

PLANNING

ECS170 Spring 2018
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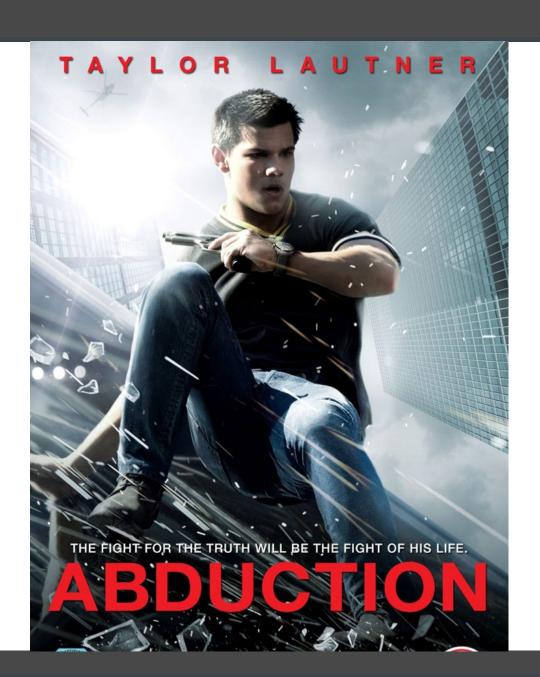
Planning Algorithms

- They search over possible action sequences (i.e. plans).
- Possibility space defined at design-time and searched from at run-time.
- Look at the possible futures created by changing the world.
- Goal-driven (mostly).

Types of Reasoning

Deduction
Induction
Abduction

Abduction!



Automated Planning

Determine sequences of actions or strategies to achieve goals.

Used in:

- Intelligent agents
- Autonomous robots
- Unmanned vehicles
- Games

Attributes of Planners

- Parallel and serial actions.
- Actions with cost
- Stochastic or deterministic effects
- Minimum required actions
- Offline and online
- Single or multiple agents
- World state fully or partially observable
- Goals achieved or maintained
- Discrete or continuous state and actions
- Durative actions

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Classical Planning Problem

- Initial world state observable and known
- Instant and deterministic actions
- Serial actions
- Single Agent

STRIPS

https://www.youtube.com/watch?v=mQ7M-zhiu7U

STRIPS

- Possible world conditions P
- Operators/actions 0. Each has four sets:
 - Condition that must be true to do the action.
 - Conditions that must be false to do the action.
 - Conditions that are true as a result of the action.
 - Conditions that are false as a result of the action.
- Initial state I
- Goal state G

STRIPS

```
STRIPS(O, s, G)
p = \text{empty plan}
loop...
        if s satisfies G then return p
        a = [an applicable action in <math>O,
                 relevant for G]
        if a = \text{null}, then return failure
        p' = STRIPS(O, s, precond(a))
        if p' = failure, then return failure
        s = apply p' to s
        s = apply a to s
        p = p + p' + a
```

Ghallab, Malik, Dana Nau, and Paolo Traverso. Automated planning: theory & practice. Access Online via Elsevier, 2004.

Simple STRIPS Encoding

Operators

Preconditions

Add List

Delete List

Initial State

Goal State

GrabSpellBook

floor(spell_book)

+inventory(spell_book)

-floor(spell_book)

