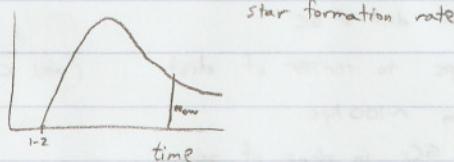


Galaxies

in general ~10 billion years old

to study galaxy evolution need large look back time

SFR



can't observe galaxies forming

3 Methods to study

1. Fossil - Milky Way + Local galaxies

2. Galaxy Evolution - look further back (limited by telescope + techniques)

3. Cosmology - environment of galaxies

Brief History

Milky Way - naked eye

Galileo: MW - lots of stars

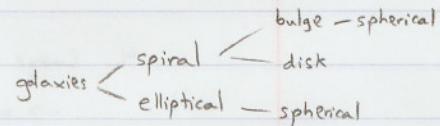
Immanuel Kant: mid 1700's MW - gravitational bound rotating disk
spiral nebulae - island universes, different orientations

Messier: late 1700's "not" comets catalog 109 (northern hemisphere)

Herschel's: William, Carolyn, John 5000 nebulae (northern + southern)
pointlike objects in nebulae, planetary nebulae

Dreyer: 1888 New General Catalog (NGC), Index Catalog (IC) 1895
(7840) (5086)

Third Earl of Rosse (William Parsons): 1845 - 72" telescope
saw star clusters in spiral galaxies



1785 - stellar gauging - counting stars
(Herschel)
thought we were near center - obscuration by dust



galaxy is flat
5:1

Kapteyn 200 locations on sky, multiple bands, many more stars
(1920)

looking for obscuration

stellar density fell to 10% local value by 2800 pc 1% by 8500 pc

→ sun near center, 10% stars within same radius

Kapteyn Universe = $\phi \sim 3 \text{ kpc}$ thickness 5 times smaller
(diameter)

very mild color shifts $A_V = C(E_{B-V})$
(dust, not gas) ↑ wrong constant

1930 Trumpler - interstellar dust using open clusters

↳ faded too fast (relative to diameter)

Harlow Shapley (1919) Globular clusters ($\sim 10^5$ stars)

Kapteyn \rightarrow Sagittarius

spherical dist of GC
15 kpc to center of dist (used Cepheids)
Diam ~ 100 kpc
few GCs in plane of galaxy
opposed island universe (galaxy big, so other structures would be really far away)

1920 Great Debate

Shapley - opposed island universe Hubble Curtis - supported Kapteyn universe + island universe

2 30mins talks

(1912 Leavitt - 1777 Cepheids in LMC, SMC still uncertain distances)

Curtis: Against Shapley's: 1. Cepheid distances untrustworthy (true: x2 wrong)

2. Distance to GCs (brightest local stars) \rightarrow x10 error
(brightest GC stars)

Support: 1. Vast range of sizes of spiral nebulae

↳ smallest must be very far away

2. Large # of novae seen in Andromeda + much fainter than MW novae

distance ~ 100 kpc size ~ 3 kpc

SN (in And) vs Novae (in MW)

3. Spectra of spirals looked like stars but broader absorption lines

↳ due to stellar motions

4. Large doppler shifts (radial motion) \rightarrow should have high proper motions

\rightarrow no proper motions \therefore must be far away

5. Dark lanes in other galaxies \rightarrow zone of avoidance in MW

Shapley: Against Curtis: 1. If spiral nebulae are same size as his MW
then they were Mpc away

2. MW would have lower surface brightness than spiral nebulae

(obscuration + environment) other galaxies have star formation

3. Spiral disks are bluer than MW (local MS population vs. all galaxy)

4. Adriaan van Maanen - "saw" spirals rotating \rightarrow small distances to keep vel. small
(false observations)

Resolved with 100" telescope (Hooker)

1925 - Hubble - Cepheids in Andromeda dist $\sim 300\text{ kpc}$ much larger than Kapteyn

proved that spiral nebulae are galaxies

1926 - distances to at least 27 Mpc (using angular sizes) $\xrightarrow{\text{observation}} \frac{1}{60}$ the radius of universe

1922 - Friedmann models

1928 - 200" Hale @ Palomar ($\$6\text{ million from Carnegie}$)

1960's - quasistellar objects $>$ high redshifts Schmitt

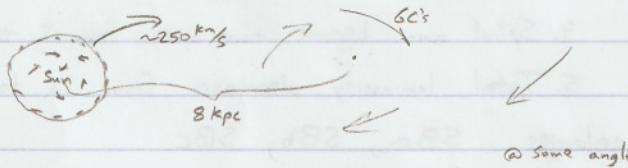
Bertil Lindblad 1920's stellar dynamics, mass of Kapteyn universe

GC's had doppler shifts of 250 km/s (escape velocity \therefore galaxy must be larger)

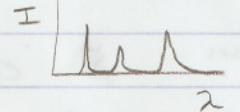
Equations for differentially rotating disks

GC's were orbiting a distant location $\sim 10^9 M_\odot$

high velocity stars - $200-300\text{ km/s}$ random directions, comparable to spheroids



1951 - detection of 21 cm

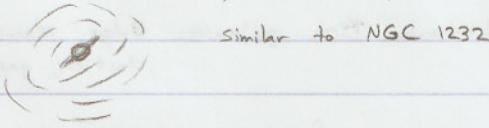


1958 - 21 cm map of galaxy



Oort \rightarrow differential motion equations

MW is multiarm spiral personal speed $\sim 250\text{ km/s}$



Oo MA

$V_{\text{Earth around Sun}} : 3 \times 10^4 \text{ m/s}$

Diameter of Earth: $1.3 \times 10^7 \text{ m}$

$$\Delta t = \frac{d}{v} = 477 \text{ s} = 7.2 \text{ min}$$

$$\text{Solar system crosses Earth } \Delta t = \frac{2.5 \times 10^5 \text{ m/s}}{(\text{Diam E})} = 59 \text{ s}$$

orbital period of solar system
 $R = 8 \text{ kpc}$

$$T = \frac{2\pi R}{v} = 7 \times 10^{15} \text{ sec} = 2.2 \times 10^8 \text{ yrs} = 220 \text{ million yrs}$$

galaxy is dynamically young

$$\frac{GM}{r^2} = \frac{v^2}{r}$$

$$M = \frac{v^2 r}{G} = 1.8 \times 10^{41} \text{ kg} = 9 \times 10^{10} M_\odot \quad (\text{100 Billion stars})$$

1944 - Baade: Mt. Wilson

Population

I - disk Andromeda, blue, metal rich

II - red, spheroids, metal poor

no stars have primordial abundances

III no metals

1/10/2007

1936 - Realm of the Nebulae - Hubble

galaxy - self gravitating system of stars $M_V < -8$ $\sim 10^6 - 10^7$ stars

Spirals: Disk - flattened structure aspect ratio (thick to diameter) $< 1:5$

Bulge - not always

Hubble's initial classification included bulges

Sa, Sb, Sc

Criteria: 1. Relative size of bulge to disk: Sa largest bulges

2. Prominence of spiral arms: Sc most prominent

3. Presence of dust + gas: Sc larger ratio of dust + gas to stars

4. Spiral arm become more open from Sa to Sc

5. Total luminosity decreases from Sa to Sc

Extra feature for bar galaxies SBa, SBb, SBc

Elliptical: Beehive of stars
(triaxial)

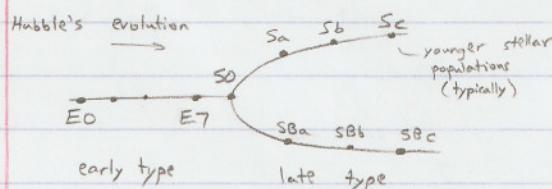


Classified by ellipticity

$$\frac{a-b}{a} = \epsilon$$

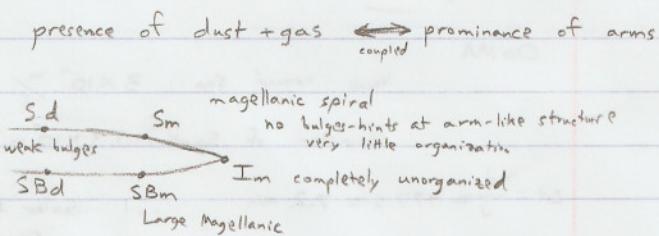
Circular EO Most elongated E7 $\frac{b}{a} \sim 0.3$ $\epsilon = 0.7$
 $\epsilon \times 10$

