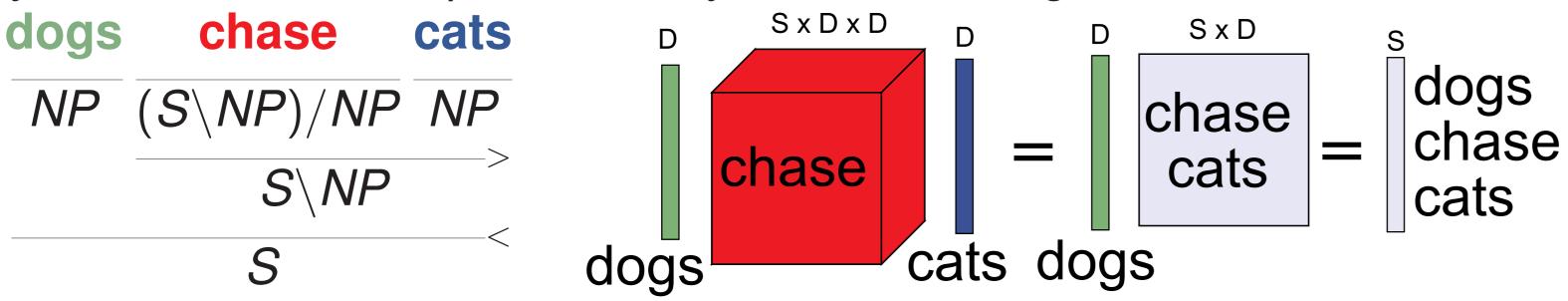
Low-Rank Tensors for Verbs in Compositional Distributional Semantics

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Tensor Models for Verbs

Syntax-driven composition (Coecke et al., 2011)

- ► Vectors for atomic CCG types (noun, noun phrase, sentence)
- ► Syntactic functions represented by matrices or higher-order tensors



► Third-order tensor \mathcal{V} for each transitive verb. Maps subject $\mathbf{s} \in \mathbb{R}^D$ and object $\mathbf{o} \in \mathbb{R}^D$ to a composed vector $(\mathcal{V}\mathbf{o})\mathbf{s} \in \mathbb{R}^S$:

$$[(\mathcal{V} \mathbf{o})\mathbf{s}]_i = \sum_{ik} \mathcal{V}_{ijk} \mathbf{o}_j \mathbf{s}_k$$

▶ Full tensors require prohibitively many parameters: $S \times D \times D$ for each verb

Low-rank approximations to tensors

- ► CP decomposition represents a tensor as a sum of vector outer products
- ▶ The number of terms in the sum, *R*, is the tensor's *rank*:

$$\mathbf{v} = \sum_{r=1}^{R} \mathbf{x}_r \otimes \mathbf{y}_r \otimes \mathbf{z}_r \qquad \mathbf{v} = \begin{bmatrix} \mathbf{z}_1 & \mathbf{y}_1 & \mathbf{z}_R & \mathbf{y}_R \\ \mathbf{y}_1 & \mathbf{y}_1 & \mathbf{y}_1 & \mathbf{y}_1 \\ \mathbf{y}_1 & \mathbf{y}_1 & \mathbf{y}_1 \\ \mathbf{x}_1 & \mathbf{x}_1 & \mathbf{x}_2 \end{bmatrix}$$

► The tensor's action on vectors is a sum, weighted using dot products:

$$(\mathbf{vo})\mathbf{s} = \sum_{r=1}^{R} (\mathbf{x}_r \cdot \mathbf{o})(\mathbf{y}_r \cdot \mathbf{s})\mathbf{z}_r$$

$$\mathbf{s} = \mathbf{v}_{\mathbf{s}} + \dots + \mathbf{v}_{\mathbf{s$$

▶ By limiting R, we force a low-rank approximation to \mathcal{V} (Lei et al. 2014, 2015)

Learning full and low-rank tensors

- \blacktriangleright Create distributional vectors for nouns s and o and SVO triples, $t_{sV\!o}$
- Learn \mathcal{V} by multi-linear regression: minimize squared residual between predicted SVO vector (\mathcal{V} o)s and actual SVO vector \mathbf{t}_{sVo}

$$L(\mathcal{V}) = \frac{1}{M_V} \sum_{i=1}^{M_V} ||(\mathcal{V} \mathbf{o}^{(i)}) \mathbf{s}^{(i)} - \mathbf{t}_{sVo}^{(i)}||_2^2$$

▶ Mini-batched ADADELTA optimization. Optimize \mathcal{V} directly for full tensors, or alternating optimization of \mathbf{x} , \mathbf{y} , and \mathbf{z} for low-rank tensors.

