## RJafroc Documentation

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## **Preface**

- This book, an extended documentation of the **RJafroc** package, is undergoing extensive edits.
- It should not be used by the casual user until I give the go ahead.
- It bypasses the file size limits of **CRAN**, currently 5 MB, which severely limits the extent of the documentation that can be included with the CRAN version of the package.
- I welcome corrections and comments by the not-so-casual-user.
- Please use the GitHub website to raise issues and comments:
  - $-\ https://github.com/dpc10ster/RJafrocBook$

## Chapter 1

## Introduction

- This is the book desribing the  ${\bf RJafroc}$  package.
- The name of the book is RJafrocBook
- Modality and treatment are used interchangeably.
- Reader is a generic radiologist, or a computer aided detection algorithm, or any algorithmic "reader"
- TBA

#### 1.1 References

## Chapter 2

### ROC DATA FORMAT

$$\begin{split} \theta &= \frac{1}{N_L N_N} \sum\nolimits_k \sum\nolimits_{k'} \sum\limits_{r=1}^{n_k^L} \sum\limits_{r'=1}^{n_{k'}^N} \psi(X_{kr}, Y_{k'r'}) \\ &\frac{d}{dx} \left( \int_a^x f(u) \, du \right) = f(x) \\ &\theta &= \frac{1}{N_L N_N} \end{split}$$

#### 2.1 Introduction

- The purpose of this vignette is to explain the data format of the input Excel file and to introduce the capabilities of the function DfReadDataFile(). Background on observer performance methods are in my book (Chakraborty, 2017).
- I will start with Receiver Operating Characteristic (ROC) data (Metz, 1978), as this is by far the simplest paradigm.
- In the ROC paradigm the observer assigns a rating to each image. A rating is an ordered numeric label, and, in our convention, higher values represent greater certainty or **confidence level** for presence of disease. With human observers, a 5 (or 6) point rating scale is typically used, with 1 representing highest confidence for *absence* of disease and 5 (or 6) representing highest confidence for *presence* of disease. Intermediate values represent intermediate confidence levels for presence or absence of disease.
- Note that location information associated with the disease, if applicable, is not collected.

• There is no restriction to 5 or 6 ratings. With algorithmic observers, e.g., computer aided detection (CAD) algorithms, the rating could be a floating point number and have infinite precision. All that is required is that higher values correspond to greater confidence in presence of disease.

#### 2.2 Note to existing users

- The Excel file format has recently undergone changes resulting in 4 extra list members in the final created dataset object (i.e., 12 members instead of 8).
- Code should run on the old format Excel files as the 4 extra list members are simply ignored.
- Reasons for the change will become clearer in these vignettes
- Basically they are needed for generalization to other data collection paradigms instead of crossed, for example to the split-plot data acquisition paradigm, and for better data entry error control.

#### 2.3 The Excel data format

- The Excel file has three worksheets.
- These are named
  - Truth,
  - NL (or FP),
  - LL (or TP).

#### 2.4 Illustrative toy file

- Toy files are artificial small datasets intended to illustrate essential features of the data format.
- The examples shown in this vignette corresponds to Excel file inst/extdata/toyFiles/ROC/rocCr.xlsx in the project directory.
- To view these files one needs to clone the source files from GitHub.

#### 2.5 The Truth worksheet

• The Truth worksheet contains 6 columns: CaseID, LesionID, Weight, ReaderID, ModalityID and Paradigm.

- For ROC data the first five columns contain as many rows as there are cases (images) in the dataset.
- CaseID: unique integers, one per case, representing the cases in the dataset.
- LesionID: integers 0 or 1, with each 0 representing a non-diseased case and each 1 representing a diseased case.
- In the current toy dataset, the non-diseased cases are labeled 1, 2 and 3, while the diseased cases are labeled 70, 71, 72, 73 and 74. The values do not have to be consecutive integers; they need not be ordered; the only requirement is that they be **unique**.
- Weight: Not used for ROC data, a floating point value, typically filled in with 0 or 1.
- ReaderID: a comma-separated listing of reader labels, each represented by a unique string, that have interpreted the case. In the example shown below each cell has the value 0, 1, 2, 3, 4 meaning that each of the readers, represented by the strings "0", "1", "2", "3" and "4", have interpreted all cases (hence the "crossed" design). With reader names that could be confused with integers, each cell in this column has to be text formatted as otherwise Excel will not accept it. [Try entering 0, 1, 2, 3, 4 in a numeric formatted Excel cell.]
- The reader names could just as well have been Rdr0, Rdr1, Rdr2, Rdr3, Rdr4. The only requirement is that they be unique strings.
- Look in in the inst/extdata/toyFiles/ROC directory for files rocCrStrRdrsTrts.xlsx and rocCrStrRdrsNonUnique.xlsx for examples of data files using longer strings for readers. The second file generates an error because the reader names are not unique.
- ModalityID: a comma-separated listing of modalities (one or more modalities), each represented by a **unique string**, that are applied to each case. In the example each cell has the value "0", "1". With treatment names that could be confused with integers, each cell has to be text formatted as otherwise Excel will not accept it.
- The treatment names could just as well have been Trt0, Trt1. Again, the only requirement is that they be unique strings.
- Paradigm: this column contains two cells, ROC and crossed. It informs the software that this is an ROC dataset, and the design is crossed, meaning each reader has interpreted each case in each modality (in statistical terminology: modality and reader factors are "crossed").
- There are 5 diseased cases in the dataset (the number of 1's in the LesionID column of the Truth worksheet).
- There are 3 non-diseased cases in the dataset (the number of 0's in the LesionID column).
- There are 5 readers in the dataset (each cell in the ReaderID column contains the string 0, 1, 2, 3, 4).
- There are 2 modalities in the dataset (each cell in the ModalityID column contains the string 0, 1).

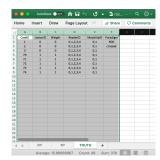


Figure 2.1: Truth worksheet for file rocCr.xlsx

#### 2.6 The structure of an ROC dataset

In the following code chunk the first statement retrieves the name of the data file, located in a hidden directory that one need not be concerned with. The second statement reads the file using the function DfReadDataFile() and saves it to object x. The third statement shows the structure of the dataset object x.

```
rocCr <- system.file("extdata", "toyFiles/ROC/rocCr.xlsx",</pre>
                        package = "RJafroc", mustWork = TRUE)
x <- DfReadDataFile(rocCr, newExcelFileFormat = TRUE)
str(x)
#> List of 12
#> $ NL
                   : num [1:2, 1:5, 1:8, 1] 1 3 2 3 2 2 1 2 3 2 ...
    $ LL
                   : num [1:2, 1:5, 1:5, 1] 5 5 5 5 5 5 5 5 5 5 5 ...
#>
    $ lesionVector : int [1:5] 1 1 1 1 1
    $ lesionID
                  : num [1:5, 1] 1 1 1 1 1
    $ lesionWeight : num [1:5, 1] 1 1 1 1 1
    $ dataType
                  : chr "ROC"
    $ modalityID : Named chr [1:2] "0" "1"
#>
     ..- attr(*, "names")= chr [1:2] "0" "1"
                  : Named chr [1:5] "0" "1" "2" "3" ...
    $ readerID
    ..- attr(*, "names")= chr [1:5] "0" "1" "2" "3" ...
    $ design
                  : chr "CROSSED"
    $ normalCases : int [1:3] 1 2 3
#>
    $ abnormalCases: int [1:5] 70 71 72 73 74
#> $ truthTableStr: num [1:2, 1:5, 1:8, 1:2] 1 1 1 1 1 1 1 1 1 1 ...
```

- In the above code chunk flag newExcelFileFormat is set to TRUE as otherwise columns D F in the Truth worksheet are ignored and the dataset is assumed to be crossed, with dataType automatically determined from the contents of the FP and TP worksheets.
- Flag newExcelFileFormat = FALSE is for compatibility with older

JAFROC format Excel files, which did not have these columns in the Truth worksheet. Its usage is deprecated.

- The dataset object x is a list variable with 12 members.
- The x\$NL member, with dimension [2, 5, 8, 1], contains the ratings of normal cases. The extra values in the third dimension, filled with NAs, are needed for compatibility with FROC datasets, as unlike ROC, false positives are possible on diseased cases.
- The x\$LL, with dimension [2, 5, 5, 1], contains the ratings of abnormal cases.
- The x\$lesionVector member is a vector with 5 ones representing the 5 diseased cases in the dataset.
- The x\$lesionID member is an array with 5 ones.
- The x\$lesionWeight member is an array with 5 ones.
- The lesionVector, lesionID and lesionWeight members are not used for ROC datasets. They are there for compatibility with FROC datasets.
- The dataType member indicates that this is an ROC dataset.
- The x\$modalityID member is a vector with two elements "0" and "1", naming the two modalities.
- The x\$readerID member is a vector with five elements "0", "1", "2", "3" and "4", naming the five readers.
- The x\$design member is CROSSED; specifies the dataset design, which
  is "CROSSED".
- The x\$normalCases member lists the integer names of the normal cases,
   1, 2, 3.
- The x\$abnormalCases member lists the integer names of the abnormal cases, 70, 71, 72, 73, 74.
- The x\$truthTableStr member quantifies the structure of the dataset, as explained in Chapter 00 Vignette #3-#5.

#### 2.7 The false positive (FP) ratings

These are found in the FP or NL worksheet, see below.



Figure 2.2: FP worksheet for file rocCr.xlsx

- It consists of 4 columns, each of length 30 (= # of modalities times number of readers times number of non-diseased cases).
- ReaderID: the reader labels: 0, 1, 2, 3 and 4. Each reader label occurs 6 times (= # of modalities times number of non-diseased cases).
- ModalityID: the modality or treatment labels: 0 and 1. Each label occurs 15 times (= # of readers times number of non-diseased cases).
- CaseID: the case labels for non-diseased cases: 1, 2 and 3. Each label occurs 10 times (= # of modalities times # of readers).
- The label of a diseased case cannot occur in the FP worksheet. If it does
  the software generates an error.
- FP\_Rating: the floating point ratings of non-diseased cases. Each row of this worksheet contains a rating corresponding to the values of ReaderID, ModalityID and CaseID for that row.

#### 2.8 The true positive (TP) ratings

These are found in the TP or LL worksheet, see below.



Figure 2.3: TP worksheet for file rocCr.xlsx

- It consists of 5 columns, each of length 50 (= # of modalities times number of readers times number of diseased cases).
- ReaderID: the reader labels: 0, 1, 2, 3 and 4. Each reader label occurs 10 times (= # of modalities times number of diseased cases).
- ModalityID: the modality or treatment labels: 0 and 1. Each label occurs 25 times (= # of readers times number of diseased cases).
- LesionID: For an ROC dataset this column contains fifty 1's (each diseased case has one lesion).
- CaseID: the case labels for non-diseased cases: 70, 71, 72, 73 and 74. Each label occurs 10 times (= # of modalities times # of readers). The label of a non-diseased case cannot occur in the TP worksheet.
- TP\_Rating: the floating point ratings of diseased cases. Each row of this worksheet contains a rating corresponding to the values of ReaderID, ModalityID, LesionID and CaseID for that row.

# 2.9 Correspondence between NL member of dataset and the FP worksheet

- The list member xNL is an array with dim = c(2,5,8,1).
  - The first dimension (2) comes from the number of modalities.
  - The second dimension (5) comes from the number of readers.
  - The third dimension (8) comes from the **total** number of cases.
  - The fourth dimension is alway 1 for an ROC dataset.
- The value of x\$NL[1,5,2,1], i.e., 5, corresponds to row 15 of the FP table, i.e., to ModalityID = 0, ReaderID = 4 and CaseID = 2.
- The value of x\$NL[2,3,2,1], i.e., 4, corresponds to row 24 of the FP table, i.e., to ModalityID 1, ReaderID 2 and CaseID 2.
- All values for case index > 3 are -Inf. For example the value of x\$NL[2,3,4,1] is -Inf. This is because there are only 3 non-diseased cases. The extra length is needed for compatibility with FROC datasets.

# 2.10 Correspondence between LL member of dataset and the TP worksheet

- The list member x\$LL is an array with dim = c(2,5,5,1).
  - The first dimension (2) comes from the number of modalities.
  - The second dimension (5) comes from the number of readers.
  - The third dimension (5) comes from the number of diseased cases.
  - The fourth dimension is alway 1 for an ROC dataset.
- The value of x\$LL[1,1,5,1], i.e., 4, corresponds to row 6 of the TP table, i.e., to ModalityID = 0, ReaderID = 0 and CaseID = 74.
- The value of x\$LL[1,2,2,1], i.e., 3, corresponds to row 8 of the TP table, i.e., to ModalityID = 0, ReaderID = 1 and CaseID = 71.
- There are no -Inf values in x\$LL: any(x\$LL == -Inf) = FALSE.

#### 2.11 Correspondence using the which function

- Converting from **names** to **subscripts** (indicating position in an array) can be confusing.
- The following example uses the which function to help out.
- The first line says that the abnormalCase named 70 corresponds to subscript 1 in the LL array case dimension.
- The second line prints the NL rating for modalityID = 0, readerID = 1 and normalCases = 1.

- The third line prints the LL rating for modalityID = 0, readerID = 1 and abnormalCases = 70.
- The last line shows what happens if one enters an invalid value for name; the result is a numeric(0).
- Note that in each of these examples, the last dimension is 1 because we are dealing with an ROC dataset.
- The reader is encouraged to examine the correspondence between the NL and LL ratings and the Excel file using this method.

```
which(x$abnormalCases == 70)
#> [1] 1
x$NL[which(x$modalityID == "0"), which(x$readerID == "1"), which(x$normalCases == 1),1]
#> [1] 2
x$LL[which(x$modalityID == "0"), which(x$readerID == "1"), which(x$abnormalCases == 70),
#> [1] 5
x$LL[which(x$modalityID == "a"), which(x$readerID == "1"), which(x$abnormalCases == 70),
#> numeric(0)
```

#### 2.12 References

## Chapter 3

## FROC data format

#### 3.1 Purpose

- Explain the data format of the input Excel file for FROC datasets.
- Explain the format of the FROC dataset.
- Explain the lesion distribution array returned by UtilLesionDistr().
- Explain the lesion weights array returned by UtilLesionWeightsDistr().
- Details on the FROC paradigm are in my book.

#### 3.2 Introduction

- See my book Chakraborty (2017) for full details.
- In the Free-response Receiver Operating Characteristic (FROC) paradigm (Chakraborty, 1989) the observer searches each case for signs of localized disease and marks and rates localized regions that are sufficiently suspicious for disease presence.
- FROC data consists of **mark-rating pairs**, where each mark is a localized-region that was considered sufficiently suspicious for presence of a localized lesion and the rating is the corresponding confidence level.
- By adopting a proximity criterion, each mark is classified by the investigator as a lesion localization (LL) if it is close to a real lesion or a non-lesion localization (NL) otherwise.
- The observer assigns a rating to each region. The rating, as in the ROC paradigm, can be an integer or quasi-continuous (e.g., 0 100), or a floating point value, as long as higher numbers represent greater confidence in presence of a lesion at the indicated region.

#### 3.3 The Excel data format

The Excel file has three worsheets. These are named Truth, NL or FP and LL or TP.

#### 3.4 The Truth worksheet

The Truth worksheet contains 6 columns: CaseID, LesionID, Weight, ReaderID, ModalityID and Paradigm.

- Since a diseased case may have more than one lesion, the first five columns contain **at least** as many rows as there are cases (images) in the dataset.
- CaseID: unique integers, one per case, representing the cases in the dataset.
- LesionID: integers 0, 1, 2, etc., with each 0 representing a non-diseased case, 1 representing the *first* lesion on a diseased case, 2 representing the second lesion on a diseased case, if present, and so on.
- The non-diseased cases are labeled 1, 2 and 3, while the diseased cases are labeled 70, 71, 72, 73 and 74.
- There are 3 non-diseased cases in the dataset (the number of 0's in the LesionID column).
- There are 5 diseased cases in the dataset (the number of 1's in the LesionID column of the Truth worksheet).
- There are 3 readers in the dataset (each cell in the ReaderID column contains 0, 1, 2).
- There are 2 modalities in the dataset (each cell in the ModalityID column contains 0, 1).
- Weight: floating point; 0, for each non-diseased case, or values for each diseased case that add up to unity.
- Diseased case 70 has two lesions, with LesionIDs 1 and 2, and weights 0.3 and 0.7. Diseased case 71 has one lesion, with LesionID = 1, and Weight = 1. Diseased case 72 has three lesions, with LesionIDs 1, 2 and 3 and weights 1/3 each. Diseased case 73 has two lesions, with LesionIDs 1, and 2 and weights 0.1 and 0.9. Diseased case 74 has one lesion, with LesionID = 1 and Weight = 1.
- ReaderID: a comma-separated listing of readers, each represented by a unique integer, that have interpreted the case. In the example shown below each cell has the value 0, 1, 2. Each cell has to be text formatted. Otherwise Excel will not accept it.
- ModalityID: a comma-separated listing of modalities (or treatments), each
  represented by a unique integer, that apply to each case. In the example
  each cell has the value 0, 1. Each cell has to be text formatted.

• Paradigm: In the example shown below, the contents are FROC and crossed. It informs the software that this is an FROC dataset and the design is "crossed", as in Vignette #1.

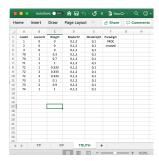


Figure 3.1: Truth worksheet for file inst/extdata/toyFiles/FROC/frocCr.xlsx

#### 3.5 The structure of an FROC dataset

The example shown above corresponds to Excel file inst/extdata/toyFiles/FROC/frocCr.xlsx in the project directory.

```
frocCr <- system.file("extdata", "toyFiles/FROC/frocCr.xlsx",</pre>
                        package = "RJafroc", mustWork = TRUE)
x <- DfReadDataFile(frocCr, newExcelFileFormat = TRUE)
str(x)
#> List of 12
#> $ NL
                  : num [1:2, 1:3, 1:8, 1:2] 1.02 2.89 2.21 3.01 2.14 ...
                  : num [1:2, 1:3, 1:5, 1:3] 5.28 5.2 5.14 4.77 4.66 4.87 3.01 3.27 3.31 3.19 ...
#> $ lesionVector : int [1:5] 2 1 3 2 1
#> $ lesionID : num [1:5, 1:3] 1 1 1 1 1 ...
#> $ lesionWeight : num [1:5, 1:3] 0.3 1 0.333 0.1 1 ...
                 : chr "FROC"
#> $ dataType
#> $ modalityID : Named chr [1:2] "0" "1"
#>
    ..- attr(*, "names")= chr [1:2] "0" "1"
                 : Named chr [1:3] "0" "1" "2"
#> $ readerID
   ..- attr(*, "names")= chr [1:3] "0" "1" "2"
#>
                 : chr "CROSSED"
#> $ design
#> $ normalCases : int [1:3] 1 2 3
#> $ abnormalCases: int [1:5] 70 71 72 73 74
#> $ truthTableStr: num [1:2, 1:3, 1:8, 1:4] 1 1 1 1 1 1 1 1 1 1 1 ...
```

 This follows the general description in Vignette #1. The differences are described below.

