

Bachelor thesis Computer Science Dynamic Event Detection in Data Streams

Author	David Pacassi Torrico Daniel Milenokvic
Main supervisor	Andreas Weiler
Sub supervisor	Kurt Stockinger
Date	

Zurich University of Applied Sciences



DECLARATION OF ORIGINALITY

Bachelor's Thesis at the School of Engineering

By submitting this Bachelor's thesis, the undersigned student confirms that this thesis is his/her own work and was written without the help of a third party. (Group works: the performance of the other group members are not considered as third party).

The student declares that all sources in the text (including Internet pages) and appendices have been correctly disclosed. This means that there has been no plagiarism, i.e. no sections of the Bachelor thesis have been partially or wholly taken from other texts and represented as the student's own work or included without being correctly referenced.

Any misconduct will be dealt with according to paragraphs 39 and 40 of the General Academic Regulations for Bachelor's and Master's Degree courses at the Zurich University of Applied Sciences (Rahmenprüfungsordnung ZHAW (RPO)) and subject to the provisions for disciplinary action stipulated in the University regulations.

City, Date:	Signature:

The original signed and dated document (no copies) must be included after the title sheet in the ZHAW version of all Bachelor thesis submitted.

${\bf Contents}$

T	Abs	stract	4
2	Int r 2.1	roduction Problem formulation	5
	$\frac{2.1}{2.2}$	Motivation	5
	$\frac{2.2}{2.3}$	Related papers	5
	2.3	Related papers	Ü
3	Met	thod	6
	3.1	Test Data	6
	3.2	Clustering method	6
		3.2.1 HDBSCAN	6
		3.2.2 K-means	6
		3.2.3 Preprocessing	6
		3.2.4 Scoring function	6
	3.3	Online Clustering	9
		3.3.1 Finding pairs clusters	9
			10
4	Imp	plementation	11
	4.1	Evaluation Framework	11
	4.2	Online Clustering	11
5	Res	sults	12
	5.1	Clustering method	12
			12
		•	12
			16
	5.2		16
6	Cor	nclusion	18
	6.1	Summary	18
	6.2	·	18
	6.3		18
7	Apr	pendix	19
			19

1 Abstract

How can events be recognized in a data streams? And what is the definition of an event? Current event recognition procedures define possible events (or event types) statically when the system starts. However, in data streams, the definition should develop dynamically over time as the data and their focus changes over time.

The first goal of this bachelor thesis is to define what an event is and how events can be recognized from static data. Depending on the definition, a suitable dataset has to be found and chosen in order to create a system which is capable of recognizing events. In the second part, the events should be recognized from a data stream and therefor support dynamic event recognition.

This work uses news API's as data streams and tries to assign the received news articles to different events. An event is defined as a list of different news articles writing about the same story. A possible event could be "Brexit" or an upcoming election. It's important to keep in mind that new events can and should be created over time.

Assigning news articles to an event can be done by clustering the news articles. In order to achieve best possible results, a comparison between different clustering techniques has been completed. It was revealed that HDBSCAN is a promising candidate for our use case as it delivered the best results.

Unfortunately HDBSCAN was not made for data coming from data streams but this thesis will show one possible solution on how to deal with this. This work was able to process up to 20'000 news articles with HDBSCAN. A possible continuation of this work could try to extend this number to process more data at once.

2 Introduction

2.1 Problem formulation

What problem do we solve?

2.2 Motivation

Why do we do this? Who might benefit from our work?

2.3 Related papers

Which papers were already published in this regard? Why are they not suitable for our use case?

3 Method

TODO introductionary paragraph

3.1 Test Data

The first important step is to create a test data set to run the evaluations with and verify them.

TODO explain the source and structrue

3.2 Clustering method

Clustering finds similarities in different news articles based on their content and groups them together, while unrelated news are regarded as noise. The challenge now araises to find an appropriate clustering method, which is able to work with data of varying densities and of high dimensionality.

TODO why hdbscan

3.2.1 HDBSCAN

HDBSCAN is a hierarchical density-based clustering algorithm [?]. It extends the well known [insert citation] DBSCAN algorithm and reduces its sensitivity for clusters of varying densities. Another important quality of HDBSCAN is, that it does not need to know the number of clusters up front.

TODO explain some more

3.2.2 K-means

KMeans is a centroid-based clustering algorithm.

