

## Homework 6: Relational Design Theory (75 points)

*Due Date: Thursday, May 26, 2016 11:45 PM, on EEE*

### Relational Design Theory [75 pts]

1. [20 pts] Suppose you are given a relation R with four attributes ABCD. For each of the following sets of FDs, assuming those are the only dependencies that hold for R, do the following: (a) Identify the candidate key(s) for R. (b) Identify the best normal form that R satisfies (1NF, 2NF, 3NF, or BCNF), and point out the dependency that violates the normal form.

1.  $C \rightarrow D, C \rightarrow A, B \rightarrow A$
2.  $A \rightarrow B, B \rightarrow C, D \rightarrow A$
3.  $AB \rightarrow D, D \rightarrow B$
4.  $A \rightarrow B, A \rightarrow C, C \rightarrow D$
5.  $BC \rightarrow A, BC \rightarrow D, A \rightarrow C, D \rightarrow B$

1. BC, not 2NF,  $C \rightarrow D$
2. D, not 3NF,  $A \rightarrow B, A \rightarrow C$
3. ACD, ABC, not BCNF,  $AB \rightarrow D$
4. A, not 3NF,  $A \rightarrow C, C \rightarrow D$
5. AB, AD, BC, CD, not BCNF,  $A \rightarrow C, D \rightarrow B$

2. [20pts] Answer following questions:

- (1) Give a set of FDs for the relation schema  $R(A,B,C,D)$  with primary key AB under which R is in 1NF but not in 2NF.

Consider the set of FD:  $AB \rightarrow CD$  and  $B \rightarrow C$ .

AB is obviously a key for this relation since  $AB \rightarrow CD$  implies  $AB \rightarrow ABCD$ . It is a primary key since there are no smaller subsets of keys that hold over  $R(A,B,C,D)$ . The FD:  $B \rightarrow C$  violates 2NF since:

$C \subseteq B$  is false; that is, it is not a trivial FD

B is not a superkey

C is not part of some key for R

B is a proper subset of the key AB (transitive dependency)

- (2) Give a set of FDs for the relation schema  $R(A,B,C,D)$  with primary key  $AB$  under which  $R$  is in 2NF but not in 3NF.

Consider the set of FD:  $AB \rightarrow CD$  and  $C \rightarrow D$ .

$AB$  is obviously a key for this relation since  $AB \rightarrow CD$  implies  $AB \rightarrow ABCD$ . It is a primary key since there are no smaller subsets of keys that hold over  $R(A,B,C,D)$ . The FD:  $C \rightarrow D$  violates 3NF but not 2NF since:

$D \subseteq C$  is false; that is, it is not a trivial FD  $C$  is not a superkey

$D$  is not part of some key for  $R$

3. [10 pts] Suppose we have a relation  $R$  with 6 attributes  $ABCDEF$ , part of its instances are listed below:

A	B	C	D	E	F
1	2	4	6	3	6
2	1	5	7	9	7
3	2	4	6	3	8
4	1	4	0	9	9

~~Try to infer all the function dependencies in relations  $R$ , and listed as follow.~~

Write down a **minimal** set of functional dependencies with at most two attributes on the left-hand side that are not violated by this instance. By “minimal” we mean no FDs in the set can be derived by the other FDs in the set. For instance, the set  $\{X \rightarrow Y, Y \rightarrow Z, X \rightarrow Z\}$  is not minimal since the last FD can be derived by the first two. The set  $\{X \rightarrow Y, Y \rightarrow Z\}$  is minimal.

( $A \rightarrow BCDEF$  and  $F \rightarrow A$ , or ,  $F \rightarrow ABCDE$  and  $A \rightarrow F$ ),  $B \rightarrow E$ ,  $E \rightarrow B$ ,  $D \rightarrow BCE$ ,  $BC \rightarrow D$

To solve this question, you first need to know how to check  $X \rightarrow Y$ . If  $X \rightarrow Y$ , this means  $X = x_1$ , the value of  $Y$  in the same record will always be  $Y = y_1$ , and we will not have  $x_1 \rightarrow y_1$  and  $x_1 \rightarrow y_2$  mapping in one relation. However, it's possible that  $x_1 \rightarrow y_1$  and  $x_2 \rightarrow y_1$ .

With this condition, we can easily know  $A \rightarrow BCDEF$ , and  $F \rightarrow ABCDE$ , since no duplicate values in  $A$  and  $F$ . Then we start from 1 attribute on left, and other attributes on right. Check condition for  $B \rightarrow C$ ,  $B \rightarrow D$ ,  $B \rightarrow E$ ,  $C \rightarrow B$  ... We don't need to include  $A$  and  $F$  on the right side, because the values in these two column are distinct and the condition will always be

true. After first round, we move on to 2 attributes on left,  $BC \rightarrow D$ ,  $BC \rightarrow E$ ,  $BD \rightarrow C$ , ... You may have  $BD \rightarrow CE$  and  $CD \rightarrow BE$  evaluated as true with the condition, but they are redundant with  $D \rightarrow BCE$ . So they will be removed from the result set.

4. [25pts] Consider the attribute set  $R = ABCDEGH$  and the FD set  $F = \{AB \rightarrow CD, AC \rightarrow B, AD \rightarrow E, B \rightarrow C, BD \rightarrow A, E \rightarrow G\}$ .

For each of the following attribute sets, do the following: (i) Compute the set of dependencies that hold over the set (ii) Name the strongest normal form that is not violated by the relation containing these attributes.

(a) ABC,

$AC \rightarrow B, B \rightarrow C$

3NF, AB, AC

(b) ABCD,

1NF

$AC \rightarrow B, B \rightarrow C, AB \rightarrow CD, BD \rightarrow A$

(c) ABCEG,

1NF

$AC \rightarrow B, B \rightarrow C, E \rightarrow G$

(d) DCEGH,

1NF

$E \rightarrow G$

(e) ACEH

BCNF None FDs OR 1NF,  $AC \rightarrow E$

\*As we didn't specify that you cannot use FDs which include other attributes to make dependency reasoning, some of you use  $AC \rightarrow B, AB \rightarrow CD, AD \rightarrow E$  to get  $AC \rightarrow E$ . In this case, both answers are correct. Same for the extra credit part.

(b) Which of the following decompositions of  $R = ABCDEGH$ , with the same set of dependencies  $F$ , is dependency-preserving? Explain why.

(a)  $\{AB, BC, ABDE, EG\}$

NO.  $AC \rightarrow B$  is not preserved.

(b)  $\{ABC, ACDE, ADG\}$

NO.  $E \rightarrow G$  is not preserved.

**Extra Credits**

[10pts] Decompose each of the attribute sets in Question 4(a) into a collection of BCNF relations if it is not in BCNF.

- (1) No dependency preserving decomposition/AB,BC (Not dependency preserving)
- (2) No dependency preserving decomposition/ABD,BC (Not dependency preserving)
- (3) No dependency preserving decomposition/ABE,BC,EG (Not dependency preserving)
- (4) DCEH, EG
- (5) ACEH is already BCNF/ACE ACH