- The x\$dataType member indicates that this is an FROC dataset.
- The x\$lesionVector member is a vector whose contents reflect the number of lesions in each diseased case, i.e., 2, 1, 3, 2, 1 in the current example.
- The x\$lesionID member indicates the labeling of the lesions in each diseased case.

```
x$lesionID
         [,1] [,2] [,3]
#> [1,]
            1
                 2 -Inf
#> [2,]
            1 - Inf - Inf
#> [3,]
            1
                  2
                       3
#> [4,]
            1
                  2 -Inf
#> [5,]
            1 - Inf - Inf
```

- This shows that the lesions on the first diseased case are labeled 1 and 2. The -Inf is a filler used to denote a missing value. The second diseased case has one lesion labeled 1. The third diseased case has three lesions labeled 1, 2 and 3, etc.
- The lesionWeight member is the clinical importance of each lesion. Lacking specific clinical reasons, the lesions should be equally weighted; this is not true for this toy dataset.

```
x$lesionWeight
#>
              [,1]
                         [,2]
                                   [,3]
#> [1,] 0.3000000 0.7000000
                                   -Inf
#> [2,] 1.0000000
                                   -Inf
                        -Inf
#> [3,] 0.3333333 0.3333333
                             0.3333333
#> [4,] 0.1000000 0.9000000
                                   -Inf
#> [5,] 1.0000000
                         -Inf
                                   -Inf
```

• The first diseased case has two lesions, the first has weight 0.3 and the second has weight 0.7. The second diseased case has one lesion with weight 1. The third diseased case has three equally weighted lesions, each with weight 1/3. Etc.

#### 3.6 The false positive (FP) ratings

These are found in the FP or NL worksheet, see below.

• It consists of 4 columns, of equal length. The common length is unpredictable. It could be zero if the dataset has no NL marks (a distinct possibility if the lesions are very easy to find and the modality and/or observer has high performance). All one knows is that the common length is an integer greater than or equal to zero.



Figure 3.2: Fig. 2: FP/NL worksheet for file inst/extdata/toyFiles/FROC/frocCr.xlsx

- In the example dataset, the common length is 22.
- ReaderID: the reader labels: these must be 0, 1, or 2, as declared in the Truth worksheet.
- ModalityID: the modality labels: must be 0 or 1, as declared in the Truth worksheet.
- CaseID: the labels of cases with NL marks. In the FROC paradigm, NL events can occur on non-diseased and diseased cases.
- FP\_Rating: the floating point ratings of NL marks. Each row of this worksheet yields a rating corresponding to the values of ReaderID, ModalityID and CaseID for that row.
- For ModalityID 0, ReaderID 0 and CaseID 1 (the first non-diseased case declared in the Truth worksheet), there is a single NL mark that was rated 1.02, corresponding to row 2 of the FP worksheet.
- Diseased cases with NL marks are also declared in the FP worksheet. Some examples are seen at rows 15, 16 and 21-23 of the FP worksheet.
- Rows 21 and 22 show that caseID = 71 got two NL marks, rated 2.24, 4.01.
- That this is the *only* case with two marks determines the length of the fourth dimension of the xNL list member, 2 in the current example. Absent this case, the length would have been one.
- In general, the case with the most NL marks determines the length of the fourth dimension of the x\$NL list member.
- The reader should convince oneself that the ratings in x\$NL reflect the contents of the FP worksheet.

#### 3.7 The true positive (TP) ratings

These are found in the TP or LL worksheet, see below.

• This worksheet can only have diseased cases. The presence of a non-

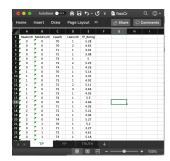


Figure 3.3: Fig. 3: TP/LL worksheet for file inst/extdata/toyFiles/FROC/frocCr.xlsx

diseased case in this worksheet will generate an error.

- The common vertical length, 31 in this example, is a-priori unpredictable. Given the structure of the Truth worsheet for this dataset, the maximum length would be 9 times 2 times 3, assuming every lesion is marked for each modality, reader and diseased case. The 9 comes from the total number of non-zero entries in the LesionID column of the Truth worksheet.
- The fact that the length is smaller than the maximum length means that there are combinations of modality, reader and diseased cases on which some lesions were not marked.
- As an example, the first lesion in CaseID equal to 70 was marked (and rated 5.28) in ModalityID 0 and ReaderID 0.
- The length of the fourth dimension of the x\$LL list member, 3 in the present example, is determined by the diseased case with the most lesions in the Truth worksheet.
- The reader should convince oneself that the ratings in x\$LL reflect the contents of the TP worksheet.

# 3.8 On the distribution of numbers of lesions in abnormal cases

Consider a much larger dataset, dataset11, with structure as shown below:

```
#> $ lesionWeight : num [1:115, 1:20] 0.167 0.25 0.143 1 0.333 ...
#> $ dataType : chr "FROC"

#> $ modalityID : Named chr [1:4] "1" "2" "3" "4"

#> .- attr(*, "names") = chr [1:4] "1" "2" "3" "4"

#> $ readerID : Named chr [1:5] "1" "2" "3" "4" ...

#> ..- attr(*, "names") = chr [1:5] "1" "2" "3" "4" ...

#> $ design : chr "CROSSED"

#> $ normalCases : int [1:43] 6 9 14 27 62 66 70 71 83 91 ...
#> $ abnormalCases: int [1:115] 1 2 3 5 7 8 10 11 13 17 ...

#> $ truthTableStr: num [1:4, 1:5, 1:158, 1:21] 1 1 1 1 1 1 1 1 1 1 ...
```

- Focus for now in the 115 abnormal cases.
- The numbers of lesions in these cases is contained in x\$lesionVector.

```
x$lesionVector

#> [1] 6 4 7 1 3 3 3 8 11 2 4 6 2 16 5 2 8 3 4 7 11 1 4 3 4

#> [26] 4 7 3 2 5 2 2 7 6 6 4 10 20 12 6 4 7 12 5 1 1 5 1 2 8

#> [51] 3 1 2 2 3 2 8 16 10 1 2 2 6 3 2 2 4 6 10 11 1 2 6 2 4

#> [76] 5 2 9 6 6 8 3 8 7 1 1 6 3 2 1 9 8 8 2 2 12 1 1 1 1 1

#> [101] 1 3 1 2 2 1 1 1 1 1 3 1 1 2 1
```

- For example, the first abnormal case contains 6 lesions, the second contains 4 lesions, the third contains 7 lesions, etc. and the last abnormal case contains 1 lesion.
- To get an idea of the distribution of the numbers of lesions per abnormal cases, one could interrogate this vector as shown below using the which() function:

```
for (el in 1:max(x$lesionVector)) cat(
  "abnormal cases with", el, "lesions = ",
 length(which(x$lesionVector == el)), "\n")
#> abnormal cases with 1 lesions = 25
#> abnormal cases with 2 lesions = 23
#> abnormal cases with 3 lesions = 13
#> abnormal cases with 4 lesions = 10
#> abnormal cases with 5 lesions = 5
#> abnormal cases with 6 lesions = 11
#> abnormal cases with 7 lesions = 6
#> abnormal cases with 8 lesions = 8
#> abnormal cases with 9 lesions = 2
#> abnormal cases with 10 lesions = 3
#> abnormal cases with 11 lesions = 3
#> abnormal cases with 12 lesions = 3
#> abnormal cases with 13 lesions = 0
```

```
#> abnormal cases with 14 lesions = 0
#> abnormal cases with 15 lesions = 0
#> abnormal cases with 16 lesions = 2
#> abnormal cases with 17 lesions = 0
#> abnormal cases with 18 lesions = 0
#> abnormal cases with 19 lesions = 0
#> abnormal cases with 20 lesions = 1
```

- This tells us that 25 cases contain 1 lesion
- Likewise, 23 cases contain 2 lesions
- Etc.

#### 3.8.1 Definition of lesDistr array

 Let us ask what is the fraction of (abnormal) cases with 1 lesion, 2 lesions etc.

```
for (el in 1:max(x$lesionVector)) cat("fraction of abnormal cases with", el, "lesions :
                                             length(which(x$lesionVector == el))/leng
#> fraction of abnormal cases with 1 lesions = 0.2173913
#> fraction of abnormal cases with 2 lesions =
#> fraction of abnormal cases with 3 lesions = 0.1130435
#> fraction of abnormal cases with 4 lesions = 0.08695652
#> fraction of abnormal cases with 5 lesions = 0.04347826
#> fraction of abnormal cases with 6 lesions = 0.09565217
#> fraction of abnormal cases with 7 lesions = 0.05217391
#> fraction of abnormal cases with 8 lesions = 0.06956522
#> fraction of abnormal cases with 9 lesions = 0.0173913
#> fraction of abnormal cases with 10 lesions = 0.02608696
#> fraction of abnormal cases with 11 lesions = 0.02608696
#> fraction of abnormal cases with 12 lesions = 0.02608696
#> fraction of abnormal cases with 13 lesions = 0
#> fraction of abnormal cases with 14 lesions = 0
#> fraction of abnormal cases with 15 lesions = 0
#> fraction of abnormal cases with 16 lesions = 0.0173913
#> fraction of abnormal cases with 17 lesions = 0
#> fraction of abnormal cases with 18 lesions = 0
#> fraction of abnormal cases with 19 lesions = 0
#> fraction of abnormal cases with 20 lesions = 0.008695652
```

- This tells us that fraction 0.217 of (abnormal) cases contain 1 lesion
- And fraction 0.2 of (abnormal) cases contain 2 lesions
- Etc.

- This information is contained the the lesDistr array
- It is coded in the Utility function UtilLesionDistr()

```
lesDistr <- UtilLesionDistr(x)</pre>
lesDistr
         [,1]
                      [,2]
   [1,]
            1 0.217391304
#>
    [2,]
            2 0.200000000
    [3,]
            3 0.113043478
    [4,]
            4 0.086956522
#>
   [5,]
            5 0.043478261
   [6,]
            6 0.095652174
            7 0.052173913
    [7,]
            8 0.069565217
   [8,]
#> [9,]
            9 0.017391304
#> [10,]
           10 0.026086957
#> [11,]
           11 0.026086957
#> [12,]
           12 0.026086957
#> [13,]
           16 0.017391304
#> [14,]
           20 0.008695652
```

- The UtilLesionDistr() function returns an array with two columns and number of rows equal to the number of distinct values of lesions per case.
- The first column contains the number of distinct values of lesions per case, 14 in the current example.
- The second column contains the fraction of diseased cases with the number of lesions indicated in the first column.
- The second column must sum to unity

```
sum(UtilLesionDistr(x)[,2])
#> [1] 1
```

• The lesion distribution array will come in handy when it comes to predicting the operating characteristics from using the Radiological Search Model (RSM), as detailed in Chapter 17 of my book.

#### 3.9 Definition of lesWghtDistr array

- This is returned by UtilLesionWeightsDistr().
- This contains the same number of rows as lesDistr.
- The number of columns is one plus the number of rows as lesDistr.
- The first column contains the number of distinct values of lesions per case, 14 in the current example.

- The second column contains the weights of cases with number of lesions per case corresponding to row 1.
- The third column contains the weights of cases with number of lesions per case corresponding to row 2.
- Etc.
- Missing values are filled with -Inf.

```
lesWghtDistr <- UtilLesionWeightsDistr(x)</pre>
cat("dim(lesDistr) =", dim(lesDistr),"\n")
\#> dim(lesDistr) = 14 2
cat("dim(lesWghtDistr) =", dim(lesWghtDistr),"\n")
\#> dim(lesWghtDistr) = 14 21
cat("lesWghtDistr = \n\n")
#> lesWqhtDistr =
lesWghtDistr
                                                  [.5]
                                                             [.6]
                                                                       [.7]
        [,1]
                   [,2]
                             [.3]
                                        [,4]
#>
    [1,]
           1 1.00000000
                             -Inf
                                        -Inf
                                                  -Inf
                                                             -Inf
                                                                       -Inf
#>
    [2,]
           2 0.50000000 0.50000000
                                        -Inf
                                                  -Inf
                                                             -Inf
                                                                       -Inf
#>
    [3,]
           3 0.33333333 0.33333333 0.333333333
                                                             -Inf
                                                  -Inf
                                                                       -Inf
           4 0.25000000 0.25000000 0.25000000 0.25000000
#>
    [4,]
                                                             -Inf
                                                                       -Inf
           5 0.20000000 0.20000000 0.20000000 0.20000000 0.20000000
    [5,]
                                                                       -Inf
#>
   16.7
           6 0.16666667 0.16666667 0.16666667 0.16666667 0.16666667
#>
    [7,]
           7 0.14285714 0.14285714 0.14285714 0.14285714 0.14285714 0.14285714
#>
    [8,]
           8 0.12500000 0.12500000 0.12500000 0.12500000 0.12500000
#>
   [9,]
           #> Γ10.7
          10 0.10000000 0.10000000 0.10000000 0.10000000 0.10000000 0.10000000
#> [11,]
          #> [12,]
          12 0.08333333 0.08333333 0.08333333 0.08333333 0.08333333 0.08333333
#> [13,]
          16 0.06250000 0.06250000 0.06250000 0.06250000 0.06250000 0.06250000
          20 0.05000000 0.05000000 0.05000000 0.05000000 0.05000000 0.05000000
#>
  [14,]
#>
              [,8]
                        [,9]
                                  [,10]
                                            [,11]
                                                       [,12]
                                                                 [,13]
                                                                        [,14]
#>
    [1,]
              -Inf
                        -Inf
                                   -Inf
                                             -Inf
                                                        -Inf
                                                                  -Inf
                                                                         -Inf
#>
    [2,]
              -Inf
                        -Inf
                                   -Inf
                                             -Inf
                                                        -Inf
                                                                  -Inf
                                                                         -Inf
#>
   [3,]
              -Inf
                        -Inf
                                   -Inf
                                             -Inf
                                                        -Inf
                                                                  -Inf
                                                                         -Inf
#>
    [4,]
              -Inf
                         -Inf
                                   -Inf
                                             -Inf
                                                        -Inf
                                                                  -Inf
                                                                         -Inf
#>
   [5,]
              -Inf
                         -Inf
                                   -Inf
                                             -Inf
                                                        -Inf
                                                                  -Inf
                                                                         -Inf
#>
   [6,]
                                             -Inf
              -Inf
                         -Inf
                                   -Inf
                                                        -Inf
                                                                  -Inf
                                                                         -Inf
#>
   [7,] 0.14285714
                         -Inf
                                   -Inf
                                             -Inf
                                                        -Inf
                                                                  -Inf
                                                                         -Inf
    [8,] 0.12500000 0.12500000
                                   -Inf
                                             -Inf
                                                        -Inf
                                                                  -Inf
                                                                         -Inf
   [9,] 0.11111111 0.11111111 0.11111111
                                             -Inf
                                                        -Inf
                                                                  -Inf
                                                                         -Inf
#> [10,] 0.10000000 0.10000000 0.10000000 0.10000000
                                                                  -Inf
                                                        -Inf
                                                                         -Inf
-Inf
                                                                         -Inf
#> [12,] 0.08333333 0.08333333 0.08333333 0.08333333 0.08333333 0.08333333
                                                                         -Inf
#> [13,] 0.06250000 0.06250000 0.06250000 0.06250000 0.06250000 0.06250000 0.0625
#> [14,] 0.05000000 0.05000000 0.05000000 0.05000000 0.05000000 0.05000000 0.0500
```

3.10. SUMMARY 31

```
[.15]
                   [,16]
                            [,17] [,18] [,19] [,20] [,21]
#>
    [1,]
            -Inf
                    -Inf
                            -Inf
                                   -Inf
                                          -Inf
                                                 -Inf
                                                        -Inf
#>
    [2,]
            -Inf
                    -Inf
                            -Inf
                                   -Inf
                                          -Inf
                                                 -Inf
                                                        -Inf
#>
    [3,]
            -Inf
                    -Inf
                            -Inf
                                   -Inf
                                          -Inf
                                                 -Inf
                                                        -Inf
#>
    [4,]
            -Inf
                    -Inf
                            -Inf
                                   -Inf
                                          -Inf
                                                 -Inf
                                                        -Inf
    [5,]
            -Inf
                                   -Inf
                                          -Inf
                                                        -Inf
#>
                    -Inf
                            -Inf
                                                 -Inf
#>
    [6,]
            -Inf
                                   -Inf
                    -Inf
                            -Inf
                                          -Inf
                                                 -Inf
                                                        -Inf
#>
    [7,]
            -Inf
                    -Inf
                            -Inf
                                   -Inf
                                          -Inf
#>
    [8,]
            -Inf
                                          -Inf
                    -Inf
                            -Inf
                                   -Inf
                                                 -Inf
                                                        -Inf
#>
    [9,]
            -Inf
                    -Inf
                            -Inf
                                   -Inf
                                          -Inf
                                                 -Inf
                                                        -Inf
#> [10,]
            -Inf
                    -Inf
                            -Inf
                                   -Inf
                                          -Inf
                                                 -Inf
                                                        -Inf
#> [11,]
            -Inf
                    -Inf
                            -Inf
                                   -Inf
                                          -Inf
#> [12,]
                                                        -Inf
            -Inf
                    -Inf
                            -Inf
                                   -Inf
                                          -Inf
                                                 -Inf
#> [13,] 0.0625 0.0625 0.0625
                                   -Inf
                                          -Inf
                                                        -Inf
                                                 -Inf
#> [14,] 0.0500 0.0500 0.0500
                                   0.05
                                          0.05
```

- Row 3 corresponds to 3 lesions per case and the weights are 1/3, 1/3 and 1/3.
- Row 13 corresponds to 16 lesions per case and the weights are 0.06250000, 0.06250000, ..., repeated 13 times.
- Note that the number of rows is less than the maximum number of lesions per case (20).
- This is because some configurations of lesions per case (e.g., cases with 13 lesions per case) do not occur in this dataset.

#### 3.10 Summary

- The FROC dataset has far less regularity in structure as compared to an ROC dataset.
- The length of the first dimension of either xNL or xLL list members is the total number of modalities, 2 in the current example.
- The length of the second dimension of either x\$NL or x\$LL list members is the total number of readers, 3 in the current example.
- The length of the third dimension of x\$NL is the total number of cases, 8 in the current example. The first three positions account for NL marks on non-diseased cases and the remaining 5 positions account for NL marks on diseased cases.
- The length of the third dimension of xLL is the total number of diseased cases, 5 in the current example.
- The length of the fourth dimension of x\$NL is determined by the case (diseased or non-diseased) with the most NL marks, 2 in the current example.
- The length of the fourth dimension of x\$LL is determined by the diseased case with the most lesions, 3 in the current example.

### 3.11 References

## Chapter 4

# ROC split plot data format

#### 4.1 Introduction

- The purpose of this vignette is to explain the data format of the input Excel file for an ROC *split-plot* dataset.
- In a split-plot dataset each reader interprets a different sub-set of cases in all modalities, i.e., the cases interpreted by different readers have no overlap.
- Each sub-set of cases can have different numbers of non-diseased and diseased cases.
- The example below assumes the same numbers of non-diseased and diseased cases.
- The data format has been extended to NewFormat to allow such datasets.

#### 4.2 The Excel data format

As before, the Excel file has three worsheets named Truth, NL or FP and LL or TP. The Excel file corresponding to the example that follows is inst/extdata/toyFiles/ROC/rocSp.xlsx.

#### 4.3 The Truth worksheet

The Truth worksheet contains 6 columns: CaseID, LesionID, Weight, ReaderID, ModalityID and Paradigm.