TODO explain some more

3.2.3 Preprocessing

3.2.4 Scoring function

The scoring function is essential for measuring the result of a clustering method. The score should reflect the quality of the individual clusters and of the clustering as a whole. The number of existing measures for clustering is vast and can be split into two main categories. Internal measures determine the score based on criteria derived from the data itself and external measures depend on criteria non-existent in the data itself such as class labels. Since the ground truth is known in our test data, we are going to apply an external measure. Initially we used Normalized Mutual Information (NMI) as our primary scoring function. The NMI is a entropy-based measure and tries to quantify the amount shared information between the clusterings. The score proved to work well for our initial evaluations, but upon closer inspection certain anomalies were found. An example is given in table 1, where K-means achieved a rather high score, regardless of the significant difference between the true amount of clusters and the approximation using \sqrt{n} .

TODO add number of estimated clusters

Algorithm	Sample Size	NMI	n_{true}	$\mid n_{\mathrm{true}} - n_{\mathrm{predicted}} \mid$
k-means	19255	0.754	600	457
hdbscan	19255	0.742	600	2

Table 1: K-Means has a higher NMI score than HDBSCAN, while having a much larger difference in number of clusters.

Other scoring functions such as V-Measure or the Adjusted Rand Index showed similar unexpected results with different clusterings. Therefore we decided to develop our own scoring function based on the ideas of Maximum Matching and the jaccard index.

TODO find citations

Calculating the score The scoring function first calculates the similarity between pairs of clusters, where each cluster belongs to a different clustering. We use the jaccard index to measure the similarity, which is defined as

$$\frac{|A \cap B|}{|A \cup B|} \tag{1}$$

To illustrate the process we start with an example. We use T and C as our clusterings, where T is the ground truth and C is the predicted clustering. The clusterings are defined as follows:

$$T = \{\{1, 2, 3\}, \{4, 5, 6, 7\}, \{8, 9\}\}$$
$$C = \{\{1, 2\}, \{3, 4, 5, 6\}, \{7\}, \{8, 9\}\}$$

We calculate the similarity as defined in Equation 1, for each possible pair between T and C starting with $t_1 = \{1, 2, 3\}$ and $c_1 = \{1, 2\}$:

$$similarity(t_1, c_1) = \frac{|t_1 \cap c_1|}{|t_1 \cup c_1|} = \frac{|\{1, 2\}|}{|\{1, 2, 3\}|} = \frac{2}{3} = 0.667$$

After doing this for each possible pair we get the similarity matrix A:

$$A = \begin{pmatrix} similarity(t_1, c_1) & \dots & similarity(t_1, c_4) \\ \vdots & \vdots & \vdots & \vdots \\ similarity(t_3, c_3) & \dots & similarity(t_3, c_4) \end{pmatrix} = \begin{pmatrix} 0.667 & 0.167 & 0 & 0 \\ 0 & 0.6 & 0.25 & 0.4 \\ 0 & 0 & 0 & 1.0 \end{pmatrix}$$

As a next step we have to select the most relevant similarity values from each row of the similarity matrix.

Finding relevant values in the similarity matrix non-trivial, since clusters do not share labels across different clusterings. To solve this, we make two assumptions:

- 1. The higher the similarity between two clusters, the more likely it is, that both clusters are describing the same group of documents.
- 2. Each cluster can be associated with a cluster from another clustering only once.

Based on those assumptions we select the highest similarity value per row, whose column is not already associated with another row. Applying this selection function f to our previously calculated similarity matrix A results in the set containing the most relevant similarity values.

$$f(A) = \begin{pmatrix} \mathbf{0.667} & 0.167 & 0 & 0 \\ 0 & \mathbf{0.6} & 0.25 & 0.4 \\ 0 & 0 & 0 & \mathbf{1.0} \end{pmatrix} = \{0.667, 0.6, 1\}$$

As we can see, there were no collisions between columns and we simply get the highest value per row. Consider the following example with an similarity matrix B, which does contain a collision:

$$f(B) = \begin{pmatrix} \mathbf{0.75} & 0.375 & 0.427 & 0.375 \\ 0.4 & \mathbf{0.667} & 0.571 & \mathbf{0.8} \\ 0.333 & 0.25 & 0.4 & \mathbf{1.0} \end{pmatrix} = \{0.75, 0.667, 1\}$$

The selected similarity for the second row is 0.667 instead of 0.8. This is because the fourth column is already associated with the third row, while having an similarity greater than 0.8. Therefore based on our assumption that clusters cannot be associated twice, the second highest similarity is used for the second column. In case no association could be found, the value would be set to zero. The full algorithm for the selection process can be found in the appendix as listing 1.