Hubble Tuning Fork



de Vaucouleurs (1959)

Lenticular (S0) galaxies: Bulge dominated
dust/less, gassless disk



presence of rings

outer ring R



inner ring r



R SB(rs)a Pec



spirals go to center

MW: SAB(rs)bc

cD

cluster
extended halo

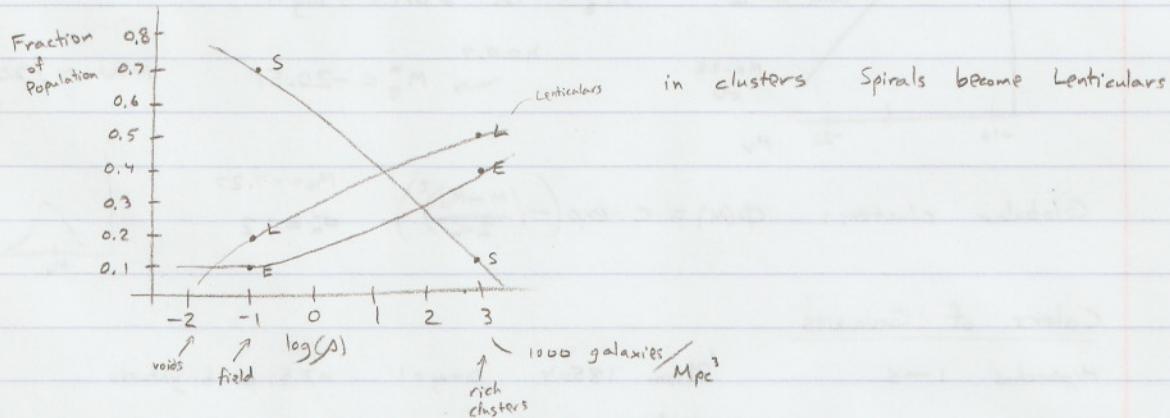
found in cores of clusters

$\sim 10^{13}$ stars

Spirals: ~70% of galaxies (brighter than -18) by number Irr more common

Ellipticals ~10% rest are Lenticulars ~20%

environment dependent Dressler (1980): Morphological Segregation



Local Group

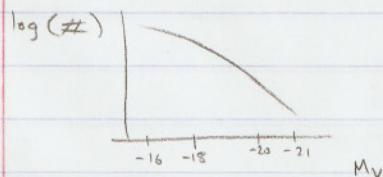
$R \sim 1.5 \text{ Mpc}$ 35 known galaxies more being found

gravitationally bound system

Bright members

Name	Classification	Distance	M_V
Andromeda M31/NGC 224	Sb	725 kpc	-21.1
Milky Way	Sbc	8 kpc	-20.6
M33/NGC 598	Sc	795 kpc	-18.9
LMC	Irr/SBm	49 kpc	-18.1
Draco DDO 208	dSph/E3	76 kpc	-8.6 faintest

3 spirals 18 dwarf ellipticals spheroidals 14 irregulars

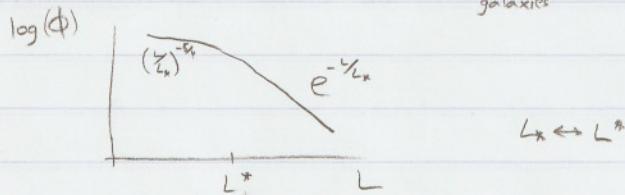


Schechter function (luminosity of galaxies)

$$\Phi(L) = c \left(\frac{L}{L_*} \right)^\alpha e^{-\frac{L}{L_*}}$$

density of galaxies
dominates for faint galaxies
 $L_* \leftrightarrow L^*$

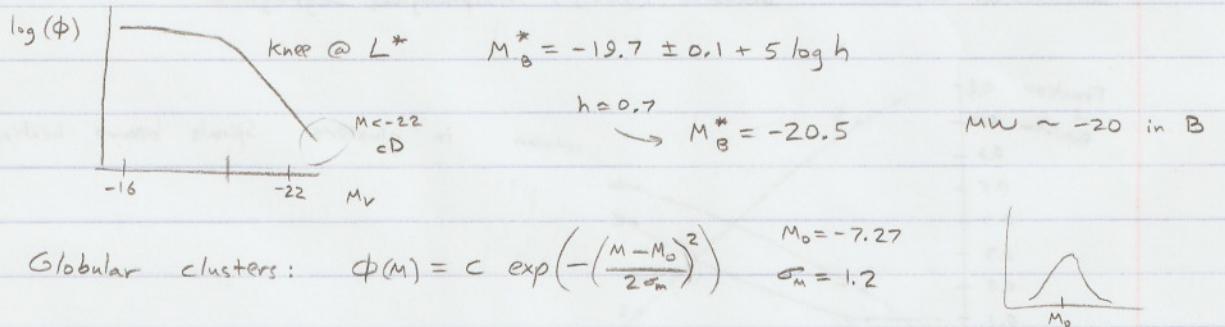
$$\alpha = -5/4$$



$$\Phi(M) = 0.4 \ln(10) \Phi^* 10^{-\frac{0.4(\alpha+1)(M^*-M)}{\text{density of galaxies at } L^* \text{ luminosity}}}$$

magnitude

at L^* luminosity



Colors of Galaxies

Hierarchies $1 \rightarrow 6$

Poisson 1850's $\Delta \text{mag} = 1$ $\times 2.511$ in brightness

$$\text{mag} = -2.5 \log f + \text{constant}$$

magnitude as function of filter (wavelength)

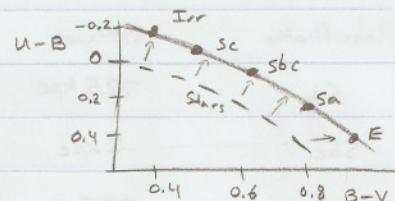
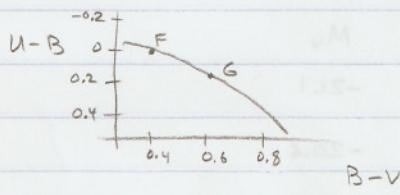
positive color $B-V > 0$ redder than Vega

Vega has same mag in all bands

$$B-V=0$$

blue-red filter

Color-Color of Stars



distribution of stars

young stars contribute to U
red giants make redder

GALEX

presented by: Michael Rich

1/22/2007

can see out to redshift ~ 1.5

made to study decline in star formation ν^{rate} in recent times

sensitive to extinction and star formation rate (SFR)

H α is star formation indicator

- drops off rapidly, extinction \therefore use UV continuum
O stars photoionize

H α $t \sim 1-10 \text{ Myr}$ UV $t \sim 10-100 \text{ Myr}$ Balmer lines $t \sim 0.1-2 \text{ Gyr}$

Far IR $t \sim 10-100 \text{ Myr}$

1960's : UV rising flux in ellipticals: hot population of stars

1970's Copernicus satellite - UV spectroscopy of ISM

1980's IUE

Galex has 1.2° FOV	5'' PSF	$1300 - 1800 \text{ \AA}$ FUV
		$1800 - 2800 \text{ \AA}$ NUV

All-Sky Imaging Survey AIS

Medium " " MIS

Deep " " DIS

Nearby Galaxy "