 The first five columns contain as many rows as there are cases in the dataset.

- CaseID: unique integers, one per case, representing the cases in the dataset
- LesionID: integers 0, representing non-diseased cases and 1 representing the diseased cases.
- The ReaderID column is a listing of readers each represented by a **unique string**. Note that, unlike the crossed design, the ReaderID column has *single values*. Each cell has to be text formatted.
- The non-diseased cases interpreted by reader with ReaderID value 1 are labeled 6, 7, 8, 9 and 10, each with LesionID value 0.
- The diseased cases interpreted by this reader are labeled 16, 17, 18, 19 and 20, each with LesionID value 1.
- The second reader, with ReaderID value 4, interprets five non-diseased cases labeled 21, 22, 23, 24 and 25, each with LesionID value 0, and five diseased cases labeled 36, 37, 38, 39 and 40, each with LesionID value 1.
- The third reader, with ReaderID value 5, interprets five non-diseased cases labeled 46, 47, 48, 49 and 50, each with LesionID value 0 and five diseased cases labeled 51, 52, 53, 54 and 55, each with LesionID value 1.
- Weight: floating point value 0 this is not used for ROC data.
- ModalityID: a comma-separated listing of modalities, each represented by a unique string. In the example shown below each cell has the value 1, 2. Each cell has to be text formatted.
- Paradigm: In the example shown in this vignette, the contents are ROC and split-plot.



Figure 4.1: Fig. 1: Truth worksheet for file inst/extdata/toyFiles/ROC/rocSp.xlsx

#### 4.4 The structure of the ROC split plot dataset

• The example shown in Fig. 1 corresponds to Excel file inst/extdata/toyFiles/ROC/rocSp.xlsx in the project directory.

```
rocSp <- system.file("extdata", "toyFiles/ROC/rocSp.xlsx",</pre>
                       package = "RJafroc", mustWork = TRUE)
x <- DfReadDataFile(rocSp, newExcelFileFormat = TRUE)
str(x)
#> List of 12
#> $ NL
                  : num [1:2, 1:3, 1:30, 1] 1 1 -Inf -Inf -Inf ...
#> $ LL
                 : num [1:2, 1:3, 1:15, 1] 5 2.3 -Inf -Inf -Inf ...
#> $ lesionVector : int [1:15] 1 1 1 1 1 1 1 1 1 1 ...
#> $ lesionID : num [1:15, 1] 1 1 1 1 1 1 1 1 1 1 ...
#> $ lesionWeight : num [1:15, 1] 1 1 1 1 1 1 1 1 1 1 ...
#> $ dataType
                 : chr "ROC"
#> $ modalityID : Named chr [1:2] "1" "2"
    ..- attr(*, "names")= chr [1:2] "1" "2"
#> $ readerID : Named chr [1:3] "1" "4" "5"
   ..- attr(*, "names")= chr [1:3] "1" "4" "5"
#> $ design
                 : chr "SPLIT-PLOT"
#> $ normalCases : int [1:15] 6 7 8 9 10 21 22 23 24 25 ...
#> $ abnormalCases: int [1:15] 16 17 18 19 20 36 37 38 39 40 ...
#> \$ truthTableStr: num [1:2, 1:3, 1:30, 1:2] 1 1 NA NA NA NA 1 1 NA NA ...
```

- DfReadDataFile() flag newExcelFileFormat must be set to TRUE for split plot data.
- The dataset object  ${\tt x}$  is a list variable with 12 members.
- There are 15 diseased cases in the dataset (the number of 1's in the LesionID column of the Truth worksheet) and 15 non-diseased cases (the number of 0's in the LesionID column).
- x\$NL, with dimension [2, 3, 30, 1], contains the ratings of normal cases.
   The extra values in the third dimension, filled with NAs, are needed for compatibility with FROC datasets.
- x\$LL, with dimension [2, 3, 15, 1], contains the ratings of abnormal cases.
- The x\$lesionVector member is a vector with 15 ones representing the 15 diseased cases in the dataset.
- The x\$lesionID member is an array with 15 ones (this member is needed for compatibility with FROC datasets).
- The x\$lesionWeight member is an array with 15 ones (this member is needed for compatibility with FROC datasets).
- The dataType member is ROC which specifies the data collection method ("ROC", "FROC", "LROC" or "ROI").
- The x\$modalityID member is a vector with two elements "1" and "2", naming the two modalities.

- The x\$readerID member is a vector with three elements "1", "4" and "5", naming the three modalities.
- The x\$design member is SPLIT-PLOT; specifies the dataset design, which can be either "CROSSED" or "SPLIT-PLOT".
- The x\$normalCases member lists the names of the normal cases, 6, 7, 8, 9, 10, 21, 22, 23, 24, 25, 46, 47, 48, 49, 50.
- The x\$abnormalCases member lists the names of the abnormal cases, 16, 17, 18, 19, 20, 36, 37, 38, 39, 40, 51, 52, 53, 54, 55.
- The x\$truthTableStr member quantifies the structure of the dataset, as explained next. It is used in the DfReadDataFile() function to check for data entry errors.

#### 4.5 The truthTableStr member

- This is a 2 x 3 x 30 x 2 array, i.e., I x J x K x (maximum number of lesions per case plus 1). The plus 1 is needed to accommodate normal cases with lesionID = 0. [Zero is not a valid array subscript in R.]
- Each entry in this array is either 1, meaning the corresponding interpretation exists, or NA, meaning the corresponding interpretation does not exist
- For example, x\$truthTableStr[1,1,1,1] is 1. This means that an interpretation exists for the first treatment (modalityID = 1), first reader (readerID = 1) and first (normal) case (caseID = 6 and lesionID = 0). This example corresponds to row 2 in the TRUTH worksheet.
- The following shows that the first reader interprets the first five normal cases in both modalities.

```
x$truthTableStr[,1,1:15,1]
         [,1] [,2] [,3] [,4] [,5] [,6] [,7] [,8]
                                                      [,9]
                                                           [,10] [,11] [,12] [,13] [,14]
#> [1,]
                       1
                             1
                                   1
                                       NA
                                             NA
                                                  NA
                                                        NA
                                                               NA
                                                                      NA
#> [2,]
                  1
                                                        NA
                                                               NA
                                                                            NA
                                                                                   NA
            1
                       1
                             1
                                   1
                                       NA
                                             NA
                                                  NA
                                                                      NA
                                                                                          NA
#>
         [,15]
#> [1,]
            NA
#> [2,]
```

• In the following all elements are NA because normal cases correspond to lesionID = 1.

```
x$truthTableStr[,1,1:15,2]
                                                [,8]
         [,1]
               [,2] [,3]
                          [,4] [,5] [,6]
                                           [,7]
                                                      [,9] [,10] [,11] [,12] [,13] [,14]
#> [1,]
           NA
                                  NA
                                       NA
                                             NA
                                                   NA
                                                        NA
                                                               NA
                                                                      NA
                                                                             NA
                                                                                   NA
                      NA
                            NA
                                                                                          NA
#> [2,]
           NA
                 NA
                      NA
                            NA
                                  NA
                                       NA
                                             NA
                                                   NA
                                                        NA
                                                               NA
                                                                      NA
                                                                             NA
                                                                                   NA
                                                                                          NA
         [,15]
```

```
#> [1,] NA
#> [2,] NA
```

• The following shows that the second reader interprets the next group of five normal cases, indexed 6 through 10, in both modalities.

```
x$truthTableStr[,2,1:15,1]
         [,1] [,2] [,3] [,4] [,5] [,6] [,7] [,8] [,9] [,10] [,11] [,12] [,13] [,14]
#> [1,]
           NA
                NA
                           NA
                                NA
                                       1
                                            1
                                                  1
                                                        1
                                                              1
                                                                    NA
                                                                          NA
                                                                                 NA
                                                                                        NA
#> [2,]
           NA
                NA
                      NA
                           NA
                                 NA
                                       1
                                             1
                                                  1
                                                        1
                                                                    NA
                                                                           NA
                                                                                 NA
                                                                                        NA
        [,15]
           NA
#> [1,]
#> [2,]
           NA
```

• The following shows that the third reader interprets the next group of five normal cases, indexed 11 through 15, in both modalities.

```
x$truthTableStr[,3,1:15,1]
        [,1] [,2] [,3] [,4] [,5] [,6] [,7] [,8] [,9] [,10] [,11] [,12] [,13] [,14]
#> [1,]
          NA
                NA
                     NA
                           NA
                                NA
                                      NA
                                           NA
                                                 NA
                                                      NA
                                                             NA
                                                                    1
                                                                           1
                                                                                 1
                                                                                        1
#> [2,]
                                                                    1
                                                                           1
                                                                                  1
          NA
                NA
                     NA
                           NA
                                NA
                                      NA
                                           NA
                                                 NA
                                                      NA
                                                             NA
                                                                                        1
#>
        [,15]
#> [1,]
             1
#> [2,]
```

• The following shows that the first reader interprets the first group of five abnormal cases, indexed 16 through 20, in both modalities.

```
x$truthTableStr[,1,16:30,2]
        [,1] [,2] [,3] [,4] [,5] [,6] [,7] [,8] [,9] [,10] [,11] [,12] [,13] [,14]
#> [1,]
                                               NA
                                                     NA
                                                           NA
                                                                  NA
           1
                1
                   1
                           1
                                 1
                                     NA
                                          NA
                                                                        NA
                                                                              NA
                                                                                     NA
#> [2,]
           1
                 1
                      1
                           1
                                 1
                                     NA
                                          NA
                                                NA
                                                     NA
                                                           NA
                                                                  NA
                                                                        NA
                                                                              NA
                                                                                     NA
        [,15]
#> [1,]
           NA
#> [2,]
```

 In the following all elements are NA because abnormal cases correspond to lesionID = 2.

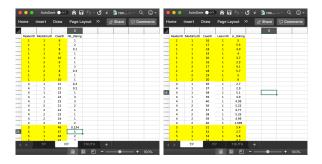


Figure 4.2: Fig. 2 FP/TP worksheets; LEFT=FP, (b) RIGHT=TP

## 4.6 The false positive (FP) ratings

- These are found in the FP or NL worksheet, see Fig. 2, left panel.
- This worksheet has the ratings of non-diseased cases.
- The common vertical length is 30 in this example (2 modalities times 3 readers times 5 non-diseased cases per reader).
- ullet ReaderID: the reader labels: these must be from 1, 4 or 5, as declared in the Truth worksheet.
- ModalityID: the modality labels: 1 or 2, as declared in the Truth worksheet.
- CaseID: the labels of non-diseased cases. Each CaseID ReaderID combination must be consistent with that declared in the Truth worsheet.
- NL\_Rating: the floating point ratings of non-diseased cases. Each row of this worksheet yields a rating corresponding to the values of ReaderID, ModalityID and CaseID for that row.

```
[,1] [,2] [,3] [,4] [,5] [,6] [,7] [,8] [,9] [,10] [,11] [,12] [,13] [,14]
#> [1,] -Inf -Inf -Inf -Inf -Inf 0.2 0.2
                               1
                                    3
                                        3 -Inf -Inf -Inf
#> [2,] -Inf -Inf -Inf -Inf -Inf 2.0 1.0
                                1
                                    1
                                        2 -Inf -Inf -Inf -Inf
     [,15]
#> [1,] -Inf
#> [2,] -Inf
x$NL[,3,1:15,1]
     [,1] [,2] [,3] [,4] [,5] [,6] [,7] [,8] [,9] [,10] [,11] [,12] [,13] [,14]
5
                                                     2
2
                                                     2
                                                          2
     [,15]
#> [1,] 2.00
#> [2,] 0.33
```

- The first line of the above code shows the ratings, in both modalities, of the first five non-diseased cases with CaseIDs 6,7,8,9,10 (indexed 1, 2, 3, 4, 5 and appearing in the first five columns) interpreted by the first reader (ReaderID 1).
- The second line shows the ratings, in both modalities, of the next five non-diseased cases with CaseIDs 21,22,23,24,25 (indexed 6, 7, 8, 9, 10and appearing in the next five columns) interpreted by the second reader (ReaderID 4).
- The third line shows the ratings, in both modalities, of the final five nondiseased cases with CaseIDs 46,47,48,49,50 (indexed 11, 12, 13, 14, 15and appearing in the final five columns) interpreted by the third reader (ReaderID 5).
- Values such as x\$NL[,,16:30,1], which are there for compatibility with FROC data, are all filled with -Inf.

# 4.7 The true positive (TP) ratings

- These are found in the TP or LL worksheet, see Fig. 2, right panel.
- This worksheet has the ratings of diseased cases.
- The common vertical length is 30 in this example (2 modalities times 3 readers times 5 diseased cases per reader).
- ReaderID: the reader labels: these must be from 1, 4 or 5, as declared in the Truth worksheet.
- ModalityID: the modality labels: 1 or 2, as declared in the Truth worksheet.
- CaseID: the labels of diseased cases. Each CaseID ReaderID combination must be consistent with that declared in the Truth worsheet.

• LL\_Rating: the floating point ratings of diseased cases. Each row of this worksheet yields a rating corresponding to the values of ReaderID, ModalityID and CaseID for that row.

```
x$LL[,1,1:15,1]
      [,1] [,2] [,3] [,4] [,5] [,6] [,7] [,8] [,9] [,10] [,11] [,12] [,13] [,14]
#> [1,] 5.0 5.5 4.9 4 3.7 -Inf -Inf -Inf -Inf -Inf
                                                    -Inf
#> [2,] 2.3 4.1 5.7 5 6.0 -Inf -Inf -Inf -Inf -Inf -Inf -Inf
                                                          -Inf
      [,15]
#> [1,] -Inf
#> [2,] -Inf
x$LL[,2,1:15,1]
      [,1] [,2] [,3] [,4] [,5] [,6] [,7] [,8] [,9] [,10] [,11] [,12] [,13] [,14]
#> [1,] -Inf -Inf -Inf -Inf -Inf 2.70 2.90 5.10 4.90 4.990 -Inf -Inf -Inf -Inf
\#>[2,] -Inf -Inf -Inf -Inf -Inf 5.22 4.77 5.33 4.99 1.999 -Inf -Inf -Inf -Inf
      [,15]
#> [1,] -Inf
#> [2,] -Inf
x$LL[,3,1:15,1]
      [,1] [,2] [,3] [,4] [,5] [,6] [,7] [,8] [,9] [,10] [,11] [,12] [,13] [,14]
2.7
5.4
                                                      2.7
      [,15]
#>
#> [1,]
         5
#> [2,]
```

- The first line of code shows the ratings, in both modalities, of the first five diseased cases with CaseIDs 16,17,18,19,20 (indexed 1, 2, 3, 4, 5and appearing in the first five columns) interpreted by the first reader (ReaderID 1).
- The second line shows the ratings, in both modalities, of the next five diseased cases with CaseIDs 36,37,38,39,40 (indexed 6, 7, 8, 9, 10and appearing in the next five columns) interpreted by the second reader (ReaderID 4).
- The third line shows the ratings, in both modalities, of the final five nondiseased cases with CaseIDs 51,52,53,54,55 (indexed 11, 12, 13, 14, 15and appearing in the final five columns) interpreted by the third reader (ReaderID 5).

### 4.8 Summary

 The FROC dataset has far less regularity in structure as compared to an ROC dataset.

- The length of the first dimension of either xNL or xLL list members is the total number of modalities, 2 in the current example.
- The length of the second dimension of either x\$NL or x\$LL list members is the total number of readers, 3 in the current example.
- The length of the third dimension of x\$NL is the total number of cases, 8 in the current example. The first three positions account for NL marks on non-diseased cases and the remaining 5 positions account for NL marks on diseased cases.
- The length of the third dimension of x\$LL is the total number of diseased cases, 5 in the current example.
- The length of the fourth dimension of x\$NL is determined by the case (diseased or non-diseased) with the most NL marks, 2 in the current example.
- The length of the fourth dimension of x\$LL is determined by the diseased case with the most lesions, 3 in the current example.

#### 4.9 References

# Chapter 5

# FROC ROC DATA FORMAT SPLIT PLOT

#### 5.1 Introduction

- The purpose of this vignette is to explain the data format of the input Excel file for an FROC *split-plot* dataset.
- In a split-plot dataset each reader interprets a sub-set of cases in all modalities.
- The cases interpreted by different readers have no overlap.
- It is assumed, for now, that each sub-set of cases has the same numbers of non-diseased and diseased cases.

#### 5.2 The Excel data format

The Excel file has three worsheets named Truth, NL or FP and LL or TP.

#### 5.3 The Truth worksheet

The Truth worksheet contains 6 columns: CaseID, LesionID, Weight, ReaderID, ModalityID and Paradigm.

• The first five columns contain as many rows as there are non-diseased cases (9) plus total number of lesions (27) in the dataset (each row with a non-zero LesionID corresponds to a lesion).

- CaseID: unique integers, one per case, representing the cases in the dataset.
- LesionID: integers 0, 1, 2, etc., with each 0 representing a non-diseased case, 1 representing the *first* lesion on a diseased case, 2 representing the second lesion on a diseased case, if present, and so on.
- The three non-diseased cases interpreted by reader with ReaderID value 0 are labeled 1, 2, 3, while the diseased cases interpreted by this reader are labeled 70, 71, 72, 73 and 74, with LesionID values ranging from 1 to 3.
- The second reader, with ReaderID value 1, interprets three non-diseased cases labeled 4, 5 and 6, each with LesionID value 0, and five diseased cases labeled 80, 81, 82, 83 and 84, with LesionID values ranging from 1 to 3.
- The third reader, with ReaderID value 2, interprets three non-diseased cases labeled 7, 8 and 9, each with LesionID value 0 and five diseased cases labeled 90, 91, 92, 93 and 94, with LesionID values ranging from 1 to 3.
- Weight: floating point value adding upto unity for diseased cases as required for FROC data.
- ModalityID: a comma-separated listing of modalities, each represented by
  a unique integer. In the example shown below each cell has the value 0,
   1. Each cell has to be text formatted.
- Paradigm: In the example shown below, the contents are FROC and split-plot.



