Association Rule Mining

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Preparing the data

In project 3 we're working with a new data set from the College Scorecard. According to the data documentation:

The College Scorecard is designed to increase transparency, putting the power in the hands of the public — from those choosing colleges to those improving college quality — to see how well different schools are serving their students.

There are a lot of variables available to us in this data set and we can use association mining to discovery trends and patterns.

Feature engineering

Feature engineering is the process of using domain knowledge or expertise to construct new variables for use in data exploration and modeling. In association rule mining, we're looking for associations between *categories* of features, so the inputs all need to be discrete. Many of the variables in your data set are already discrete, like state or locale, but we'll need to use some feature engineering to coerce other variables of interest.

discretize

The arules package provides a function that can help you create discrete variables from continuous ones, called discretize:

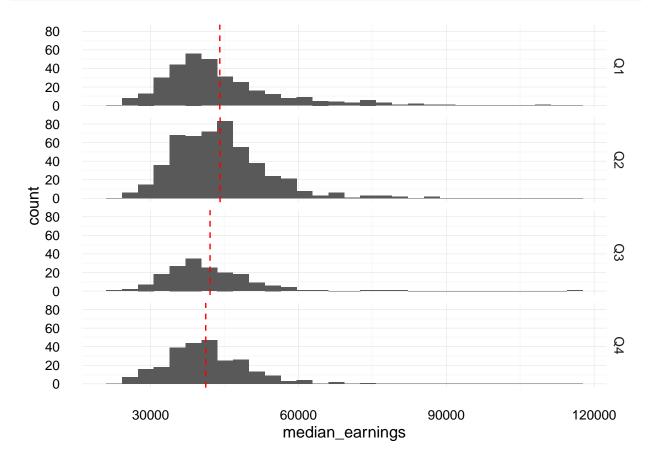
```
colleges =
  colleges %>%
   mutate(cost_category = discretize(cost))
# the default results in only 3 bins of uneven size
table(colleges$cost_category)
##
## [-1643,28095) [28095,57832) [57832,87570]
                           320
##
            5971
colleges =
  colleges %>%
   mutate(cost category = discretize(cost, method = 'frequency', categories = 4))
# that's better
table(colleges$cost_category)
## [-1643, 9387) [ 9387,15114) [15114,20541) [20541,87570]
            1575
                          1572
                                         1574
                                                       1573
```

discretize can break your variable up with several different methods, e.g. equal interval length, equal frequency, clustering-based, and custom interval discretization. Also you can specify categories to get as many or as few as you like. See ?discretize for details.

SAT performance spread

Let's make a couple new features based on the variables available. I'm curious about the spread in student performance at schools, so to investigate that I can compute the difference between the top 75% and the bottom 25% of performance on the SATs.

```
# difference between Q3 and Q1.
colleges =
  colleges %>%
    mutate(sat_verbal_spread = discretize(sat_verbal_quartile_3 - sat_verbal_quartile_1,
```



STEM schools

I have a feeling that there are interesting patterns earnings patterns for schools where students primarily study science, technology, engineering, and math (STEM) fields. So, I can make a variable indicating whether a school has a large proportion of STEM students.

Generating rules

Before we start association rule mining, we need to select out the columns to mine. Remember, this algorithm works on discrete, categorical data so we need to remove or convert numerical columns.

```
colleges features =
  colleges %>%
    select(state, locale, control, pred_deg, historically_black,
         men_only, women_only, religious, online_only,
         earnings_quartiles, debt_quartiles, high_stem, sat_verbal_spread,
         sat_math_spread, sat_writing_spread)
```

Then we're going to load our data into a transaction object in the arules package. Each row of college_features represents a 'transaction.'

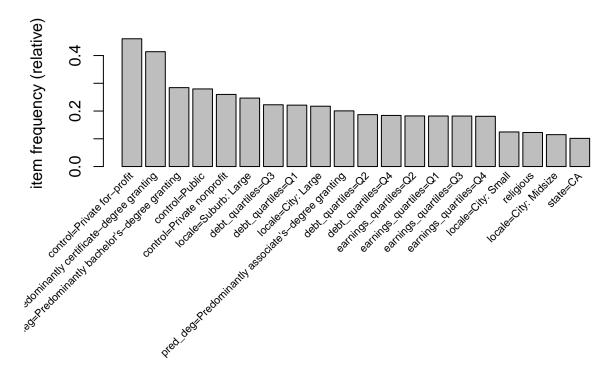
```
college_features = as(college_features, 'transactions')
```