UV Emission - young stars forming, old stars burning He

Downsizing — SF moves to smaller galaxies

Lyman Break Galaxies

Galactic Center

presented by: Mark Morris

1/24/2007

12 μm — see Zodaical light

Evidence of bar: 1) Large, non-circular gas motions

2) Near-IR light distribution

3) Detailed gas kinematic models

4) Source count asymmetries

5) Large microlensing optical depth (probability of microlensing)

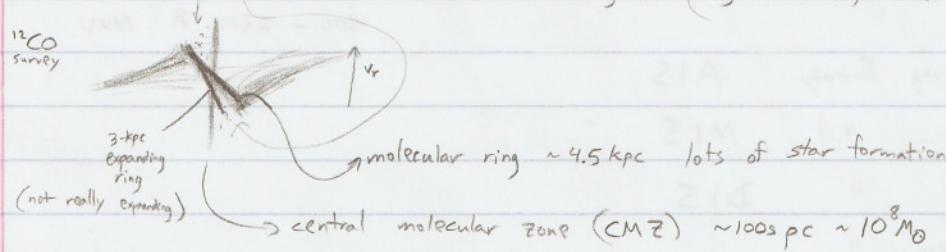
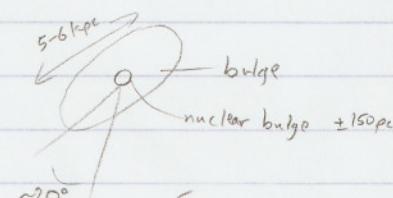
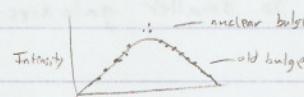


axisymmetric $\Sigma \sim 1 \times 10^{-6}$
bar model/observational $\Sigma \sim 2.3 \times 10^{-6}$

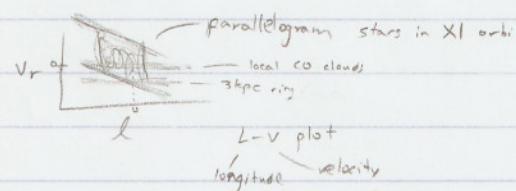
Length of bar: 3.5 kpc Axis ratio 1:(0.3-0.4):0.3

Bulge/Disk near-IR luminosity ratio: ~ 0.2
 $\rho(\phi) \propto e^{im\phi}$ bars are $m=2$ modes density wave but less affected by differential rotation

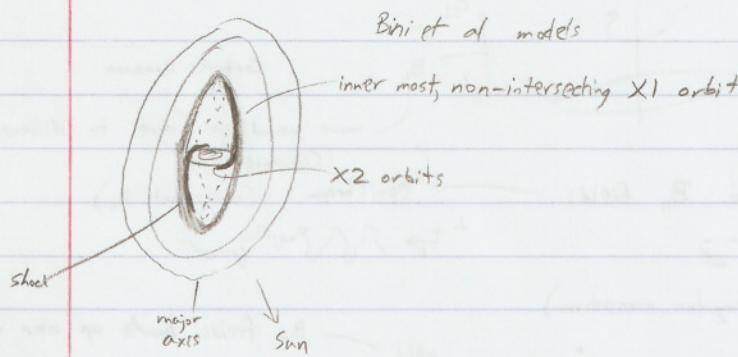
no evidence for dark matter in the inner galaxy

inside end of bar \rightarrow minimum in molecular gas (gas shocks, loose angular momentum \rightarrow falls in)Mass of bulge $\sim 1.3 \times 10^{10} M_\odot$ Nuclear bulge stellar density $\propto r^{-1.8}$ "central stellar cusp" "r^-2 cluster" \rightarrow center of galaxy
(few 100 pc) ongoing star formation (not in old bulge) nuclear stellar disk ~ 230 pc - r
 ~ 45 pc - scale height $\sim 1.4 \times 10^9 M_\odot \sim 2.5 \times 10^9 L_\odot$ gas layer scale height - 30 pc
Stars in nuclear bulge - 70 pc \rightarrow potential problem

\hookrightarrow solution: stars scattering from molecular clouds increases scale height for stars

 \hookrightarrow result of sustained star formation in CMZ

9



carbon monosulfide (CS) probes denser gas — don't see parallelogram

"clouds" in galactic center are streams (sheared clouds)

CMZ

$10^{5-6} M_{\odot}$ 10^4 cm^{-3} density $T \sim 70 \text{ K}$
core density 10^{5-6} cm^{-3}
line width $10-20 \text{ km/s}$

Cloud in galactic disk

density 10^{2-5} cm^{-3}
core density 10^4 cm^{-3} $T \sim 5-15 \text{ K}$
line width $< 5 \text{ km/s}$

$$\langle n \rangle \geq 10^4 \text{ cm}^{-3} \left(\frac{75 \text{ pc}}{R_{\text{gc}}} \right)^{1.8}$$

density criteria

$$\langle n \rangle \sim 10^3 \text{ cm}^{-3} \left(\frac{\Delta r}{R_{\text{gc}}} \right)^2 \quad (?)$$

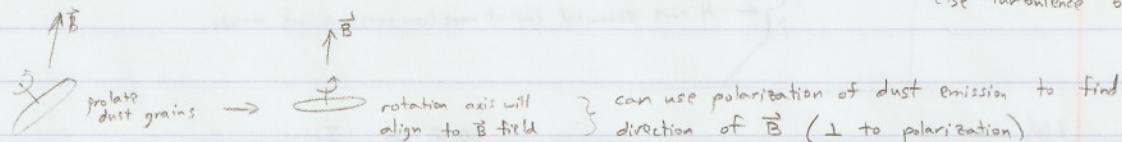
virial criteria

else they get strongly sheared and broken apart
(clouds)

CMZ is tilted to our plane (warped)

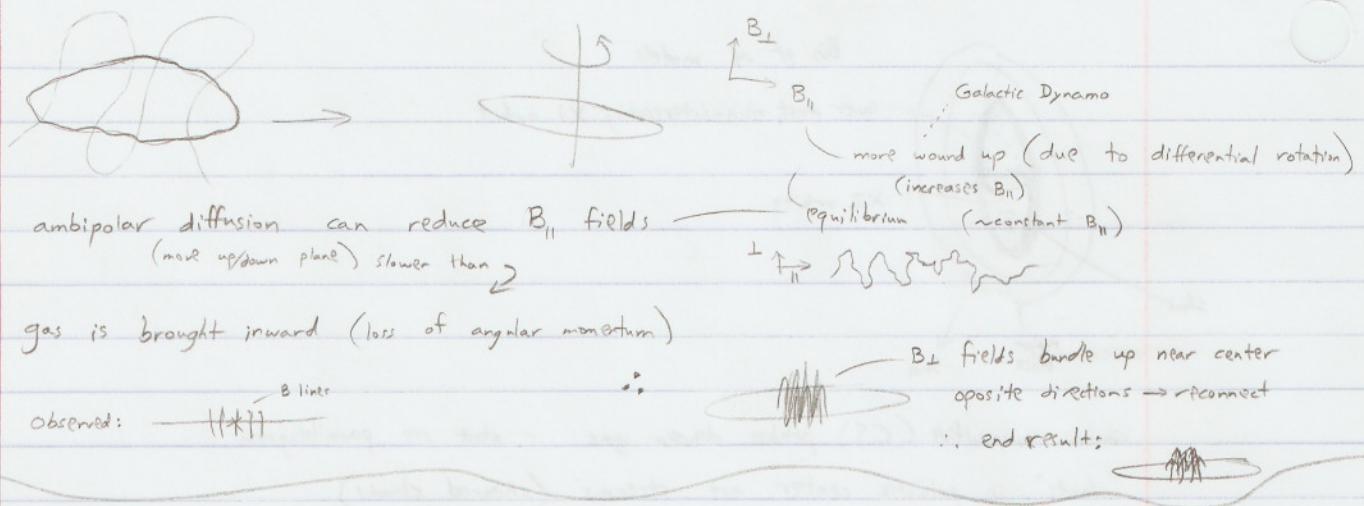
radio filaments \perp to galaxy plane in bulge

nonthermal radiation \rightarrow synchrotron \rightarrow traces out \vec{B} lines \sim milliGauss fields
else turbulence breaks it up



can allow for magnetic reconnection between HII clouds (\vec{B} parallel to plane due to shear)
and radio filaments ($\vec{B} \perp$ to plane) \Rightarrow acceleration of e^- along filaments





