

# Selecting differentially expressed genes with R or TmeV

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## Retrieving the den Boer normalized dataset

Here we will use data from the microarray series [GSE13425](#), which was retrieved from the [Gene Expression Omnibus \(GEO\)](#) database. In this experiment, the authors applied a supervised classification method to define a transcriptomic signature, in order to classify samples from acute lymphoblastic leukemia (ALL). Lymphoblastic leukemia is characterized by the abnormal clonal proliferation, within the bone marrow, of lymphoid progenitors blocked at a precise stage of their differentiation.

Data were produced using Affymetrix geneChips (Affymetrix Human Genome U133A Array, HGU133A). Information related to this platform are available on GEO website under identifier [GPL96](#).

## Loading data into R

### Protocol

- Start R.
- Have a look at the description of the `read.table()` function.
- We will now load three data tables into R using the `read.table` function. The function allows us to directly read the tables from the web server. We will successively load 3 files providing complementary information.
  - the expression matrix (`GSE13425_Norm_Whole.txt`)
    - \* Contains genes as rows and samples as columns.
    - \* Data were previously normalized using `rma` algorithm (they are thus transformed in logarithm base 2).
  - the A/P/M matrix (`GSE13425_AMP_Whole.txt`)
    - \* Indicates whether a gene was called **A**bsent, **P**resent or **M**arginal.
  - Phenotypic data (`GSE13425_phenoData.txt`)
    - \* The `GSE13425_phenoData.txt` file contains phenotypic information about samples.

```
## Get some help about the read.table fonction
#?read.table

## Define the URL of the example data sets
url.course <- "http://pedagogix-tagc.univ-mrs.fr/courses/ASG1"
url.base <- file.path(url.course, "data/marrays/")

## Load expression values
expr.file <- file.path(url.base, "GSE13425_Norm_Whole.txt")
expr.matrix <- read.table(expr.file, sep="\t", head=T, row=1)

## Load phenotypic data
pheno <- read.table(file.path(url.base, 'phenoData_GSE13425.tab'),
                    sep='\t', head=TRUE, row=1)

## Load Absent/Marginal/Present (AMP) calls
amp <- read.table(file.path(url.base, "GSE13425_AMP_Whole.txt"),
                  sep="\t", head=T, row=1)
```

We will now define a directory to store the results on our computer.

```
## Define the output directory. You can adapt this to your local configuration.
dir.output <- "~/ASG1_practicals/GSE13425"

## Create the output directory (if it does not exist yet)
dir.create(dir.output, showWarnings=FALSE, recurs=TRUE)

## Change directory to dir.output
setwd(dir.output)
```

## Exercise

- How many rows and columns does the object `expr.matrix` contain
- Does it correspond to the dimensions of the A/P/M matrix ?
- Which information is available about samples ?
- How many samples from each tumor subtype are present in the DenBoer dataset ?

[View solution](#) | [Hide solution](#)

```
## Check the dimension of the different tables
# an alternative is to use nrow and ncol
dim(expr.matrix)
```

## Solution

```
## [1] 22283 190
```

```
dim(amp)
```

```
## [1] 22283 190
```

```
dim(pheno)
```

```
## [1] 190 4
```

```
colnames(pheno)
```

```
## [1] "Sample.title" "Sample.source.name.ch1"
## [3] "Sample.characteristics.ch1" "Sample.description"
```

The field “sample title” of the `pheno` table indicates the subtype of each ALL tumour. We can use the R function `table()` to count the number of samples assigned to each tumour class.

```
table(pheno$Sample.title)
```

```
##
##          BCR-ABL BCR-ABL + hyperdiploidy E2A-rearranged (E-sub)
##              4              1              4
## E2A-rearranged (E) E2A-rearranged (EP) hyperdiploid
##              1              8              44
##              MLL          pre-B ALL          T-ALL
##              4              44              36
## TEL-AML1 TEL-AML1 + hyperdiploidy
##              43              1
```

We can convert the vector to a single-column data frame, to enhance its readability, and use this data frame to select the subtypes represented by at least 10 samples.

```
print(as.data.frame(table(pheno$Sample.title)))
```

```
##              Var1 Freq
## 1          BCR-ABL    4
## 2 BCR-ABL + hyperdiploidy  1
## 3   E2A-rearranged (E-sub)  4
## 4       E2A-rearranged (E)  1
## 5       E2A-rearranged (EP)  8
## 6          hyperdiploid  44
## 7              MLL    4
## 8          pre-B ALL  44
## 9              T-ALL  36
## 10         TEL-AML1  43
## 11 TEL-AML1 + hyperdiploidy  1
```

```
## Sort subtypes by decreasing number of samples
samples.per.subtype <- as.data.frame(sort(table(pheno$Sample.title),
                                             decreasing=TRUE))
print(samples.per.subtype)
```

```
##              sort(table(pheno$Sample.title), decreasing = TRUE)
## hyperdiploid                                           44
## pre-B ALL                                           44
## TEL-AML1                                           43
## T-ALL                                           36
## E2A-rearranged (EP)                                           8
## BCR-ABL                                           4
## E2A-rearranged (E-sub)                                           4
## MLL                                           4
## BCR-ABL + hyperdiploidy                                           1
## E2A-rearranged (E)                                           1
## TEL-AML1 + hyperdiploidy                                           1
```

```
## Select subtypes represented by at least 10 samples
samples.per.subtype > 10
```

```
##              sort(table(pheno$Sample.title), decreasing = TRUE)
## hyperdiploid                                           TRUE
## pre-B ALL                                           TRUE
## TEL-AML1                                           TRUE
## T-ALL                                           TRUE
## E2A-rearranged (EP)                                           FALSE
## BCR-ABL                                           FALSE
## E2A-rearranged (E-sub)                                           FALSE
## MLL                                           FALSE
## BCR-ABL + hyperdiploidy                                           FALSE
## E2A-rearranged (E)                                           FALSE
## TEL-AML1 + hyperdiploidy                                           FALSE
```

```
rownames(samples.per.subtype)[samples.per.subtype > 10]
```

```
## [1] "hyperdiploid" "pre-B ALL"      "TEL-AML1"      "T-ALL"
```