As a final step the average is calculated from the sum of the similarity with respect to the difference in predicted clusters to the true amount of clusters. In case the predicted amount is lower a normal average will already result in a lower score, since each real cluster without a matching predicted cluster counts as zero. However if there are more predicted clusters than true ones, each true cluster will have a value and the score would appear the same as if there was a perfect prediction in the amount of clusters. To take this into account, the difference is added to the number of true clusters as shown in Equation 2.

$$\frac{s_{similarity}}{c_{true} + max(0, c_{predicted} - c_{true})} \tag{2}$$

Where $s_{similarity}$ is the sum of the similarity values, $c_{predicted}$ is the number of predicted clusters and c_{true} is the number of true clusters. Using our previously selected similarity values $S = f(A) = \{0.667, 0.6, 1\}$ with $c_{true} = 3$ and $c_{predicted} = 4$, the calculation for the final average would be done as follows:

$$score = \frac{\sum_{i=1}^{|S|} S_i}{c_{true} + max(0, c_{predicted} - c_{true})}$$

$$= \frac{0.667 + 0.6 + 1}{3 + max(0, 4 - 3)} = \frac{2.267}{3 + max(0, 1)}$$

$$= \frac{2.267}{3 + 1} = \frac{2.267}{4}$$

$$= \mathbf{0.567}$$

The final score for the evaluation of the predicted cluster C with the true cluster is 0.567.

-	Test scenarios with ground truth $T = \{\{1, 2, 3\}, \{4, 5, 6, 7\}, \{8, 9\}\}$							
Nr.	Predicted Clustering C	NMI	ARI	M-Score				
1	$C = \{\{1, 2, 3\}, \{4, 5, 6, 7\}, \{8, 9\}\}$	1.0	1.0	1.0				
2	$C = \{\{1, 2\}, \{3, 4, 5, 6\}, \{7, 8, 9\}\}\$	0.564	0.308	0.644				
3	$C = \{\{1, 2, 3\}, \{4, 5, 6\}, \{7\}, \{8, 9\}\}\$	0.895	0.771	0.688				
4	$C = \{\{1, 2, 3\}, \{4, 5\}, \{6, 7\}, \{8\}, \{9\}\}$	0.821	0.591	0.467				
5	$C = \{\{1\}, \{2\}, \{3\}, \{4\}, \{5\}, \{6\}, \{7\}, \{8\}, \{9\}\}\}$	0.651	0	0.12				
6	$C = \{\{1, 2, 3, 4, 5\}, \{6, 7, 8, 9\}\}$	0.434	0.182	0.367				
7	$C = \{\{1, 2, 3, 4, 5, 6, 7, 8, 9\}\}\$	0.0	0	0.148				
8	$C = \{\{7, 2, 4\}, \{8, 9, 6, 3\}, \{1, 5\}\}$	0.219	-0.108	0.383				

Table 2: Direct comparison of different scoring functions

Comparison against other measures The test scenarios in table 2 show the resulting scores of our similarity score, NMI and completeness. It is important to note that NMI and completeness work with cluster labels assigned to each document, instead of considing elements inside a single cluster. This means the clustering will be flattened into one dimension, where each document is assigned the label of the cluster it appears in. The array containing the labels for the first scenario would look as follows: C = [1, 1, 1, 2, 2, 2, 2, 3, 3].

As a final note, repeating the evaluation shown in table 1 a second time using the average similarity per clustering, the score (Table 3) for K-means is much lower than HDBSCAN. This reflects what we would expect based on the big difference in the amount of predicted clusters.

Algorithm	Sample Size	Similarity	n_{true}	$\mid n_{\mathrm{true}} - n_{\mathrm{predicted}} \mid$
k-means	19255	0.137	600	457
hdbscan	19255	0.605	600	2

Table 3: The similarty score reflects the difference in number of predicted clusters.