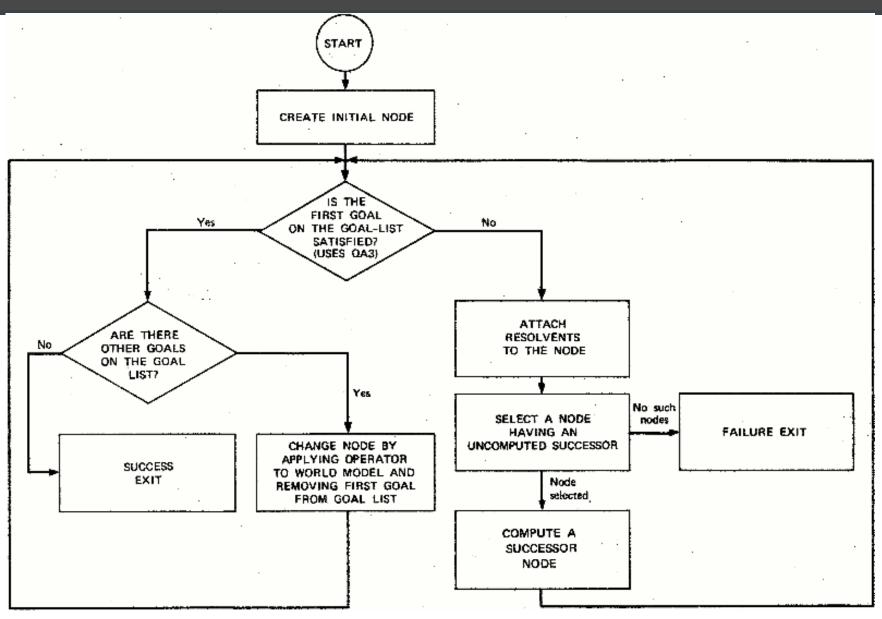
Initial State

floor(spell_book)

Goal State

inventory(spell_book)

The Original STRIPS Algorithm



STRIPS Vagaries Explained

Resolvents are metric of how relevant the next possible actions are.

Compute a successor node: adds a node to the internal A*.

That's right: A*!

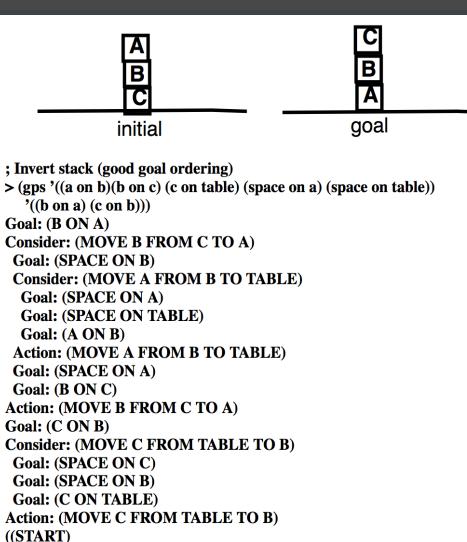
Both developed at SRI AI center.

STRIPS uses it to expand plans based on: g(n)+h(n) cost evaluation.

What could you use as the heuristic?

In a sense, this gives forward and backward search to the goal.

STRIPS - Block World



(EXECUTING (MOVE A FROM B TO TABLE))

(EXECUTING (MOVE C FROM TABLE TO B)))

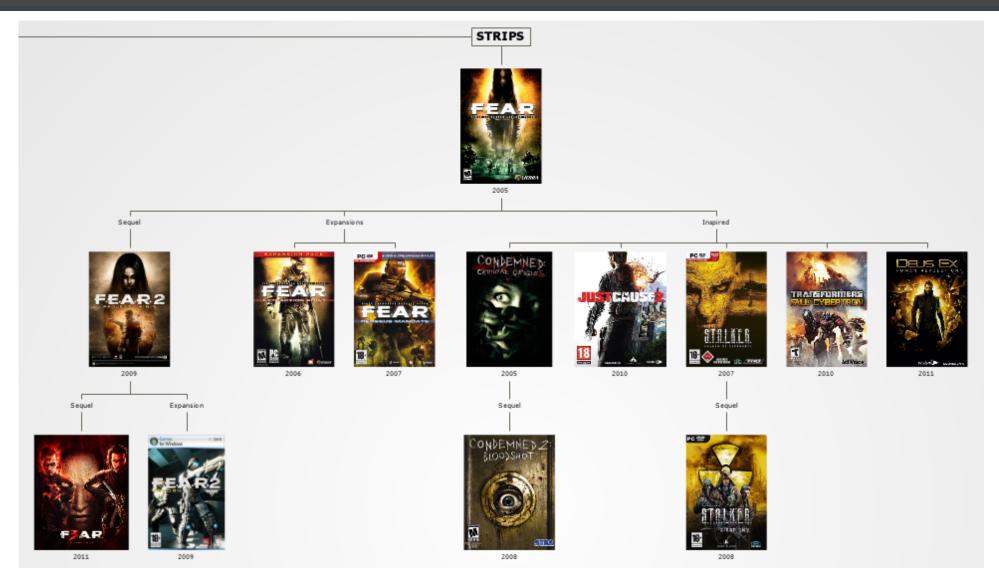
(EXECUTING (MOVE B FROM C TO A))

Ghallab, Malik, Dana Nau, and Paolo Traverso. Automated planning: theory & practice. Access Online via Elsevier, 2004.