## Interpretation

The dataset from DenBoer contains **190 samples** belonging to **various tumour classes**. We can already notice that there is an **important imbalance** between the sizes of the tumour classes: T-ALL, pre-B ALL, TEL-AML1 and hyperdiploid are each represented by more than 40 samples, whereas the other classes (e.g. BCR-ABL, E2A-rearranged) are represented by a handful of samples.

The number of samples per group is a very important factor for selecting differentially expressed genes: in general, **the power of the tests** (i.e. the capacity to detect effectively differentially expressed genes) **increases with group sizes**.

---

## Basics about Welch's t test

Welch's test is a variant of the classical Student test, whose goal is to test the equality between two means.

$$H_0 : m_{g,1} = m_{g,2}$$

where  $m_{g,1}$  and  $m_{g,2}$  represent the **respective mean expression values for a given gene  $g$  in two populations** (for example, all existing patients suffering from T-ALL versus all patients suffering from pre-B ALL). Of course, we do not dispose of measurements for all the patients suffering from these two types of ALL in the world (the population). We only dispose of two sets of samples, covering 36 (T-ALL) and 44 (pre-B ALL) patients, respectively. On the basis of these samples, we will estimate how likely it is that genes  $g$  is generally expressed at similar levels in the populations from which the samples were drawn.

The essential difference between **Student** and **Welch** is that the proper Student test relies on the assumption that the two sampled populations have the **same variance**, whereas Welch's test is designed to treat populations with **unequal variances**.

When detecting differentially expressed genes, **we cannot assume equal variance**. Indeed, a typical case would be that a gene of interest is expressed at very low level in the first group, and high level in the second group. The inter-individual fluctuations in expression values are expected to be larger when the gene is expressed at a high level than when it is poorly expressed. It is thus generally recommended to use Welch rather than Student test when analyzing microarray expression profiles.

**BEWARE:** Student and Welch tests **assume data normality**. Affymetrix microarray intensities are far from the normal distribution, even after log transformation. However, **t-test is robust to non-normality if there is a sufficient number of samples per group**. In the subsequent exercise, we will apply Welch test to detect genes differentially expressed between cancer types represented by ~40 samples each. We are thus in **reasonably good conditions** to run a Welch test. Nevertheless, in a next section we will also apply a non-parametric test (Wilcoxon), which does not rely on an assumption of normality.

Welch's t-test defines the t statistic by the following formula:

$$t = \frac{\bar{x}_1 - \bar{x}_2}{\sqrt{\frac{s_1^2}{n_1} + \frac{s_2^2}{n_2}}}$$

Where:

- $\bar{x}_i$  is the sample mean,
- $s_i^2$  the sample variance,
- $n_i$  the sample size.

The `t.test()` function can be used to calculate this score (and additional informations such as `p.value`). This function returns an **S3 object** whose slots can be listed using the `names()` function and accessed using the **\$ operator** (such as with lists in R).

### A first intuition

In order to get an intuition of the  $t$  statistics, let us create artificial datasets and compute the associated  $t$  value. In the following example  $x$  and  $y$  can be viewed as the expression values for gene  $g$  in two different classes of cancer.

Assuming that each group contains 4 patients, we will generate 4 random numbers following a normal distribution, to simulate the groups 1 and 2. We deliberately set the means to the same values (to fall under the null hypothesis), but we generate them with different standard deviations.

```
x <- rnorm(n=4, mean=6, s=1)
y <- rnorm(n=4, mean=6, s=2)
```

- Compute the associated  $t$  value using the `mean`, `sd` and `sqrt` functions.

[View solution](#) | [Hide solution](#)

```
# Compute the t statistics manually
nx <- length(x)
ny <- length(y)
diff <- mean(x) - mean(y)
t.obs <- diff/sqrt((sd(x)^2)/nx + (sd(y)^2)/ny)

# print the result
print(t.obs) # or t.obs or show(t.obs)
```

### Solution

```
## [1] -0.4015133
```

- Now we can check that the same result is obtained using the `t.test` function implemented in R.

[View solution](#) | [Hide solution](#)

```
## Run the Welch test (this is specified by indicating that we don't expect equal variances)
simulated.welch <- t.test(x,y, var.equal=FALSE)
print(simulated.welch)
```

### Solution

```
##
## Welch Two Sample t-test
##
## data: x and y
## t = -0.4015, df = 3.718, p-value = 0.71
## alternative hypothesis: true difference in means is not equal to 0
## 95 percent confidence interval:
## -5.673890 4.277562
## sample estimates:
## mean of x mean of y
## 5.513864 6.212029
```

```
## Note: during the practical, each student should obtain a different result, since values were generated
```

```
## Retrieve the t statistics
names(simulated.welch)
```

```
## [1] "statistic" "parameter" "p.value" "conf.int" "estimate"
## [6] "null.value" "alternative" "method" "data.name"
```

```
simulated.welch$statistic
```

```
## t
## -0.4015133
```

```
## Compare the t statistics computed by the t.test() function and your manual computation
t.obs
```

```
## [1] -0.4015133
```

```
simulated.welch$statistic == t.obs
```

```
## t
## TRUE
```

---

## Applying Welch's t-test to the den Boer dataset

We would like to define genes that discriminate between “hyperdiploid” tumors and tumors of all the other subtypes represented by at least 10 samples in Den Boer dataset.