Once our data is a transaction object, we can inspect the itemsets which are just the characteristics corresponding with each college.

```
# view the itemsets
inspect(college_features[1:5])
```

```
##
     items
                                                           transactionID
## 1 {state=AL,
##
      locale=City: Midsize,
##
      control=Public,
##
      pred_deg=Predominantly bachelor's-degree granting,
##
      historically_black,
##
      earnings_quartiles=Q2,
##
      debt_quartiles=Q4,
##
      high stem,
##
      sat_verbal_spread=Q1,
##
      sat_math_spread=Q2}
                                                                        1
## 2 {state=AL,
##
      locale=City: Midsize,
##
      control=Public,
##
      pred deg=Predominantly bachelor's-degree granting,
      earnings_quartiles=Q4,
##
      debt_quartiles=Q3,
##
##
      sat_verbal_spread=Q3,
                                                                        2
##
      sat_math_spread=Q4}
## 3 {state=AL,
##
      locale=City: Midsize,
      control=Private nonprofit,
##
##
      pred_deg=Predominantly bachelor's-degree granting,
##
      religious,
      earnings_quartiles=Q3}
                                                                        3
##
## 4 {state=AL,
      locale=City: Midsize,
##
##
      control=Public,
##
      pred_deg=Predominantly bachelor's-degree granting,
```

```
##
      earnings_quartiles=Q4,
##
      debt_quartiles=Q3,
      high stem,
##
##
      sat_verbal_spread=Q4,
##
      sat_math_spread=Q4}
                                                                        4
## 5 {state=AL,
##
      locale=City: Midsize,
      control=Public,
##
##
      pred_deg=Predominantly bachelor's-degree granting,
##
      historically_black,
##
      earnings_quartiles=Q2,
##
      debt_quartiles=Q4,
##
      sat_verbal_spread=Q2,
                                                                        5
##
      sat_math_spread=Q2}
summary(college_features)
## transactions as itemMatrix in sparse format with
   7308 rows (elements/itemsets/transactions) and
    105 columns (items) and a density of 0.05871713
##
## most frequent items:
##
                            control=Private for-profit
##
                                                   3365
  pred_deg=Predominantly certificate-degree granting
##
##
                                                   3025
##
    pred_deg=Predominantly bachelor's-degree granting
##
                                                   2078
##
                                        control=Public
##
                                                   2044
##
                             control=Private nonprofit
##
                                                   1899
##
                                                (Other)
##
                                                  32645
##
## element (itemset/transaction) length distribution:
## sizes
                           7
                                         10
                                                    12
                5
                     6
                                8
                                     9
                                               11
##
     14 679 1858 3051
                        392
                              283
                                   639
                                        370
                                               21
                                                     1
##
##
      Min. 1st Qu.
                    Median
                               Mean 3rd Qu.
                                                Max.
##
     3.000
             5.000
                     6.000
                              6.165
                                      6.000 12.000
##
## includes extended item information - examples:
       labels variables levels
##
## 1 state=AK
                  state
                             ΔK
## 2 state=AL
                  state
                             AL
## 3 state=AR
                  state
                             AR
## includes extended transaction information - examples:
     transactionID
## 1
                 1
## 2
                 2
## 3
                 3
```



The summary of the data set provides an overview of the most frequent items along with other distributional details. Further, we can see which characteristics are the most common in the data set the itemFrequencyPlot().

