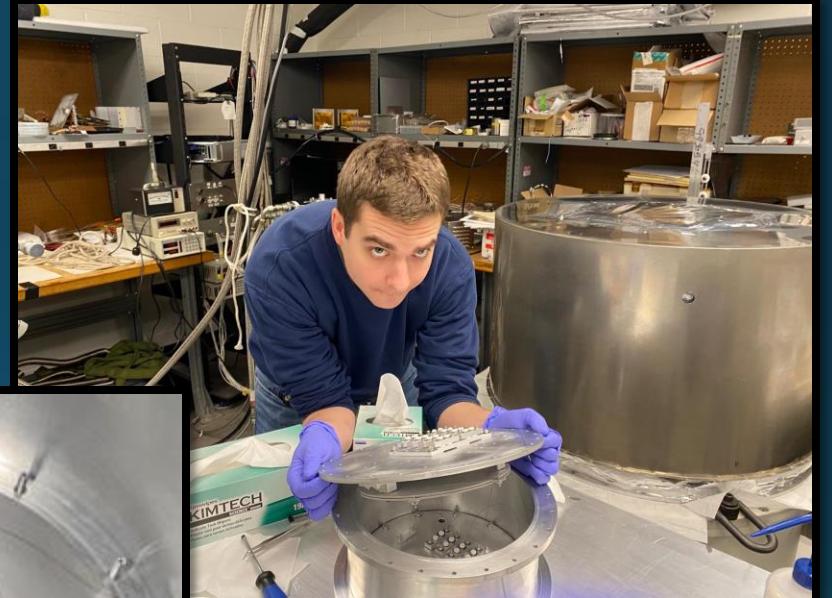
$Q \sim 2$  million at 254 kHz achieved at Princeton test stand