One possibility would be to iterate over all probesets, and to successively run the R method `t.test()` on each one. This would however be quite inefficient, and the results would not be very easy to handle, since it would be a list of objects of the class `t.test`.

Instead, we will use a custom function that runs Student or Welch test in parallel on all the elements of a data table.

## Running t-tests on each row of a data matrix

**Installing the qvalue library** First we need to check if the *qvalue* library is installed (we will give more information about q-values in the next sessions).

```
### Running t-tests on each row of a data matrix
## We must first check if the q-value library from Bioconductor has
## been installed (if not, will be installed here)
if (!require("qvalue")) {
  source("http://bioconductor.org/biocLite.R")
  biocLite("qvalue")
}
```

```
## Loading required package: qvalue
```

**Loading the function *t.test.multi()*** The we will load a custom script written by J. van Helden (**Note:** the utilities for this course will soon be converted to an R package, in order to facilitate their installation and use).

```
## Load a custom the library for multiple t tests
url.stats4bioinfo <- "http://pedagogix-tagc.univ-mrs.fr/courses/statistics_bioinformatics"
source(file.path(url.stats4bioinfo, 'R-files/config.R'))
```

```
## [1] "Data repository http://pedagogix-tagc.univ-mrs.fr/courses/statistics_bioinformatics/data"
## [1] "R scripts source http://pedagogix-tagc.univ-mrs.fr/courses/statistics_bioinformatics/R-files"
## [1] "Results will be saved to /Users/jvanheld/course_stats_bioinfo/results"
## [1] "Figures will be saved to /Users/jvanheld/course_stats_bioinfo/figures"
```

```
source(file.path(url.stats4bioinfo, 'R-files/util/util_student_test_multi.R'))
```

For the sake of curiosity, you can also have a look at the [R code](#).