STRIPS - Monkey

```
Initial state: At(A), Level(low), BoxAt(C), BananasAt(B)
Goal state: Have(Bananas)
Actions:
        // move from X to Y
                                                                    // move monkey and box from X to Y
        Move(X, Y)
                                                                    MoveBox(X, Y)_{\_}
        Preconditions: At(X), Level(low)
                                                                    Preconditions: At(X), BoxAt(X), Level(low)
                                                                    Postconditions: BoxAt(Y), not BoxAt(X), At(Y), not At(X)
        Postconditions: not At(X), At(Y)
        // climb up on the box
                                                                    // take the bananas
        ClimbUp(Location)
                                                                    TakeBananas(Location)
        Preconditions: At(Location), BoxAt(Location), Level(low)
                                                                    Preconditions: At(Location), BananasAt(Location),
        Postconditions: Level(high), not Level(low)
                                                                                         Level(high)
                                                                    Postconditions: Have(bananas)
        // climb down from the box
        ClimbDown(Location)
        Preconditions: At(Location), BoxAt(Location), Level(high)
        Postconditions: Level(low), not Level(high)
```

STRIPS in Games



http://aigamedev.com/open/review/planning-in-games/

Implementations of STRIPS

- http://www.primaryobjects.com/2015/11/06/artificialintelligence-planning-with-strips-a-gentle-introduction/
- https://stripsfiddle.herokuapp.com/

In this example, each element in the state vector takes on Boolean values

```
Recipe: true if character has a recipe
Pizza Phone #: true if character has a phone number for ordering pizza
Food: true if something to eat is in possession
Ingredients: true if the ingredients to make the recipe are in possession
Silverware: true if the silverware is in possession
Hungry: true if the character is hungry
Requires Silverware: true if the food requires silverware to eat
```

Look up recipe (lur)

P: {N, _, _, _, _, _, _} E: {Y, _, _, _, _, _, _, _}

Look up phone number (luph)

P: {_, N, _, _, _, _}

E: { _, Y, _, _, _, _, _}

Shop for ingredients (sfi)

P: {Y, _, _, N, _, _, _}

E: {_, _, _, Y, _, _, _}

Call Pizza (cp)

P: { _, Y, N, _, _, _, _}

E: {_, _, Y, _, _, _, N}

Cook (c)

P: {Y, _, N, Y, _, _, _}

E: {_, _, Y, N, _, Y}

Get silverware (gs)

P: { _, _, _, N, _, _}

E: {_, _, _, _, Y, _, _}

Eat with silverware (ews)

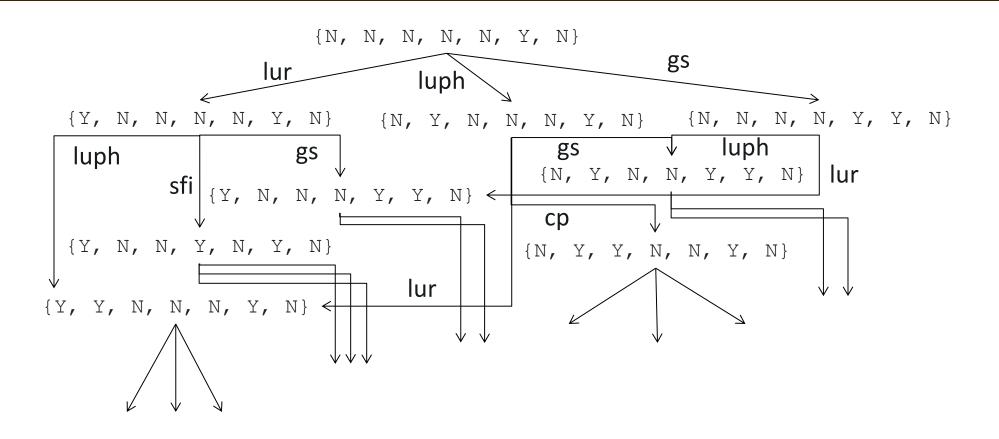
P: { , , Y, , Y, Y}

E: {_, _, N, _, _, N, _}

Eat with hands (ewh)