Al 1100 parallel-plate capacitor



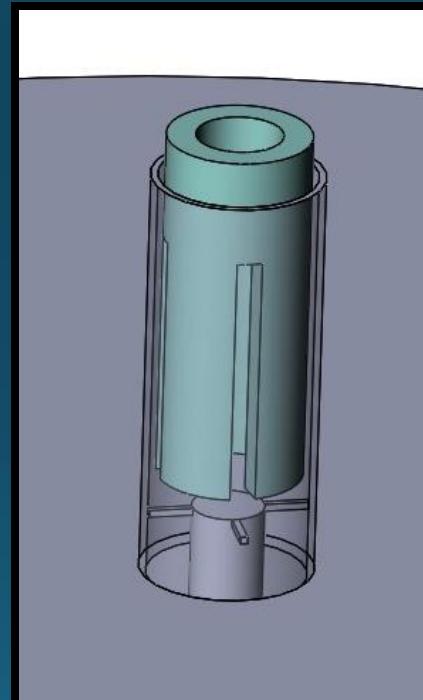
Tensioned NbTi wire on sapphire rods



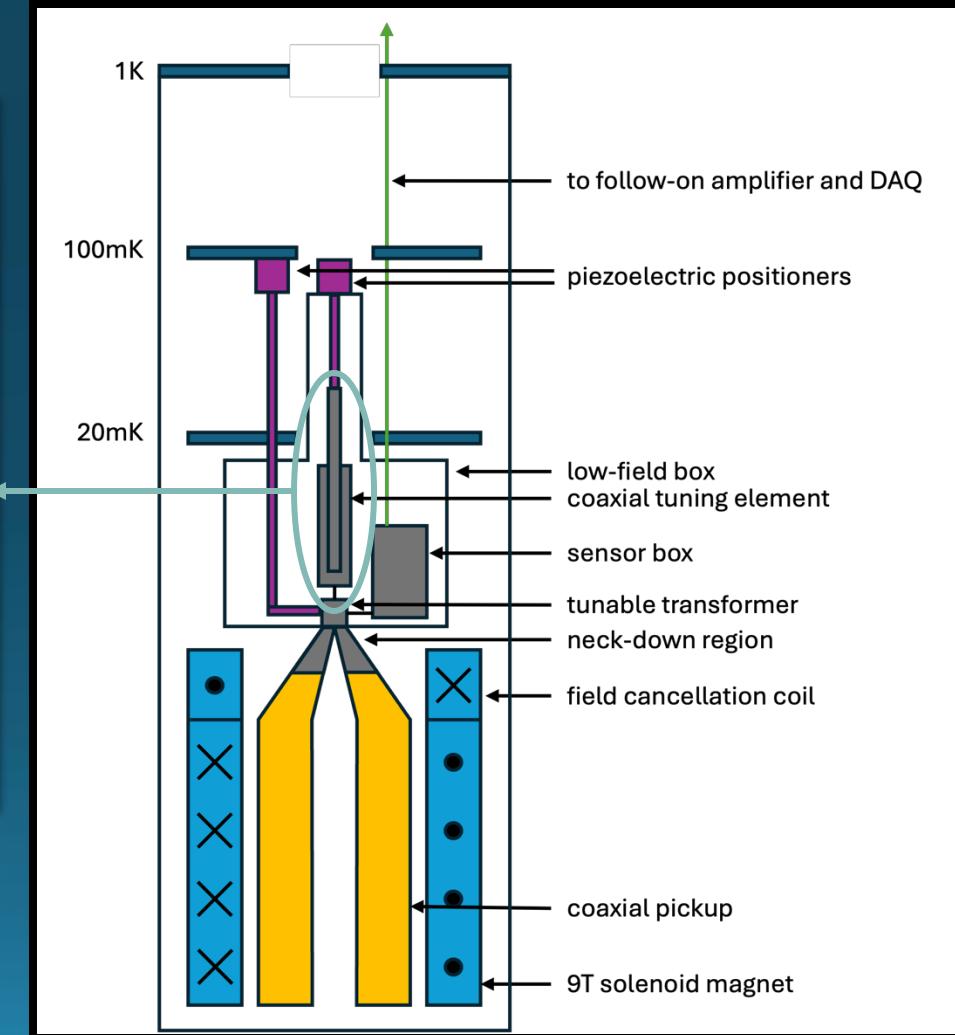
Roman Kolevatov closing up LC resonator apparatus

# Resonator for solenoid

- At high frequencies, a little bit of parasitic L or C can kill your sensitivity!