**Defining sample groups** We will select genes differentially expressed between one subtype of interest (for example *hyperdiploid*) and all the other types of ALL represented by at least 10 samples. For the rest of the tutorial, we will refer to these subtypes as “*Other*”.

```
## Classes to keep
print("Selecting cancer subtypes with >= 10 samples")
```

```
## [1] "Selecting cancer subtypes with >= 10 samples"
```

```
class.freq <- table(pheno$Sample.title)
classes.to.keep <- names(class.freq[class.freq>10])
subtype.of.interest <- "hyperdiploid"
classes.other <- setdiff(classes.to.keep, subtype.of.interest)
print(classes.to.keep)
```

```
## [1] "hyperdiploid" "pre-B ALL"    "T-ALL"        "TEL-AML1"
```



```
## Define a Boolean vector indicating which samples belong
## to the two selected subtypes.
samples.to.keep <- pheno$Sample.title %in% classes.to.keep
sum(samples.to.keep)
```

```
## [1] 167
```

```
## Extract a subset of expression matrix with only the two selected sets
expr.matrix.kept <- expr.matrix[,samples.to.keep]

## Export the table with the selected samples, in order to open it with TMEV
setwd(dir.output)
file <- paste(sep=" ", "GSE13425_Norm_", subtype.of.interest, "_vs_Other_ge10samples.txt")
write.table(expr.matrix.kept,
            file,
            col.names=NA, quote=F, sep="\t")

## Define a vector with the sample types for the two selected cancer subtype
sample.group <- as.vector(pheno[samples.to.keep, "Sample.title"])
names(sample.group) <- names(expr.matrix[samples.to.keep])
sample.group[sample.group != subtype.of.interest] = "Other"
print(sample.group)
```

```
##      GSM338666      GSM338667      GSM338668      GSM338669      GSM338670
##      "Other"      "Other"      "Other"      "Other"      "Other"
##      GSM338671      GSM338672      GSM338673      GSM338674      GSM338675
##      "Other"      "Other"      "Other"      "Other"      "Other"
##      GSM338676      GSM338677      GSM338678      GSM338679      GSM338680
##      "Other"      "Other"      "Other"      "Other"      "Other"
##      GSM338681      GSM338682      GSM338683      GSM338684      GSM338685
##      "Other"      "Other"      "Other"      "Other"      "Other"
##      GSM338686      GSM338687      GSM338688      GSM338689      GSM338690
##      "Other"      "Other"      "Other"      "Other"      "Other"
##      GSM338691      GSM338692      GSM338693      GSM338694      GSM338695
##      "Other"      "Other"      "Other"      "Other"      "Other"
##      GSM338696      GSM338697      GSM338698      GSM338699      GSM338700
##      "Other"      "Other"      "Other"      "Other"      "Other"
##      GSM338701      GSM338702      GSM338703      GSM338704      GSM338705
##      "Other"      "Other"      "Other"      "Other"      "Other"
##      GSM338706      GSM338707      GSM338708      GSM338709      GSM338710
##      "Other"      "Other"      "Other"      "Other"      "Other"
##      GSM338711      GSM338712      GSM338713      GSM338714      GSM338715
##      "Other"      "Other"      "Other"      "Other"      "Other"
##      GSM338716      GSM338717      GSM338718      GSM338719      GSM338720
##      "Other"      "Other"      "Other"      "Other"      "Other"
##      GSM338721      GSM338722      GSM338723      GSM338724      GSM338725
##      "Other"      "Other"      "Other"      "Other"      "Other"
##      GSM338726      GSM338727      GSM338728      GSM338729      GSM338730
##      "Other"      "Other"      "Other"      "Other"      "Other"
##      GSM338731      GSM338732      GSM338733      GSM338734      GSM338735
##      "Other"      "Other"      "Other"      "Other"      "Other"
##      GSM338736      GSM338737      GSM338738      GSM338739      GSM338740
```

```

##      "Other"      "Other"      "Other"      "Other"      "Other"
##      GSM338741    GSM338742    GSM338743    GSM338744    GSM338746
##      "Other"      "Other"      "Other"      "Other"      "hyperdiploid"
##      GSM338747    GSM338748    GSM338749    GSM338750    GSM338751
##      "hyperdiploid" "hyperdiploid" "hyperdiploid" "hyperdiploid" "hyperdiploid"
##      GSM338752    GSM338753    GSM338754    GSM338755    GSM338756
##      "hyperdiploid" "hyperdiploid" "hyperdiploid" "hyperdiploid" "hyperdiploid"
##      GSM338757    GSM338758    GSM338759    GSM338760    GSM338761
##      "hyperdiploid" "hyperdiploid" "hyperdiploid" "hyperdiploid" "hyperdiploid"
##      GSM338762    GSM338763    GSM338764    GSM338765    GSM338766
##      "hyperdiploid" "hyperdiploid" "hyperdiploid" "hyperdiploid" "hyperdiploid"
##      GSM338767    GSM338768    GSM338769    GSM338770    GSM338771
##      "hyperdiploid" "hyperdiploid" "hyperdiploid" "hyperdiploid" "hyperdiploid"
##      GSM338772    GSM338773    GSM338774    GSM338775    GSM338776
##      "hyperdiploid" "hyperdiploid" "hyperdiploid" "hyperdiploid" "hyperdiploid"
##      GSM338777    GSM338778    GSM338779    GSM338780    GSM338781
##      "hyperdiploid" "hyperdiploid" "hyperdiploid" "hyperdiploid" "hyperdiploid"
##      GSM338782    GSM338783    GSM338784    GSM338785    GSM338786
##      "hyperdiploid" "hyperdiploid" "hyperdiploid" "hyperdiploid" "hyperdiploid"
##      GSM338787    GSM338788    GSM338789    GSM338812    GSM338813
##      "hyperdiploid" "hyperdiploid" "hyperdiploid"      "Other"      "Other"
##      GSM338814    GSM338815    GSM338816    GSM338817    GSM338818
##      "Other"      "Other"      "Other"      "Other"      "Other"
##      GSM338819    GSM338820    GSM338821    GSM338822    GSM338823
##      "Other"      "Other"      "Other"      "Other"      "Other"
##      GSM338824    GSM338825    GSM338826    GSM338827    GSM338828
##      "Other"      "Other"      "Other"      "Other"      "Other"
##      GSM338829    GSM338830    GSM338831    GSM338832    GSM338833
##      "Other"      "Other"      "Other"      "Other"      "Other"
##      GSM338834    GSM338835    GSM338836    GSM338837    GSM338838
##      "Other"      "Other"      "Other"      "Other"      "Other"
##      GSM338839    GSM338840    GSM338841    GSM338842    GSM338843
##      "Other"      "Other"      "Other"      "Other"      "Other"
##      GSM338844    GSM338845    GSM338846    GSM338847    GSM338848
##      "Other"      "Other"      "Other"      "Other"      "Other"
##      GSM338849    GSM338850    GSM338851    GSM338852    GSM338853
##      "Other"      "Other"      "Other"      "Other"      "Other"
##      GSM338854    GSM338855
##      "Other"      "Other"

```

```
table(sample.group)
```

```

## sample.group
## hyperdiploid      Other
##           44         123

```

```

## Export sample groups, which will be used in other practicals
## (e.g. supervised classification)
setwd(dir.output)
file <- paste(sep="",
              "GSE13425_Norm_", subtype.of.interest, "_vs_Other_sample_groups.txt")
write.table(as.data.frame(sample.group),
            file,

```

```
col.names=FALSE,
row.names=TRUE,
quote=F, sep="\t")
```

**Compute Welch t-test for each gene** We will now apply the **Welch test** on **each gene** of the Den Boer dataset, in order to select genes differentially expressed between the subtype of interest (*“hyperdiploid”*) and the other subtypes represented by at least 10 genes.

```
## Run the Welch test on each probesets of the DenBoer expression matrix.
## We will store the result in a table called "DEG" for "Differentially expressed genes", which will la
denboer.deg <- t.test.multi(expr.matrix.kept, sample.group, volcano.plot=FALSE)
```

```
## [1] "Fri Mar 6 15:37:06 2015 - Multiple t-test started"
## [1] "Fri Mar 6 15:37:08 2015 - Multiple t-test done"
```

```
## Inspect the result table
dim(denboer.deg)
```

```
## [1] 22283 17
```

```
names(denboer.deg)
```

```
## [1] "mean.Other" "mean.hyperdiploid" "means.diff"
## [4] "var.est.Other" "var.est.hyperdiploid" "sd.est.Other"
## [7] "sd.est.hyperdiploid" "st.err.diff" "t.obs"
## [10] "df.welch" "P.value" "E.value"
## [13] "sig" "fwer" "q.value"
## [16] "fdr" "rank"
```

```
## Select genes with a stringent threshold on E-value
eval.threshold <- 0.05
significant.probesets <- denboer.deg$E.value <= eval.threshold
table(significant.probesets) ## Count the number of significant probesets
```

```
## significant.probesets
## FALSE TRUE
## 20921 1362
```