Stellar Populations

presented by: Michael Rich

1/29/2007

low mass $M < 1.5 M_{\odot}$

pp chain radiative core He flash

 $1.5 < M/M_{\odot} < 9$ intermediate mass

CNO cycle conv. core He igniter non degenerate

 $M > 9 M_{\odot}$ high mass

CNO cycle

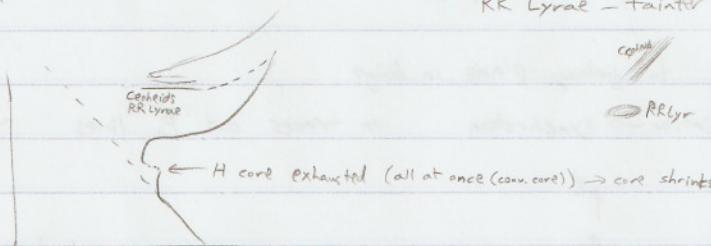
$$E_{pp} \sim T^4 \quad E_{CNO} \sim T^{16} \quad E_{3\alpha} \sim T^{20} \quad \text{CNO cycle in H burning shell}$$

$$RG \sim 5 \times 10^8 \text{ yrs} \quad HB \sim 10^8 \text{ yrs} \quad (\text{low mass})$$

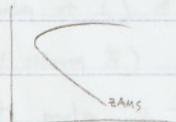
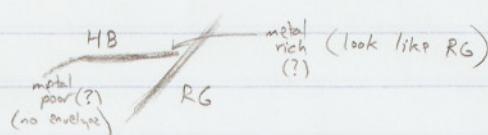
AGB - thermal pulses (He shell flashes) - water Masers, etc.

intermediate

RR Lyrae - fainter than Cepheids, still He burning



high mass

SN Ia $0.7 M_{\odot}$ Irons $0.07 M_{\odot}$ LighterSN II $0.07 M_{\odot}$ Irons $0.7 M_{\odot}$ Lighter 10^{10} yrs or older \rightarrow you get RR Lyraeso if you see RR Lyrae \Rightarrow older than 10^{10} yrs

HB is good age indicator

Best: WD cooling

Second best: MS turn off

Fuel Consumption Theorem

Renzini, Buzzoni 1986 also Renzini 1998 AJ

$$n_j = B L_T t_j \quad \text{life time in phase } j$$

\downarrow $2 \times 10^{-11} \text{ stars/yr}$ (death rate) L_T in L_\odot Ex: How many RG stars in M31?

\uparrow $L_{\text{V, total}}$

good for older than 10^9 yrs

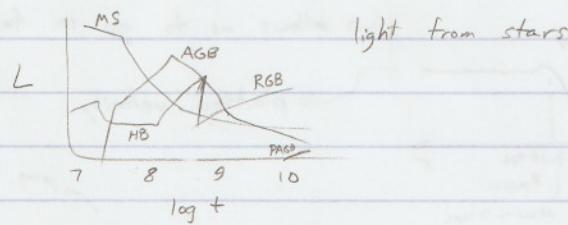
UV excess, UV rising flux \rightarrow seen in elliptical galaxies

PN nebula core? no - short lived

HB stars without envelopes turning into AGBs?

Extreme HB stars in metal rich populations?

Bulges are Mg enhanced



Kennicutt (?) 1988

Kennicutt-Schmidt law (?)

blue-red dichotomy

blue (SF)

red (no SF, ellipticals)

no H α line

M_r
(magnitudes)

NUV-r (color)

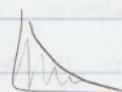
AGNs type 2

Kennicutt or b parameter

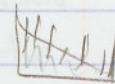
$$b = \frac{\text{SFR}}{\langle \text{SFR} \rangle}$$

b=1 constant

b<1



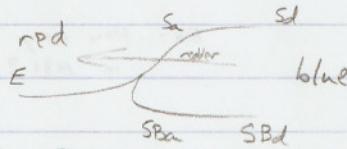
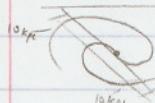
b>1



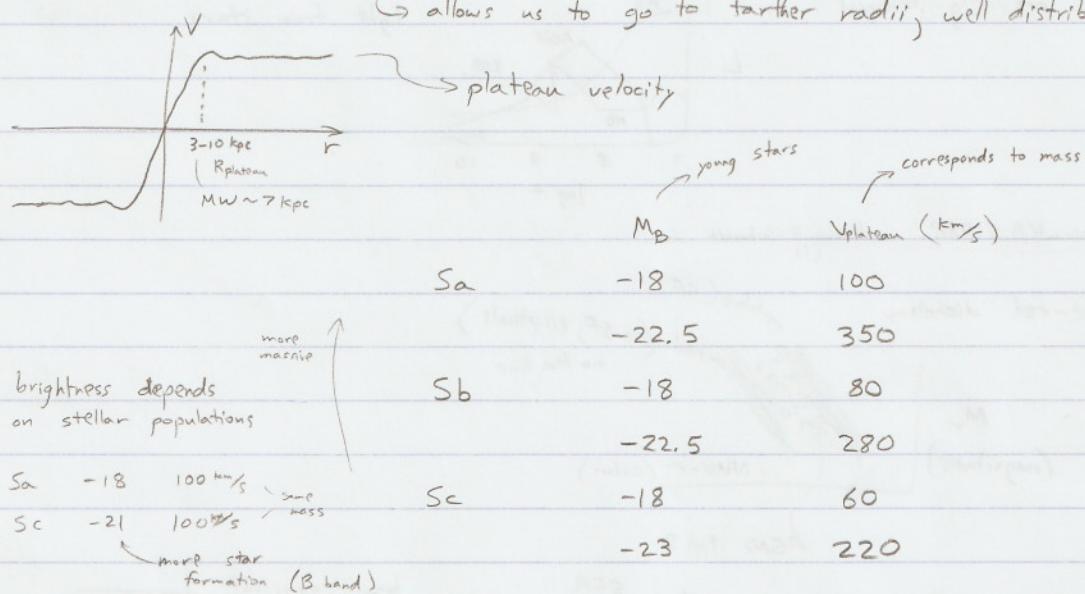
1/31/2007

SA \rightarrow no bar SAB \rightarrow weak bar SB \rightarrow bar

Hubble, de Vaucouleurs system are down to $M_B < -18$
faint galaxies don't fit into system (usually satellites)

Rotation curves

Galaxy spectra dominated by stars

also get emission lines from star formation regions \hookrightarrow absorption lines21 cm emission \rightarrow cold atomic gas \hookrightarrow allows us to go to farther radii, well distributed through galaxy

Diameter of galaxies \rightarrow when drop out to 25 mag/arcsec² — D_{25}
surface brightness is independent of distance (not true for cosmology)

de Vaucouleurs

$$\log(V_{\text{plat}}) + \log\left(\frac{2 R_{\text{plat}}}{D_{25}}\right) = 2.18 \pm 0.03$$

more massive galaxies achieve peak V faster compared to D_{25}

MW: $V_{\text{plat}} = 225 \text{ km/s}$
 $R_{\text{plat}} = 7 \text{ kpc}$

$$\geq D_{25} = 23.4 \text{ kpc} \quad \text{measured } 23.1$$

Masses

$$\frac{GM(r)m}{r^2} = \frac{v^2}{r} m$$

$$\text{Solar system } M(r) = M \quad V = \sqrt{\frac{GM}{r}}$$

$$\text{galaxies } V = V_{\text{plat}} \quad M(r) = \frac{V_{\text{plat}}^2 r}{G} \quad \text{valid in spherical systems (far away from disk)}$$