3.3 Online Clustering

Detecting events in a stream of news articles will be achieved by using an online clustering approach. The events of interest for this application are the discovery of new topics and the extension of existing topics. Thus we define our two events as follows:

- Topic added: A new cluster of news articles appears in the data stream.
- Topic extended: An existing topic is extended by additional news articles.

HDBSCAN will be applied as the clustering method, using the optimal settings as discovered in the preivous evaluation. Additional preprocessing of news articles before clustering is going to be explored as part of evaluation as well and will be implemented accordingly for the online clustring.

Since HDBSCAN only supports static datasets, the clustering will be done in batches using a time based sliding window approach. Events are detected by comparing the resulting clusters with the previous ones.

3.3.1 Finding pairs clusters

To be able to compare clusters of different batches with each other, we have to find pairs of clusters between batches, which describe the same topic. This is done by applying the same assumptions as for the scoring function used in the evaluation. Therefore clusters are paired based on their similarity

calculated with the jaccard index as shown in equation 1. If the similarity is above a certain threshold, both clusters are seen as describing the same topic.

3.3.2 Sliding window

An important consideration for determining existing or new clusters is the overlap of samples between batches. If the overlap is too small, similar clusters will no longer be detected as such, which would result in an increasingly high error rate. Finding optimal values for the step size between batches and the number of samples for each batch is therefore essential for our online clustering approach.

4 Implementation

4.1 Evaluation Framework

The evaluation process is done with our own evaluation framework. The framework allows for automated and repeatable evaluation runs. Results are stored in a database for later analysis. The main features include:

- Defining the number of stories to run the evaluation with and load all news articles from those stories.
- Repeating evaluation runs with different sets of data.
- Providing different vectorizers for converting the textual data into a vector space model.
- Defining a range for each parameter of a clustering method and running it with each possible combination of those parameters.
- Storing the result the result in a database and creating relations between news articles, clusters and evaluation runs. This allows for manual inspection and analysis of individual articles inside a predicted cluster.

The implementation is done with Python. Clustering methods and vectorizers are provided by the Scikit-learn library. We decided to use Scikit-learn because of its rich documentation, the wide range of tools and algorithms it provides for clustering and our previous experience with it. Additionally the framework runs in a fully dockerized environment, which includes the database. This makes it very easy to run locally or on a server.

4.2 Online Clustering

- * Near duplicate detection for clusters with MinHash and LSH $O(\log n)$ * source https://towardsdatascience.com/uslocality-sensitive-hashing-49f6d1f6134
- * simulate an dynamic stream from our static dataset

5 Results

5.1 Clustering method

The goal of this evaluation is to measure the accuracy of HDBSCAN, with different parameters and preprocessing methods. The most suitable approach will then be used for the online clustering to detect changes in a news stream.

5.1.1 Setup

Text Preprocessing The first step in working with text is to apply Natural Language Processing techniques for improving the quality of the data before clustering it. We look the five different preprocessing methods as described in section ?? and evaluate each. The methods are:

- Full text with stop word removal
- Keyterms
- Named Entities
- Lemmatization
- Stemmatization

Text Vectorization Before the text can be clustered, it has to be transformed into a vector space model. We look at two different models:

- Word Count
- Tfidf

Parameters HDBSCAN has a range of parameters, which can be tuned to fit our dataset. We focus on the two primary ones:

- Min cluster size: The minimum size of a cluster. We run the evaluation with a range from two to nine as the $min_cluster_size$.
- Metric: The distance measure between points. We apply the metrics "cosine" and "euclidean".

The primary parameter for K-Means is the number of clusters. Since K-Means is used as a baseline to evaluate HDBSCAN, we provide the true number of clusters for each run. Therefore K-Means runs with an optimal starting point.

Running the evaluation The evaluation is done with different sets of news articles per run. This means if we define a run to use 30 stories and set it to repeat five times, each repeat will load 30 different stories from the dataset. This is done to get a more diverse set of samples. Each run will be repeated at least three times. Lower numbers of stories allow for more repetitions due to lower processing times.