Figure 5.1: Two views of Truth worksheet for file frocSp.xlsx

#### 5.4 The structure of the FROC split plot dataset

The example shown in Fig. 1 corresponds to Excel file inst/extdata/toyFiles/FROC/frocSp.xlsx in the project directory.

```
frocSp <- system.file("extdata", "toyFiles/FROC/frocSp.xlsx",</pre>
                       package = "RJafroc", mustWork = TRUE)
x <- DfReadDataFile(frocSp, newExcelFileFormat = TRUE)
str(x)
#> List of 12
#> $ NL
                  : num [1:2, 1:3, 1:24, 1:3] 1.02 2.89 -Inf -Inf -Inf ...
#> $ LL
                  : num [1:2, 1:3, 1:15, 1:3] 5.28 5.2 -Inf -Inf -Inf ...
#> $ lesionVector : int [1:15] 2 1 3 2 1 2 1 3 2 1 ...
#> $ lesionID : num [1:15, 1:3] 1 1 1 1 1 1 1 1 1 1 ...
#> $ lesionWeight : num [1:15, 1:3] 0.3 1 0.333 0.1 1 ...
                 : chr "FROC"
#> $ dataType
#> $ modalityID : Named chr [1:2] "0" "1"
   ..- attr(*, "names")= chr [1:2] "0" "1"
                 : Named chr [1:3] "0" "1" "2"
#> $ readerID
    ..- attr(*, "names")= chr [1:3] "0" "1" "2"
               : chr "SPLIT-PLOT"
#> $ design
#> $ normalCases : int [1:9] 1 2 3 4 5 6 7 8 9
#> $ abnormalCases: int [1:15] 70 71 72 73 74 80 81 82 83 84 ...
#> \$ truthTableStr: num [1:2, 1:3, 1:24, 1:4] 1 1 NA NA NA NA 1 1 NA NA \ldots
```

- Flag newExcelFileFormat must be set to TRUE for split plot data.
- The dataset object x is a list variable with 12 members.
- Note that the dataType member is FROC and the design member is SPLIT-PLOT.
- There are 15 diseased cases in the dataset (the number of 1's in the LesionID column of the Truth worksheet) and 9 non-diseased cases (the number of 0's in the LesionID column).
- The x\$lesionVector member is a vector with 15 ones representing the 15 diseased cases in the dataset.
- The x\$lesionID member is a 15 x 3 array labeling the lesions in the dataset.
- The x\$lesionWeight member is a 15 x 3 array.

```
x$lesionVector
#> [1] 2 1 3 2 1 2 1 3 2 1 2 1 3 2 1
x$lesionID
#> [,1] [,2] [,3]
#> [1,] 1 2 -Inf
#> [2,] 1 -Inf -Inf
#> [3,] 1 2 3
```

```
[4,]
                  2 -Inf
#>
    [5,]
               -Inf -Inf
    [6,]
                  2 -Inf
#>
             1
    [7,]
               -Inf -Inf
#>
#>
    [8,]
             1
                  2
                        3
    [9,]
                  2 - Inf
#>
             1
#>
   [10,]
               -Inf -Inf
             1
   [11,]
             1
                  2 -Inf
#> [12,]
               -Inf -Inf
             1
#> [13,]
                  2
                  2 -Inf
#> [14,]
             1
#> [15,]
             1 - Inf - Inf
x$lesionWeight
#>
               [,1]
                                     [,3]
                          [,2]
#>
    [1,] 0.3000000 0.7000000
                                     -Inf
    [2,] 1.0000000
                          -Inf
                                     -Inf
    [3,] 0.3333333 0.3333333 0.3333333
#>
    [4,] 0.1000000 0.9000000
#>
                                     -Inf
    [5,] 1.0000000
                          -Inf
                                     -Inf
    [6,] 0.3000000 0.7000000
                                     -Inf
    [7,] 1.0000000
#>
                          -Inf
                                     -Inf
#>
    [8,] 0.3333333 0.3333333 0.3333333
    [9,] 0.1000000 0.9000000
                                     -Inf
#> [10,] 1.0000000
                          -Inf
                                     -Inf
#> [11,] 0.3000000 0.7000000
                                     -Inf
#> [12,] 1.0000000
                          -Inf
                                     -Inf
#> [13,] 0.3333333 0.3333333 0.33333333
#> [14,] 0.1000000 0.9000000
                                     -Inf
#> [15,] 1.0000000
                          -Inf
                                     -Inf
```

- The x\$truthTableStr member is a 2 x 3 x 24 x 4 array, i.e., I x J x K x (maximum number of lesions per case plus 1). The plus 1 is needed to accommodate normal cases with lesionID = 0.
- Each entry in this array is either 1, meaning the corresponding interpretation exists, or NA, meaning the corresponding interpretation does not exist.
- For example, x\$truthTableStr[1,1,1,1] is 1. This means that an interpretation exists for the first treatment (modalityID = 0), first reader (readerID = 0) and first (normal) case caseID = 1 and lesionID = 0. This example corresponds to row 2 in the TRUTH worksheet.
- x\$truthTableStr[1,1,4,1] is NA, which means an interpretation does not exist for the first treatment, first reader and fourth (normal) case.
- However, x\$truthTableStr[1,2,4,1] is 1, which means an interpretation does exist for the first treatment, second reader and fourth (normal) case. This example corresponds to row 5 in the TRUTH worksheet.

- Likewise, x\$truthTableStr[1,1,10,3] is 1, which means an interpretation does exist for the first treatment, first reader, tenth (abnormal) case and lesionID = 2. This example corresponds to row 12 in the TRUTH worksheet.
- As an aside, in the FROC paradigm an interpretation need not yield a
  mark-rating pair. An interpretation means the reader was "exposed to"
  and had the opportunity to mark the corresponding treatment-readercase-lesion combination.
- The reader should confirm that the contents of x\$truthTableStr summarizes the structure of the data in the TRUTH worksheet.

#### 5.5 The false positive (FP) ratings

These are found in the FP or NL worksheet, see Fig. 2.

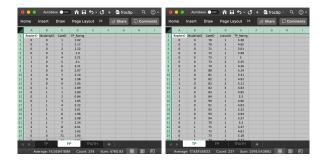


Figure 5.2: NL/FP worksheet, left, and LL/TP worksheet, right, for file froc Sp.xlsx  $\,$ 

- This worksheet has the ratings of non-diseased cases.
- The common vertical length is 30 in this example (2 modalities times 3 readers times 5 non-diseased cases per reader).
- ullet ReaderID: the reader labels: these must be from 0, 1 or 2, as declared in the Truth worksheet.
- ModalityID: the modality labels: 0 or 1, as declared in the Truth worksheet.
- CaseID: the labels of non-diseased cases. Each CaseID, ModalityID, ReaderID combination must be consistent with that declared in the Truth worsheet.
- FP\_Rating: the floating point ratings of non-diseased cases. Each row of this worksheet yields a rating corresponding to the values of ReaderID, ModalityID and CaseID for that row. Each CaseID, ModalityID, ReaderID combination must be consistent with that declared in the Truth worsheet.

```
x$NL[,1,1:9,1]
#>      [,1] [,2] [,3] [,4] [,5] [,6] [,7] [,8] [,9]
#> [1,] 1.02 2.22 1.90 -Inf -Inf -Inf -Inf -Inf -Inf -Inf
#> [2,] 2.89 0.84 1.85 -Inf -Inf -Inf -Inf -Inf -Inf
x$NL[,2,1:9,1]
#>      [,1] [,2] [,3] [,4] [,5] [,6] [,7] [,8] [,9]
#> [1,] -Inf -Inf -Inf 2.21 3.10 2.21 -Inf -Inf -Inf
#> [2,] -Inf -Inf -Inf 3.22 3.01 1.96 -Inf -Inf -Inf
x$NL[,3,1:9,1]
#>      [,1] [,2] [,3] [,4] [,5] [,6] [,7] [,8] [,9]
#> [1,] -Inf -Inf -Inf -Inf -Inf 2.14 1.98 1.95
#> [2,] -Inf -Inf -Inf -Inf -Inf -Inf 2.24 4.01 1.65
```

- The first line of the above code shows the ratings, in both modalities, of the first three non-diseased cases with CaseIDs 1,3,3 (indexed 1, 2, 3 and appearing in the first three columns) interpreted by the first reader (ReaderID 0).
- The second line shows the ratings, in both modalities, of the next three non-diseased cases with CaseIDs 4,5,6 (indexed 4, 5, 6 and appearing in the next three columns) interpreted by the second reader (ReaderID 1).
- The third line shows the ratings, in both modalities, of the final three non-diseased cases with CaseIDs 7,8,9 (indexed 7, 8, 9and appearing in the final three columns) interpreted by the third reader (ReaderID 2).
- Values such as x\$NL[,,16:30,1], which are there for compatibility with FROC data, are all filled with -Inf.

# 5.6 The true positive (TP) ratings

These are found in the TP or LL worksheet, see below.

- This worksheet has the ratings of diseased cases.
- The common vertical length is 30 in this example (2 modalities times 3 readers times 5 diseased cases per reader).
- ReaderID: the reader labels: these must be from 0, 1 or 2, as declared in the Truth worksheet.
- ModalityID: the modality labels: 0 or 1, as declared in the Truth worksheet.
- CaseID: the labels of diseased cases. Each CaseID, ModalityID, ReaderID combination must be consistent with that declared in the Truth worsheet.
- TP\_Rating: the floating point ratings of diseased cases. Each row of this worksheet yields a rating corresponding to the values of ReaderID, ModalityID and CaseID for that row. Each CaseID, ModalityID,

5.7. SUMMARY 49

ReaderID combination must be consistent with that declared in the Truth worsheet.

```
x$LL[,1,1:15,1]
     [,1] [,2] [,3] [,4] [,5] [,6] [,7] [,8] [,9] [,10] [,11] [,12] [,13] [,14]
[,15]
#> [1,] -Inf
#> [2,] -Inf
x$LL[,2,1:15,1]
    [,1] [,2] [,3] [,4] [,5] [,6] [,7] [,8] [,9] [,10] [,11] [,12] [,13] [,14]
#> [1,] -Inf -Inf -Inf -Inf -Inf 5.14 3.31 4.92 4.95 5.30 -Inf -Inf -Inf -Inf
#> [2,] -Inf -Inf -Inf -Inf -Inf 4.77 3.19 5.20 5.39 5.01 -Inf -Inf -Inf -Inf
    [,15]
#> [1,] -Inf
#> [2,] -Inf
x$LL[,3,1:15,1]
     [,1] [,2] [,3] [,4] [,5] [,6] [,7] [,8] [,9] [,10] [,11] [,12] [,13] [,14]
#>
    [,15]
#> [1,] 5.27
#> [2,] 4.78
```

- The first line of code shows the ratings, in both modalities, of the first five diseased cases with CaseIDs 70,71,72,73,74 (indexed 1, 2, 3, 4, 5 and appearing in the first five columns) interpreted by the first reader (ReaderID 0).
- The second line shows the ratings, in both modalities, of the next five diseased cases with CaseIDs 80,81,82,83,84 (indexed 6, 7, 8, 9, 10 and appearing in the next five columns) interpreted by the second reader (ReaderID 1).
- The third line shows the ratings, in both modalities, of the final five nondiseased cases with CaseIDs 90,91,92,93,94 (indexed 11, 12, 13, 14, 15 and appearing in the final five columns) interpreted by the third reader (ReaderID 2).

# 5.7 Summary

TBA

# 5.8 References

# Chapter 6

# QUICK START DBM1

#### 6.1 Introduction

- This vignette is intended for those seeking a quick transition from Windows JAFROC to RJafroc.
- Described first is the structure of an RJafroc dataset followed by how to read a JAFROC format Excel file to create an RJafroc dataset.

#### 6.2 An ROC dataset

Dataset dataset03 corresponding to the Franken ROC data (Franken et al., 1992) is predefined. The following code shows the structure of this dataset.

```
#> $ abnormalCases: int [1:67] 34 35 36 37 38 39 40 41 42 43 ...
#> $ truthTableStr: num [1:2, 1:4, 1:100, 1:2] 1 1 1 1 1 1 1 1 1 1 ...
```

- It is a list with 8 members. The false positive ratings are contained in {NL}, an array with dimensions [1:2,1:4,1:100,1]. The first index corresponds to treatments, and since the dataset has 2 treatments, the corresponding dimension is 2. The second index corresponds to readers, and since the dataset has 4 readers, the corresponding dimension is 4. The third index corresponds to the total number of cases. Since the dataset has 100 cases, the corresponding dimension is 100. But, as you can see from the code below, the entries in this array for cases 34 through 100 are -Inf: i.e., all(dataset03\$NL[1,1,34:100,1] == -Inf) = TRUE.
- This is because in the ROC paradigm false positive are not possible on diseased cases. So the actual FP ratings are contained in the first 33 elements of the array. How did I know that there are 33 non-diseased cases? This can be understood in several ways.
- LL is an array with dimensions [1:2,1:4,1:67,1]. This implies 67 diseased cases, and by subtraction from 100, there must be 33 non-diseased cases.
- The list member lesionVector is a vector with length 67, implying 33 non-diseased cases.
- The list members lesionID and lesionWeight are arrays with dimensions [1:67,1] containing ones. Again, these imply 67 diseased cases.
- The fields lesionVector, lesionID and lesionWeight, while not needed for ROC data, are needed for the FROC paradigm.

The dataType list member is the character string "ROC", characterizing the ROC dataset.

```
dataset03$dataType
#> [1] "ROC"
```

The modalityID list member is a character string with two entries, "TREAT1" and "TREAT2", corresponding to the two modalities.

```
dataset03$modalityID
#> TREAT1 TREAT2
#> "TREAT1" "TREAT2"
```

The readerID list member is a character string with four entries, "READER\_1", "READER\_3" and "READER\_4" corresponding to the four readers.

```
dataset03$readerID
#> READER_1 READER_2 READER_3 READER_4
#> "READER_1" "READER_2" "READER_4"
```

Here are the actual ratings for cases 1:34.

```
dataset03$NL[1,1,1:33,1]
#> [1] 3 1 2 2 2 2 2 4 1 1 4 2 1 2 4 2 1 2 1 2 4 2 3 2 2 2 4 3 2 2 2 5 3
```

- This says that for treatment 1 and reader 1, (non-diseased) case 1 was rated 3, case 2 was rated 1, cases 3-7 were rated 2, case 8 was rated 4, etc.
- As another example, for treatment 2 and reader 3, the FP ratings are:

```
dataset03$NL[2,3,1:33,1]
#> [1] 3 1 2 2 2 2 4 4 2 3 2 2 1 3 2 4 2 3 2 2 2 2 2 4 2 2 1 2 2 2 2 4 2
```

# 6.3 Creating a dataset from a JAFROC format file

There is a file RocData.xlsx that is part of the package installation. Since it is a system file one must get its name as follows.

```
fileName <- "RocData.xlsx"
sysFileName <- system.file(paste0("extdata/",fileName), package = "RJafroc", mustWork = TRUE)</pre>
```

Next, one uses  ${\tt DfReadDataFile}()$  as follows, assuming it is a JAFROC format file.

```
#> ...- attr(*, "names")= chr [1:5] "0" "1" "2" "3" ...
#> $ design : chr "CROSSED"
#> $ normalCases : int [1:69] 1 2 3 4 5 6 7 8 9 10 ...
#> $ abnormalCases: int [1:45] 70 71 72 73 74 75 76 77 78 79 ...
#> $ truthTableStr: num [1:2, 1:5, 1:114, 1:2] 1 1 1 1 1 1 1 1 1 1 ...
```

Analysis is illustrated for dataset03, but one could have used the newly created dataset ds.

#### 6.4 Analyzing the ROC dataset

This illustrates the StSignificanceTesting() function. The significance testing method is specified as "DBMH" and the figure of merit FOM is specified as "Wilcoxon".

```
ret <- StSignificanceTesting(dataset03, FOM = "Wilcoxon", method = "DBMH")
print(ret)
#> $fomArray
            RdrREADER_1 RdrREADER_2 RdrREADER_3 RdrREADER_4
#> TrtTREAT1 0.8534600 0.8649932
                                     0.8573044
                                                 0.8152420
#> TrtTREAT2 0.8496156
                          0.8435097 0.8401176
                                                 0.8143374
#>
#> $anovaY
#>
        Source
                         SS DF
#> 1
       Row1_T 0.02356541 1 0.023565410
#> 2
       Row2_R 0.20521800
                            3 0.068406000
       Row3_C 52.52839868 99 0.530589886
#> 3
#> 4
     Row4_TR 0.01506079
                            3 0.005020264
       Row5_TC 6.41004881 99 0.064747968
#> 5
#> 6
       Row6_RC 39.24295381 297 0.132131158
      Row7_TRC 22.66007764 297 0.076296558
#> 8 Row8_Total 121.08532315 799
#>
#> $anovaYi
#> Source DF TrtTREAT1 TrtTREAT2
       R 3 0.04926635 0.02415991
        C 99 0.29396753 0.30137032
#> 3
        RC 297 0.10504787 0.10337984
#>
#> $varComp
                       varC
                                   varTR
                                                varTC
                                                          varRC
                                                                   varErr
            varR.
#> 1 3.775568e-05 0.05125091 -0.0007127629 -0.002887147 0.0279173 0.07629656
```

```
#> $FTestStatsRRRC
      fRRRC ndfRRRC ddfRRRC
                            pRRRC
#> 1 4.694058 1 3 0.1188379
#>
#> $ciDiffTrtRRRC
              TrtDiff Estimate StdErr DF t PrGTt CILower
#>
#> 1 TrtTREAT1-TrtTREAT2 0.01085482 0.005010122 3 2.166577 0.1188379 -0.005089627
#> 1 0.02679926
#>
#> $ciAvqRdrEachTrtRRRC
#> Treatment Area StdErr DF CILower CIUpper
#> 1 TrtTREAT1 0.8477499 0.02440215 70.12179 0.7990828 0.8964170
#> 2 TrtTREAT2 0.8368951 0.02356642 253.64403 0.7904843 0.8833058
#>
#> $FTestStatsFRRC
#> fFRRC ndfFRRC ddfFRRC pFRRC
#>
#> $ciDiffTrtFRRC
            Treatment Estimate StdErr DF t PrGTt
#>
#> 1 TrtTREAT1-TrtTREAT2 0.01085482 0.01799277 99 0.6032876 0.547697 -0.02484675
#> CIUpper
#> 1 0.04655638
#>
#> $ciAvgRdrEachTrtFRRC
#> Treatment Area StdErr DF CILower CIUpper
#> 1 TrtTREAT1 0.8477499 0.02710939 99 0.7939590 0.9015408
#> 2 TrtTREAT2 0.8368951 0.02744860 99 0.7824311 0.8913591
#>
#> $msAnovaEachRdrFRRC
#> Source DF RdrREADER_1 RdrREADER_2 RdrREADER_3 RdrREADER_4
C 99 0.2038747746 0.22344191 0.21424677 2.854199e-01
#> 3 TC 99 0.0915587344 0.08027926 0.06122898 6.057067e-02
#>
#> $ciDiffTrtEachRdrFRRC
       Reader
                     Treatment Estimate StdErr DF
#>
#> 1 RdrREADER_1 TrtTREAT1-TrtTREAT2 0.0038444143 0.04279223 99 0.08983908
#> 2 RdrREADER 2 TrtTREAT1-TrtTREAT2 0.0214834916 0.04006975 99 0.53615233
#> 3 RdrREADER_3 TrtTREAT1-TrtTREAT2 0.0171867933 0.03499399 99 0.49113552
#> 4 RdrREADER_4 TrtTREAT1-TrtTREAT2 0.0009045681 0.03480536 99 0.02598933
#> PrGTt CILower CIUpper
#> 1 0.9285966 -0.08106465 0.08875348
#> 2 0.5930559 -0.05802359 0.10099057
```

```
#> 3 0.6244176 -0.05224888 0.08662247
#> 4 0.9793182 -0.06815683 0.06996596
#>
#> $FTestStatsRRFC
       fRRFC ndfRRFC ddfRRFC
                    1
#> 1 4.694058
                            3 0.1188379
#> $ciDiffTrtRRFC
               Treatment
                           Estimate
                                         StdErr DF
#> 1 TrtTREAT1-TrtTREAT2 0.01085482 0.005010122 3 2.166577 0.1188379 -0.005089627
       CIUpper
#> 1 0.02679926
#> $ciAvgRdrEachTrtRRFC
     Treatment
                    Area
                             StdErr DF
                                         CILower
                                                    CIUpper
#> 1 TrtTREAT1 0.8477499 0.01109801 3 0.8124311 0.8830687
#> 2 TrtTREAT2 0.8368951 0.00777173 3 0.8121620 0.8616282
```

#### 6.5 Explanation of the output

The function returns a long unwieldy list. Let us consider them one by one. The function UtilOutputReport(), which can generate an Excel file report, making it much easier to visualize the results, is described in another vignette.