- Solution: coaxial pickup and tuning
  - Currents are fully enclosed – less loss
  - Analytically calculable impedance
- Similar thermal and Q considerations



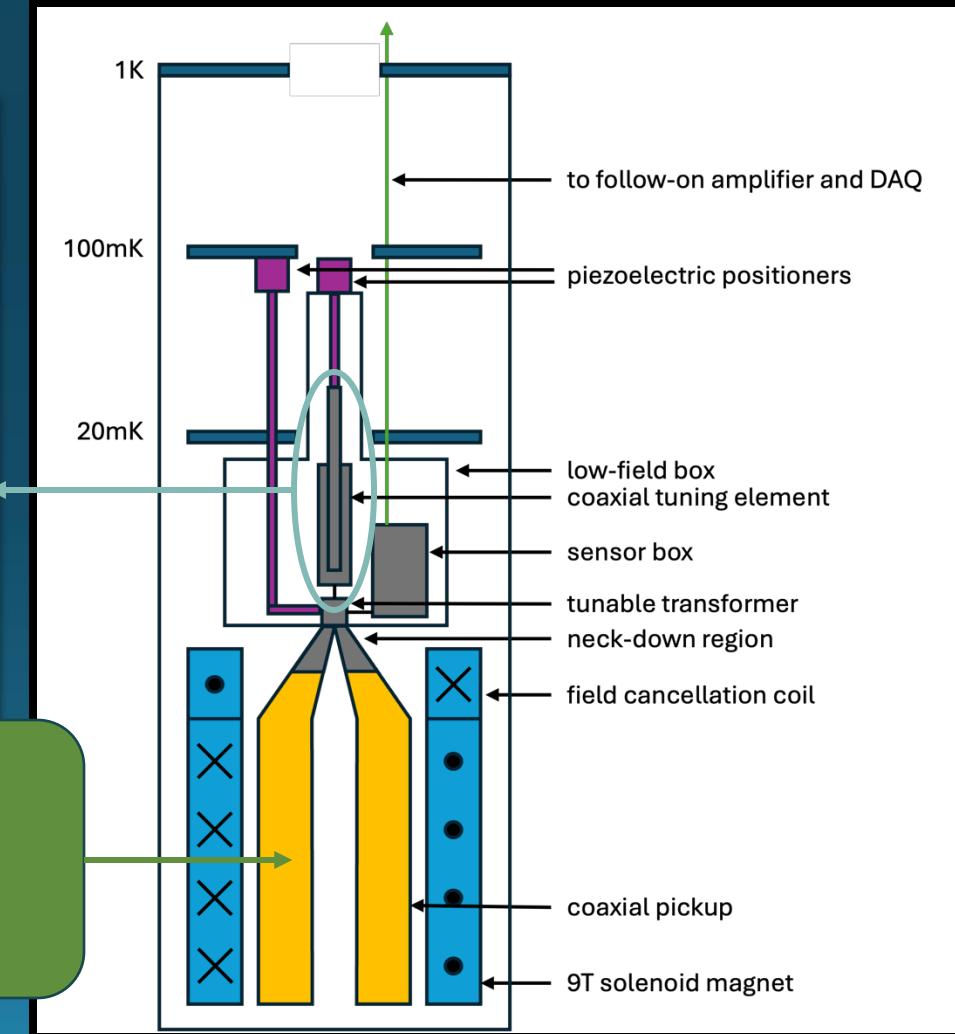
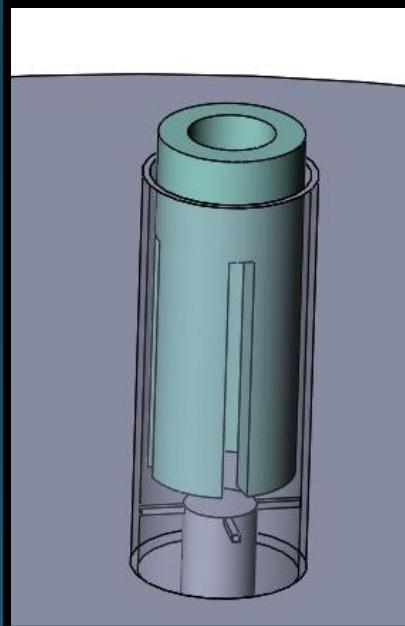
Coaxial tuner concept