**Comparing sample means** We will compare the mean expression value between hyperdiploids and the other selected subtypes, and highlight the significant genes.

```
## Plot the gene-wise means
plot(denboer.deg[, c("mean.Other", "mean.hyperdiploid")], col="darkgray")
grid()

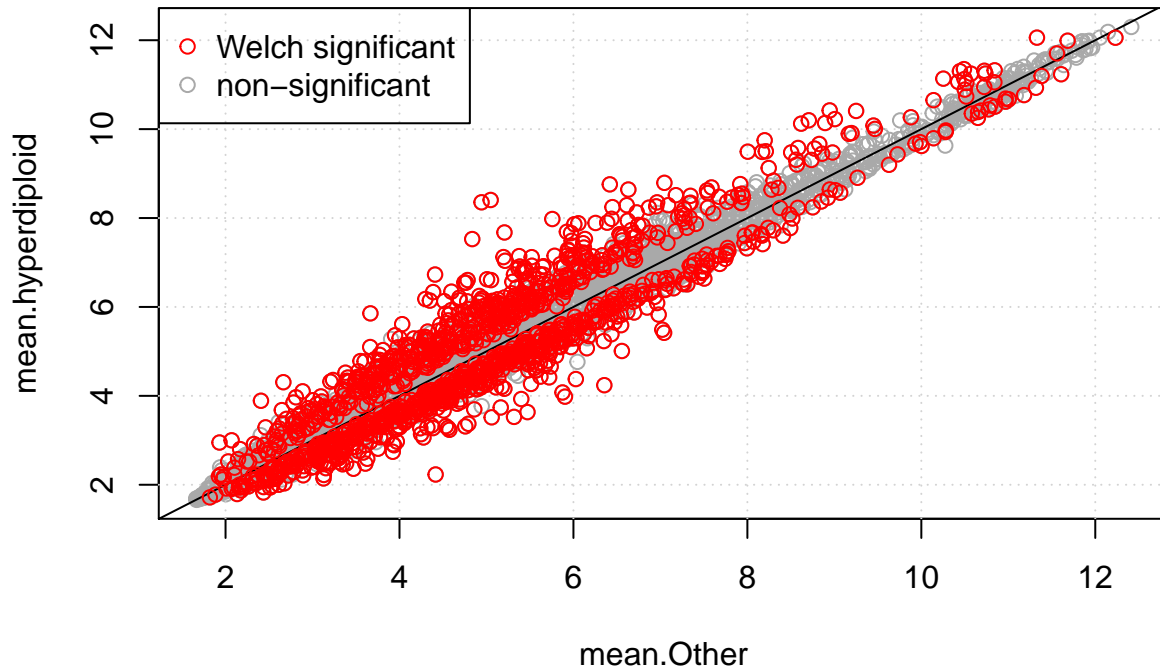
abline(a=0,b=1, col="black") # Draw the diagonal line

## Highlight significant genes
lines(denboer.deg[significant.probesets,
```

```

c("mean.Other", "mean.hyperdiploid"]],
type='p', col="red")
legend("topleft", col=c("red", "darkgray"),
      legend=c("Welch significant", "non-significant"),
      pch=1)

```



### Exercise

- How do you explain that the regions covered by gray (non-significant) and red (significant) probesets overlap on the mean-mean plot ?

[View solution](#) | [Hide solution](#)

**Solution** The significance of a Welch (or a Student) test depends not only on the differences between the means, but also on the estimation of the standard deviation of this difference. In other terms, a same difference (or a same ratio) between two means could be either significant or not, depending on whether the two groups to be compared have a high or low variance.

---

## Comparing the p-values of Welch and Wilcoxon tests

### The apply function

The **apply** function can be used to apply a given function to a matrix or data.frame. This function has three required arguments:

```
args(apply)
```

```
## function (X, MARGIN, FUN, ...)  
## NULL
```

- X the matrix/data.frame
- MARGIN: 1 or 2 depending on whether the function has to be applied on rows or columns, respectively.

### Defining a new function: `return.t()`

In the line below, we define a function called **`return.t()`**, to run the Welch test on a single probeset of the microarray table.

```
## Define a function to return the p-value of a Welch test  
return.t <- function(x,y){ t.test(x[y=="subtype.of.interest"], x[y=="Other"], alternative="two.sided", v
```

- Use this function to compute the p-value of the Welch's t test for all probesets of `expr.matrix`.
- Define a similar function to compute the p-value of Wilcoxon's test to each probeset.
- Draw a plot to compare the p-values returned by the respective tests.

[View solution](#) | [Hide solution](#)

```
## Define a function to return the p-value of a Wilcoxon test  
return.wilcox <- function(x,y){ wilcox.test(x[y=="Other"], x[y=="hyperdiploid"], alternative="two.sided"  
  
## Compute the pvalues and create a data frame with the results of the Welch and Wilcoxon tests  
denboer.deg$welch.pval <- apply(expr.matrix.kept,1,return.t,sample.group)  
denboer.deg$wilcox.pval <- apply(expr.matrix.kept,1,return.wilcox,sample.group)  
  
## Check that all P-values are equal when computed with my  
## custom Welch function, or with the return.t function  
all(denboer.deg$welch.pval == denboer.deg$Pvalue)
```

