

Problem 1: Given a system $\frac{dx}{dt} = \begin{bmatrix} 0 & 1 & 2 \\ 0 & -2 & 3 \\ 0 & 0 & 0 \end{bmatrix} x + \begin{bmatrix} 1 \\ 1 \\ 0 \end{bmatrix} u$ **and the vector output**

$$y = \begin{bmatrix} 0 & 1 & 0 \end{bmatrix} x + 2u$$

- What are the eigenvalues of matrix A?
- Compute the transfer function G(s).
- Find the pole(s) of the transfer function.
- Explain the difference you see between the eigenvalues of A and the poles of the system.
- Is the system BIBO stable? Why?

Problem 2: If the output of the system in problem 1 is changed into $y = \begin{bmatrix} 1 & 0.5 & 0 \end{bmatrix} x$

- What is the new transfer function?
- Find the poles.
- Is the system with new output still BIBO stable? Why?
- Compare the BIBO stability of the systems from both problems. Explain why they are identical/different.