5.1.2 Evaluation

The first run is done with 60 stories, which results in approximately 2000 news articles, over five repetitions. Table 4 shows the resulting accuracy for each parameter in combination with each preprocessing method and vector space model. The highest score per parameter is highlighted as bold. The first insight we get is the variety in accuracy scores for different min cluster sizes. The lowest min cluster size results in the lowest accuracy, while increasing this parameter leads to an increasingly

better score. The highest accuracy is reached with a min cluster size of six, while increasing it further reduces the score again. The large difference in accuracies between different min cluster sizes, shows the importance this parameters has on the quality of the clustering and requires some knowledge of the data beforehand. In our case we have a wide range of different cluster sizes as shown in figure 1, with clusters containing as little as two news articles. Based on this distribution we expected the min size cluster size to be low. The distribution also explains the drop in accuracy after a min cluster size of 6, since an increasingly number of clusters are being ignored.

Clustering	Word Count				Tfidf					
HDBSCAN	Full Text	Keyterms	Entities	Lemmatized	Stemmed	Full Text	Keyterms	Entities	Lemmatized	Stemmed
min_size: 2, metric: cosine	0.289	0.265	0.223	0.305	0.297	0.286	0.268	0.26	0.296	0.3
min_size: 2, metric: euclidean	0.101	0.093	0.110	0.101	0.106	0.301	0.170	0.241	0.306	0.301
min_size: 3, metric: cosine	0.488	0.456	0.465	0.48	0.487	0.472	0.446	0.457	0.493	0.478
min_size: 3, metric: euclidean	0.172	0.129	0.176	0.174	0.182	0.472	0.306	0.464	0.500	0.478
min_size: 4, metric: cosine	0.630	0.555	0.625	0.552	0.577	0.577	0.586	0.646	0.589	0.581
min_size: 4, metric: euclidean	0.320	0.182	0.214	0.315	0.332	0.611	0.416	0.559	0.613	0.615
min_size: 5, metric: cosine	0.716	0.652	0.656	0.718	0.718	0.688	0.664	0.632	0.686	0.692
min_size: 5, metric: euclidean	0.355	0.217	0.266	0.41	0.389	0.703	0.512	0.607	0.686	0.692
min_size: 6, metric: cosine	0.693	0.715	0.608	0.701	0.708	0.738	0.729	0.613	0.751	0.747
min_size: 6, metric: euclidean	0.179	0.280	0.292	0.202	0.164	0.738	0.408	0.622	0.778	0.763
min_size: 7, metric: cosine	0.631	0.611	0.552	0.643	0.634	0.689	0.685	0.553	0.718	0.722
min_size: 7, metric: euclidean	0.122	0.392	0.307	0.073	0.099	0.689	0.336	0.539	0.718	0.722
min_size: 8, metric: cosine	0.571	0.603	0.514	0.592	0.574	0.685	0.647	0.531	0.711	0.695
min_size: 8, metric: euclidean	0.056	0.339	0.338	0.025	0.057	0.685	0.286	0.522	0.711	0.695
min_size: 9, metric: cosine	0.542	0.569	0.476	0.544	0.541	0.602	0.614	0.499	0.637	0.640
min_size: 9, metric: euclidean	0.065	0.236	0.310	0.025	0.033	0.602	0.216	0.475	0.637	0.640
K-Means										
n_cluster: n_true	0.531	0.588	0.514	0.536	0.536	0.713	0.653	0.584	0.672	0.693

Table 4: Accuracy for combinations of parameter and preprocessing with a sample size of 60 stories (approx. 2000 articles)

Comparing the two vector models, shows the majority of best scores per parameter achieved by Tfidf. Additionally the different metrics show a significant difference when using the vector model based on word count. With Tfidf the difference between both metrics is often negligible.

As for the optimal preprocessing, lemmatization appears to provide the highest accuray in general or at least being fairly close to the highest score. This is to be expected, since lemmatization reduces the dimensions by grouping words into their base form, while still retaining most of the text. In contrast to keyterm and entity extraction, which both result in a drastic reduction of the dimensions, and therefore less detail. It is important to note, that we used pretrained models for keyterm and entity extraction. Specifically training on a news corpus might improve the performance of both methods, but it was decided as to be out of scope for this thesis.

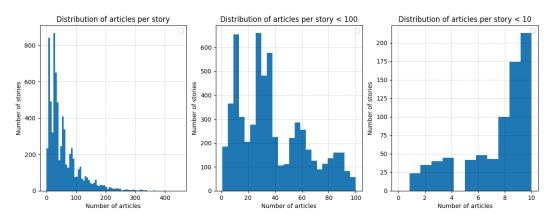


Figure 1: Distribution of cluster sizes.