Next, use the apriori() function to find all rules with a specified minimum support and confidence, e.g. support = 0.01 and confidence = 0.6.

```
## Apriori
##
## Parameter specification:
##
    confidence minval smax arem aval originalSupport support minlen maxlen
##
                         1 none FALSE
                                                  TRUE
##
    target
             ext
##
     rules FALSE
##
## Algorithmic control:
##
    filter tree heap memopt load sort verbose
##
       0.1 TRUE TRUE FALSE TRUE
                                          TRUE
##
##
  Absolute minimum support count: 73
##
## set item appearances ...[0 item(s)] done [0.00s].
## set transactions ...[105 item(s), 7308 transaction(s)] done [0.00s].
```

```
## sorting and recoding items ... [76 item(s)] done [0.00s].
## creating transaction tree ... done [0.00s].
## checking subsets of size 1 2 3 4 5 6 done [0.00s].
## writing ... [930 rule(s)] done [0.00s].
## creating S4 object ... done [0.00s].
# print distribution information
summary(rules)
## set of 930 rules
## rule length distribution (lhs + rhs):sizes
        3
           4
                5
##
   55 376 376 115
##
##
##
     Min. 1st Qu. Median
                             Mean 3rd Qu.
    2.000 3.000
                    4.000
                            3.618
##
                                    4.000
                                            6.000
##
## summary of quality measures:
##
      support
                     confidence
                                           lift
## Min.
          :0.01013 Min. :0.6000
                                    Min. : 1.314
  1st Qu.:0.01177 1st Qu.:0.6667
                                      1st Qu.: 2.517
## Median :0.01574 Median :0.8045
                                      Median : 3.389
   Mean :0.02188
                    Mean :0.8118
                                      Mean : 3.748
                                      3rd Qu.: 3.848
##
   3rd Qu.:0.02217
                     3rd Qu.:0.9638
## Max.
         :0.30624
                     Max. :1.0000
                                      Max.
                                             :18.213
##
## mining info:
##
               data ntransactions support confidence
                             7308
                                     0.01
   college_features
items(rules)
## itemMatrix in sparse format with
## 930 rows (elements/transactions) and
## 105 columns (items)
# view the rules
inspect(head(rules))
##
    lhs
                               rhs
                                                                                     support confiden
## 1 {state=PR}
                            => {earnings_quartiles=Q1}
                                                                                  0.01272578 0.69402
## 2 {state=AZ}
                            => {control=Private for-profit}
                                                                                  0.01135742 0.66400
## 3 {state=CO}
                            => {control=Private for-profit}
                                                                                  0.01039956
                                                                                              0.60800
## 4 {historically_black}
                            => {pred_deg=Predominantly bachelor's-degree granting} 0.01122058 0.82828
                                                                                  0.01587302 0.72955
## 5 {state=NJ}
                            => {locale=Suburb: Large}
## 6 {sat_writing_spread=Q4} => {sat_verbal_spread=Q4}
                                                                                  0.01067323
                                                                                              0.65546
# sort the rules by lift
inspect(head(sort(rules, by = 'lift')))
```

```
##
     lhs
                                                                                       support confidenc
                                                          => {sat_verbal_spread=Q4} 0.01067323
## 1 {sat_writing_spread=Q4}
                                                                                                0.655462
## 2 {religious,
      sat_math_spread=Q4}
                                                          => {sat_verbal_spread=Q4} 0.01053640 0.626016
##
## 3 {control=Private nonprofit,
##
      religious,
                                                          => {sat_verbal_spread=Q4} 0.01053640
##
      sat_math_spread=Q4}
                                                                                                0.626016
## 4 {pred_deg=Predominantly bachelor's-degree granting,
##
      religious,
                                                          => {sat_verbal_spread=Q4} 0.01026273 0.619834
##
      sat_math_spread=Q4}
## 5 {control=Private nonprofit,
      pred_deg=Predominantly bachelor's-degree granting,
##
##
      religious,
##
      sat_math_spread=Q4}
                                                          => {sat_verbal_spread=Q4} 0.01026273 0.619834
## 6 {pred_deg=Predominantly bachelor's-degree granting,
##
      sat_math_spread=Q1,
                                                          => {sat_verbal_spread=Q1} 0.01313629
##
      sat_writing_spread=Q1}
                                                                                                0.750000
# view quality metrics
quality(rules) = cbind(quality(rules), coverage = coverage(rules))
head(quality(rules))
##
        support confidence
                                lift
                                       coverage
## 1 0.01272578  0.6940299  3.810646  0.01833607
## 2 0.01135742 0.6640000 1.442054 0.01710454
## 3 0.01039956 0.6080000 1.320435 0.01710454
## 4 0.01122058 0.8282828 2.912941 0.01354680
## 5 0.01587302 0.7295597 2.957084 0.02175698
```

The result of mining the colleges data associations between the characteristics expressed in the form of rules. We end up producing 930 such associations, or rules.

For an overview of the rules <code>summary()</code> can be used. It shows the number of rules, the most frequent items contained in the left-hand-side and the right-hand-side and their respective length distributions and summary statistics for the quality measures returned by the mining algorithm.