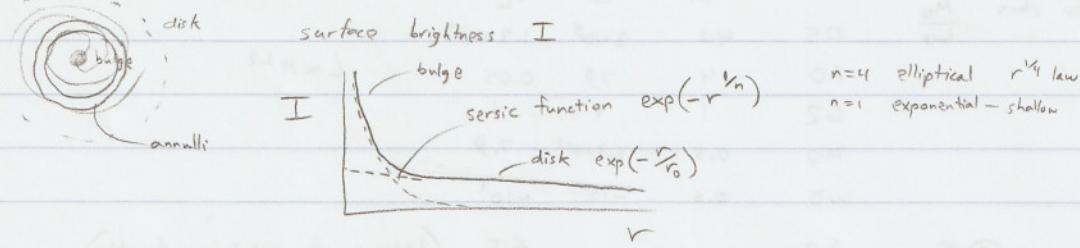
$$\text{thin disk approx: } M(r) = \frac{2V^2 r}{\pi G} \quad 35\% \text{ less mass is needed for same vel.}$$

Dynamical masses: $10^9 - 10^{13} M_\odot$

$$\text{MW: } 8.5 \text{ kpc} \rightarrow M = 4.1 \times 10^{11} M_\odot \quad M(60 \text{ kpc}) = 5 \times 10^{12} M_\odot \quad \sim 100 \text{ times the luminous matter}$$

in field: galaxies separated by 20 times diameter $1-2 \times 10^{12} M_\odot$ about right

$$\text{M31} \quad 3.4 \times 10^{11} M_\odot \text{ to } 10 \text{ kpc} \quad \sim 10^{12} M_\odot @ 100 \text{ kpc}$$

Light Distribution in Spirals

$$\text{Disk: } I = I_0 e^{-r/r_0}$$

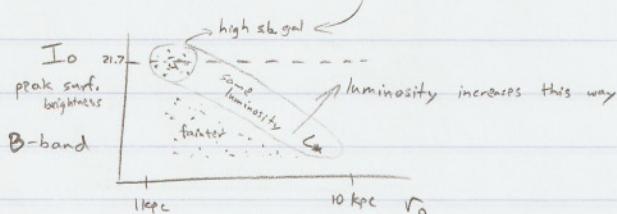
↑ peak surface brightness

$$1970 \quad \text{Freeman law: } I_0(B) = 21.7 \pm 0.3 \text{ mag/arcsec}^2$$

believed to be same for all galaxies

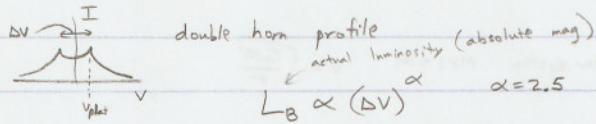
$$L = 4\pi r_0^2 I_0$$

↳ selection effect



$$\text{MW: } r_0 = 5 \text{ kpc}$$

Tully - Fischer 1975 21 cm line widths



Aaronson + Mould (1983) larger sample

$$L_B \propto (\Delta V)^{3.5}$$

$$L_H \propto (\Delta V)^{4.3}$$

Distance indicator

B - 420 nm - sensitive to SFR

H - 1.6 μm - sensitive to stellar mass

higher SFR greatly increase L_B

much tighter relationship

$$\frac{GM}{r_0^2} \propto \frac{V^2}{r_0}$$

$$V \propto \sqrt{\frac{M}{r_0}}$$

Assume: $\frac{M}{L} \sim \text{constant}$ for galaxies (not true)

$$V \propto \sqrt{\frac{L}{r_0}}$$

bright galaxies: Freeman law \sim right $L \propto r_0^2 I_0$ $r_0 \propto \sqrt{L}$

$$V \propto \sqrt{\frac{L}{\sqrt{L}}} = \sqrt[4]{L}$$

$$L \propto V^4$$

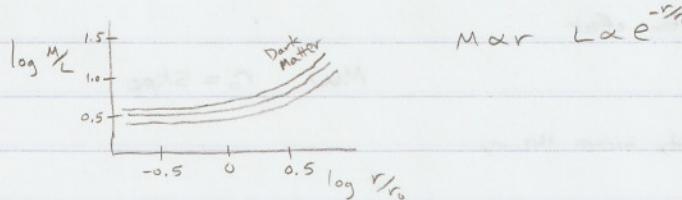
more massive systems
have higher $\frac{M}{L}$ ratios
in B-band
 $\therefore \alpha < 4$

in H-band, more massive gal.
have lower $\frac{M}{L} \Rightarrow \alpha > 4$

for stars	$\frac{M_0}{L_0}$	M	L	M/L
	0.5	40	3×10^5	1.3×10^{-4}
	A0	4	79	0.05
	G2	1	1	1
	M0	0.5	6.3×10^{-2}	7.9
	WD	0.6	$\sim 10^{-3}$	$\sim 10^3$

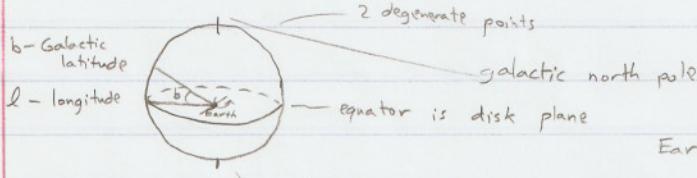
$\alpha @ r_0$ (because of initial mass function)

$\sim r_0$ stars dominate	S0	6.5
	Sa	5.1
	Sb	4.3
	Sc	3.9
	Sd	3.7



$$M \propto r L \propto e^{-\alpha r}$$

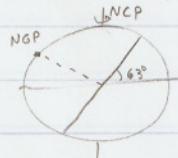
Galactic Coordinates



Earth's axis is tipped 63° to galactic plane

G. Center $\alpha = 17^\circ 45.7^\mathrm{m}$
 $\delta = -29^\circ 0.0'$

} Sagittarius



Frames of reference

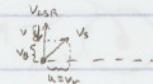
Fundamental Standard of Rest \rightarrow center of mass of galaxies

Local Standard of Rest \rightarrow ideal circular orbit at 8 kpc

$$C_{R_0}$$

peculiar motions - deviations from LSR

$$U = V_R - V_{R, \text{LSR}} = V_R \quad \text{radial} \quad V = V_\theta - V_{\theta, \text{LSR}} \quad \text{theta}$$



Measured

$$\begin{aligned} U &= u_{\text{star}} - u_\odot & V &= v_{\text{star}} - v_\odot & W &= w_{\text{star}} - w_\odot \\ &= V_r - V_{r\odot} & &= V_\theta - V_{\theta\odot} & &= V_z - V_{z\odot} \end{aligned}$$

$V_{\theta, \text{LSR}}$ is determined statistically: average of many stars

$$u_\odot = -\bar{U} = -9 \text{ km/s} \quad v_\odot = -\bar{V} = 12 \text{ km/s} \quad w_\odot = -\bar{W} = 7 \text{ km/s}$$

we move towards GC

we are moving to $l = 53^\circ \quad b = 25^\circ$

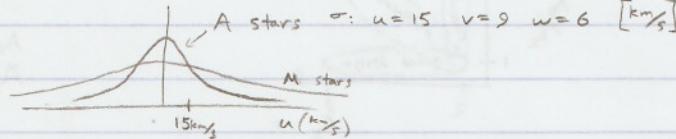
$$v_{\text{pec}} = (u_\odot^2 + v_\odot^2 + w_\odot^2)^{1/2} = 16.5 \text{ km/s}$$

young stars have low v_{pec}
old stars have higher
(interaction with GMCs)