After determining the optimal settings for text preprocessing and vectorization, we increase the sample

sizes for our evaluation runs, to get a deeper insight into the behaviour of HDBSCAN with larger datasets. Figure 2 shows the scores achieved with different parameters over an increasingly large set of samples. Based on this figure we see the metric *cosine* to be generally better than *euclidean*, even if *euclidean* is occasionally more accurate.

TODO explain why cosine is generally better than euclidean TODO explain min cluster sizes, but run with lemmatization

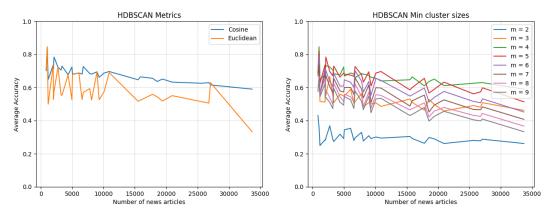


Figure 2: Accuracies for different parameters

One of the advantages HDBSCAN has over other clustering algorithms, is the ability to work with noise, since we intent on applying it in an online setting, where noisy data is to be expected. At the same time, the number of articles classified as noise should be kept to a minimum. However the noise ratio shown in Figure 3 is higher, than we would expect it to be based on our test data. A variety of factors play into the high noise ratio. One major influence is due to the used $min_cluster_size$. Each news article belonging to a cluster ignored due to a size too small, will be counted as noise. In addition to the false positives due to the min cluster size, the test data does still contain noisy data, even after our efforts in cleaning up the data as good as possible. Nontheless the expected noise ratio based on the test data is less than 10%, nowhere close to the 20% of the current evaluation. Decreasing the noise ratio is certainly an important part in future improvements.

TODO calculate expected noise ratio based our min cluster sizes.

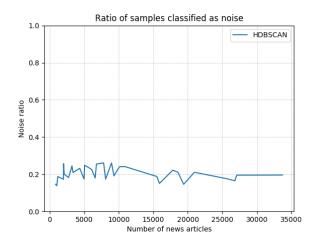


Figure 3: Number of news articles classified as noise.

Having found the optimal settings to run HDBSCAN with, we can start comparing the overall performance with K-Means. Figure 4 shows a similar behaviour for both clustering methods in value

and variance of the accuracy. Although HDBSCAN is generally more accurate than K-Means, the difference gets smaller with an increase in the sample size.

Increasing the sample size results for both HDBSCAN and K-means in a small loss regarding the accuracy as can be seen in figure 4. However the accuracy seems to stabilize around the 0.7 mark.

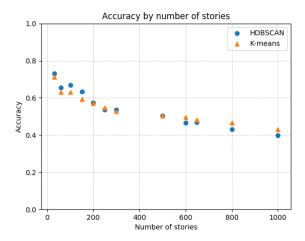


Figure 4: Comparison of the average accuracy between K-means and HDBSCAN

While HDBSCAN and K-means provide a similar accuracy, the biggest difference can be noted in the processing time in relation to the number of samples. K-means has a time complexity of $O(n^2)$ in contrast to HDBSCAN with a time complexity of $O(n\log(n))$, which is demonstrated by figure 5. Although running the evaluation has also shown the space complexity for HDBSCAN to be substantially higher for larger amounts of samples than with K-means. Trying to run HDBSCAN with 100'000 news articles caused in a memory error, even with 64GB of RAM, while K-means was able to complete the clustering.

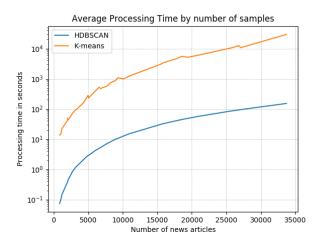


Figure 5: Processing time in seconds

Figure 6 shows, that the difference between predicted over the true number of clusters is fairly low and appears to be roughly linear with the overall number of clusters.

As a final note, we compare HDBSCAN with six different clustering methods taken from scikit-learn. Each method is run with a variety of parameters and the best scores are shown in figure 7. HDBSCAN provides the highest accuracy, while being still being one of the fastest algorithms. Based on this data, we can assume HDBSCAN to be a good candidate for our use case.