P: { , , Y, , N, Y, N}

E: { _ , _ , N, _ , _ , N, _ }



```
Initial State: { N, N, N, N, N, Y, N}
Goal State: { _, _, _, _, _, N, _}
```

Heuristic: number of state elements different from goal

```
Open list: [{N, N, N, N, Y, N} cost 1]
```

Valid actions: lur, luph, gs

Open list:

```
{Y, N, N, N, N, Y, N} lur cost: 2,
{N, Y, N, N, N, Y, N} luph cost: 2,
{N, N, N, N, Y, N} gs cost: 2
```

```
Closed list: [{N, N, N, N, N, Y, N} cost: 1]
```

```
Look up recipe (lur)
                                 Cook (c)
P: {N, _, _, _, _, _}
                                 P: {Y, _, N, Y, _, _, _}
                                 E: { , , Y, N, , , Y}
E: {Y, , , , , }
Look up phone # (luph)
                                 Get silverware (gs)
P: { , N, , , , , }
                                 P: { , , , , N, , }
                                 E: {_, _, _, _, Y, _, _}
E: {_, Y, _, _, _, _, _}
Shop for ingredients (sfi)
                                  Eat w/silverware (ews)
P: {Y, , , N, , , }
                                 P: { , , Y, , Y, Y, Y}
E: {_, _, _, Y, _, _, _}
                                 E: {_, _, N, _, _, N, _}
Call Pizza (cp)
                                 Eat w/ hands (ewh)
P: {_, Y, N, _, _, _, _}
                                 P: {_, _, Y, _, N, Y, N}
E: {_, _, Y, _, _, _, N}
                                  E: { , , N, , , N, }
```

```
{Y, N, N, N, N, Y, N} lur cost: 2
Valid actions: luph, sfi, gs
Open list:
{N, Y, N, N, N, Y, N} luph cost: 2,
{N, N, N, N, Y, Y, N} gs cost: 2
{Y, Y, N, N, N, Y, N} luph cost: 3
{Y, N, N, Y, N, Y, N} sfi cost: 3
{Y, N, N, N, Y, Y, N} gs cost: 3
Closed list:
{N, N, N, N, N, Y, N} cost: 1
```

{Y, N, N, N, Y, N} lur cost: 2

Look up recipe (lur) Cook (c) P: {N, _, _, _, _, _} P: {Y, _, N, Y, _, _, _} E: {Y, , , , , } E: { , , Y, N, , , Y} Look up phone # (luph) Get silverware (gs) P: { , N, , , , , } P: { , , , , N, , } E: {_, Y, _, _, _, _, _} E: {_, _, _, _, Y, _, _} Shop for ingredients (sfi) Eat w/silverware (ews) P: {Y, , , N, , , } P: { , , Y, , Y, Y, Y} E: {_, _, _, Y, _, _, _} E: {_, _, N, _, _, N, _} Call Pizza (cp) Eat w/ hands (ewh) P: {_, Y, N, _, _, _, _} P: {_, _, Y, _, N, Y, N} E: {_, _, Y, _, _, _, N} E: {_, _, N, _, _, N, _}

```
{N, Y, N, N, N, Y, N} luph cost: 2, Valid actions: lur (duplicate state), cp, gs
Open list:
```

```
{N, N, N, N, Y, Y, N} gs cost: 2
{Y, Y, N, N, N, Y, N} luph cost: 3
{Y, N, N, Y, N, Y, N} sfi cost: 3
{Y, N, N, N, Y, Y, N} gs cost: 3
{N, Y, Y, N, N, Y, N} cp cost: 3
{N, Y, N, N, Y, Y, N} gs cost: 3
```