Increasing rule size with maxlen

6 0.01067323 0.6554622 18.213375 0.01628352

By default, rules will not exceed 6 objects in size, but you can change that length constraint with maxlen.

```
# allow rules to up to size 10
long_rules = apriori(college_features,
                     parameter = list(sup = 0.001, conf = 0.6,
                                       target = 'rules', maxlen = 10))
## Apriori
##
## Parameter specification:
   confidence minval smax arem aval original Support support minlen maxlen
##
##
           0.6
                  0.1
                                                  TRUE
                                                         0.001
                                                                           10
                         1 none FALSE
                                                                     1
  target
             ext
```

```
##
     rules FALSE
##
## Algorithmic control:
   filter tree heap memopt load sort verbose
##
       0.1 TRUE TRUE FALSE TRUE
##
## Absolute minimum support count: 7
##
## set item appearances ...[0 item(s)] done [0.00s].
## set transactions ...[105 item(s), 7308 transaction(s)] done [0.00s].
## sorting and recoding items ... [98 item(s)] done [0.00s].
## creating transaction tree ... done [0.00s].
## checking subsets of size 1 2 3 4 5 6 7 8 done [0.01s].
## writing ... [25755 rule(s)] done [0.00s].
## creating S4 object ... done [0.01s].
inspect(head(sort(long_rules, by = 'lift'), 2))
##
     lhs
                                                                             support confidence
                                                             rhs
                                                                                                    lift
## 1 {state=NY,
##
      pred_deg=Predominantly bachelor's-degree granting,
##
      earnings_quartiles=Q1}
                                                          => {men_only} 0.001231527
                                                                                            0.9 99.65455
## 2 {state=NY,
##
      control=Private nonprofit,
##
      pred_deg=Predominantly bachelor's-degree granting,
```

=> {men_only} 0.001231527

=> {earnings_quartiles=Q4} 0.01190476 0.79816

0.9 99.65455

Investigate interesting patterns

sat_verbal_spread=Q2}

earnings_quartiles=Q1}

##

##

It's common for the result of association rule mining to produce a huge amount of rules. The subset() function can be used to narrow in on the results by filtering on characteristics of interest.

For example, let's filter for control=Private for profit to see what is associated with that.

```
high_earners = subset(rules, subset = rhs %in% 'earnings_quartiles=Q4' & lift > 1)
inspect(head(high_earners, n = 5, by = 'lift'))
```

```
##
     lhs
                                                             rhs
                                                                                         support confiden
## 1 {locale=Suburb: Large,
      pred_deg=Predominantly bachelor's-degree granting,
##
      sat_math_spread=Q2}
                                                          => {earnings_quartiles=Q4} 0.01176793
##
                                                                                                   0.81904
## 2 {locale=Suburb: Large,
##
      sat_math_spread=Q2}
                                                          => {earnings_quartiles=Q4} 0.01190476
                                                                                                  0.80555
## 3 {locale=Suburb: Large,
      pred_deg=Predominantly bachelor's-degree granting,
      sat_verbal_spread=Q2}
                                                          => {earnings_quartiles=Q4} 0.01122058
                                                                                                  0.80392
##
## 4 {locale=City: Large,
##
      pred_deg=Predominantly bachelor's-degree granting,
##
      sat_verbal_spread=Q2}
                                                          => {earnings_quartiles=Q4} 0.01163109
                                                                                                  0.80188
## 5 {locale=City: Large,
```

Visualizing with arulesViz

The authors of arules followed on that package with arulesViz, which provides lots of great pre-packaged visualization for exploring your association rules.

```
# arules plot template
plot(x,
    method = NULL,
    measure = 'support',
    shading = 'lift',
    interactive = FALSE,
    data,
    control = ...)
```

where:

- x: is the set of rules to be visualized
- method: the visualization method
- measure: and shading contain the interest measures used by the plot
- interactive: indicates whether you want to interactively explore
- data: can contain the transaction data set used to mine the rules
- control: list with further control arguments to customize the plot

```
install.packages('arulesViz', dependencies = TRUE)

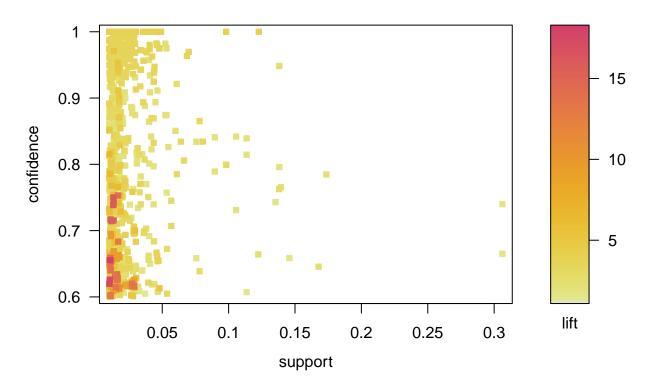
# you might need to install Rgraphviz from this repository
source('http://bioconductor.org/biocLite.R')
biocLite('Rgraphviz')

library(arulesViz)
```