# Resonator for solenoid

- At high frequencies, a little bit of parasitic L or C can kill your sensitivity!
- Solution: coaxial pickup and tuning
  - Currents are fully enclosed – less loss
  - Analytically calculable impedance
- Similar thermal considerations

Baseline material: high purity copper  
Possible upgrade: HTS  $\text{MgB}_2$   
 $H_{c2}(T=0\text{K}) \sim 13\text{-}18\text{ T}$   
 $H_{c1}(T=0\text{K}) \sim 0.03\text{ T}$

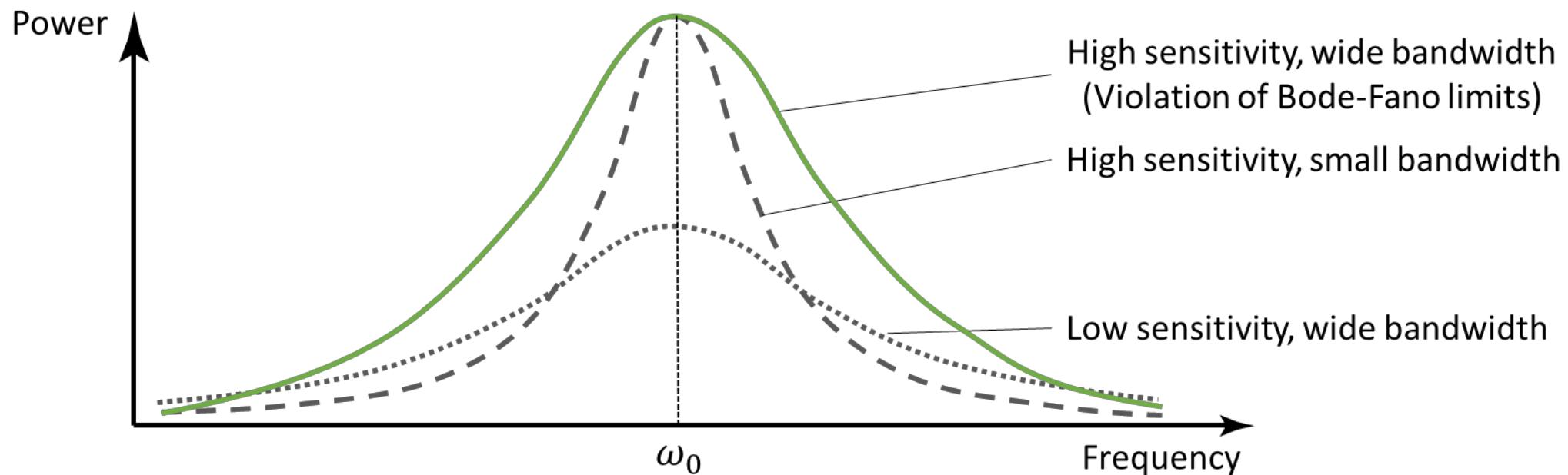


# Ambitious ideas: Bode-Fano evasion

# Bode-Fano Limits

- Bode-Fano limit: A complex load having energy storage elements limits the bandwidth of the match achieved by a matching network
- Criteria (assumptions): Passivity, Linearity, Time Invariance

Removing some of these assumptions could bypass the Bode-Fano limits



# Technology 3: Low-frequency quantum sensors

$$\frac{d\nu}{dt} \propto c_{\text{PU}}^4 \frac{Q (B_0^2 V \cdot V^{2/3})^2}{k_B T \eta}$$



beyond SQL  
amplifiers

# Technology 3: Low-frequency quantum sensors

$$\frac{d\nu}{dt} \propto c_{\text{PU}}^4 \frac{Q (B_0^2 V \cdot V^{2/3})^2}{k_B T \eta}$$



beyond SQL  
amplifiers

Next lecture!

# An alternative low-mass technique: Superconducting Radio-Frequency (SRF) cavities

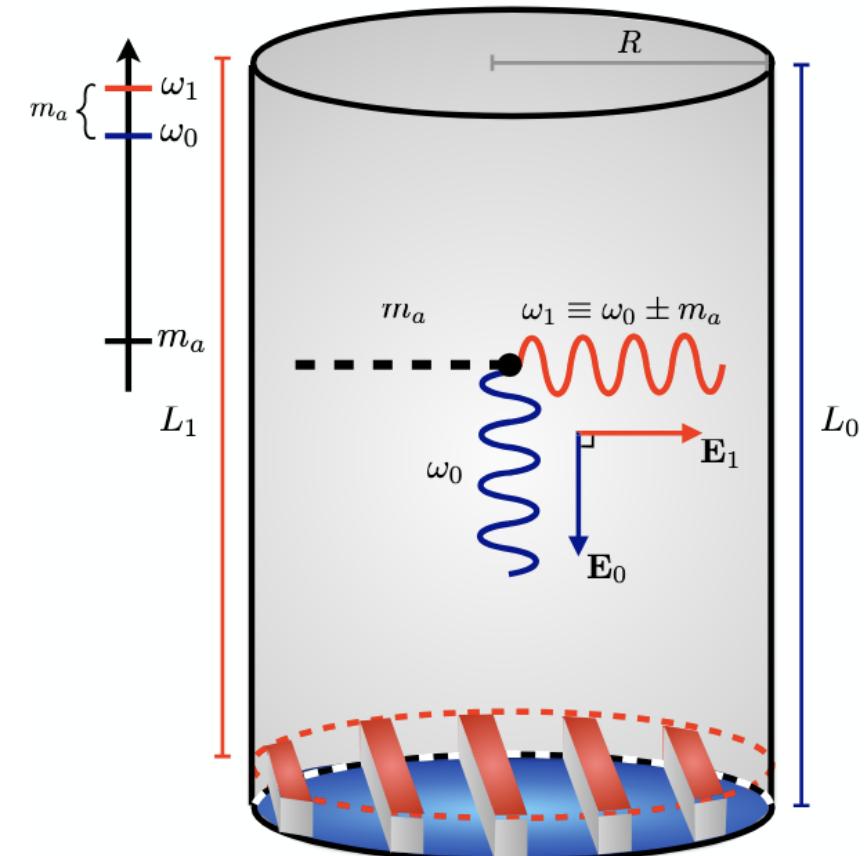
- Accelerator cavities can get Q factors  $\sim 10^{11}$



