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## Problem 1

```
%desired s=-1+-2j;
%s^2+2s+5=0;

a=[0 0 -2; 1 0 -5; 0 1 -4];
b=[1;1;0];
P=ctrb(a,b)
rnk=rank(P);
if rnk==length(a)
    disp('Controllable');
else
    disp('Not Controllable');
    rnk
end

%assuming
c=[0 0 1];

[num,den]=ss2tf(a,b,c,0)

syms s
frac=(s+1)/(s^3+4*s^2+5*s+2)
frac1=simplifyFraction(frac)
if frac1==frac
    disp('Minimal form')
else
    disp('non-minimal')
end

num1=[0 0 1];
den1=[1 3 2];

[a1,b1,c1,d1]=tf2ss(num1,den1)

p1=ctrb(a1,b1);
if rank(p1)==length(a1)
    disp('Controllable');
else
    disp('Not Controllable');
end
```

```
de=[-1+2*j -1-2*j];
K=place(a1,b1,de)
```

```
abk=a1-b1*K
bk=b1
ck=c1
dk=d1
```

$P =$

```
      1      0      -2
      1      1      -5
      0      1      -3
```

*Not Controllable*

$rnk =$

```
      2
```

$num =$

```
      0      0      1.0000      1.0000
```

$den =$

```
      1.0000      4.0000      5.0000      2.0000
```

$frac =$

$(s + 1)/(s^3 + 4s^2 + 5s + 2)$

$frac1 =$

$1/(s^2 + 3s + 2)$

*non-minimal*

$a1 =$

```
      -3      -2
      1      0
```

$b1 =$

```
      1
      0
```

$c1 =$

$0 \quad 1$

$d1 =$

$0$

*Controllable*

$K =$

$-1.0000 \quad 3.0000$

$abk =$

$-2.0000 \quad -5.0000$   
 $1.0000 \quad 0$

$bk =$

$1$   
 $0$

$ck =$

$0 \quad 1$

$dk =$

$0$

## Problem 5/CME 8.4a

```
%Uses minimal realization from CME 5.4
%Uses minimal realization from CME 5.4
num1=[0 0 10]
den1=[1 4 68]

%minimal form state-space realization
[a,b,c,d]=tf2ss(num1,den1)

sys=ss(a,b,c,d);
ts=2;
PO=2/100;
```

```
z=sqrt((log(P0))^2/(pi^2+(log(P0))^2));
wn=4/(z*ts);

eq=[1 2*z*wn wn^2];

%desired eigenvalues
ev=roots(eq)
ev1=ev';
ev2=10*ev1

L=place(a',c',ev2)'

K=acker(a,b,ev1)

a1=a-b*K;
b1=b;
c1=c;
d1=d;

sys2=ss(a1,b1,c1,d1);

a2=a1-L*c
b2=b;
c2=c;
d2=d;

sys3=ss(a2,b2,c2,d2);

sys1=ss(a,b,c,d);
subplot(3,1,1),stepplot(sys1);
title('Open loop step response');
subplot(3,1,2),stepplot(sys2);
title('Closed loop step response');
subplot(3,1,3),stepplot(sys3);
title('Closed loop step response with observer');

stepinfo(sys2)
stepinfo(sys3)

%You can see from the stepinfo, the observer improves results further
    than
%just a controller. It reduces overshoot and, more noticeably, the
    times it
%takes to reach steady state

num1 =

    0      0     10

den1 =
```

1      4      68

$a =$

-4      -68  
1      0

$b =$

1  
0

$c =$

0      10

$d =$

0

$ev =$

-2.0000 + 1.6061i  
-2.0000 - 1.6061i

$ev2 =$

-20.0000 -16.0612i -20.0000 +16.0612i

$L =$

44.5963  
3.6000

$K =$

0      -61.4204

$a2 =$

-4.0000 -452.5423  
1.0000 -36.0000

$ans =$

```

    RiseTime: 0.9328
    SettlingTime: 1.4044
    SettlingMin: 1.3796
    SettlingMax: 1.5502
    Overshoot: 2.0000
    Undershoot: 0
    Peak: 1.5502
    PeakTime: 1.9572

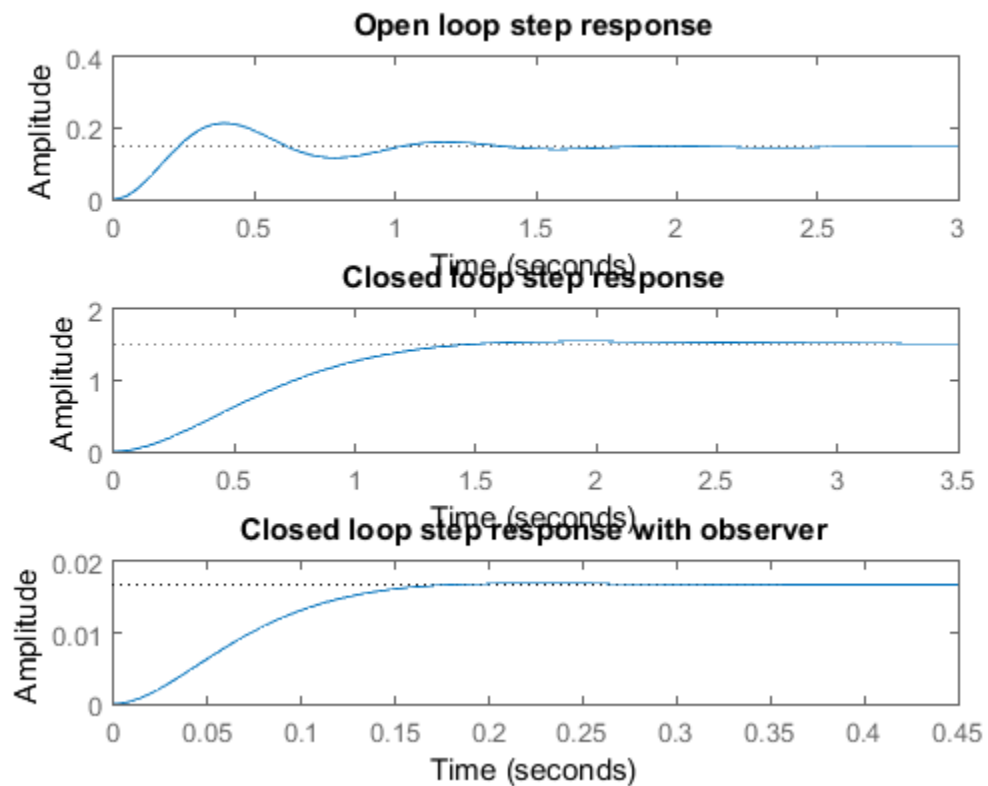
```

ans =

```

    RiseTime: 0.1040
    SettlingTime: 0.1601
    SettlingMin: 0.0152
    SettlingMax: 0.0170
    Overshoot: 1.1311
    Undershoot: 0
    Peak: 0.0170
    PeakTime: 0.2234

```



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