We can start with a visualization of association rules as a scatter plot with two measures on the axes. The default plot() for association rules is a scatter plot using support and confidence on the axes. Lift is used as the color of the points.

```
plot(rules)
```

Scatter plot for 930 rules



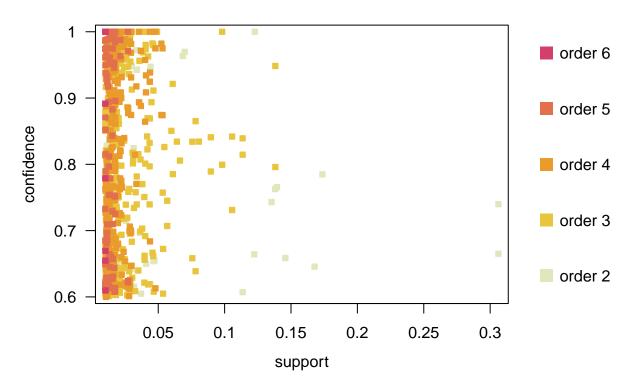
head(quality(rules))

```
##
        support confidence
                                lift
                                       coverage
                           3.810646 0.01833607
## 1 0.01272578
                0.6940299
## 2 0.01135742
                0.6640000
                            1.442054 0.01710454
## 3 0.01039956
                 0.6080000
                            1.320435 0.01710454
## 4 0.01122058
                 0.8282828
                            2.912941 0.01354680
## 5 0.01587302
                 0.7295597
                           2.957084 0.02175698
## 6 0.01067323
                0.6554622 18.213375 0.01628352
```

Another version of the scatter plot called two-key plot. Here support and confidence are used for the x and y-axes and the color of the points indicates the 'order,' i.e., the number of items contained in the rule:

```
plot(rules, shading = 'order')
```

Scatter plot for 930 rules

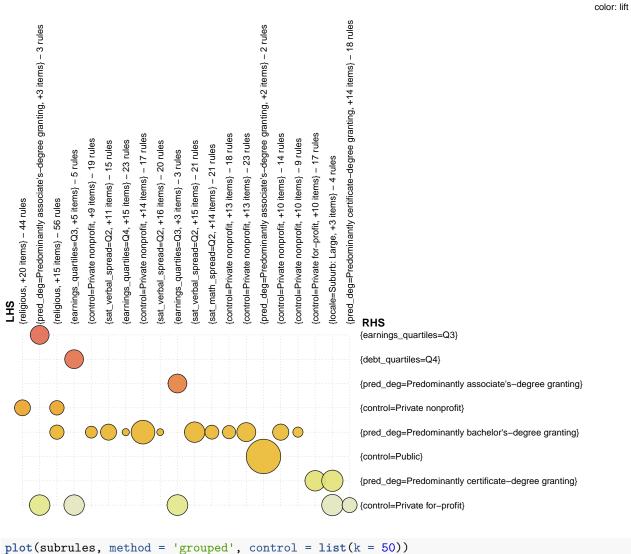


We can filter to narrow in on rules of interest:

```
subrules = rules[quality(rules)$confidence > 0.9]
plot(subrules, method = 'grouped')
```