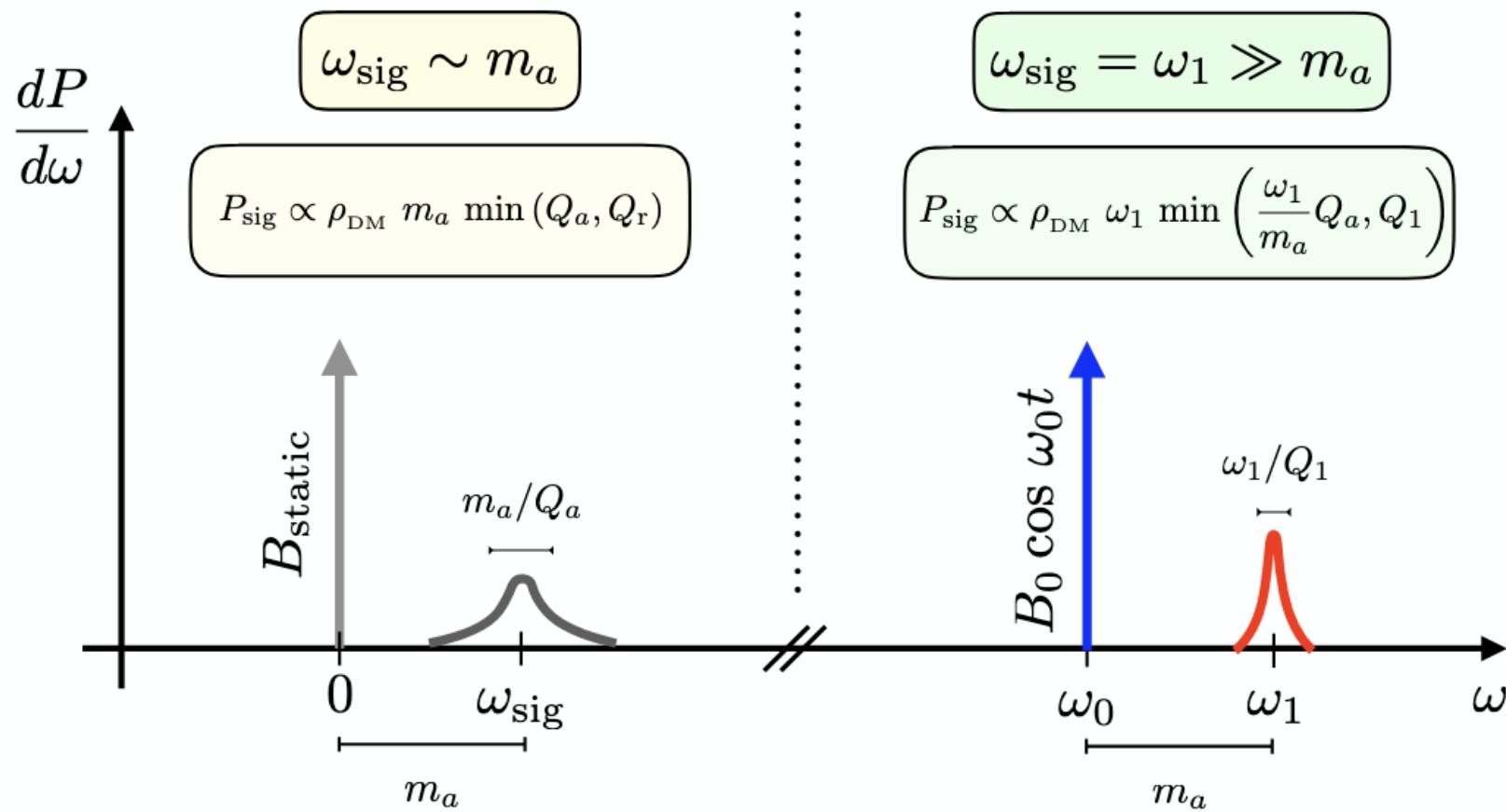
# An alternative low-mass technique: Superconducting Radio-Frequency (SRF) cavities

- Accelerator cavities can get Q factors  $\sim 10^{11}$
- Heterodyne approach
  - Drive GHz cavity mode,  $\omega_0$
  - Axion interacts, driving signal mode

$$\omega_1 = \omega_0 \pm m_a$$



# Method comparison



# SRF signal

$$P_{\text{sig}} \sim (g_{a\gamma\gamma}^2 \rho_{\text{DM}}) (B_0^2 V) (Q_1 / \omega_1)$$