### Solution

```
## [1] TRUE
```

```
## Select genes passing the p-value threshold, corrected by bonferoni's rule  
pval.threshold <- eval.threshold/nrow(expr.matrix)  
denboer.deg$welch.selected <- denboer.deg$welch.pval < pval.threshold  
denboer.deg$wilcox.selected <- denboer.deg$wilcox.pval < pval.threshold  
  
## Count selected genes for Welch and Wilcoxon tests, resp  
sum(denboer.deg$welch.selected)
```

```
## [1] 1362
```

```
sum(denboer.deg$wilcox.selected)
```

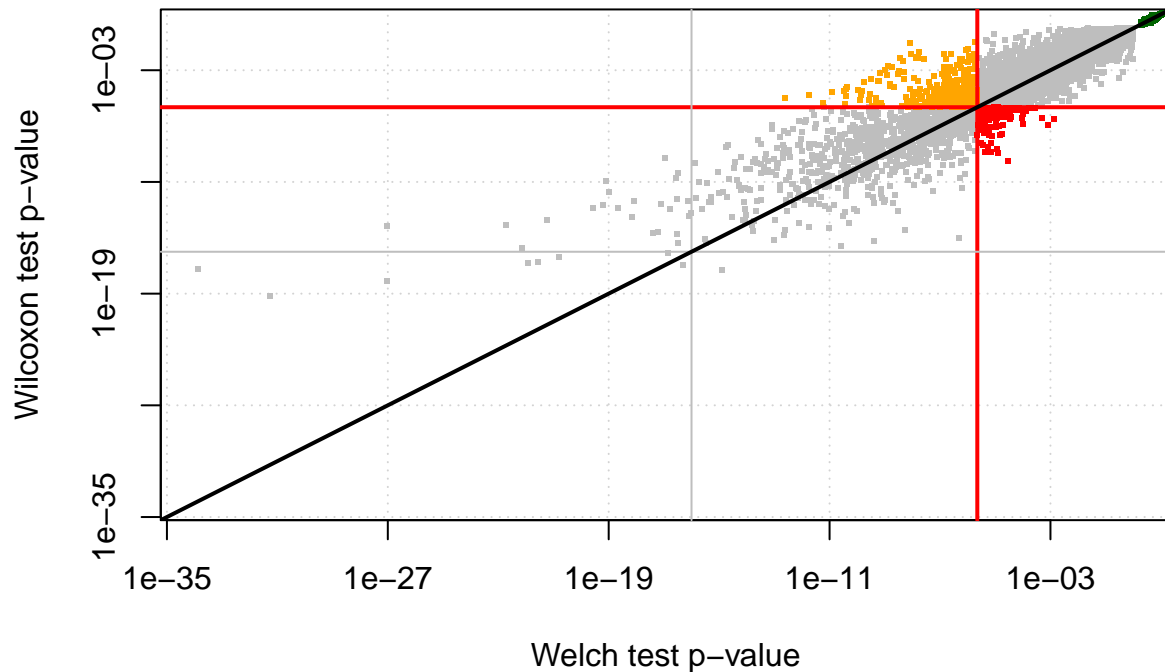
```
## [1] 1169
```

```
## Compute a contingency table counting the number of  
## consistent / different results between Welch and Wilcoxon tests  
table(denboer.deg$welch.pval < pval.threshold,  
       denboer.deg$wilcox.pval < pval.threshold)
```

```
##  
##          FALSE  TRUE  
##  FALSE 20767   154  
##   TRUE   347  1015
```

```
#####  
## Plot the respective p-values returned by the two tests  
pch <- "."  
cex <- 3  
min.pval <- min(denboer.deg$welch.pval, denboer.deg$wilcox.pval)  
plot(denboer.deg$welch.pval,  
     denboer.deg$wilcox.pval,  
     log="xy", panel.first=grid(),  
     xlim=c(min.pval, 1), ylim=c(min.pval, 1),  
     col="gray",  
     xlab="Welch test p-value",  
     ylab="Wilcoxon test p-value",  
     main=paste("DEG selection in Den Boer (2009)",  
                 subtype.of.interest, " vs other"),  
     pch=pch, cex=cex)  
  
## Highlight in green the genes selected by both methods  
welch.and.wilcox <- (denboer.deg$welch.pval < pval.threshold) &  
                    (denboer.deg$wilcox.pval < pval.threshold)  
points(denboer.deg[welch.and.wilcox, ], col="darkgreen", pch=pch, cex=cex)  
  
## Highlight probesets whose selection is affected by the choice of the test  
wilcox.not.welch <- denboer.deg$welch.pval >= pval.threshold & denboer.deg$wilcox.pval < pval.threshold  
points(denboer.deg[wilcox.not.welch,c("welch.pval", "wilcox.pval")], col="red", pch=pch, cex=cex)  
  
welch.not.wilcox <- denboer.deg$welch.pval < pval.threshold & denboer.deg$wilcox.pval >= pval.threshold  
points(denboer.deg[welch.not.wilcox,c("welch.pval", "wilcox.pval")], col="orange", pch=pch, cex=cex)  
  
## Draw lines to display the thresholds on the respective tests  
abline(v=pval.threshold,col="red", lwd=2)  
abline(h=pval.threshold,col="red", lwd=2)  
abline(h=1e-16,col="gray") ## Draw the limit of floating point calculation, which is the limit for p.val  
abline(v=1e-16,col="gray")  
abline(a=0,b=1, col="black", lwd=2)
```

## DEG selection in Den Boer (2009), hyperdiploid vs other



```
## Export the table with the results (Welch + Wilcoxon tests)
setwd(dir.output)
file <- paste(sep="",
              "GSE13425_Norm_", subtype.of.interest, "_vs_Other_sample_Welch.tab")
write.table(format(denboer.deg, digits=4),
            file,
            col.names=NA,
            row.names=TRUE,
            quote=F, sep="\t")
```

---

### Drawing a volcano plot

The volcano plot is a classical representation of differential expression analysis. In this diagram, the **x axis** represents the log ratio and the **y axis** the result of a statistic expressed as  $-\log_{10}(p - \text{value})$ .