Stellar type

pec. vel. dist. - Gaussian

$$\text{M stars } \sigma: u = 30 \quad v = 15 \quad w = 11$$



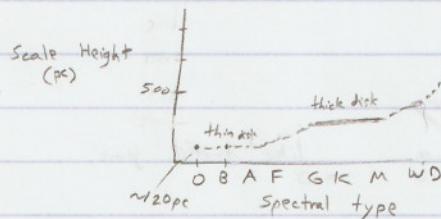
initially u & v are similar and small

High velocity stars $\sigma_v > 65 \text{ km/s} \leftarrow v_{\text{pec}}$ old stars, low net rotation, spherical distribution

typical stars:

apogalacticon $< 40 \text{ kpc}$
(farthest point in orbit around gal.)

typical 15 kpc
perigalacticon $\sim 4 \text{ kpc}$



$$V_{\text{LSR}} = 220 \text{ km/s}$$

Spiral Galaxies

2/5/2007

(M51) Grand Design Spiral

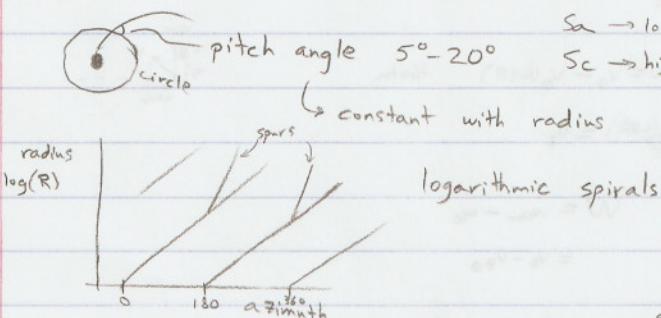


~10%

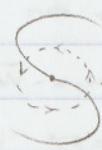
Multiarm spirals



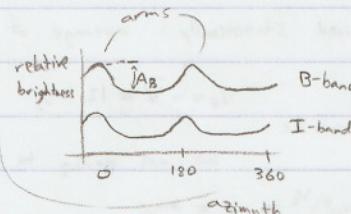
Flocculent galaxies


 $S_a \rightarrow$ lower pitch angles
 $S_c \rightarrow$ higher pitch angles

Arm-Interarm contrast



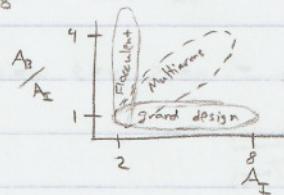
A: ratio of peak to valley height



in grand design

$$\frac{A_B}{A_I} \sim 1$$

$$A_I \approx 2-8$$

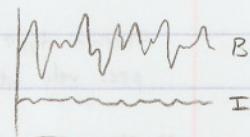


stellar density is higher in arms

Flocculent

$$A_B = 2-8$$

$$A_I \approx 2$$



Winding problem — arms don't wind up multiple times

inner region $\propto r$ $\omega = \text{constant}$ (angular freq)@ 5 kpc $V \approx 200 \text{ km/s}$ Period = $1.5 \times 10^8 \text{ yrs}$ Age $\sim 10^{10} \text{ yrs}$ $\rightarrow 66 \text{ orbits}$ @ 25 kpc $V \approx 200 \text{ km/s}$ Period = $7.5 \times 10^8 \text{ yrs}$ $\rightarrow 13 \text{ orbits}$ \Rightarrow pattern not rotating with stars

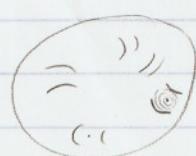
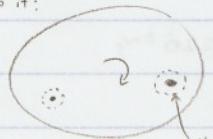
Lin + Shu 1964-1970 Density Wave Theory

Spiral is a semi-stationary density wave like traffic jams

Contagious / Stochastic Star Formation Seiden + Gerola 1978

Toomre criteria — includes angular momentum and Jeans mass } how much to form stars

close to it:



explanation for flocculent

explains high $\frac{A_B}{A_I}$

Motion of stars with peculiar velocities

Cylindrical coordinates

$$-\frac{\partial u}{\partial r} = \ddot{r} - \dot{\theta}^2 r \quad -\frac{\partial u}{\partial \theta} = r \ddot{\theta} + 2\dot{r}\dot{\theta} \quad -\frac{\partial u}{\partial z} = \ddot{z}$$

$$\hat{z}: \quad u = kz \quad \frac{\partial u}{\partial z} = k \quad \ddot{z} = -k \quad \text{oscillatory functions}$$

Period of z oscillation
for Sun ~ 65 million yrs

$$r = R + x \quad x < \frac{R}{10}$$

$$\theta = \underbrace{\Omega t}_\text{pure circular rotation} + y$$

$$x, y \rightarrow \text{deviations} \quad \dot{y} < \frac{\Omega}{10}$$

$$\Omega = \frac{v_{\text{LSR}}}{R}$$

$$\dot{r} = \dot{x} \quad \ddot{r} = \ddot{x} \quad \dot{\theta} = \Omega + \dot{y} \quad \ddot{\theta} = \ddot{y}$$



$$\hat{\theta}: \quad \dot{\theta} = (R+x)\dot{y} + 2\dot{x}(\Omega + \dot{y}) = R\ddot{y} + x\ddot{y} + 2\dot{x}\Omega + 2\dot{x}\dot{y}$$

$$\alpha = R\ddot{y} + 2\dot{x}\Omega \quad \ddot{\alpha} = R\ddot{y} + 2\dot{x}\ddot{\Omega}$$

$$R\ddot{y} = \alpha - 2\dot{x}\Omega$$

Small

Small

$$\hat{r}: \quad -\frac{\partial u}{\partial r} = \ddot{x} - (\Omega + \dot{y})^2(R+x) = \ddot{x} - R\Omega^2 - \Omega^2x - 2\dot{y}R\Omega - 2x\dot{y}\Omega - \dot{y}^2/R - x\dot{y}^2$$

$$-\frac{\partial u}{\partial r} \approx \ddot{x} - R\Omega^2 - \Omega^2x - 2\dot{y}R\Omega$$

$$= \ddot{x} - R\Omega^2 - \Omega^2x - 2\alpha\Omega + 4x\Omega^2 = \ddot{x} + 3\Omega^2x - R\Omega^2 - 2\alpha\Omega$$

$$\frac{\partial u}{\partial r} = -\text{acc.} = \frac{v_{\text{LSR}}^2}{r}$$

$$\text{case 1: } \frac{\partial u}{\partial r} = \frac{v_{\text{LSR}}^2}{r}$$

v_{LSR} = constant with radius

$$v_{\text{LSR}} = \Omega R$$

$$\frac{\partial u}{\partial r} = \frac{\Omega^2 R^2}{R+x}$$

Case 2: inner region

$$v_{\text{LSR}} \sim r \quad v_{\text{LSR}} = cr \quad \frac{\partial u}{\partial r} = \frac{c^2 r^2}{r} = c^2 r = c^2(R+x) \quad \rightarrow \text{HW}$$

Case 1:

$$-\frac{\Omega^2 R^2}{R+x} \approx \ddot{x} + 3\Omega^2x - R\Omega^2 - 2\alpha\Omega$$

$$-\Omega^2 R^2 \approx \ddot{x}R + \cancel{\ddot{x}x} + 3\Omega^2xR + 3\Omega^2x^2 - \cancel{R^2\Omega^2} - \cancel{Rx\Omega^2} - 2\alpha R\Omega - 2\alpha x\Omega$$

$$\alpha = \ddot{x}R + 3\Omega^2xR - R\Omega^2 - 2\alpha R\Omega \quad -\ddot{x}R = 2xR\Omega^2 - 2\alpha R\Omega$$

$$x = x_0 \sin(\Omega t) \quad \Omega = \sqrt{2\alpha^2} = \sqrt{2}\Omega$$

ignore (just an offset)