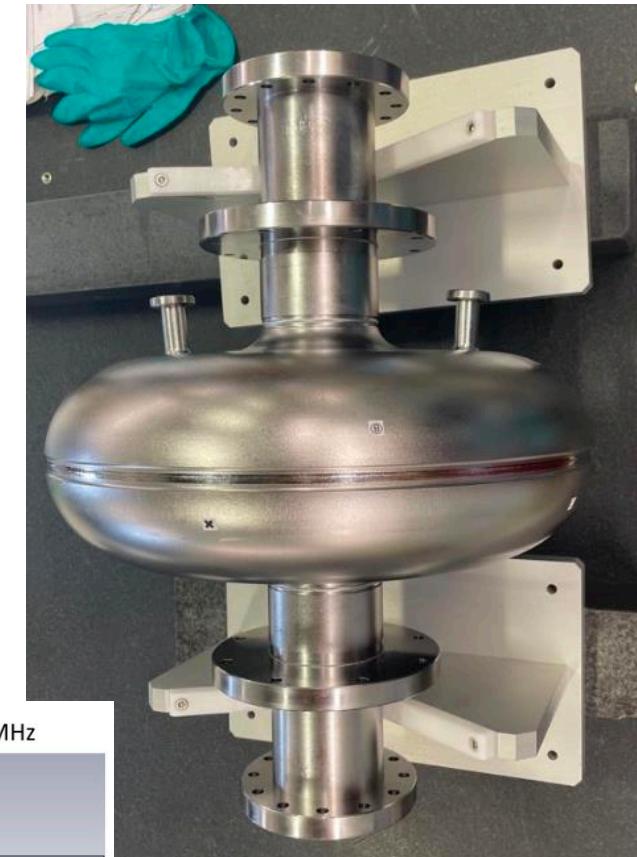
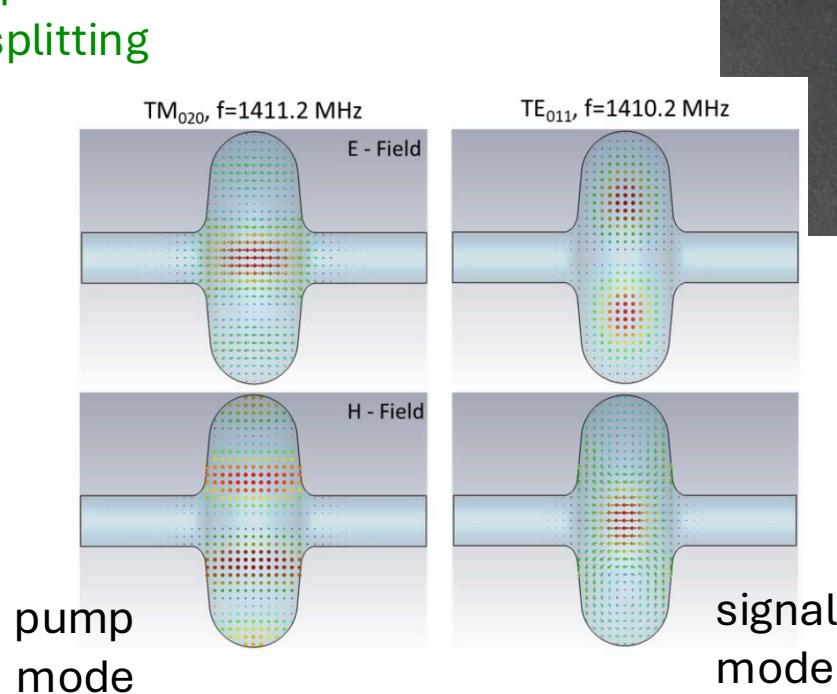
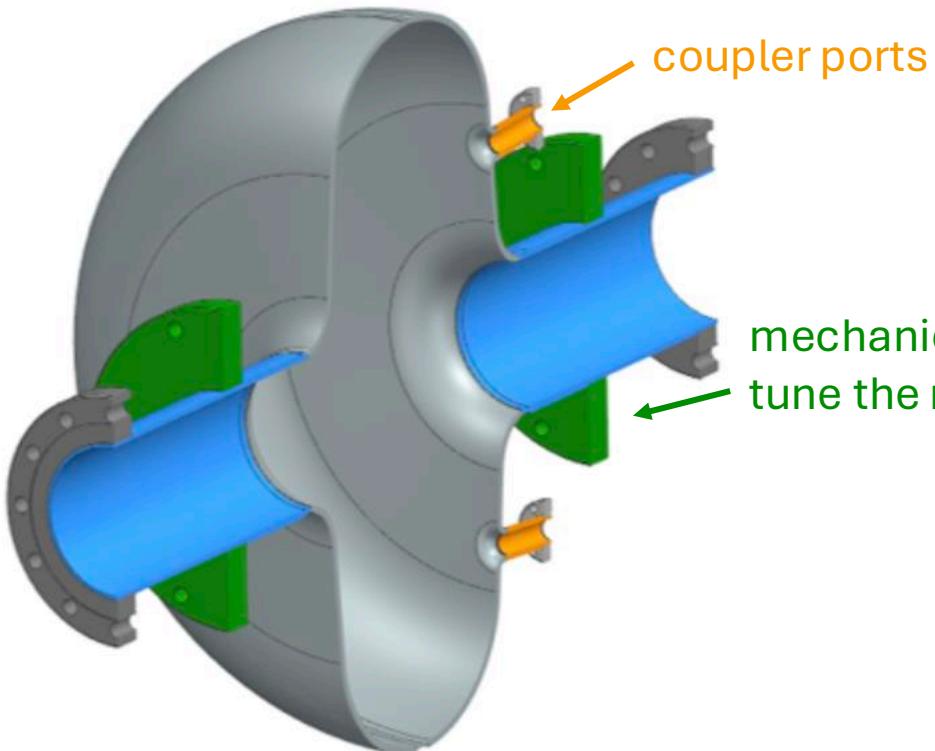
energy stored in driven mode