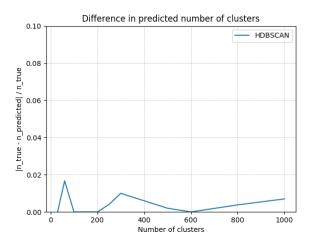


Figure 6: Ratio of difference over predicted with true number of clusters

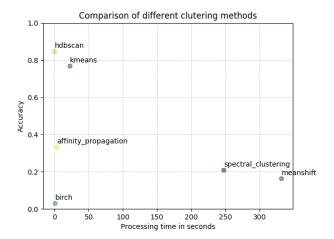


Figure 7: Comparison of different clustering methods with a sample size of approximately 1000 news articles

5.1.3 Conclusion

The evaluation has shown HDBSCAN to be a good candidate to use for news clustering. It provides an better accuracy than K-means, while being significantly faster to process. The predicted number of clusters is consistent with an increasing number of samples and fairly close the truth. Additionally we have shown the required preprocessing and vectorization steps with the ideal parameters to achieve the most accurate results for our dataset. On the flip side the noise ratio is quite high and the space complexity is problematic with larger datasets. Overall HDBSCAN provides an acceptable accuracy, while still leaving room for further improvements.

5.2 Evaluation of online clustering

TODO new topic, topic extended

TODO cluster stability

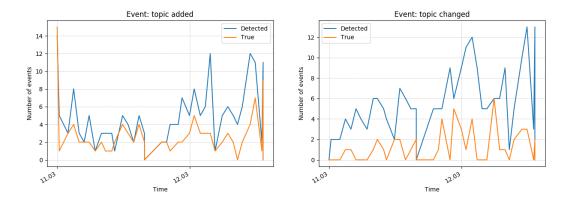


Figure 8: Comparison between detected and true events \cdot

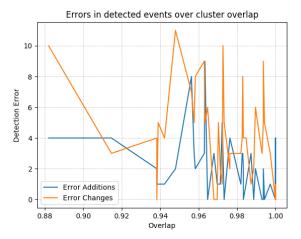


Figure 9: Plot work in progress

6 Conclusion

6.1 Summary

Short summary of this work.

6.2 Advantages and Drawbacks

What are the Advantages and Drawbacks of our work?

6.3 Further Improvements

How can this work be improved further?

^{*} improving space complexity and noise ratio of hdbscan * alternatively use hdbscan as an approximation for the number of clusters and a different clustering algorighm for the acutal creation of the clusters.

7 Appendix

7.1 Algorithm for Accuracy Selection

```
def select_max_values(self, accuracy_matrix):
2
           unique\_indicies = dict()
3
           row\_index = 0
           nrows = len(accuracy_matrix)
4
           while row_index < nrows:
6
               ignore\_indicies = set()
               max_value_found = False
8
9
               while not max_value_found:
                   \max_{\text{value}} = 0
11
                   column = 0
                    for col_index, value in enumerate(accuracy_matrix[row_index]):
13
                        if value >= max_value and col_index not in ignore_indicies:
14
                            max_value = value
                            column = col_index
17
                    if (
18
                        max_value > 0
19
                        and column in unique_indicies
20
                        and unique_indicies [column]["row_index"] != row_index
21
                        and unique_indicies [column]["max_value"] > 0
22
                   ):
23
                        if unique_indicies [column]["max_value"] < max_value:
24
                            # The column is already used, but we found a better
25
                            # candidate. We use the new candidate and set the
26
                            # cursor to the old one to find a new max value.
27
                            old_row_index = unique_indicies [column]["row_index"]
28
                            unique_indicies [column]["row_index"] = row_index
29
                            row\_index = old\_row\_index
30
31
                            unique_indicies [column]["max_value"] = max_value
                            max_value_found = True
33
                        else:
                            # The column is already used by a better candidate.
34
                            ignore_indicies.add(column)
35
                    else:
36
                        # If max_value is greater than 0, we store the value as a
37
                        # new candiate. Otherwise either the row does not match
38
                        # any other column or the max_value was low and got
39
                        # overriden by previous tries and no other match is available.
40
                        if \max_{\text{value}} > 0:
41
                            # The column is free to use
42
                            unique_indicies [column] = {
43
                                 "row_index": row_index,
44
                                "max_value": max_value,
45
46
                            }
                        max_value_found = True
47
                        row\_index += 1
48
49
           return unique_indicies
```

Listing 1: Select relevant accuracy values from a accuracy matrix.