#### 6.5.1 FOMs

• fomArray contains the [1:2,1:4] FOM values.

```
ret$fomArray

#> RdrREADER_1 RdrREADER_2 RdrREADER_3 RdrREADER_4

#> TrtTREAT1 0.8534600 0.8649932 0.8573044 0.8152420

#> TrtTREAT2 0.8496156 0.8435097 0.8401176 0.8143374
```

This shows the 2 x 4 array of FOM values.

#### 6.5.2 Pseudovalue ANOVA table

 anovaY, where the Y denotes that these are pseudovalue based, is the ANOVA table.

```
ret$anovaY
#>
        Source
#> 1
        Row1_T
               0.02356541 1 0.023565410
#> 2 Row2_R 0.20521800 3 0.068406000
       Row3_C 52.52839868 99 0.530589886
#> 3
#> 4
      Row4_TR 0.01506079
                           3 0.005020264
#> 5
      Row5_TC 6.41004881 99 0.064747968
#> 6 Row6_RC 39.24295381 297 0.132131158
#> 7 Row7_TRC 22.66007764 297 0.076296558
#> 8 Row8_Total 121.08532315 799
```

#### 6.5.3 Pseudovalue ANOVA table, each treatment

• anovaYi is the ANOVA table for individual treatments.

```
ret$anovaYi

#> Source DF TrtTREAT1 TrtTREAT2

#> 1 R 3 0.04926635 0.02415991

#> 2 C 99 0.29396753 0.30137032

#> 3 RC 297 0.10504787 0.10337984
```

The 0 and 1 headers come from the treatment names.

#### 6.5.4 Pseudovalue Variance Components

• varComp is the variance components (needed for sample size estimation).

```
ret$varComp

#> varR varC varTR varTC varRC varErr

#> 1 3.775568e-05 0.05125091 -0.0007127629 -0.002887147 0.0279173 0.07629656
```

#### 6.5.5 Random-reader random-case (RRRC) analysis

• ret\$FTestStatsRRRC\$fRRRC is the F-statistic for testing the NH that the treatments have identical FOMs. RRRC means random-reader random-case generalization.

```
ret$FTestStatsRRRC$fRRRC
#> [1] 4.694058
```

#### 6.5.5.1 F-statistic and p-value for RRRC analysis

 ret\$FTestStatsRRRC\$ddfRRRC is the denominator degrees of freedom of the F-statistic.

```
ret$FTestStatsRRRC$ddfRRRC
#> [1] 3
```

• ret\$FTestStatsRRRC\$pRRRC is the p-value of the test.

```
ret$FTestStatsRRRC$pRRRC
#> [1] 0.1188379
```

#### 6.5.5.2 Confidence Intervals for RRRC analysis

• ciDiffTrtRRC is the 95% confidence interval of reader-averaged differences between treatments.

• ciAvgRdrEachTrtRRRC is the 95% confidence interval of reader-averaged FOMs for each treatments.

```
ret$ciAvgRdrEachTrtRRRC
#> Treatment Area StdErr DF CILower CIUpper
#> 1 TrtTREAT1 0.8477499 0.02440215 70.12179 0.7990828 0.8964170
#> 2 TrtTREAT2 0.8368951 0.02356642 253.64403 0.7904843 0.8833058
```

#### 6.5.6 Fixed-reader random-case (FRRC) analysis

#### 6.5.6.1 F-statistic and p-value for FRRC analysis

• ret\$FTestStatsFRRC\$fFRRC is the F-statistic for fixed-reader random-case analysis.

```
ret$FTestStatsFRRC$fFRRC

#> [1] 0.363956
```

• ret\$FTestStatsFRRC\$ndfFRRC is the numerator degrees of freedom of the F-statistic, always one less than the number of treatments.

```
ret$FTestStatsFRRC$ndfFRRC
#> [1] 1
```

• ret\$FTestStatsFRRC\$ddfFRRC is the denominator degrees of freedom of the F-statistic, for fixed-reader random-case analysis.

```
ret$FTestStatsFRRC$ddfFRRC
#> [1] 99
```

• ret\$FTestStatsFRRC\$pFRRC is the p-value for fixed-reader random-case analysis.

```
ret$FTestStatsFRRC$pFRRC
#> [1] 0.547697
```

#### 6.5.6.2 Confidence Intervals for FRRC analysis

• ciDiffTrtFRRC is the 95% CI of reader-average differences between treatments for fixed-reader random-case analysis

• ret\$ciAvgRdrEachTrtFRRC is the 95% CI of reader-average FOMs of each treatment for fixed-reader random-case analysis

```
ret$ciAvgRdrEachTrtFRRC

#> Treatment Area StdErr DF CILower CIUpper

#> 1 TrtTREAT1 0.8477499 0.02710939 99 0.7939590 0.9015408

#> 2 TrtTREAT2 0.8368951 0.02744860 99 0.7824311 0.8913591
```

#### 6.5.6.3 ANOVA for FRRC analysis

• ret\$msAnovaEachRdrFRRC is the mean-squares ANOVA for each reader

#### 6.5.6.4 Confidence Intervals for FRRC analysis

• ciDiffTrtFRRC is the CI for reader-averaged treatment differences, for fixed-reader random-case analysis

```
ret$ciDiffTrtFRRC

#> Treatment Estimate StdErr DF t PrGTt CILower

#> 1 TrtTREAT1-TrtTREAT2 0.01085482 0.01799277 99 0.6032876 0.547697 -0.02484675

#> CIUpper

#> 1 0.04655638
```

#### 6.5.7 Random-reader fixed-case (RRFC) analysis

#### 6.5.7.1 F-statistic and p-value for RRFC analysis

 $\bullet\,$  ret\$FTestStatsRRFC\$fRRFC is the F-statistic for for random-reader fixed-case analysis

```
ret$FTestStatsRRFC$fRRFC
#> [1] 4.694058
```

-  ${\tt ret\$FTestStatsRRFC\$ddfRRFC} \ {\tt is} \ {\tt the} \ {\tt ddf} \ {\tt for} \ {\tt for} \ {\tt random-reader} \ {\tt fixed-case} \\ {\tt analysis}$ 

```
ret$FTestStatsRRFC$ddfRRFC
#> [1] 3
```

• ret\$FTestStatsRRFC\$pRRFC is the p-value for for random-reader fixed-case analysis

```
ret$FTestStatsRRFC$pRRFC
#> [1] 0.1188379
```

#### 6.5.7.2 Confidence Intervals for RRFC analysis

• ciDiffTrtRRFC is the CI for reader-averaged inter-treatment FOM differences for random-reader fixed-case analysis

```
ret$ciDiffTrtRRFC

#> Treatment Estimate StdErr DF t PrGTt CILower

#> 1 TrtTREAT1-TrtTREAT2 0.01085482 0.005010122 3 2.166577 0.1188379 -0.005089627

#> CIUpper

#> 1 0.02679926
```

• ciAvgRdrEachTrtRRFC is the CI for treatment FOMs for each reader for random-reader fixed-case analysis

```
ret$ciAvgRdrEachTrtRRFC

#> Treatment Area StdErr DF CILower CIUpper

#> 1 TrtTREAT1 0.8477499 0.01109801 3 0.8124311 0.8830687

#> 2 TrtTREAT2 0.8368951 0.00777173 3 0.8121620 0.8616282
```

#### 6.6 ORH significance testing

Simply change method = "DBMH" to method = "ORH".

```
ret <- StSignificanceTesting(dataset03, FOM = "Wilcoxon", method = "ORH")
str(ret)
#> List of 14
#> $ fomArray
                         : num [1:2, 1:4] 0.853 0.85 0.865 0.844 0.857 ...
   ..- attr(*, "dimnames")=List of 2
    ....$ : chr [1:2] "TrtTREAT1" "TrtTREAT2"
   ....$ : chr [1:4] "RdrREADER_1" "RdrREADER_2" "RdrREADER_3" "RdrREADER_4"
#> $ meanSquares
                        :'data.frame': 1 obs. of 3 variables:
#>
    ..$ msT : num 0.000236
    ..$ msR : num 0.000684
    ..$ msTR: num 5.02e-05
                         :'data.frame': 1 obs. of 6 variables:
#> $ varComp
    ..$ varR : num 2.33e-05
    ..$ varTR: num -0.000684
    ..$ cov1 : num 0.000792
    ..$ cov2 : num 0.000484
    ..$ cov3 : num 0.000513
    ..$ var : num 0.00153
#> $ FTestStatsRRRC
                         :'data.frame': 1 obs. of 4 variables:
#> ..$ fRRRC : num 4.69
```

```
#> ..$ ndfRRRC: num 1
    ..$ ddfRRRC: num 3
    ..$ pRRRC : num 0.119
#> $ ciDiffTrtRRRC :'data.frame': 1 obs. of 8 variables:
   ..$ Treatment: chr "TrtTREAT1-TrtTREAT2"
#>
    ..$ Estimate : num 0.0109
    ..$ StdErr : num 0.00501
    ..$ DF : num 3
#>
#>
    ..$ t
               : num 2.17
    ..$ PrGTt : num 0.119
#>
    ..$ CILower : num -0.00509
#>
   ..$ CIUpper : num 0.0268
#> $ ciAvqRdrEachTrtRRRC : 'data.frame': 2 obs. of 6 variables:
   ..$ Treatment: Factor w/ 2 levels "TrtTREAT1", "TrtTREAT2": 1 2
    ..$ Area : num [1:2] 0.848 0.837
#>
   ..$ StdErr : num [1:2] 0.0244 0.0236
#>
    ..$ DF : num [1:2] 70.1 253.6
    ..$ CILower : num [1:2] 0.799 0.79
   ..$ CIUpper : num [1:2] 0.896 0.883
#> $ FTestStatsFRRC :'data.frame': 1 obs. of 4 variables:
   ..$ fFRRC : num 0.364
#>
#>
   ..$ ndfFRRC: num 1
   ..$ ddfFRRC: num Inf
    ..$ pFRRC : num 0.546
#> $ ciDiffTrtFRRC :'data.frame': 1 obs. of 8 variables:
   ..$ Treatment: chr "TrtTREAT1-TrtTREAT2"
   ..$ Estimate : num 0.0109
#>
#> ..$ StdErr : num 0.018
#> ..$ DF
               : num Inf
               : num 0.603
    ..$ t
#>
#> ..$ PrGTt : num 0.546
    ..$ CILower : num -0.0244
#>
    ..$ CIUpper : num 0.0461
#> $ ciAuqRdrEachTrtFRRC :'data.frame': 2 obs. of 6 variables:
   ..$ Treatment: Factor w/ 2 levels "TrtTREAT1", "TrtTREAT2": 1 2
   ..$ Area : num [1:2] 0.848 0.837
#>
    ..$ StdErr : num [1:2] 0.0271 0.0274
#>
#>
    ..$ DF : num [1:2] Inf Inf
    ..$ CILower : num [1:2] 0.795 0.783
    ..$ CIUpper : num [1:2] 0.901 0.891
#>
#> $ ciDiffTrtEachRdrFRRC:'data.frame': 4 obs. of 9 variables:
   ..$ Reader : Factor w/ 4 levels "RdrREADER_1",..: 1 2 3 4
#>
   ..$ Treatment: Factor w/ 1 level "TrtTREAT1-TrtTREAT2": 1 1 1 1
    ..$ Estimate : num [1:4] 0.003844 0.021483 0.017187 0.000905
#>
    ..$ StdErr : num [1:4] 0.0428 0.0401 0.035 0.0348
```

```
#> ..$ DF : num [1:4] Inf Inf Inf
               : num [1:4] 0.0898 0.5362 0.4911 0.026
    ..$ t
    ..$ PrGTt : num [1:4] 0.928 0.592 0.623 0.979
   ..$ CILower : num [1:4] -0.08 -0.0571 -0.0514 -0.0673
#> ..$ CIUpper : num [1:4] 0.0877 0.1 0.0858 0.0691
#> $ varCovEachRdr :'data.frame': 4 obs. of 3 variables:
   ..$ Reader: Factor w/ 4 levels "RdrREADER_1",..: 1 2 3 4
   ..$ Var : num [1:4] 0.00148 0.00152 0.00138 0.00173
   ..$ Cov1 : num [1:4] 0.000562 0.000716 0.000765 0.001124
#> $ FTestStatsRRFC :'data.frame': 1 obs. of 4 variables:
   ..$ fRRFC : num 4.69
#> ..$ ndfRRFC: num 1
#> ..$ ddfRRFC: num 3
    ..$ pRRFC : num 0.119
#> $ ciDiffTrtRRFC :'data.frame': 1 obs. of 8 variables:
   ..$ Treatment: chr "TrtTREAT1-TrtTREAT2"
#>
    ..$ Estimate : num 0.0109
    ..$ StdErr : num 0.00501
   ..$ DF : num 3
   ..$ t
               : num 2.17
   ..$ PrGTt : num 0.119
#>
#>
    ..$ CILower : num -0.00509
   ..$ CIUpper : num 0.0268
#> $ ciAvgRdrEachTrtRRFC : 'data.frame': 2 obs. of 6 variables:
   ..$ Treatment: Factor w/ 2 levels "TrtTREAT1", "TrtTREAT2": 1 2
   ..$ Area : num [1:2] 0.848 0.837
   ..$ StdErr : num [1:2] 0.0111 0.00777
#> ..$ DF : num [1:2] 3 3
    ..$ CILower : num [1:2] 0.812 0.812
#>
#> ..$ CIUpper : num [1:2] 0.883 0.862
```

#### 6.7 References

# Chapter 7

# QUICK START DBM2

#### 7.1 Introduction

This vignette illustrates significance testing using the DBMH method. But, instead of the unwieldy output in *QuickStartDBMH.html*, it generates an Excel output file containing the following worksheets:

- Summary
- FOMs
- RRRC
- FRRC
- RRFC
- ANOVA

# 7.2 Generating the Excel output file

This illustrates the UtilOutputReport() function. The significance testing method is "DBMH", the default, and the figure of merit FOM is "Wilcoxon". Note ReportFileExt = "xlsx" telling the function to create an Excel output file. The Excel output is created in a temporary file.

```
ret <- UtilOutputReport(dataset03, FOM = "Wilcoxon", overWrite = TRUE, ReportFileExt = "xlsx")
#>
#> Output file name is: /var/folders/d1/mx6dcbzx3v39r260458z2b200000gn/T//RtmpkRxBJc/RJafrod
```

# 7.3 ORH significance testing

```
Simply change method = "DBMH" (the default) to method = "ORH".
```

```
ret <- UtilOutputReport(dataset03, FOM = "Wilcoxon", method = "ORH", overWrite = TRUE,
#>
#> Output file name is: /var/folders/d1/mx6dcbzx3v39r260458z2b200000gn/T//RtmpkRx
```

# Chapter 8

# BACKGROUND ON THE F-DISTRIBUTION

#### 8.1 Introduction

Since it plays an important role in sample size estimation, it is helpful to examine the behavior of the F-distribution. In the following ndf = numerator degrees of freedom, ddf = denominator degrees of freedom and ncp = non-centrality parameter (i.e., the  $\Delta$  appearing in Eqn. (11.6) of (Chakraborty, 2017)).

The use of three R functions is demonstrated.

- qf(p,ndf,ddf) is the quantile function of the F-distribution for specified values of p, ndf and ddf, i.e., the value x such that fraction p of the area under the F-distribution lies to the right of x. Since ncp is not included as a parameter, the default value, i.e., zero, is used. This is called the *central* F-distribution.
- df(x,ndf,ddf,ncp) is the probability density function (pdf) of the F-distribution, as a function of x, for specified values of ndf, ddf and ncp.
- pf(x,ndf,ddf,ncp) is the probability (or cumulative) distribution function of the F-distribution for specified values of ndf, ddf and ncp.

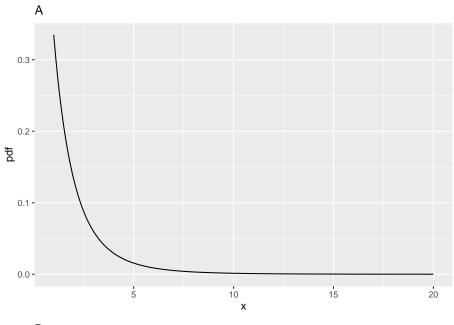
# 8.2 Effect of ncp for ndf = 2 and ddf = 10

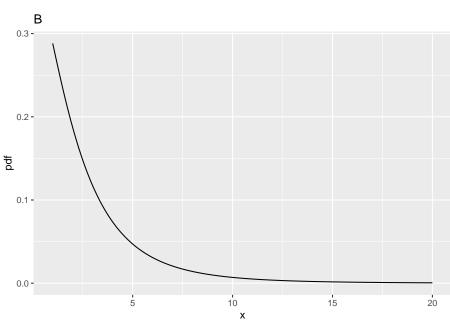
• Four values of ncp are considered (0, 2, 5, 10) for ddf = 10.

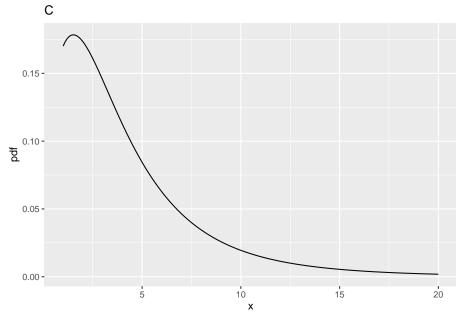
• fCrit is the critical value of the F distribution, i.e., that value such that fraction  $\alpha$  of the area is to the right of the critical value, i.e., fCrit is identical to:

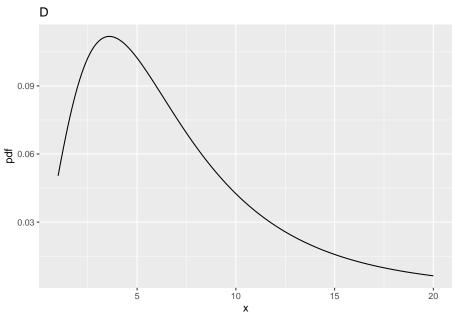
 $F_{1-\alpha,ndf,ddf}$ 

```
ndf \leftarrow 2; ddf \leftarrow 10; ncp \leftarrow c(0,2,5,10)
alpha \leftarrow 0.05
fCrit <- qf(1-alpha, ndf,ddf)</pre>
x \leftarrow seq(1, 20, 0.1)
myLabel <- c("A", "B", "C", "D")</pre>
myLabelIndx <- 1
pFgtFCrit <- NULL
for (i in 1:length(ncp))
  y <- df(x,ndf,ddf,ncp=ncp[i])
  pFgtFCrit <- c(pFgtFCrit, 1-pf(fCrit, ndf, ddf, ncp = ncp[i]))</pre>
for (i in 1:length(ncp))
  y <- df(x,ndf,ddf,ncp=ncp[i])
  curveData <- data.frame(x = x, pdf = y)</pre>
  curvePlot <- ggplot(data = curveData, mapping = aes(x = x, y = pdf)) +</pre>
    geom_line() +
    ggtitle(myLabel[myLabelIndx]);myLabelIndx <- myLabelIndx + 1</pre>
  print(curvePlot)
fCrit_2_10 <- fCrit # convention fCrit_ndf_ddf</pre>
```









	ndf	ddf	fCrit	ncp	pFgtFCrit
A	2	10	4.102821	0	0.0500000
В	2	10	4.102821	2	0.1775840
С	2	10	4.102821	5	0.3876841
$\overline{D}$	2	10	4.102821	10	0.6769776

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#### 8.3 Comments

#### 8.3.1 Fig. A

- This corresponds to ncp = 0, i.e., the central F-distribution.
- The integral under this distribution is unity (this is also true for all plots in this vignette).
- The critical value, fCrit in the above code block, is the value of x such that the probability of exceeding x is α. The corresponding parameter alpha is defined above as 0.05.
- In the current example fCrit = 4.102821. Notice the use of the quantile function qf() to determine this value, and the default value of ncp, namely zero, is used; specifically, one does not pass a 4th argument to qf().
- The decision rule for rejecting the NH uses the NH distribution of the F-statistic, i.e., reject the NH if F >= fCrit. As expected, prob > fCrit = 0.05 because this is how fCrit was defined.