Distributional Vectors

- Corpus: October 2013 Wikipedia download
- SVO triples determined using verb dependencies
- ► Distributional context: most frequent lemmatized words within sentence boundaries

Count vectors

- ► Count co-occurrences between nouns (or SVO triples) and context words
- ▶ Re-weight and filter rare contexts, reduce to 100 dimensions with SVD

Prediction vectors

- ► Use skip-gram model (Mikolov et al.) to predict context words from nouns and SVO triples
- ► Hierarchical sampling, 100-dimensional vectors

Evaluation Tasks

- ► Compose the learned V, s, o into vectors for new SVO triples
- ► Compare to human rankings of SVO triple similarity (Spearman correlation)

Verb disambiguation

- ► Grefenstette & Sadrzadeh, 2011
- Same subject and object, verb changes to highlight word senses
- sim(report draw attention, report attract attention) > sim(report draw attention, report depict attention)

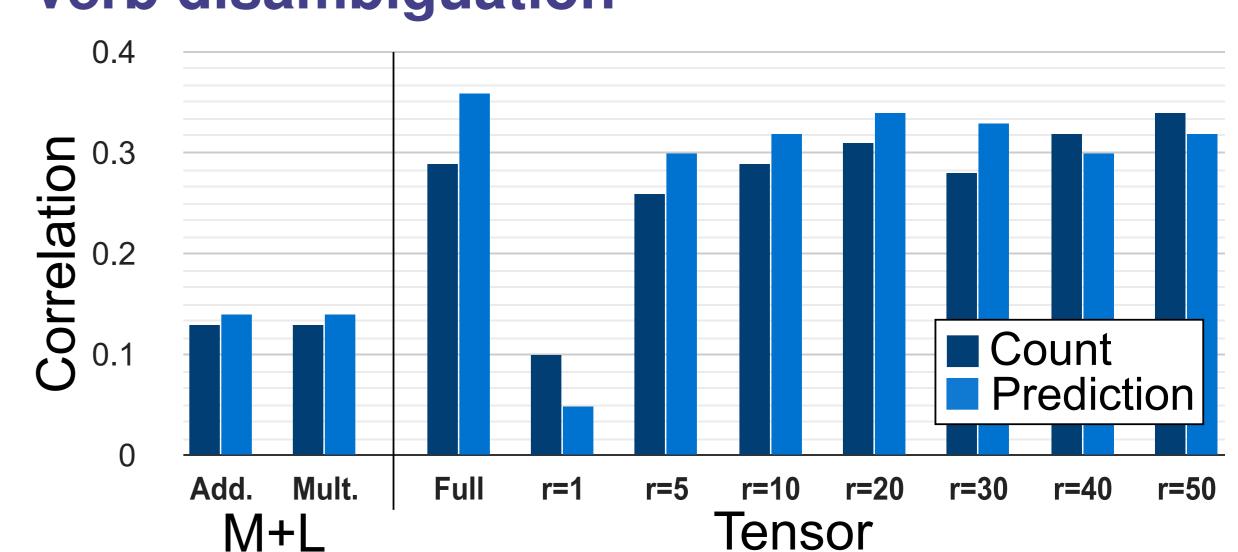
Sentence similarity

- ► Kartsaklis & Sadrzadeh, 2013
- Subject, object, and verb all vary:
- sim(programme offer support, service provide help) > sim(author write book, delegate buy land)

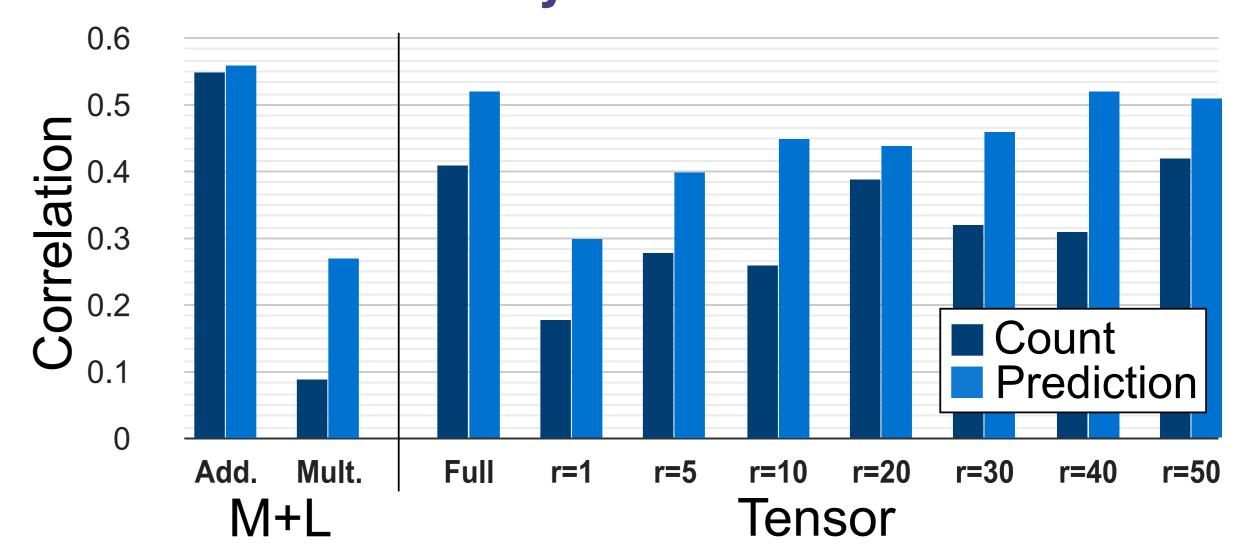
Results

- ► Low-rank tensor performance generally increases with rank
- ► Best low-rank comparable to full tensors for prediction vectors; slightly higher for count vectors
- ► Tensor methods better than element-wise vector addition or multiplication (Mitchell & Lapata, 2008) for verb disambiguation, but worse than addition for sentence similarity

Verb disambiguation



Sentence similarity



- Large reduction in parameters: R = 50 requires 15,000 parameters per verb; full tensor has 1 million
- ► Efficiently trainable with backpropagation: never have to store full tensors, and 2x faster to train per verb