decay time of signal mode

Lower  $B_0$ , higher  $Q$  than lumped-element experiments

# In real life

SHADE (Superconducting Heterodyne Axion Dark matter Experiment)

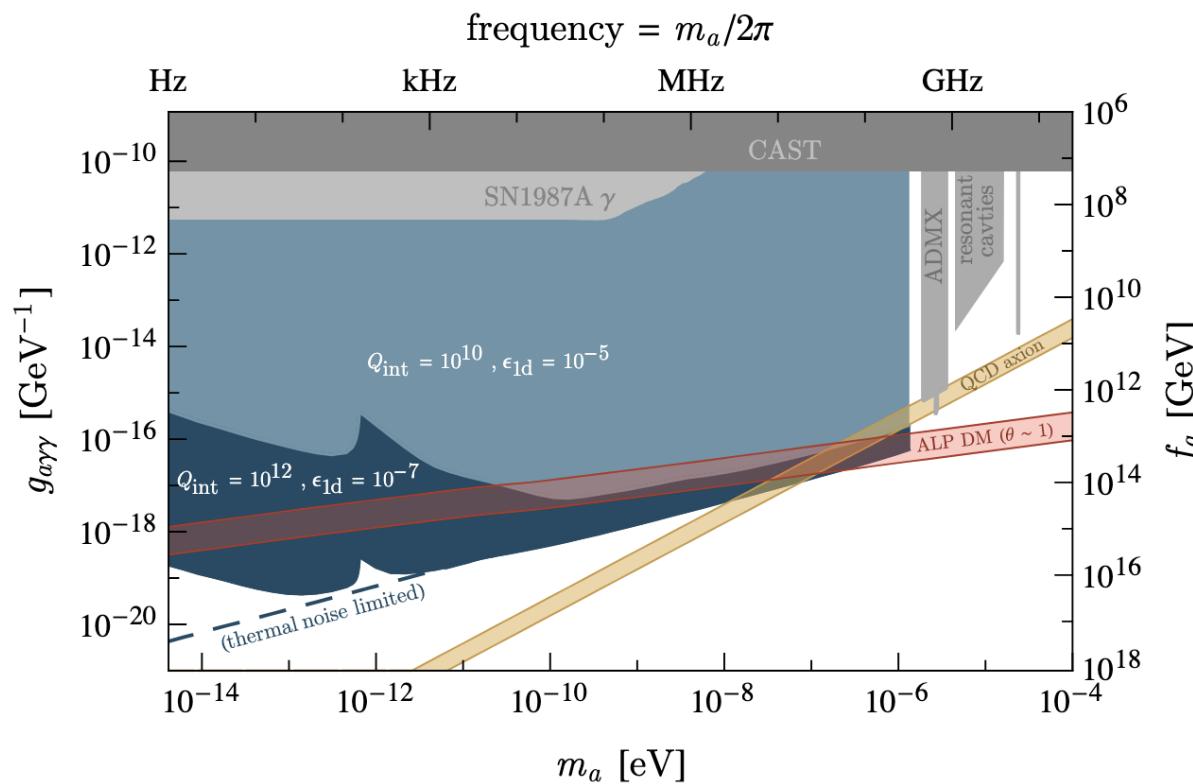


# Challenges

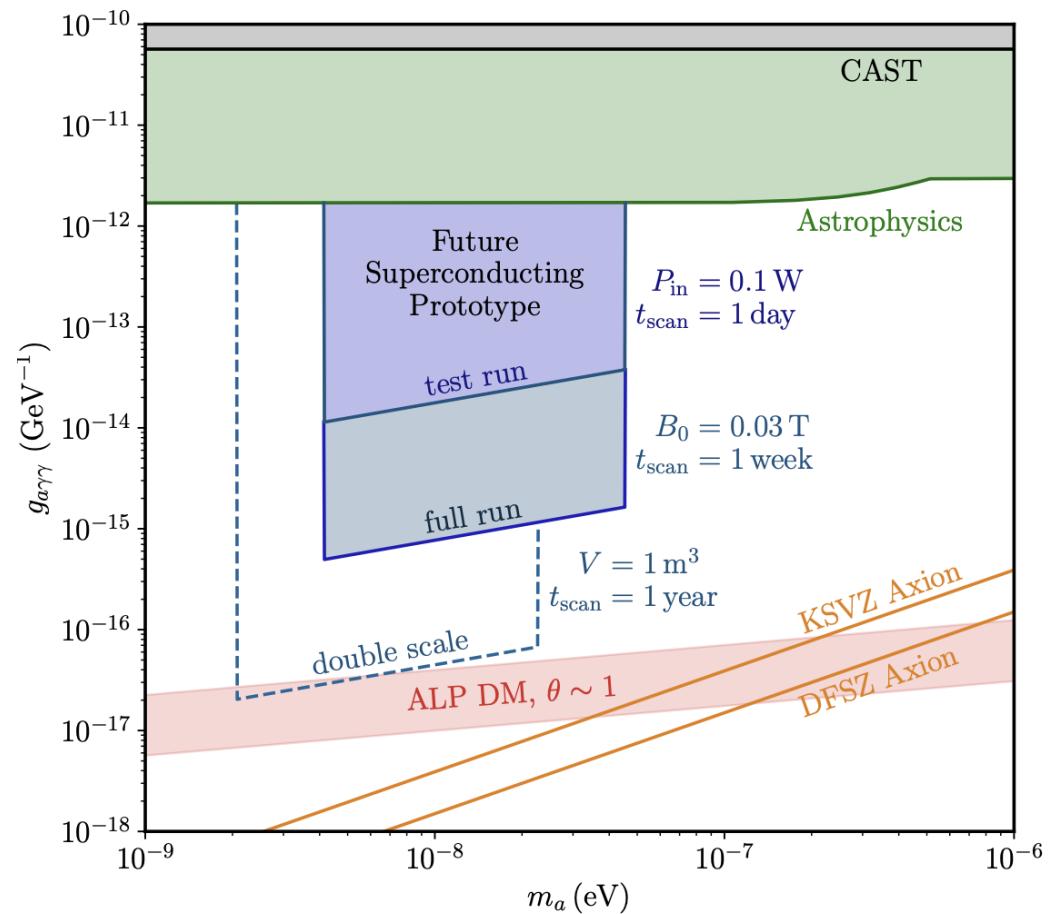
- Tuning reliability and calibration
- Mode leakage
- Vibrations/microphonics

# Reach

Initial theorist reach: *Berlin et al. 2020*



Updated experimentalist reach: *Li et al. 2025*



# Review of today

- Dark matter axion expected signal and detection regimes
- Low mass axion motivation
- Lumped-element detection with LC circuits
- Technology development for QCD axion reach with DM Radio
- Alternative low-mass method with SRF cavities