#### 8.3.2 Fig. B

- This corresponds to ncp = 2, ndf = 2 and ddf = 10.
- The distribution is slightly shifted to the right as compared to Fig. A, thereby making it more likely that the observed value of the F-statistic will exceed the critical value determined for the NH distribution.
- In fact, prob > fCrit = 0.177584, i.e., the *statistical power* (compare this to Fig. A where prob > fCrit was 0.05).

#### 8.3.3 Fig. C

- This corresponds to ncp = 5, ndf = 2 and ddf = 10.
- Now prob > fCrit = 0.3876841.
- Power has increased compared to Fig. B.

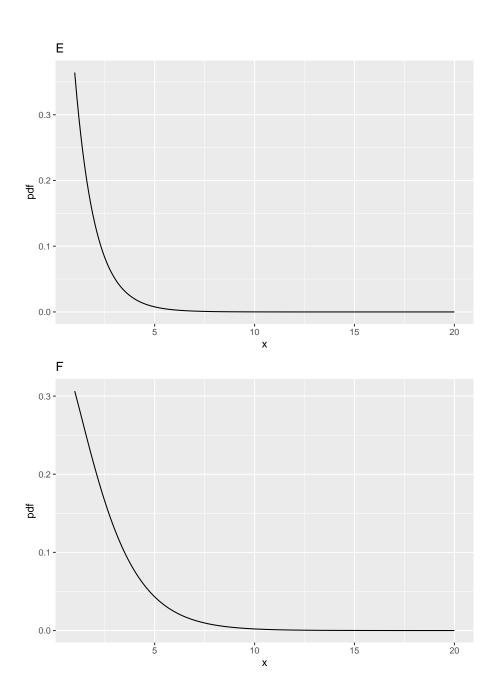
#### 8.3.4 Fig. D

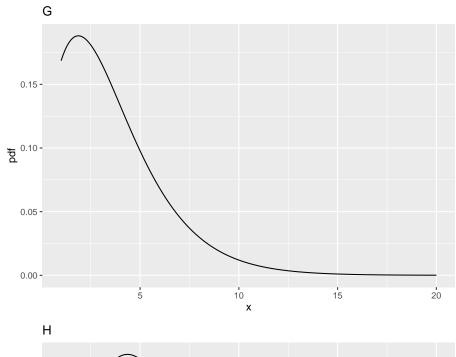
- This corresponds to ncp = 10, ndf = 2 and ddf = 10.
- Now prob > fCrit is 0.6769776.
- Power has increased compared to Fig. C.
- The effect of the shift is most obvious in Fig. C and Fig. D.
- Considering a vertical line at x = 4.102821, fraction 0.6769776 of the probability distribution in Fig. D lies to the right of this line
- Therefore the NH is likely to be rejected with probability 0.6769776.

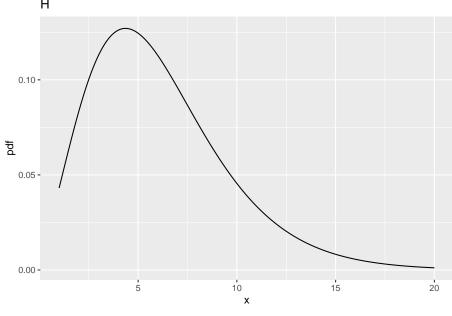
### **8.3.5** Summary

The larger that non-centrality parameter, the greater the shift to the right of the F-distribution, and the greater the statistical power.

# 8.4 Effect of ncp for ndf = 2 and ddf = 100







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	ndf	ddf	fCrit	ncp	pFgtFCrit
A	2	10	4.102821	0	0.0500000
В	2	10	4.102821	2	0.1775840
С	2	10	4.102821	5	0.3876841
D	2	10	4.102821	10	0.6769776
Е	2	100	3.087296	0	0.0500000
F	2	100	3.087296	2	0.2199264
G	2	100	3.087296	5	0.4910802
Η	2	100	3.087296	10	0.8029764

### 8.5 Comments

- All comparisons in this sections are at the same values of ncp defined above.
- And between ddf = 100 and ddf = 10.

## 8.5.1 Fig. E

- This corresponds to ncp = 0, ndf = 2 and ddf = 100.
- The critical value is fCrit\_2\_100 = 3.0872959. Notice the decrease compared to the previous value for ncp = 0, i.e., 4.102821, for ddf = 10.
- One expects that increasing ddf will make it more likely that the NH will be rejected, and this is confirmed below.
- All else equal, statistical power increases with increasing ddf.

### 8.5.2 Fig. F

- This corresponds to ncp = 2, ndf = 2 and ddf = 100.
- The probability of exceeding the critical value is prob > fCrit\_2\_100 = 0.2199264, greater than the previous value, i.e., 0.177584 for ddf = 10.

### 8.5.3 Fig. G

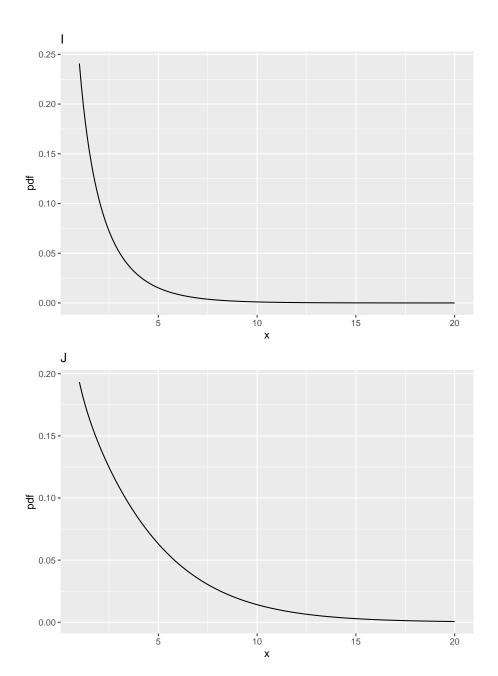
- This corresponds to ncp = 5, ndf = 2 and ddf = 100.
- The probability of exceeding the critical value is prob > fCrit\_2\_100 = 0.4910802.
- This is greater than the previous value, i.e., 0.3876841 for ddf = 10.

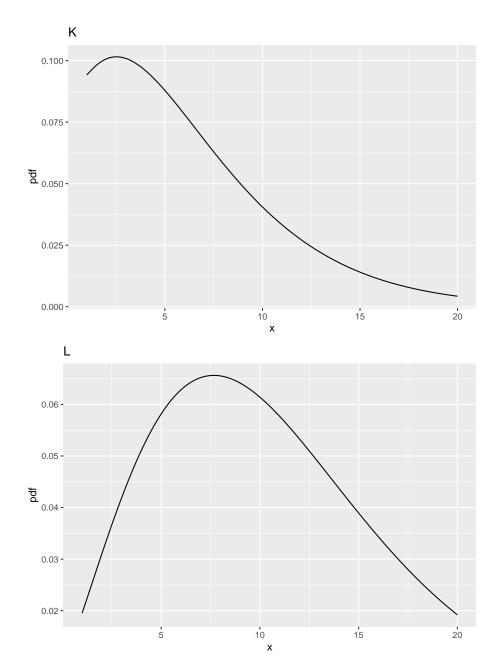
#### 8.5.4 Fig. H

• This corresponds to ncp = 10, ndf = 2 and ddf = 100.

- The probability of exceeding the critical value is prob > fCrit\_2\_100 is 0.8029764
- This is greater than the previous value, i.e., 0.6769776 for  $\mathtt{ddf} = 10$ .

# $8.6 \quad \text{Effect of ncp for ndf} = 1, \, \text{ddf} = 100$





8.7. COMMENTS 79

	ndf	ddf	fCrit	ncp	pFgtFCrit
A	2	10	4.102821	0	0.0500000
В	2	10	4.102821	2	0.1775840
С	2	10	4.102821	5	0.3876841
D	2	10	4.102821	10	0.6769776
E	2	100	3.087296	0	0.0500000
F	2	100	3.087296	2	0.2199264
G	2	100	3.087296	5	0.4910802
Η	2	100	3.087296	10	0.8029764
I	1	100	3.936143	0	0.0500000
J	1	100	3.936143	2	0.2883607
K	1	100	3.936143	5	0.6004962
L	1	100	3.936143	10	0.8793619

# 8.7 Comments

- All comparisons in this sections are at the same values of ncp defined above and at ddf = 100.
- And between ndf = 1 and ndf = 2.

### 8.7.1 Fig. I

- This corresponds to ncp = 0, ndf = 1 and ddf = 100.
- The critical value is  $fCrit_1_100 = 3.936143$ .
- Notice the increase in the critical value as compared to the corresponding value for ndf = 2, i.e., 3.0872959.
- One might expect power to decrease, but see below.

### 8.7.2 Fig. J

- This corresponds to ncp = 2, ndf = 1 and ddf = 100.
- Now prob > fCrit\_1\_100 = 0.2883607, larger than the previous value 0.2199264.
- The power has actually increased.

### 8.7.3 Fig. K

- This corresponds to ncp = 5, ndf = 1 and ddf = 100°,
- Now prob > fCrit\_1\_100 = 0.6004962, larger than the previous value 0.4910802.
- Again, the power has actually increased.

# 8.7.4 Fig. L

- This corresponds to ncp = 10, ndf = 1 and ddf = 100
- Now prob > fCrit\_1\_100 is 0.8793619, larger than the previous value 0.8029764.
- The power has actually increased.

# 8.8 Summary

- Power increases with increasing ddf and ncp.
- The effect of increasing ncp is quite dramatic. This is because power depends on the square of ncp.
- Decreasing ndf also increases power. At first glance this may seem counterintuitive, as fCrit has gone up, but is explained by the differing shapes of the two distributions: the pdf is broader for ndf = 1 as compared to ndf = 2 (compare Fig. L to H).

# 8.9 References

# Chapter 9

# ROC-DBMH sample size from first principles

### 9.1 Introduction

The starting point is a **pilot** study. The variability in this dataset (specifically the variance components, subsequently converted to mean squares), obtained by running the significance testing function StSignificanceTesting(), is used to extrapolate to the necessary numbers of readers and cases, in the **pivotal** study, to achieve the desired power. In this example, the observed effect size in the pilot study is used as the anticipated effect size for the pivotal study – this is generally not a good idea as discussed in **Chapter 11** under "Cautionary notes". Shown below, and the reader should confirm, is a first principles implementation of the relevant formulae in **Chapter 11**.

# 9.2 Sample size estimation using the DBMH method

The Van Dyke dataset in file VanDyke.lrc, in "MRMC" format, is regarded as a pilot study. The command rocData <- DfReadDataFile(fileName, format = "MRMC") reads the data and saves it to a dataset object rocData. For more on data formats click here. The next line uses the function StSignificanceTesting() to apply method = "DBMH" analysis, the default, using the FOM = "Wilcoxon" figure of merit. The next line extracts the variance components varYTR, varYTC and varYEps (the Y's denote pseudovalue based values). The next line extracts the effect size.

```
alpha <- 0.05
rocData <- dataset02 ##"VanDyke.lrc"
#fileName <- dataset03 ## "Franken1.lrc"
retDbm <- StSignificanceTesting(dataset = rocData, FOM = "Wilcoxon", method = "DBMH")
varYTR <- retDbm$varComp$varTR; varYTC <- retDbm$varComp$varTC; varYEps <- retDbm$varComp$varComp$varComp$varComp$varComp$varComp$varComp$varComp$varComp$varComp$varComp$varComp$varComp$varComp$varComp$varComp$varComp$varComp$varComp$varComp$varComp$varComp$varComp$varComp$varComp$varComp$varComp$varComp$varComp$varComp$varComp$varComp$varComp$varComp$varComp$varComp$varComp$varComp$varComp$varComp$varComp$varComp$varComp$varComp$varComp$varComp$varComp$varComp$varComp$varComp$varComp$varComp$varComp$varComp$varComp$varComp$varComp$varComp$varComp$varComp$varComp$varComp$varComp$varComp$varComp$varComp$varComp$varComp$varComp$varComp$varComp$varComp$varComp$varComp$varComp$varComp$varComp$varComp$varComp$varComp$varComp$varComp$varComp$varComp$varComp$varComp$varComp$varComp$varComp$varComp$varComp$varComp$varComp$varComp$varComp$varComp$varComp$varComp$varComp$varComp$varComp$varComp$varComp$varComp$varComp$varComp$varComp$varComp$varComp$varComp$varComp$varComp$varComp$varComp$varComp$varComp$varComp$varComp$varComp$varComp$varComp$varComp$varComp$varComp$varComp$varComp$varComp$varComp$varComp$varComp$varComp$varComp$varComp$varComp$varComp$varComp$varComp$varComp$varComp$varComp$varComp$varComp$varComp$varComp$varComp$varComp$varComp$varComp$varComp$varComp$varComp$varComp$varComp$varComp$varComp$varComp$varComp$varComp$varComp$varComp$varComp$varComp$varComp$varComp$varComp$varComp$varComp$varComp$varComp$varComp$varComp$varComp$varComp$varComp$varComp$varComp$varComp$varComp$varComp$varComp$varComp$varComp$varComp$varComp$varComp$varComp$varComp$varComp$varComp$varComp$varComp$varComp$varComp$varComp$varComp$varComp$varComp$varComp$varComp$varComp$varComp$varComp$varComp$varComp$varComp$varComp$varComp$varComp$varComp$varComp$varComp$varComp$varComp$varComp$varComp$varComp$varComp$varComp$varComp$varComp$varComp$varComp$varCo
```

The *observed* effect size is effectSize = -0.0438003, which, in this example, is used as the *anticipated* effect size, generally not a good idea. See Chapter 11 for nuances regarding the choice of this all important value. The following code snippet reveals the names and array indexing of the pseudovalue variance components.

```
retDbm$varComp
#> varR varC varTR varTC varRC varErr
#> 1 0.001534999 0.02724923 0.0002004025 0.0119753 0.01226473 0.0399716
```

For example, the treatment-reader pseudovalue variance component is the third element of retDbm\$varComp.

## 9.2.1 Random reader random case (RRRC)

This illustrates random reader random case sample size estimation. Assumed are 10 readers and 163 cases in the pivotal study. The non-centrality parameter is defined by:

$$\Delta = \frac{JK\sigma_{Y;\tau}^2}{\left(\sigma_{Y;\varepsilon}^2 + \sigma_{Y;\tau RC}^2\right) + K\sigma_{Y;\tau R}^2 + J\max\left(\sigma_{Y;\tau C}^2,0\right)}$$

The sampling distribution of the F-statistic under the AH is:

$$F_{AH|R} \equiv \frac{MST}{MSTC} \sim F_{I-1,(I-1)(K-1),\Delta}$$

Also,  $\sigma_{Y;\tau}^2 = d^2/2$ , where d is the observed effect size, i.e., effectSize. The formulae for calculating the mean-squares are in (Hillis and Berbaum, 2004), implemented in UtilMeanSquares().

```
#RRRC

J <- 10;K <- 163
ncp <- (0.5*J*K*(effectSize)^2)/(K*varYTR+max(J*varYTC,0)+varYEps)
MS <- UtilMeanSquares(rocData, FOM = "Wilcoxon", method = "DBMH")
ddf <- (MS$msTR+max(MS$msTC-MS$msTRC,0))^2/(MS$msTR^2)*(J-1)</pre>
```

```
FCrit <- qf(1 - alpha, 1, ddf)
Power1 <- 1-pf(FCrit, 1, ddf, ncp = ncp)</pre>
```

The next line calculates the non centrality parameter, ncp = 8.1269825. Note that effectSize enters as the square. The UtilMeanSquares() function returns the mean-squares as a list (ignore the last two rows of output for now).

```
str(MS)
#> List of 9
\#> $ msT
              : num 0.547
#> $ msR
              : num 0.437
#> $ msC
              : num 0.397
#> $ msTR
              : num 0.0628
#> $ msTC
              : num 0.0521
#> $ msRC
              : num 0.0645
            : num 0.04
#> $ msTRC
#> $ msCSingleT: num [1:2] 0.336 0.16
#> $ msCSingleR: num [1:5] 0.1222 0.2127 0.1365 0.0173 0.1661
```

The next line calculates ddf = 12.822129. The remaining lines calculate the critical value of the F-distribution, FCrit = 4.680382 and statistical power = 0.7494133, which by design is close to 80%, i.e., the numbers of readers and cases were chosen to achieve this value.

#### 9.2.2 Fixed reader random case (FRRC)

This code illustrates fixed reader random case sample size estimation. Assumed are 10 readers and 133 cases in the pivotal study. The formulae are:

$$\Delta = \frac{JK\sigma_{Y;\tau}^2}{\sigma_{Y;\varepsilon}^2 + \sigma_{Y;\tau RC}^2 + J\sigma_{Y;\tau C}^2}$$

The sampling distribution of the F-statistic under the AH is:

$$F_{AH|R} \equiv \frac{MST}{MSTC} \sim F_{I-1,(I-1)(K-1),\Delta}$$

```
#FRRC
ncp <- (0.5*J*K*(effectSize)^2)/(max(J*varYTC,0)+varYEps)
ddf <- (K-1)
FCrit <- qf(1 - alpha, 1, ddf)
Power2 <- 1-pf(FCrit, 1, ddf, ncp = ncp)</pre>
```

This time non centrality parameter, ncp = 7.9873835, ddf = 132, FCrit = 3.912875 and statistical power = 0.8011167. Again, be design, this is close to 80%. Note that when readers are regarded as a fixed effect, fewer cases are needed to achieve the desired power. Freezing out a source of variability results in a more stable measurement and hence fewer cases are needed to achieve the desired power.

# 9.2.3 Random reader fixed case (RRFC)

This code illustrates random reader random case sample size estimation. Assumed are 10 readers and 53 cases in the pivotal study. The formulae are:

$$\Delta = \frac{JK\sigma_{Y;\tau}^2}{\sigma_{Y:\varepsilon}^2 + \sigma_{Y:\tau RC}^2 + K\sigma_{Y;\tau R}^2}$$

The sampling distribution of the F-statistic under the AH is:

$$F_{AH|C} \equiv \frac{MST}{MSTR} \sim F_{I-1,(I-1)(J-1),\Delta}$$

```
#RRFC
ncp <- (0.5*J*K*(effectSize)^2)/(K*varYTR+varYEps)
ddf <- (J-1)
FCrit <- qf(1 - alpha, 1, ddf)
Power3 <- 1-pf(FCrit, 1, ddf, ncp = ncp)</pre>
```

This time non centrality parameter, ncp = 10.0487164, ddf = 9, FCrit = 5.117355 and statistical power = 0.8049666. Again, be design, this is close to 80%.

