Question 3 :

If we express as the convolution F then :

from the linearity of the convolution :

And Given that

We get that :

meaning the smoothed signal is bandlimited as well