$$R\dot{y} = \alpha - 2x_0 \sin(\Omega t)\Omega$$

$$R\dot{y} = \alpha t + \frac{2x_0 \cos(\Omega t)\Omega}{\Omega}$$

$$y = \frac{\alpha}{R}t + \frac{2x_0 \Omega}{R\Omega} \cos(\Omega t)$$

α must be zero for closed loops

$$y = \frac{2x_0 \Omega}{R\Omega} \cos(\Omega t)$$

$$y = \frac{\sqrt{2}x_0}{R} \cos(\Omega t)$$

epicycles

$$xR = \sqrt{2}x_0$$

$$\Omega = \sqrt{2}\Omega = 1.4\Omega$$



1.41 loops per orbit

$$\text{Sun} \quad \dot{x} = u = -9 \text{ km/s} \quad (\text{inwards}) \quad \dot{y} = \frac{v}{R} = \frac{12 \text{ km/s}}{8 \text{ kpc}} = 1.5 \frac{\text{km}}{\text{s.kpc}} \quad (\text{forward})$$

$$\dot{x} = x_0 \omega \cos(\omega t) = x_0 \sqrt{2} \Omega \cos(\omega t) \quad \dot{y} = -\frac{2x_0 \Omega}{R} \sin(\omega t)$$

$$\Omega_{\text{esc}} = \frac{v_{\text{LSR}}}{R} = \frac{220 \text{ km/s}}{8 \text{ kpc}} = 27.5 \frac{\text{km}}{\text{s.kpc}} \quad T = \frac{2\pi}{\Omega} = 220 \text{ million yrs}$$

$$\Omega = \sqrt{2} \Omega = 38.8 \frac{\text{km}}{\text{s.kpc}} \quad T_{\text{peri}} = 156 \text{ million yrs}$$

$$\dot{x} = 38.8 x_0 \cos(\omega t) = -9 \text{ km/s} \quad x_0 \cos(\omega t) = -0.232 \text{ kpc}$$

$$\dot{y} = -6.88 \frac{\text{km}}{\text{s.kpc}} x_0 \sin(\omega t) = 1.5 \frac{\text{km}}{\text{s.kpc}} \quad x_0 \sin(\omega t) = 0.218 \text{ kpc}$$

$$x_0^2 \cos^2 + x_0^2 \sin^2 = x_0^2 = 0.10 \quad x_0 = 0.32 \text{ kpc} \quad \gamma_0 = \frac{\sqrt{2} x_0}{R} = 0.056 \text{ radians}$$

$$\gamma_0 R = 0.45 \text{ kpc}$$

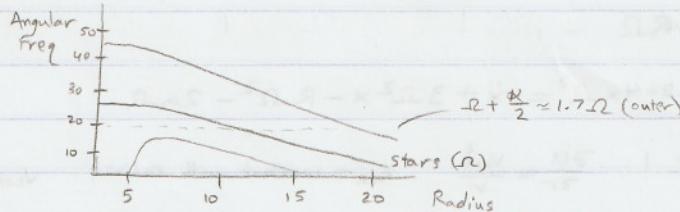
$$\Omega_F = \Omega_0 + \frac{\omega}{m}$$

frame rotating

$$\Omega_F = \Omega_F t = \Omega_0 t + 2\pi \quad \text{if it caught up to star at same epicycle position}$$

$$(\Omega_0 + \frac{\omega}{m})t = -\Omega_0 t + 2\pi \quad \frac{\omega}{m}t = 2\pi \quad m = \frac{\omega t}{2\pi}$$

m : # orbits completed before lagging the star



tidal forces stimulate $m=2$ mode

→ tides

Ellipticals (Chpt 4)

presented by: Matt Malkan

2/12/2007

$$E_n \quad n=10 \left(1-\frac{b}{a}\right) \quad E_0 \dots E_7$$



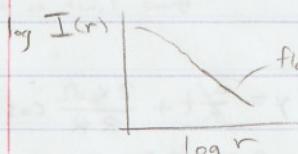
1 long axis (rotation)
2 short identical } prolate spheroid



1 short
2 long } oblate spheroid

planets are oblate spheroids
due to rotation

Surface brightness $I(r)$ along major axis



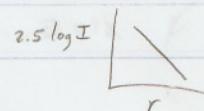
flat portion $\sim r^n$ $n \sim -2$

Hubble's formula $I(r) \propto r^{-2}$ (1930)

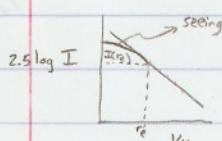
$$L = \int_r^\infty I(r) r^2 dr \sim \ln r \int_r^\infty \dots$$

$$I(r) = \left(\frac{r}{r_a} + 1\right)^{-2} \quad \text{Hubble's law}$$

$$\text{Disks} \quad I(r) \sim e^{-br}$$



Pg. 11



de Vaucouleur's γ_4 law

$$I(r) = I_e 10^{-3.33 \left(\left(\frac{r}{r_e} \right)^{1/4} - 1 \right)}$$

Define r_e so that integral captures half of light

$$\int_0^{r_e} I(r) 2\pi r dr = \frac{1}{2} I_{\text{tot}}$$

$$I_{\text{tot}} = \int_0^{\infty} I(r) 2\pi r dr$$

$n=4$ great fits for ellipticals

violent relaxation - last stages of mergers, effective at distributing grav. potential energy



Φ changes $\rightarrow \Phi(t)$ rapid change

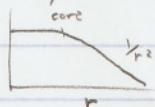
as stars move they change their potential

As potential changes with time it gives energy to objects

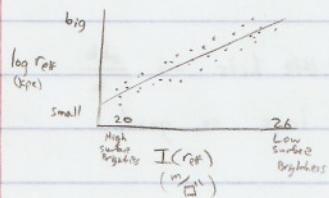
more E to larger mass \rightarrow tries to get same E per unit mass \rightarrow same velocity dispersion

most likely velocity dist'n \rightarrow Maxwellian $\propto v^2 e^{-\frac{v^2}{2\sigma^2}}$ isothermal

Isothermal Sphere: $n(r) \propto r^{-2}$ far away



2 body relaxation: 2 objects (stars) get close, massive stars give energy to lighter stars
 \therefore massive stars sink to center, lighter stars more extended \rightarrow after many relaxation times



Kormendy relation



isophote twist \Rightarrow not oblate or prolate but triaxial

spectral lines broadened by random motions

predict oblates have more rotation \rightarrow rotationally supported

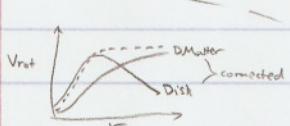
bright ellipticals \rightarrow little rotation

dimmer ellipticals \rightarrow some rotation

Faber-Jackson relation pg. 356

$$L \propto \sigma^4$$

brighter galaxies \rightarrow more dispersion



plot $L \propto \frac{r_{\text{eff}}}{\sigma_{\text{eff}}^4}$ } 3D space: all ellipticals lie together on a plane

Fundamental Plane

related to strength of $\langle M_g \rangle$ line

(negative a_2) disk isophotes
 (big a_2) boxy isophotes

$$r(\theta) = a_0 + a_1 \cos \theta + b_1 \sin \theta + \text{higher terms}$$

ellipse

boxy/peanuts
disky

presented by: Matt Malkan

2/14/2007

largest galaxies are cD — made by mergers

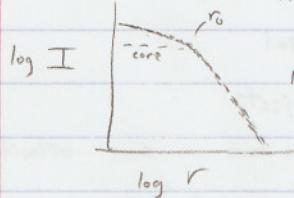
shells in ellipticals could be evidence of mergers

Possible that ellipticals experienced mergers at some time

Faber-Jackson + Kormendy relations } fundamental plane

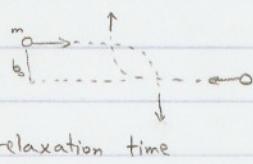
 L, σ I, r_e I, r_e, σ

Hubble images revealed core regions



Nuker Law fitted with 2 power laws

"Collisions" between stars



$$b_0 = \frac{G(m_1+m_2)}{V_{\text{rel}}^2}$$

loses memory of initial direction

relaxation time

$$\tau = \frac{1}{n \sigma v} \quad \text{hard collision} \quad \sigma = \pi b_0^2$$

cross section

$$\tau = \frac{1}{n \pi G^2 (m_1+m_2)^2 V_{\text{rel}}} = \frac{v^3}{\pi n G^2 (m_1+m_2)^2} \quad \text{for hard collisions} \rightarrow \text{not exactly for stars}$$

stars: many little hits $\rightarrow \frac{db}{b}$ random walk

integrate: logs so good

$$\tau_{\text{relax}} = \frac{v^3}{\pi G^2 n (m_1+m_2)^2 \ln N} \quad \text{size of system}$$

$$\text{or } \tau_{\text{relax}} = \frac{G^{-1/2} m^{1/2} N^{1/2} R^{3/2}}{4\pi \ln N} \quad \text{for G.C. } \sim 10^8 \text{ yrs}$$