# 9.3 Summary

For 10 readers, the numbers of cases needed for 80% power is largest (163) for RRRC, intermediate (133) for FRRC and least for RRFC (53). For all three analyses, the expectation of 80% power is met.

### 9.4 References

# Chapter 10

# Proper ROCs

- 10.1 Helper functions
- 10.2 Definitions of PROPROC parameters in terms of binormal model parameters

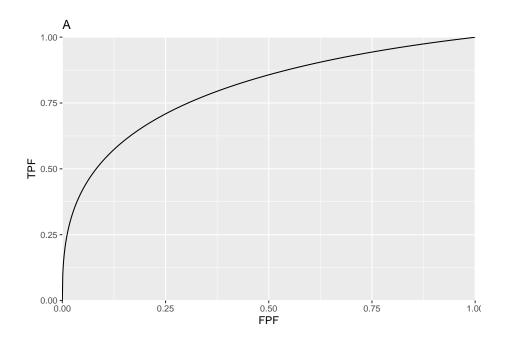
$$c = \frac{b-1}{b+1}$$

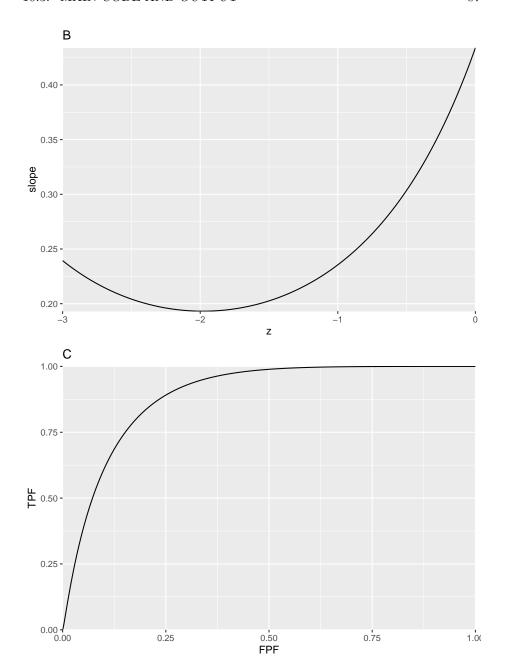
$$d_a = \frac{\sqrt{2}a}{\sqrt{1+b^2}}$$

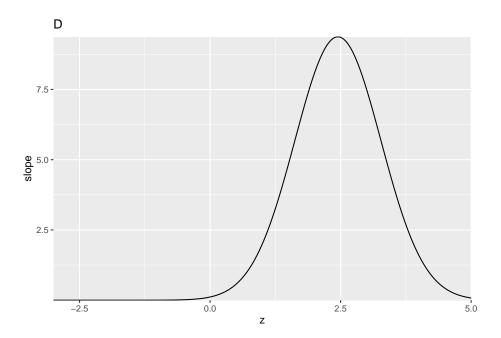
# 10.3 Main code and output

```
c1Arr <- c(-0.1322804, 0.2225588); daArr <- c(1.197239, 1.740157)
myLabel <- c("A", "B", "C", "D")
myLabelIndx <- 1
for (i in 1:2)
{
    c1 <- c1Arr[i]
    da <- daArr[i]
    ret <- Transform2ab(da, c1)
    a <- ret$a;b <- ret$b
    if (i == 1) z <- seq(-3, 0, by = 0.01) # may need to adjust limits to view detail of slope plot if (i == 2) z <- seq(-3, 5, by = 0.01) # may need to adjust limits to view detail of slope plot</pre>
```

```
FPF \leftarrow seq(0.0, 1, 0.001)
TPF <- rocY(FPF, a, b)</pre>
rocPlot <- data.frame(FPF = FPF, TPF = TPF)</pre>
plotRoc <- ggplot(rocPlot, aes(x = FPF, y = TPF)) +</pre>
  geom_line() +
 scale_x_continuous(expand = c(0, 0)) +
  scale_y_continuous(expand = c(0, 0))
  ggtitle(myLabel[myLabelIndx]);myLabelIndx <- myLabelIndx + 1</pre>
slope <-b*dnorm(a-b*z)/dnorm(-z) # same as likelihood ratio</pre>
slopePlot <- data.frame(z = z, slope = slope)</pre>
p \leftarrow ggplot(slopePlot, aes(x = z, y = slope)) +
  geom_line() +
  scale_x_continuous(expand = c(0, 0)) +
  scale_y_continuous(expand = c(0, 0)) +
  ggtitle(myLabel[myLabelIndx]);myLabelIndx <- myLabelIndx + 1</pre>
print(plotRoc);print(p)
```







# 10.4 Discussion

Plot A is for c1 = -0.1322804, da = 1.197239 while plot C is for c1 = 0.2225588, da = 1.740157. Plots B and D are the corresponding slope plots as functions of the binormal model z-sample. In plot A, the slope is infinite near the origin and the curve approaches the upper-right corner with finite slope. The situation is reversed in plot C where the slope is finite near the origin and the curve approaches the upper-right corner with zero slope.

These two readers are from a clinical dataset, dataset01. Highest rating inferred ROC data from original FROC data, were analyzed by PROPROC and the resulting parameter values are coded here. They were chosen as they demonstrate key differences in the shapes of proper ROC plots. Plot A corresponds to a negative value of c1, which implies b < 1. The slope of the proper ROC is infinite near the origin and approaches a positive constant near the upper right corner of the ROC. Plot C is for a positive value of c1, i.e., for b > 1. Now the slope of the proper ROC is finite near the origin and approaches zero near the upper right corner.

Considering plot D, as one "cuts" the slope axis horizontally with a sliding threshold, starting with very high values and moving downwards, the slope of the ROC curve starts at the origin with a large but finite value. This corresponds to the peak in plot D. Above the peak, there are no solutions for z. The slope decreases monotonically to zero, corresponding to the flattening out of the slope

### at zero for $z \sim -2$ .

The two values of **z** corresponding to each cut implies, of course, that the binormal model based proper algorithm has to do a lot of bookkeeping, since each horizontal cut splits the decision axis into 3 regions. One can think of shrinking each of plots B & D horizontally to zero width, and all that remains is the slope axis with a thick vertical line superimposed on it, corresponding to the horizontally collapsed curves. In plot B the vertical line extends from positive infinity down to about 0.1, and represents the range of decision variable samples encountered by the observer on the likelihood ratio scale. In plot D the vertical line extends from a finite value (~9.4) to zero. For the stated binormal model parameters values outside of these ranges are not possible.

# Chapter 11

# Metz Eqn36 numerical check

# 11.1 Helper functions

# 11.2 Main code and output

```
npts <- 10000
for (i in 1:2) {
  for (j in 1:5) {
    C \leftarrow c1[i,j]
    da <- d_a1[i,j]</pre>
    ret <- GetLimits(da,C)</pre>
    LL <- ret$LL;UL <- ret$UL
    vc <- seq (LL, UL, length.out = npts)
    TPF <- TruePositiveFraction (vc, da, C)
    FPF <- FalsePositiveFraction (vc, da, C)
    FPF <- rev(FPF); TPF <- rev(TPF)</pre>
    df2 <- data.frame(FPF = FPF, TPF = TPF)</pre>
    # do integral numerically
    numAuc <- trapz(FPF, TPF)</pre>
    # Implement Eqn. 36 from Metz-Pan paper
    rho <- -(1-C^2)/(1+C^2); sigma <- rbind(c(1, rho), c(rho, 1))
    lower \leftarrow \text{rep}(-\text{Inf}, 2); \text{upper} \leftarrow c(-\text{da/sqrt}(2), 0)
    aucProproc <- pnorm(da/sqrt(2)) + 2 * pmvnorm(lower, upper, sigma = sigma)</pre>
    aucProproc <- as.numeric(aucProproc)</pre>
    cat("i = ", i,"j = ", j,"C = ", C, ", da = ", da, "aucProproc = ", aucProproc, "Norm. Diff. =
```

```
}  
#> i = 1 j = 1 C = -0.1322804 , da = 1.197239 aucProproc = 0.8014164 Norm. Diff. = #> i = 1 j = 2 C = -0.08696513 , da = 1.771176 aucProproc = 0.8947898 Norm. Diff. #> i = 1 j = 3 C = -0.1444419 , da = 1.481935 aucProproc = 0.8526605 Norm. Diff. = #> i = 1 j = 4 C = 0.08046016 , da = 1.513757 aucProproc = 0.8577776 Norm. Diff. = #> i = 1 j = 5 C = 0.2225588 , da = 1.740157 aucProproc = 0.8909392 Norm. Diff. = #> i = 2 j = 1 C = -0.08174248 , da = 0.6281251 aucProproc = 0.6716574 Norm. Diff. #> i = 2 j = 2 C = 0.04976448 , da = 0.9738786 aucProproc = 0.7544739 Norm. Diff. #> i = 2 j = 3 C = -0.1326126 , da = 1.155871 aucProproc = 0.7931787 Norm. Diff. = #> i = 2 j = 4 C = 0.1182226 , da = 1.620176 aucProproc = 0.8740274 Norm. Diff. = #> i = 2 j = 5 C = 0.0781033 , da = 0.8928816 aucProproc = 0.7360989 Norm. Diff. =
```

# 11.3 Discussion

Note the close correspondence between the formula, Eqn. 36 in the Metz-Pan paper and the numerical estimate. As a historical note, Eqn. 31 and Eqn. 36 (they differ only in parameterizations) in the referenced publication are provided without proof – it was probably obvious to Prof Metz or he wanted to leave it to us "mere mortals" to figure it out, as a final parting gesture of his legacy. The author once put a significant effort into proving it and even had a bright graduate student from the biostatistics department work on it to no avail. The author has observed that these equations always yield very close to the numerical estimates, to within numerical precisions, so the theorem is correct empirically, but he has been unable to prove it analytically. It is left as an exercise for a gifted reader to prove/disprove these equations.

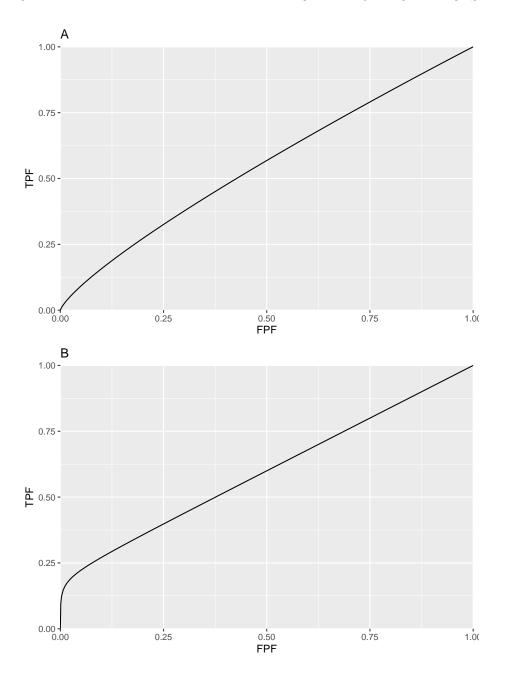
# Chapter 12

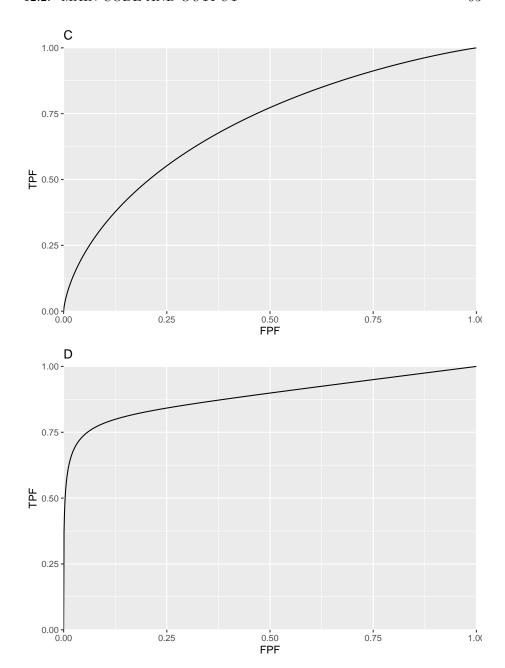
# **CBM Plots**

# 12.1 Helper functions

# 12.2 Main code and output

```
#> Fig. A : mu = 1 , alpha = 0.2
#> Fig. B : mu = 3 , alpha = 0.2
#> Fig. C : mu = 1 , alpha = 0.8
#> Fig. D : mu = 3 , alpha = 0.8
```



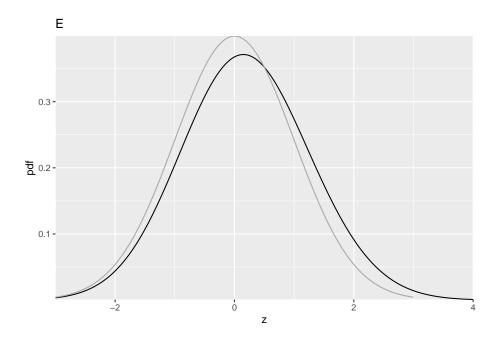


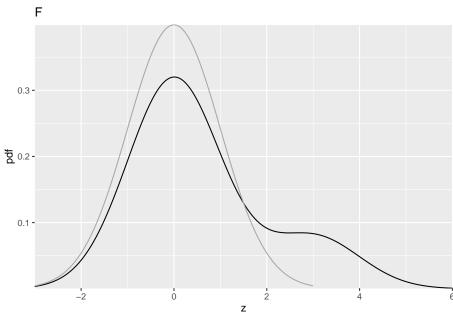
# 12.3 Comments

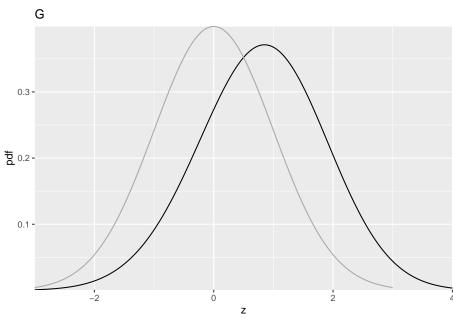
Plots A - D show ROC curves predicted by the CBM model; the corresponding values of the mu and alpha parameters are indicated above the plots. For small mu and/or alpha the curve approaches the chance diagonal, consistent with the notion that if the lesion is not visible, performance can be no better than chance level.

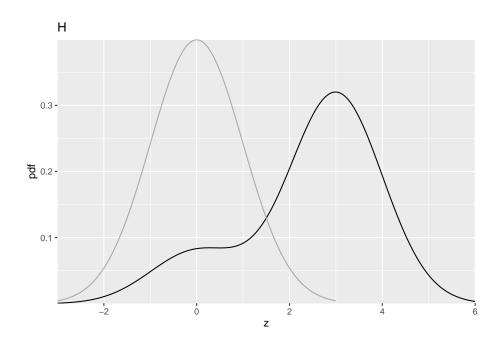
# 12.4 pdf plots

```
#> Fig. E : mu = 1 , alpha = 0.2
#> Fig. F : mu = 3 , alpha = 0.2
#> Fig. G : mu = 1 , alpha = 0.8
#> Fig. H : mu = 3 , alpha = 0.8
```







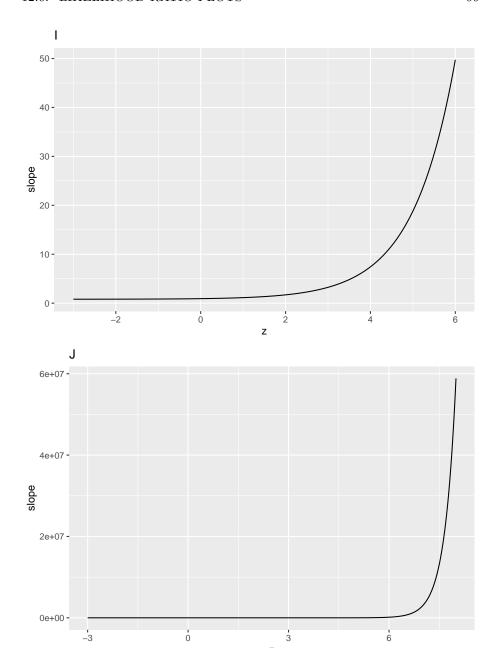


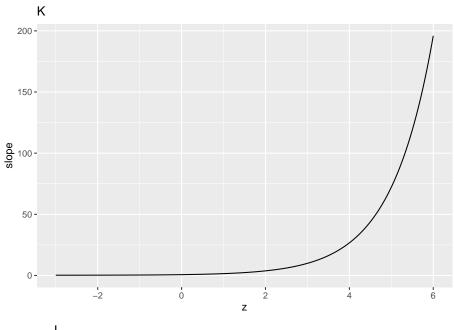
# 12.5 Comments

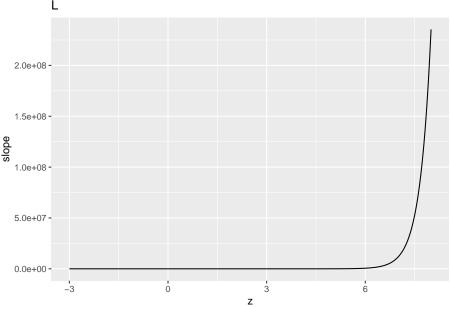
The dark line is the diseased distribution. The grey line is the non-diseased distribution. The bimodal diseased distribution is clearly evident in plots F and H.

# 12.6 likelihood ratio plots

```
#> Fig. I : mu = 1 , alpha = 0.2
#> Fig. J : mu = 3 , alpha = 0.2
#> Fig. K : mu = 1 , alpha = 0.8
#> Fig. L : mu = 3 , alpha = 0.8
```







# 12.7 Comments

Close examination of the region near the flat part shows it does not plateau at zero; rather the minimum is at 1 - alpha, explaining the non-zero limiting slope of the predicted curve near (1, 1).

# Chapter 13

# ROI paradigm data

# 13.1 Introduction; this vignette is under construction!

- In the region-of-interest (ROI) paradigm (Obuchowski, 1997, Obuchowski et al. (2000)) each case is regarded as consisting of  $Q_k$  ( $Q_k \geq 1$ ) "quadrants" or "regions-of-interest" or ROIs, where k is the case index (k = 1, 2, ..., K) and K is the total number of cases (i.e., case-level non-diseased plus case-level diseased cases). Each ROI needs to be classified, by the investigator, as either ROI-level-non-diseased (i.e., it has no lesions) or ROI-level-diseased (i.e., it has at least one lesion). Note the distinction between case-level and ROI-level truth states. One can have ROI-level non-diseased regions in a case-level diseased case. A case-level diseased case must contain at least one ROI-level diseased region and a case-level non-diseased case cannot have any ROI-level diseased regions.
- The observer gives a single rating (in fact an ordered label) to each ROI, denoted  $R_{kr}$  ( $r=1, 2, ..., Q_k$ ). Here r is the ROI index and k is the case index. The rating can be an integer or quasi- continuous (e.g., 0 100), or a floating point value, as long as higher numbers represent greater confidence in presence of one or more lesions in the ROI.
- The ROI paradigm is not restricted to 4 or even a constant number of ROIs per case. That is the reason for the k subscript in  $Q_k$ .
- The ROI data structure is a special case of the FROC data structure, the essential difference being that the number of ratings per case is an a-priori known value, equal to  $Q_k$ .
- ROI-level non-diseased region ratings are stored in the NL field and ROI-level diseased region ratings are stored in the LL field.
- One can think of the ROI paradigm as similar to the FROC paradigm, but

with localization accuracy restricted to belonging to a region (one cannot distinguish multiple lesions within a region). Unlike the FROC paradigm, a rating *is required* for every ROI.

