Question 3:

If we express as the convolution F then :

From the linearity of the convolution:

And Given that

We get that :

meaning the smoothed signal is bandlimited as well