Closed list:

```
{N, N, N, N, N, Y, N} cost: 1
{Y, N, N, N, N, Y, N} lur cost: 2
{N, Y, N, N, N, Y, N} luph cost: 2
```

```
Look up recipe (lur)
                                 Cook (c)
P: {N, _, _, _, _, _}
                                 P: {Y, _, N, Y, _, _, _}
E: {Y, , , , , }
                                 E: { , , Y, N, , , Y}
Look up phone # (luph)
                                 Get silverware (gs)
P: { , N, , , , , }
                                  P: { , , , , N, , }
E: {_, Y, _, _, _, _, _}
                                 E: {_, _, _, _, Y, _, _}
Shop for ingredients (sfi)
                                  Eat w/silverware (ews)
P: {Y, , , N, , , }
                                 P: { , , Y, , Y, Y, Y}
E: {_, _, _, Y, _, _, _}
                                 E: {_, _, N, _, _, N, _}
Call Pizza (cp)
                                  Eat w/ hands (ewh)
P: {_, Y, N, _, _, _, _}
                                 P: {_, _, Y, _, N, Y, N}
E: {_, _, Y, _, _, _, N}
                                  E: { , , N, , , N, }
```

```
{N, N, N, N, Y, Y, N} gs cost: 2
Valid actions: lur (duplicate), luph (duplicate)
Open list:
```

```
{Y, Y, N, N, N, Y, N} luph cost: 3
{Y, N, N, Y, N, Y, N} sfi cost: 3
{Y, N, N, N, Y, Y, N} gs cost: 3
{N, Y, Y, N, N, Y, N} cp cost: 3
{N, Y, N, N, Y, Y, N} gs cost: 3
```

Closed list:

```
{N, N, N, N, N, Y, N} cost: 1
{Y, N, N, N, N, Y, N} lur cost: 2
{N, Y, N, N, N, Y, N} luph cost: 2
{N, N, N, N, Y, Y, N} gs cost: 2
```

Look up recipe (lur) Cook (c) P: {N, _, _, _, _, _} P: {Y, _, N, Y, _, _, _} E: {Y, , , , , } E: { , , Y, N, , , Y} Look up phone # (luph) Get silverware (gs) P: { , N, , , , , } P: { , , , , N, , } E: {_, Y, _, _, _, _, _} E: {_, _, _, _, Y, _, _} Shop for ingredients (sfi) Eat w/silverware (ews) P: {Y, , , N, , , } P: { , , Y, , Y, Y, Y} E: {_, _, _, Y, _, _, _} E: {_, _, N, _, _, N, _} Call Pizza (cp) Eat w/hands (ewh) P: {_, Y, N, _, _, _, _} P: {_, _, Y, _, N, Y, N} E: {_, _, Y, _, _, _, N} E: { , , N, , , N, }

```
{N, Y, N, N, N, Y, N} luph cost: 2, Valid actions: lur (duplicate state), cp, gs
Open list:
```

```
{N, N, N, N, Y, Y, N} gs cost: 2
{Y, Y, N, N, N, Y, N} luph cost: 3
{Y, N, N, Y, N, Y, N} sfi cost: 3
{Y, N, N, N, Y, Y, N} gs cost: 3
{N, Y, Y, N, N, Y, N} cp cost: 3
{N, Y, N, N, Y, Y, N} gs cost: 3
```

Closed list:

```
{N, N, N, N, N, Y, N} cost: 1
{Y, N, N, N, N, Y, N} lur cost: 2
{N, Y, N, N, N, Y, N} luph cost: 2
```

Look up recipe (lur) Cook (c) P: {N, _, _, _, _, _} P: {Y, _, N, Y, _, _, _} E: {Y, , , , , } E: { , , Y, N, , , Y} Look up phone # (luph) Get silverware (gs) P: { , N, , , , , } P: { , , , , N, , } E: {_, Y, _, _, _, _, _} E: {_, _, _, _, Y, _, _} Shop for ingredients (sfi) Eat w/silverware (ews) P: {Y, , , N, , , } P: { , , Y, , Y, Y, Y} E: {_, _, _, Y, _, _, _} E: {_, _, N, _, _, N, _} Call Pizza (cp) Eat w/ hands (ewh) P: {_, Y, N, _, _, _, _} P: {_, _, Y, _, N, Y, N} E: {_, _, Y, _, _, _, N} E: { , , N, , , N, }

```
{N, N, N, N, Y, Y, N} gs cost: 2
Valid actions: lur (duplicate), luph (duplicate)
Open list:
```

```
{Y, Y, N, N, N, Y, N} luph cost: 3
{Y, N, N, Y, N, Y, N} sfi cost: 3
{Y, N, N, N, Y, Y, N} gs cost: 3
{N, Y, Y, N, N, Y, N} cp cost: 3
{N, Y, N, N, Y, Y, N} gs cost: 3
```

Closed list:

```
{N, N, N, N, N, Y, N} cost: 1
{Y, N, N, N, N, Y, N} lur cost: 2
{N, Y, N, N, N, Y, N} luph cost: 2
{N, N, N, N, Y, Y, N} gs cost: 2
```