### Computing the log ratio

#### Exercise

- Calculate for each gene its average expression level in the “hyperdiploid” and “other” classes.
- Calculate the difference of the mean for each gene (log ratio).

[View solution](#) | [Hide solution](#)

```

rowMeans.other <- apply(expr.matrix.kept[,sample.group== "Other"], 1, mean)
rowMeans.hyperdiploid <- apply(expr.matrix.kept[,sample.group== "hyperdiploid"], 1, mean)
diff <- rowMeans.other - rowMeans.hyperdiploid
range(diff)

```

## Solution

```
## [1] -3.410530  2.184311
```

## Volcano plot

## Exercise

- Draw a volcano plot.
- Use the identify function to find the names of some interesting genes.

[View solution](#) | [Hide solution](#)

```

## Compute the significance, i.e. -log10 of the p-value
t.res <- denboer.deg$welch.pval
mlt <- -log10(t.res)

## Draw the Volcano plot
plot(diff,mlt,pch=1,cex=0.7,
      xlab="Log ratio (base 2)",
      ylab="log10(1/p-value)",
      col="darkgray")
grid()

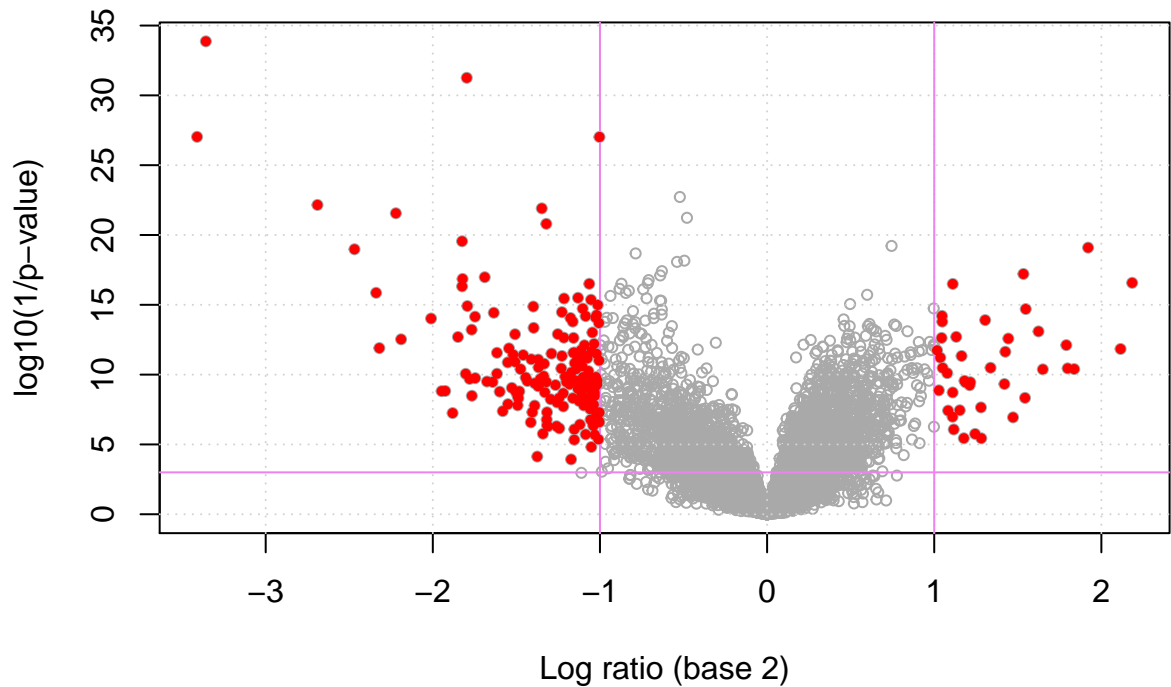
## Draw the selection thresholds
abline(v=c(-1,1), col="violet")
abline(h=3, col="violet")

## Select probesets based on two criteria (fold change + p-value)
retained <- (abs(diff) > 1) & (t.res < 1e-3)

## Color the selected probesets
points(diff[retained],mlt[retained],col="red",cex=0.7,pch=16)

```





Solution

## Significance Analysis of Microarrays (SAM)

What is SAM ?

Probably the most popular method for differential expression analysis of microarray data is “Significance Analysis of Microarrays” (SAM). SAM will compute for each gene a score  $d$  which is close to the  $t$  statistics of the welch’s test. However, it won’t require any assumption about the data distribution. In order to compute the expected distribution of  $d$  under the null hypothesis SAM will perform a set of permutations on the class labels, and compute each time a simulated sets of results for the  $d$  statistics. The observed and simulated results will be used to compute FDR values. Sam is implemented in several R libraries (e.g: *siggene*). Here we will use a more interactive program called [“MultiExperiment Viewer \(MeV\)”](#).

### Installing Mev on Linux system

If you are working on a Linux system, the commands below can be used to download and compule MeV on the Linux console.

