Chapter 2.4: Interpreting Derivatives Calculus I

College of the Atlantic. Fall 2014

- 1. Let V(t) be the volume, in gallons, of the water in the bathtub as a function of time in seconds.
 - (a) What are the units of V'(t)?
 - (b) What does V'(t) indicate in practical terms?
 - (c) What does it mean if V'(t) is negative?
 - (d) Sketch a possible V(t) that corresponds to someone filling up the tub, taking a bath, and then draining the tub.
 - (e) Sketch a possible V'(t) that corresponds to someone filling up the tub, taking a bath, and then draining the tub.
- 2. Let s(t) be the height of a sunflower plant, in centimeters, as a function of time. Let t be measured in days since the seed germinates.
 - (a) What is the meaning of s(20)?
 - (b) What is the meaning of $s^{-1}(30)$?
 - (c) What is the meaning of s(12) = 7.8?
 - (d) What are the units of s'(t)?
 - (e) What is the meaning of s'(12) = 1.5?
 - (f) Based on the above, estimate the value of s(14). Why is your answer only an estimate?
 - (g) Using your knowledge of sunflowers, sketch a possible graph for s(t).
 - (h) Sketch a possible graph for s'(t).
- 3. Let f(r) give the area in cm² of a pizza as a function of its radius r in cm.
 - (a) Algebraically determine the derivative of f(r) as a function of r.
 - (b) What is the meaning of f(5)?
 - (c) What is the meaning of $f^{-1}(200)$?
 - (d) What is the meaning of f'(6)?
 - (e) Why is f'(6) > f'(5)?
- 4. Let g(v) be the fuel efficiency in mpg of a car traveling at v miles per hour. What is the practical meaning of the statement:

$$q'(55) = -0.54$$
?