

Naïve Bayes Hypothesis

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Example

f_1	f_2	f_3	f_4	y
0	1	1	0	1
0	0	1	1	1
1	0	1	0	1
0	0	1	1	1
0	0	0	0	1
1	0	0	1	0
1	1	0	1	0
1	0	0	0	0
1	1	0	1	0
1	0	1	1	0

$R_1(1,1) = 1/5$: fraction of all positive examples that have feature 1 on

$R_1(0,1) = 4/5$: fraction of all positive examples that have feature 1 off

Example (Cont.)

f_1	f_2	f_3	f_4	y
0	1	1	0	1
0	0	1	1	1
1	0	1	0	1
0	0	1	1	1
0	0	0	0	1
1	0	0	1	0
1	1	0	1	0
1	0	0	0	0
1	1	0	1	0
1	0	1	1	0

$R_1(1,1) = 1/5$: fraction of all positive examples that have feature 1 on

$R_1(0,1) = 4/5$: fraction of all positive examples that have feature 1 off

$R_1(1,0) = 5/5$: fraction of all negative examples that have feature 1 on

$R_1(0,0) = 0/5$: fraction of all negative examples that have feature 1 off

Example (cont.)

f_1	f_2	f_3	f_4	y
0	1	1	0	1
0	0	1	1	1
1	0	1	0	1
0	0	1	1	1
0	0	0	0	1
1	0	0	1	0
1	1	0	1	0
1	0	0	0	0
1	1	0	1	0
1	0	1	1	0

$$R_1(1,1) = 1/5 \quad R_1(0,1) = 4/5$$

$$R_1(1,0) = 5/5 \quad R_1(0,0) = 0/5$$

$$R_2(1,1) = 1/5 \quad R_2(0,1) = 4/5$$

$$R_2(1,0) = 2/5 \quad R_2(0,0) = 3/5$$

$$R_3(1,1) = 4/5 \quad R_3(0,1) = 1/5$$

$$R_3(1,0) = 1/5 \quad R_3(0,0) = 4/5$$

$$R_4(1,1) = 2/5 \quad R_4(0,1) = 3/5$$

$$R_4(1,0) = 4/5 \quad R_4(0,0) = 1/5$$

Prediction

- These R values actually represent the hypothesis and is used to classify the new input.

$R_1(1,1) = 1/5$	$R_1(0,1) = 4/5$
$R_1(1,0) = 5/5$	$R_1(0,0) = 0/5$
$R_2(1,1) = 1/5$	$R_2(0,1) = 4/5$
$R_2(1,0) = 2/5$	$R_2(0,0) = 3/5$
$R_3(1,1) = 4/5$	$R_3(0,1) = 1/5$
$R_3(1,0) = 1/5$	$R_3(0,0) = 4/5$
$R_4(1,1) = 2/5$	$R_4(0,1) = 3/5$
$R_4(1,0) = 4/5$	$R_4(0,0) = 1/5$

New $x = \langle 0,0,1,1 \rangle$

$$S(1) = R_1(0,1) \times R_2(0,1) \times R_3(1,1) \times R_4(1,1) = .205$$

$$S(0) = R_1(0,0) \times R_2(0,0) \times R_3(1,0) \times R_4(1,0) = 0$$

$S(1) > S(0)$, so predict class 1