Look up recipe (lur) Cook (c) P: {N, _, _, _, _, _} P: {Y, _, N, Y, _, _, _} E: {Y, , , , , } E: { , , Y, N, , , Y} Look up phone # (luph) Get silverware (gs) P: { , N, , , , , } P: { , , , , N, , } E: {_, Y, _, _, _, _, _} E: {_, _, _, _, Y, _, _} Shop for ingredients (sfi) Eat w/silverware (ews) P: {Y, , , N, , , } P: { , , Y, , Y, Y, Y} E: {_, _, _, Y, _, _, _} E: {_, _, N, _, _, N, _} Call Pizza (cp) Eat w/hands (ewh) P: {_, Y, N, _, _, _, _} P: {_, _, Y, _, N, Y, N} E: {_, _, Y, _, _, _, N} E: { , , N, , , N, }

DIY: 6 Steps Left

```
{Y, Y, N, N, N, Y, N} luph cost: 3
Valid actions: sfi, cp, gs
Open list:
{Y, N, N, Y, N, Y, N} sfi cost: 3
{Y, N, N, N, Y, Y, N} gs cost: 3
{N, Y, Y, N, N, Y, N} cp cost: 3
{N, Y, N, N, Y, Y, N} gs cost: 3
{Y, Y, N, N, Y, Y, N} gs cost: 3
{Y, Y, N, N, Y, N} gs cost: 4
{Y, Y, N, Y, N, Y, N} sfi cost: 4
{Y, Y, N, N, Y, N} gs cost: 4
```

Closed list:

```
{N, N, N, N, N, Y, N} cost: 1
{Y, N, N, N, N, Y, N} lur cost: 2
{N, Y, N, N, N, Y, N} luph cost: 2
{N, N, N, N, Y, Y, N} gs cost: 2
{Y, Y, N, N, N, Y, N} luph cost: 3
```

```
Look up recipe (lur)
                                 Cook (c)
P: {N, _, _, _, _, _}
                                  P: {Y, _, N, Y, _, _, _}
E: {Y, , , , , , }
                                  E: { , , Y, N, , , Y}
Look up phone # (luph)
                                  Get silverware (gs)
P: { , N, , , , , }
                                  P: { , , , , N, , }
E: {_, Y, _, _, _, _, _}
                                  E: {_, _, _, _, Y, _, _}
Shop for ingredients (sfi)
                                  Eat w/silverware (ews)
P: {Y, , , N, , , }
                                  P: { , , Y, , Y, Y, Y}
E: {_, _, _, Y, _, _, _}
                                  E: {_, _, N, _, _, N, _}
                                  Eat w/ hands (ewh)
Call Pizza (cp)
P: {_, Y, N, _, _, _, _}
                                  P: {_, _, Y, _, N, Y, N}
E: {_, _, Y, _, _, _, N}
                                  E: {_, _, N, _, _, N, _}
```

```
Valid actions: luph (duplicate), c, gs
Open list:
{N, Y, Y, N, N, Y, N} cp cost: 3 {N, N, N, N, Y, Y, N} gs cost: 2
{Y, Y, N, Y, N, Y, N} sfi cost: 4 {Y, N, N, Y, N, Y, N} sfi cost: 3
\{Y, Y, Y, N, N, Y, N\} cp cost: 4
{Y, Y, N, N, Y, Y, N} gs cost: 4
{Y, N, Y, Y, N, Y, Y} c cost: 4
{Y, N, N, Y, Y, Y, N} gs cost: 4
```