# 13.2 An example ROI dataset

An example simulated ROI dataset is included as datasetROI.

```
str(datasetROI)
#> List of 8
#> $ NL
                  : num [1:2, 1:5, 1:90, 1:4] 0.95 0.927 0.556 0.805 1.421 ...
                : num [1:2, 1:5, 1:40, 1:4] 1.57 2.31 2.3 2.34 2.34 ...
#> $ LL
#> $ lesionVector: int [1:40] 2 3 2 2 3 3 1 2 3 3 ...
               : num [1:40, 1:4] 2 1 1 1 1 2 4 1 1 1 ...
#> $ lesionWeight: num [1:40, 1:4] 0.5 0.333 0.5 0.5 0.333 ...
   \$ dataType
                : chr "ROI"
   $ modalityID : Named chr [1:2] "1" "2"
    ..- attr(*, "names")= chr [1:2] "1" "2"
    $ readerID : Named chr [1:5] "1" "2" "3" "4" ...
    ..- attr(*, "names")= chr [1:5] "1" "2" "3" "4" ...
datasetROI$NL[1,1,1,]
#> [1] 0.9498680 -0.0582497 -0.7763780 0.0120730
mean(datasetROI$NL[,,1:50,])
#> [1] 0.1014348
datasetROI$NL[1,1,51,]
#> [1] 1.01867 0.34710
                          -Inf
                                  -Inf
datasetROI$lesionVector[1]
#> [1] 2
datasetROI$LL[1,1,1,]
#> [1] 1.56928 2.05945
                          -Inf
x <- datasetROI$LL;mean(x[is.finite(x)])</pre>
#> [1] 1.815513
```

Examination of the output reveals that:

- This is a 2-treatment 5-reader dataset, with 50 non-diseased cases and 40 diseased cases, and  $Q_k=4$  for all k.
- For treatment 1, reader 1, case 1 (the 1st non-diseased case) the 4 ratings are 0.949868, -0.0582497, -0.776378, 0.012073. The mean of all ratings on non-diseased cases is 0.1014348.
- For treatment 1, reader 1, case 51 (the 1st diseased case) the NL ratings are 1.01867, 0.3471. There are only two finite values because this case

has two ROI-level-diseased regions, and 2 plus 2 makes for the assumed 4-regions per case. The corresponding \$lesionVector field is 2.

• The ratings of the 2 ROI-level-diseased ROIs on this case are 1.56928, 2.05945. The mean rating over all ROI-level-diseased ROIs is 1.8155127.

### 13.3 The ROI Excel data file

- An Excel file in JAFROC format containing simulated ROI data corresponding to datasetROI, is included with the distribution. The first command (below) finds the location of the file and the second command reads it and saves it to a dataset object ds. !!!DPC!!!
- The DfReadDataFile function automatically recognizes that this is an ROI dataset. Its structure is similar to the JAFROC format Excel file, with some important differences, noted below. It contains three worksheets:

```
## fileName <- system.file(
## "extdata", "RoiData.xlsx", package = "RJafroc", mustWork = TRUE)
## ds <- DfReadDataFile(fileName)
## ds$dataType</pre>
```

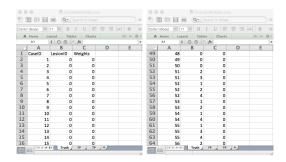


Figure 13.1: Fig. 1 two views of Truth worksheet

- The Truth worksheet, Fig. 1, indicates which cases are diseased and which are non-diseased and the number of ROI-level-diseased region on each case.
  - There are 50 non-diseased cases (labeled 1-50) under column CaseID and 40 diseased cases (labeled 51-90).
  - The LesionID field for each non-diseased case (e.g., CaseID = 1) is zero and there is one row per case. For diseased cases, this field has a variable number of entries, ranging from 1 to 4. As an example,

there are two rows for  ${\tt CaseID}=51$  in the Excel file: one with  ${\tt LesionID}=2$  and one with  ${\tt LesionID}=3$ .

- The Weights field is always zero (this field is not used in ROI analysis).

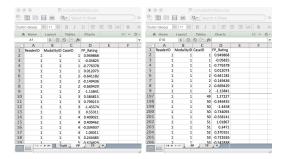


Figure 13.2: Fig. 2 two views of FP worksheet

- The FP (or NL) worksheet this lists the ratings of ROI-level-non-diseased regions.
  - For ReaderID = 1, ModalityID = 1 and CaseID = 1 there are 4 rows, corresponding to the 4 ROI-level-non-diseased regions in this case. The corresponding ratings are 0.949868, -0.0582497, -0.776378, 0.012073. The pattern repeats for other treatments and readers, but the rating are, of course, different.
  - Each CaseID is represented in the FP worksheet (a rare exception could occur if a case-level diseased case has 4 diseased regions).



Figure 13.3: Fig. 2 TP worksheet

• The TP (or LL) worksheet - this lists the ratings of ROI-level-diseased regions.

- Because non-diseased cases generate TPs, one does not find any entry with CaseID = 1-50 in the TP worksheet.
- The lowest CaseID in the TP worksheet is 51, which corresponds to the first diseased case.
- There are two entries for this case, corresponding to the two ROI-level-diseased regions present in this case. Recall that corresponding to this CaseID in the Truth worksheet there were two entries with LesionID = 2 and 3. These must match the LesionID's listed for this case in the TP worksheet. Complementing these two entries, in the FP worksheet for CaseID = 51, there are 2 entries corresponding to the two ROI-level-non-diseased regions in this case.
- One should confirm that for each diseased case the sum of the number of entries in the TP and FP worksheets is always 4.

# 13.4 Next, TBA

The next vignette illustrates significance testing for this paradigm.

# 13.5 References

# Chapter 14

# Analyzing data acquired according to the ROI paradigm

# 14.1 Introduction; this vignette is under construction!

# 14.2 Note to self (10/29/19) !!!DPC!!!

The FOM and DeLong method implementations need checking with a toy dataset.

### 14.3 Introduction

- For an ROI dataset StSignificanceTesting() automatically defaults to method = "ORH", covEstMethod = "DeLong" and FOM = "ROI".
- The covariance estimation method is based on the original DeLong method (DeLong et al., 1988), which is valid only for the trapezoidal AUC, i.e. ROC data, as extended by (Obuchowski, 1997) to ROI data, see formula below.
- The essential differences from conventional ROC analyses are in the definition of the ROI figure of merit, see below, and the procedure developed by (Obuchowski, 1997) for estimating the covariance matrix. Once the

covariances are known, method = "ORH" can be applied to perform significance testing, as described in (Obuchowski and Rockette, 1995) and (Chakraborty, 2017, Chapter 10).

# 14.4 The ROI figure of merit

Let  $X_{kr}$  denote the rating for the r<sup>th</sup> lesion-containing ROI in the k<sup>th</sup> case and let  $n_k^L$  be the total number of lesion-containing ROIs in the k<sup>th</sup> case. Similarly, let  $Y_{kr}$  denote the rating for the r<sup>th</sup> lesion-free ROI in the k<sup>th</sup> case and  $n_k^N$  denote the total number of lesion-free ROIs in the k<sup>th</sup> case. Let  $N_L$  denote the total number of lesion-containing ROIs in the image set and  $N_N$  denote the total number of lesion-free ROIs. These are given by:

$$N_L = \sum\nolimits_k {n_k^L}$$

and

$$N_N = \sum\nolimits_k n_k^N$$

The ROI figure of merit  $\theta$  is defined by:

$$\theta = \frac{1}{N_L N_N} \sum\nolimits_k \sum\nolimits_{k'} \sum\limits_{r=1}^{n_k^L} \sum\limits_{r'=1}^{n_{k'}^N} \psi(X_{kr}, Y_{k'r'})$$

The kernel function  $\Psi(X,Y)$  is defined by:

$$\psi(X, Y) = \begin{bmatrix} 1 & \text{if} & X < Y \\ 0.5 & \text{if} & X = Y \\ 0 & \text{if} & X > Y \end{bmatrix}$$

The ROIs are *effectively regarded as mini-cases* and one calculates the FOM as the Wilcoxon statistic considering the mini-cases as actual cases. The correlations between the ratings of ROIs on the same case are accounted for in the analysis.

# 14.5 Calculation of the ROI figure of merit.

```
UtilFigureOfMerit(datasetROI, FOM = "ROI")
#> Rdr1 Rdr2 Rdr3 Rdr4 Rdr5
#> Trt1 0.9057239 0.8842834 0.8579279 0.9350207 0.8352103
#> Trt2 0.9297186 0.9546035 0.8937652 0.9531716 0.8770076
fom <- UtilFigureOfMerit(datasetROI, FOM = "ROI")</pre>
```

- If the correct FOM is not supplied, it defaults to FOM = ROI.
- This is a 2-treatment 5-reader dataset.
- For treatment 1, reader 1 the figure of merit is 0.9057239.
- For treatment 2, reader 5 the figure of merit is 0.8770076.
- Etc.

# 14.6 Significance testing

When dataset\$dataType == "ROI" the FOM defaults to "ROI" (meaning the above formula) and the covariance estimation method defaults to covEstMethod = "DeLong".

```
ret <- StSignificanceTesting(datasetROI, FOM = "Wilcoxon")</pre>
#> ROI dataset: forcing method = `ORH`, covEstMethod = `DeLong` and FOM = `ROI`.
str(ret)
#> List of 14
#> $ fomArray
                        : num [1:2, 1:5] 0.906 0.93 0.884 0.955 0.858 ...
    ..- attr(*, "dimnames")=List of 2
   ....$ : chr [1:2] "Trt1" "Trt2"
#> ....$ : chr [1:5] "Rdr1" "Rdr2" "Rdr3" "Rdr4" ...
#> $ meanSquares
                        :'data.frame': 1 obs. of 3 variables:
#>
    ..$ msT : num 0.00361
   ..$ msR : num 0.00256
   ..$ msTR: num 0.000207
#> $ varComp
                        :'data.frame': 1 obs. of 6 variables:
   ..$ varR : num 0.00108
   ..$ varTR: num 0.000153
#>
    ..$ cov1 : num 0.000247
    ..$ cov2 : num 0.000187
    ..$ cov3 : num 0.000154
    ..$ var : num 0.000333
#> $ FTestStatsRRRC :'data.frame': 1 obs. of 4 variables:
    ..$ fRRRC : num 9.76
   ..$ ndfRRRC: num 1
#>
   ..$ ddfRRRC: num 12.8
    ..$ pRRRC : num 0.00817
#> $ ciDiffTrtRRRC
                         :'data.frame': 1 obs. of 8 variables:
   ..$ Treatment: chr "Trt1-Trt2"
#> ..$ Estimate : num -0.038
#> ..$ StdErr : num 0.0122
```

```
#> ..$ DF : num 12.8
               : num -3.12
#>
    \dots \$ t
    ..$ PrGTt : num 0.00817
   ..$ CILower : num -0.0643
#> ..$ CIUpper : num -0.0117
#> $ ciAvqRdrEachTrtRRRC :'data.frame': 2 obs. of 6 variables:
   ..$ Treatment: Factor w/ 2 levels "Trt1", "Trt2": 1 2
   ..$ Area : num [1:2] 0.884 0.922
   ..$ StdErr : num [1:2] 0.0232 0.0197
    ..$ DF : num [1:2] 12.2 10.1
#>
    ..$ CILower : num [1:2] 0.833 0.878
#> ..$ CIUpper : num [1:2] 0.934 0.966
#> $ FTestStatsFRRC :'data.frame': 1 obs. of 4 variables:
#> ..$ fFRRC : num 16.6
   ..$ ndfFRRC: num 1
#>
#> ..$ ddfFRRC: num Inf
    ..$ pFRRC : num 4.58e-05
#> $ ciDiffTrtFRRC :'data.frame': 1 obs. of 8 variables:
   ..$ Treatment: chr "Trt1-Trt2"
#> ..$ Estimate : num -0.038
#> ..$ StdErr : num 0.00933
    ..$ DF : num Inf
#> ..$ t
               : num -4.08
#> ..$ PrGTt : num 4.58e-05
    ..$ CILower : num -0.0563
#>
    ..$ CIUpper : num -0.0197
#> $ ciAvgRdrEachTrtFRRC : 'data.frame': 2 obs. of 6 variables:
#> ..$ Treatment: Factor w/ 2 levels "Trt1", "Trt2": 1 2
    ..$ Area : num [1:2] 0.884 0.922
#>
   ..$ StdErr : num [1:2] 0.0163 0.0129
#> ..$ DF : num [1:2] Inf Inf
    ..$ CILower : num [1:2] 0.852 0.896
#>
    ..$ CIUpper : num [1:2] 0.916 0.947
#> $ ciDiffTrtEachRdrFRRC:'data.frame': 5 obs. of 9 variables:
   ..$ Reader : Factor w/ 5 levels "Rdr1", "Rdr2", ..: 1 2 3 4 5
#> ..$ Treatment: Factor w/ 1 level "Trt1-Trt2": 1 1 1 1 1
    ..$ Estimate : num [1:5] -0.024 -0.0703 -0.0358 -0.0182 -0.0418
    ..$ StdErr : num [1:5] 0.01025 0.01448 0.01648 0.00928 0.01398
   ..$ DF : num [1:5] Inf Inf Inf Inf Inf ..$ t : num [1:5] -2.34 -4.86 -2.17 -
                : num [1:5] -2.34 -4.86 -2.17 -1.96 -2.99
#>
     ..\$ \ \textit{PrGTt} \qquad : \ \textit{num} \ [1:5] \ 1.93e-02 \ 1.20e-06 \ 2.97e-02 \ 5.05e-02 \ 2.79e-03 
   ..$ CILower : num [1:5] -0.0441 -0.0987 -0.0681 -0.0363 -0.0692
#> ..$ CIUpper : num [1:5] -3.90e-03 -4.19e-02 -3.53e-03 3.88e-05 -1.44e-02
#> $ varCovEachRdr : 'data.frame': 5 obs. of 3 variables:
#> ..$ Reader: Factor w/ 5 levels "Rdr1", "Rdr2", ...: 1 2 3 4 5
```

```
#> ..$ Var : num [1:5] 0.000269 0.000227 0.000481 0.000168 0.000522
    ..$ Cov1 : num [1:5] 0.000216 0.000122 0.000345 0.000125 0.000424
#> $ FTestStatsRRFC
                     :'data.frame': 1 obs. of 4 variables:
   ..$ fRRFC : num 17.5
#> ..$ ndfRRFC: num 1
#>
    ..$ ddfRRFC: num 4
#>
    ..$ pRRFC : num 0.0139
#> $ ciDiffTrtRRFC
                     :'data.frame': 1 obs. of 8 variables:
   ..$ Treatment: chr "Trt1-Trt2"
#>
    ..$ Estimate : num -0.038
#>
   ..$ StdErr : num 0.00909
   ..$ DF
              : num 4
#>
   ..$ t
               : num -4.18
    ..$ PrGTt : num 0.0139
#>
    ..$ CILower : num -0.0633
#>
   ..$ CIUpper : num -0.0128
#> $ ciAvgRdrEachTrtRRFC :'data.frame': 2 obs. of 6 variables:
    ..$ Treatment: Factor w/ 2 levels "Trt1", "Trt2": 1 2
   ..$ Area : num [1:2] 0.884 0.922
#> ..$ StdErr : num [1:2] 0.0175 0.0157
#> ..$ DF
               : num [1:2] 4 4
#>
    ..$ CILower : num [1:2] 0.835 0.878
#> ..$ CIUpper : num [1:2] 0.932 0.965
```

- While ret is a list with many (22) members, their meanings should be clear from the notation. As an example:
- The variance components are given by:

```
ret$varComp

#> varR varTR cov1 cov2 cov3 var

#> 1 0.001082359 0.0001526084 0.0002465125 0.0001870571 0.0001543764 0.0003333119
```

### 14.6.1 RRRC analysis

```
ret$FTestStatsRRRC$fRRRC
#> [1] 9.763602
ret$FTestStatsRRRC$ndfRRRC
#> [1] 1
ret$FTestStatsRRRC$ddfRRRC
#> [1] 12.82259
ret$FTestStatsRRRC$pRRRC
#> [1] 0.008173042
```

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- The F-statistic is, with ndf = 1 and ddf =, which yields a p-value of.
- The confidence interval for the reader averaged difference between the two treatments is given by:

```
ret$ciDiffTrtRRRC

#> Treatment Estimate StdErr DF t PrGTt CILower

#> 1 Trt1-Trt2 -0.03802005 0.01216768 12.82259 -3.124676 0.008173042 -0.06434373

#> CIUpper

#> 1 -0.01169636
```

• The FOM difference (treatment 1 minus 2) is -0.03802, which is significant, p-value = 0.008173, F-statistic = 9.7636016, ddf = 12.8225898. The confidence interval is (-0.0643437, -0.0116964).

### 14.6.2 FRRC analysis

```
ret$FTestStatsFRRC$fFRRC
#> [1] 16.6135
ret$FTestStatsFRRC$ndfFRRC
#> [1] 1
ret$FTestStatsFRRC$ddfFRRC
#> [1] Inf
ret$FTestStatsFRRC$pFRRC
#> [1] 4.582365e-05
```

- The F-statistic is 16.6135014, with ndf = 1 and ddf = Inf, which yields a p-value of  $4.5823651 \times 10^{-5}$ .
- The confidence interval for the reader averaged difference between the two treatments is given by:

```
ret$ciDiffTrtFRRC

#> Treatment Estimate StdErr DF t PrGTt CILower

#> 1 Trt1-Trt2 -0.03802005 0.009327861 Inf -4.075966 4.582365e-05 -0.05630232

#> CIUpper
#> 1 -0.01973778
```

#### 14.6.3 RRFC analysis

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```
ret$FTestStatsRRFC$fRRFC
#> [1] 17.48107
ret$FTestStatsRRFC$ndfRRFC
#> [1] 1
ret$FTestStatsRRFC$ddfRRFC
#> [1] 4
ret$FTestStatsRRFC$pRRFC
#> [1] 0.01390667
```

- The F-statistic is 17.4810666, with ndf = 1 and ddf = 4, which yields a p-value of 0.0139067.
- The confidence interval for the reader averaged difference between the two treatments is given by:

```
ret$ciDiffTrtRRFC

#> Treatment Estimate StdErr DF t PrGTt CILower

#> 1 Trt1-Trt2 -0.03802005 0.00909345 4 -4.181037 0.01390667 -0.06326751

#> CIUpper

#> 1 -0.01277258
```

# 14.7 Summary

TBA

# 14.8 References

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