Grouped matrix for 352 rules

size: support color: lift

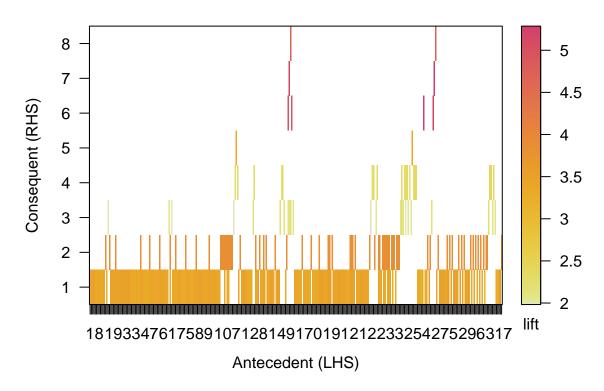


Grouped matrix for 352 rules

size: support color: lift

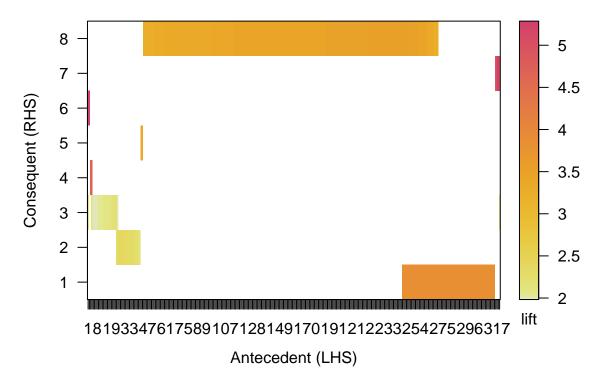
```
ociate's-degree granting, +2 items} - 2 rules
                                                      granting, +2 items} - 2 rules
                                                                                  ree granting, +3 items} - 2 rules
                                                                                        RHS
                                                                                        {earnings_quartiles=Q3}
                                                                                       {debt_quartiles=Q4}
                                                                                        {pred_deg=Predominantly associate's-degree granting}
                                                                                        {control=Private nonprofit}
             {pred_deg=Predominantly bachelor's-degree granting}
                                                                                        {control=Public}
                                                                                        {pred_deg=Predominantly certificate-degree granting}
                                                                         (control=Private for-profit)
plot(subrules,
        method = 'matrix',
        measure = 'lift')
```

Matrix with 352 rules



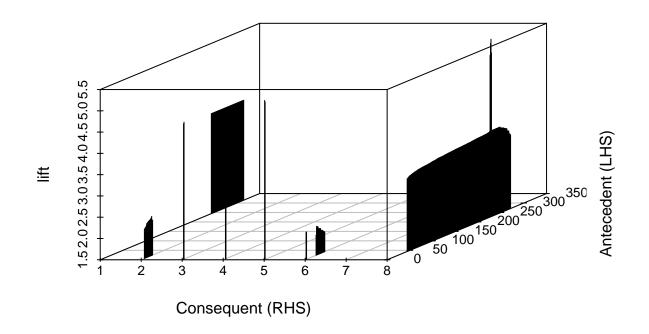
```
# reorder based on
plot(subrules,
    method = 'matrix',
    measure = 'lift',
    control = list(reorder = TRUE))
```

Matrix with 352 rules



```
plot(subrules,
    method = 'matrix3D',
    measure = 'lift',
    control = list(reorder = TRUE))
```

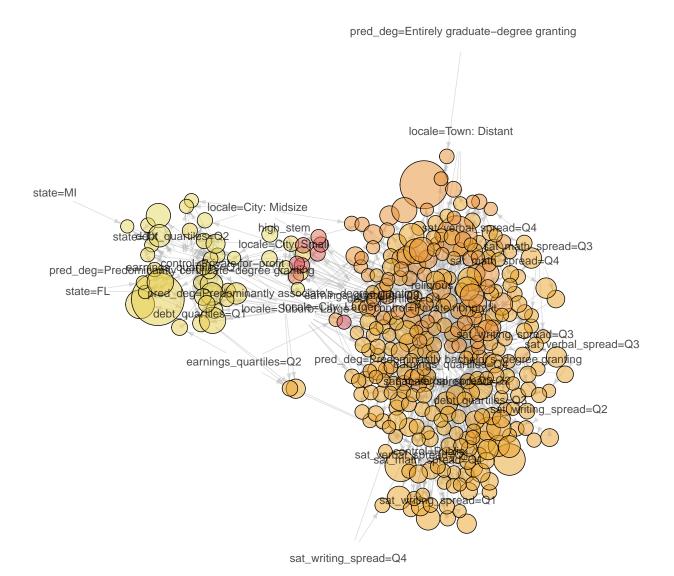
Matrix with 352 rules



```
# plot a graph
plot(subrules, method = 'graph')
```

Graph for 352 rules

size: support (0.01 – 0.138) color: lift (1.966 – 5.27)



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