{Y, N, N, Y, N, Y, N} sfi cost: 3

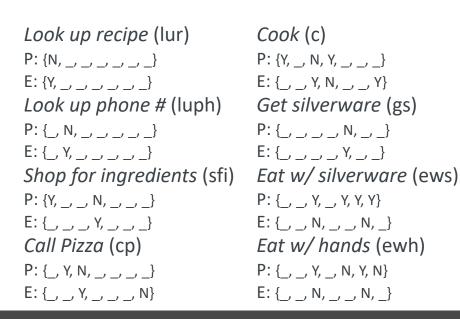
Closed list:

```
{N, N, N, N, N, Y, N} cost: 1
                                 {Y, N, N, N, N, Y, N} lur cost: 2
{Y, N, N, N, Y, Y, N} gs cost: 3 {N, Y, N, N, N, Y, N} luph cost: 2
{N, Y, N, N, Y, Y, N} gs cost: 3 {Y, Y, N, N, N, Y, N} luph cost: 3
```

```
Look up recipe (lur)
                                 Cook (c)
P: {N, _, _, _, _, _, _}
                                 P: {Y, _, N, Y, _, _, _}
E: {Y, , , , , }
                                 E: { , , Y, N, , , Y}
Look up phone # (luph)
                                 Get silverware (gs)
P: { , N, , , , , }
                                 P: { , , , , N, , }
E: {_, Y, _, _, _, _, _}
                                 E: {_, _, _, _, Y, _, _}
Shop for ingredients (sfi)
                                 Eat w/silverware (ews)
P: {Y, , , N, , , }
                                 P: { , , Y, , Y, Y, Y}
E: {_, _, _, Y, _, _, _}
                                 E: {_, _, N, _, _, N, _}
Call Pizza (cp)
                                 Eat w/ hands (ewh)
P: {_, Y, N, _, _, _, _}
                                 P: {_, _, Y, _, N, Y, N}
E: {_, _, Y, _, _, _, N}
                                 E: { , , N, , , N, }
```

```
{Y, N, N, Y, Y, N} gs cost: 3 Closed list:
Valid actions: luph (dup), sfi (dup) { N, N, N, N, N, Y, N} cost: 1
Open list:
\{N, Y, N, N, Y, Y, N\} gs cost: 3 \{N, N, N, N, Y, Y, N\} gs cost: 2
{Y, Y, Y, N, N, Y, N} cp cost: 4 {Y, N, N, Y, N, Y, N} sfi cost: 3
{Y, Y, N, N, Y, Y, N} gs cost: 4 {Y, N, N, N, Y, Y, N} gs cost: 3
{Y, N, Y, Y, N, Y, Y} c cost: 4
{Y, N, N, Y, Y, Y, N} gs cost: 4
```

```
{Y, N, N, N, N, Y, N} lur cost: 2
{N, Y, Y, N, N, Y, N} cp cost: 3 {N, Y, N, N, N, Y, N} luph cost: 2
{Y, Y, N, Y, N, Y, N} sfi cost: 4 {Y, Y, N, N, N, Y, N} luph cost: 3
```



```
{N, Y, Y, N, N, Y, N} cp cost: 3 Closed list:
Valid actions: lur (dup), gs, ewh {N, N, N, N, N, Y, N} cost: 1
Open list:
                                        {Y, N, N, N, N, Y, N} lur cost: 2
{N, Y, N, N, Y, Y, N} gs cost: 3 {N, Y, N, N, N, Y, N} luph cost: 2
{Y, Y, N, Y, N, Y, N} sfi cost: 4{N, N, N, N, Y, Y, N} gs cost: 2
{Y, Y, Y, N, N, Y, N} cp cost: 4 {Y, Y, N, N, N, Y, N} luph cost: 3
{Y, Y, N, N, Y, Y, N} gs cost: 4 {Y, N, N, Y, N, Y, N} sfi cost: 3
{Y, N, Y, Y, N, Y, Y} c cost: 4 {Y, N, N, N, Y, Y, N} gs cost: 3
{Y, N, N, Y, Y, Y, N} gs cost: 4 {N, Y, Y, N, N, Y, N} cp cost: 3
                                                             Look up recipe (lur)
                                                                                  Cook (c)
\{N, Y, Y, N, Y, Y, N\} gs cost: 4
                                                             P: {N, _, _, _, _, _}
{N, Y, N, N, N, N} ewh cost: 3
                                                             E: {Y, , , , , , }
                                                                                  E: { , , Y, N, , , Y}
                                                             Look up phone # (luph)
                                                                                  Get silverware (gs)
                                                             P: { , N, , , , , }
                                                                                  P: { , , , , N, , }
                                                             E: {_, Y, _, _, _, _, _}
                                                                                  E: {_, _, _, _, Y, _, _}
                                                                                  Eat w/silverware (ews)
                                                             Shop for ingredients (sfi)
                                                             P: {Y, , , N, , , }
                                                                                  P: { , , Y, , Y, Y, Y}
                                                             E: {_, _, _, Y, _, _, _}
                                                                                  E: {_, _, N, _, _, N, _}
                                                             Call Pizza (cp)
                                                                                  Eat w/ hands (ewh)
                                                             P: {_, Y, N, _, _, _, _}
                                                                                  P: {_, _, Y, _, N, Y, N}
                                                             E: {_, _, Y, _, _, _, N}
                                                                                  E: {_, _, N, _, _, N, _}
```

```
Closed list:
\{N, Y, N, N, Y, Y, N\} gs cost: 3
                                       {N, N, N, N, N, Y, N} cost: 1
Valid actions: lur (dup), cp (dup)
                                       {Y, N, N, N, N, Y, N} lur cost: 2
Open list:
                                       {N, Y, N, N, N, Y, N} luph cost: 2
{Y, Y, N, Y, N, Y, N} sfi cost: 4
                                       \{N, N, N, N, Y, Y, N\} gs cost: 2
\{Y, Y, Y, N, N, Y, N\} cp cost: 4
                                       {Y, Y, N, N, N, Y, N} luph cost: 3
                                       {Y, N, N, Y, N, Y, N} sfi cost: 3
{Y, Y, N, N, Y, Y, N} gs cost: 4
                                       \{Y, N, N, N, Y, Y, N\} gs cost: 3
{Y, N, Y, Y, N, Y, Y} c cost: 4
                                       \{N, Y, Y, N, N, Y, N\} cp cost: 3
{Y, N, N, Y, Y, Y, N} gs cost: 4
                                       \{N, Y, N, N, Y, Y, N\} gs cost: 3
\{N, Y, Y, N, Y, Y, N\} gs cost: 4
{N, Y, N, N, N, N, N} ewh cost: 3
```