### Filtering genes on the basis of the absent/marginal/present (A/M/P) filter

The classical processing pipeline defined by Affymetrix associates a qualitative tag to each probeset, with three possible values:

- absent (A)
- marginal (M)
- present (P)

An **absent** call means that no significant signal was detected with the associated probeset. However, this “absence” might either indicate that the gene is not expressed in this particular sample, or that the gene is undetectable (irrespective of its expression level) due to some technical problem with this specific probeset.

It became a classical practice to filter out the genes called “absent” on an important fraction of the samples in a given series, by implicitly assuming that their recurrent absence reveals a technical problem rather than a biologically relevant effect (repression of the gene).

In the following exercise, we will apply an A/M/P filter to discard the genes declared absent in at least 30% of the genes.

### Exercise

- Select genes giving a signal (“present” call) in at least 30% of the selected samples.

[View solution](#) | [Hide solution](#)

```
## Select a subset of the A/M/P matrix
amp.sub <- amp[,samples.to.keep]
dim(amp)
```

### Solution

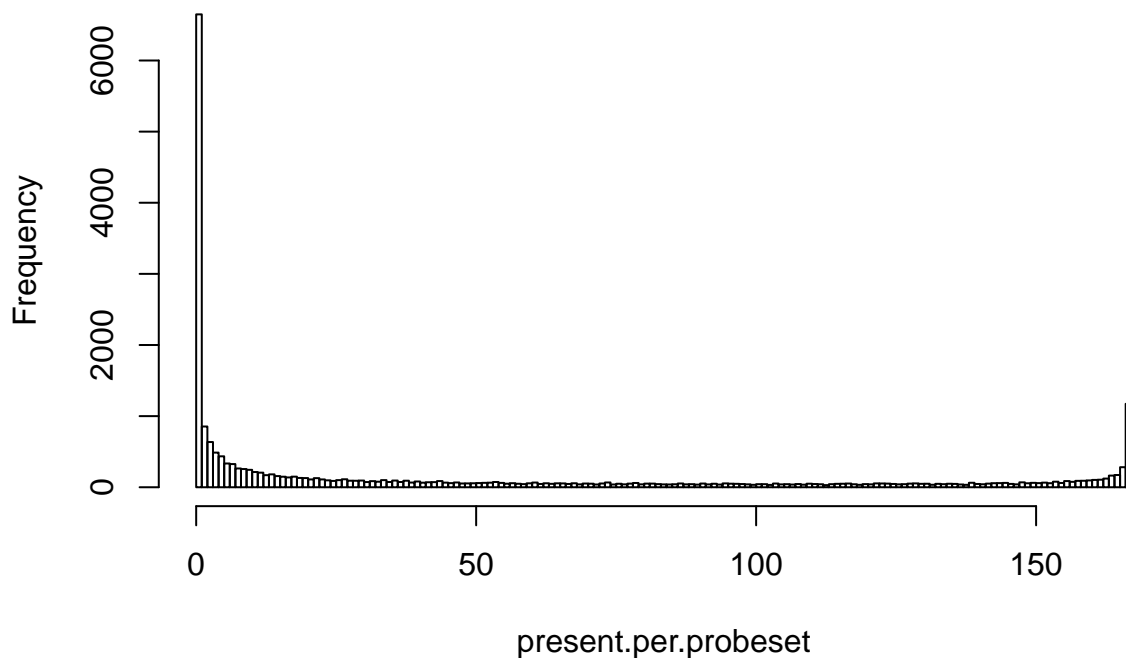
```
## [1] 22283    190
```

```
dim(amp.sub)
```

```
## [1] 22283    167
```

```
## Count the number of "Present" calls per probeset
isPresent <- amp.sub == "P"
present.per.probeset <- rowSums(isPresent)
hist(present.per.probeset, breaks=0:ncol(amp.sub))
```

## Histogram of present.per.probeset



```
## "Present filter": Select probeset declared present in at least 25% of the samples
retained <- rowSums(isPresent) >= 0.25*ncol(expr.matrix.kept)
table(retained) ## Count number of retained and rejected probesets
```

```
## retained
## FALSE TRUE
## 14013 8270
```

```
## Select a subset of the matrix with the retained probesets only
expr.matrix.kept <- expr.matrix.kept[retained, ]

## Check the number of probes (rows) and samples (columns) of the
## selected expression table
print(dim(expr.matrix.kept))
```

```
## [1] 8270 167
```

```
## Export the table with the selected samples, in order to open it with TMEV
setwd(dir.output)
file <- paste(sep=" ", "GSE13425_Norm_", subtype.of.interest, "_vs_Other_present30pc.txt")
write.table(expr.matrix.kept,
            file,
            col.names=NA, quote=F, sep="\t")
```

## Applying SAM algorithm with MeV

### Protocol

- Load the file using “File > Load data > Select file loader Tab delimited”.
  - **Browse** to file “GSE13425\_Norm\_hypermultiploid\_vs\_Other.txt”, click on the **upper-leftmost expression value** and click on the **load** button.
  - Select **Adjust data > Gene/Rows adjustment > median center Genes/Rows**
  - Select **Analysis > Statistics > SAM**
  - Set all samples from GSM338746.CEL.gz to GSM338789.CEL.gz to class B.
  - Set the number of permutations to 500, select **Construct hierarchical clustering** and click " OK“.
  - Accept default parameters for hierarchical clustering.
  - Set the **delta value to 2** and click OK.
  - Select Analysis **results > SAM > Hierarchical trees > All Significant genes**.
  - Select **Display > Set color scale limits** and set **lower limit to -4, midpoint value to 0** and **upper limit to 4**.
  - Set **Display > Set Element Size** to **5x2**.
  - To store the resulting file right click to select the whole gene tree and select **Save cluster**.
-