Look up recipe (lur) Cook (c) P: {N, _, _, _, _, _, _} P: {Y, _, N, Y, _, _, _} E: {Y, , , , , } E: { , , Y, N, , , Y} Look up phone # (luph) Get silverware (gs) P: { , N, , , , , } P: { , , , , N, , } E: {_, Y, _, _, _, _, _} E: {_, _, _, _, Y, _, _} Shop for ingredients (sfi) Eat w/silverware (ews) P: {Y, , , N, , , } P: { , , Y, , Y, Y, Y} E: {_, _, _, Y, _, _, _} E: {_, _, N, _, _, N, _} Eat w/ hands (ewh) Call Pizza (cp) P: {_, _, Y, _, N, Y, N} P: {_, Y, N, _, _, _, _} E: {_, _, Y, _, _, _, N} E: {_, _, N, _, _, N, _}

```
{N, Y, N, N, N, N, N} ewh cost: 3 Popped Goal!
```

Closed list:

```
{N, N, N, N, N, Y, N} cost: 1
{Y, N, N, N, N, Y, N} lur cost: 2
{N, Y, N, N, N, Y, N} luph cost: 2
{N, N, N, N, Y, Y, N} gs cost: 2
{Y, Y, N, N, N, Y, N} luph cost: 3
{Y, N, N, Y, N, Y, N} sfi cost: 3
{Y, N, N, N, Y, N, Y, N} gs cost: 3
{N, Y, Y, N, N, Y, N} cp cost: 3
{N, Y, N, N, Y, Y, N} gs cost: 3
```

Plan: look up phone number, call pizza, eat with hands

Look up recipe (lur)	Cook (c)
P: {N, _, _, _, _, _}	P: {Y, _, N, Y, _, _, _}
E: {Y, _, _, _, _, _}	E: {_, _, Y, N, _, _, Y}
Look up phone # (luph)	Get silverware (gs)
P: {_, N, _, _, _, _, _}	P: {_, _, _, _, N, _, _}
E: {_, Y, _, _, _, _}	E: {_, _, _, _, Y, _, _}
Shop for ingredients (sfi)	Eat w/silverware (ews)
P: {Y, _, _, N, _, _, _}	P: {_, _, Y, _, Y, Y, Y}
E: {_, _, _, Y, _, _, _}	E: {_, _, N, _, _, N, _}
Call Pizza (cp)	Eat w/ hands (ewh)
P: {_, Y, N, _, _, _, _}	P: {_, _, Y, _, N, Y, N}
E: {_, _, Y, _, _, N}	E: {_, _, N, _, _, N, _}