 $\hookrightarrow \tau_r \ll \tau_h$ energy goes to equipartition:

$$m_1 v_1^2 = m_2 v_2^2 \quad \text{higher } v^2 \text{ in lower mass stars}$$

Active Galaxies

Active — lots of energy produced that is not from stars and their processes

Broad emission lines in Seyfert 1/Quasars \rightarrow obviously not stellar

- widths: high velocities
1000s km/s tend to be more luminous + farther away but Seyfert 1 \approx Quasars
maybe caused by gravity or radiative accelerations

- large range of ionizations ex: NV — soft x-rays — not O stars ($2-4 \times 10^4 K$)
Mg II \rightarrow singly ionized
 \hookrightarrow uv photons

continuum radiation — non stellar engine

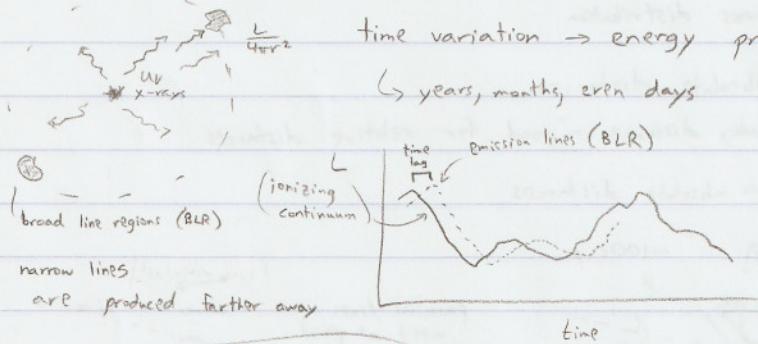
$$\text{ionization parameter } U = \frac{\int L_{\text{ion}} d\nu / h\nu}{4\pi r^2} \leftarrow \# \text{ of ionizing photons}$$

for AGNs $U \sim 100$ high

narrow lines occur in different regions than broad lines

[forbidden] — lower densities
slower velocities

high v
high density



*Cross correlation function
in Fig 5.6 (handout)*

NGC 5548 — 20 day delay

2/21/2007

Extragalactic Distance Scale from George Djorgovski in Caltech

$$t_H = \frac{1}{H_0} \quad D_H = \frac{c}{H_0} \quad \text{Hubble distance}$$

$$D \approx \frac{cz}{H_0}$$

presented by: Shoko Sakai

in 1930s $H_0 = 560 \frac{\text{km}}{\text{s mpc}}$ $t_H \sim 2 \text{ Gyr}$

Brade: identified 2 types of Cepheids

some HII regions thought to be stars

then: $\frac{1930s}{1970s(?)} \frac{100}{50}$

Cosmological principle: universe is homogeneous + isotropic

— scales larger than $\sim 100 \text{ Mpc}$

redshift surveys reveal large scale structures

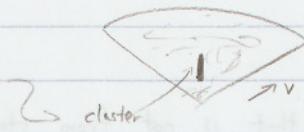
as seen in WMAP or radio sources

3D distribution of galaxies

~ 20 galaxies in local group

Local supercluster: $\sim 60 \text{ Mpc}$ centered on Virgo Cluster (local group in outskirts)

"Finger of God" effect



"Great Wall" ~100 Mpc structure in CfA2 redshift survey



Recent redshift surveys

2dF (2 degree field) ~250,000 galaxies $z \sim 0.3$ 5% sky

SDSS ~565,000 galaxies

pencil beam surveys: go deep in sky in small area

$$V_{\text{total}} = V_{\text{Hubble}} + V_{\text{pec, radial}}$$

$$\begin{matrix} V_{\text{pec}} \\ V_{\text{pec, rad}} \end{matrix} \rightarrow V_H$$

~~measure H(z)~~
 $V_{\text{pec}} \sim 100 \text{ km/s}$ so need high V_H to measure H_0 accurately

CMB Dipole: we are moving wrt CMB at ~620 km/s towards $b = 27^\circ$ $\ell = 268^\circ$

$$V_H = H_0 D \quad V_t = H_0 D + V_{\text{pec}}$$

V_{pec} field will give mass distribution

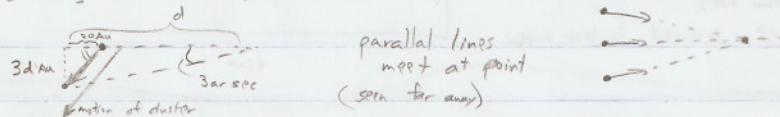
Distance ladders Absolute distances

Secondary distance \rightarrow good for relative distances

— parallax + proper motions \rightarrow absolute distances

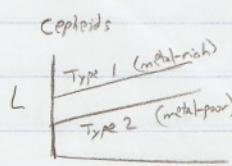
$$(d = \frac{1}{p} \quad d: [\text{pc}] \quad p: [\text{arcsec}]) \quad \sim 100 \text{ pc}$$

— Moving cluster method



— Main Sequence Fittings

— Variable Stars



Mv -4 to -7 magnitudes

Cepheids are high mass Pop I

RR Lyrae are low mass Pop II

10⁸K

need extinction corrections — since Pop I

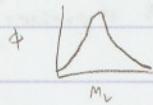
P-L relation calibrated using distance to LMC

RR Lyrae: fainter, short periods, found in areas with less dust
calibrated with GC distances or Magellanic clusters

— Baade-Wesselink Method — pulsating stars $f_1 = \frac{4\pi R_1^2 \sigma T_1^4}{4\pi D^2} \quad f_2 = \frac{4\pi R_2^2 \sigma T_2^4}{4\pi D^2}$

from spectroscopic obs: $R_2 = R_1 + \Delta R = R_1 + \int_{t_1}^{t_2} v(t) dt$ 3 eqs, solve for R_1, R_2, D

- Galaxy Cluster Luminosity Function out to 200 Mpc

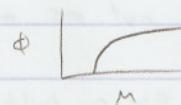


assume peak always at $M_B = -6.6 \pm 0.3$

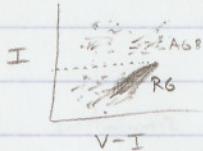
not as precise

- Planetary Nebula Luminosity Function strong emission in [OIII] $\lambda = 5007 \text{ Å}$

there is a sharp cutoff at bright end



- Tip of the Red Giant Branch good out to ~20 Mpc



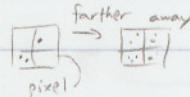
$$M_I = -4.1 \pm 0.1 \approx \text{constant}$$

- Surface Brightness Fluctuations (SBF)

$$\langle N \rangle = n(DSB)^2$$

stars / area

long. resolution



$$f = \frac{L}{4\pi D^2} \quad F = \langle N \rangle f = nL \frac{SB^2}{4\pi}$$

average flux has dispersion $\langle N \rangle^{1/2}$ (Poisson)

$$\sigma_F = \langle N \rangle^{1/2} f \propto \frac{1}{D}$$

$$\frac{\sigma_F^2}{F} = f \leftarrow \text{can use this for relative distances}$$

calibrated with M31

- Tully-Fisher Relation $L \sim v_{\text{rot}}^8 \quad \gamma \approx 4$

K-correction - at diff. redshifts you sample a diff. area of spectrum for same filter

- Fundamental Plane Relation (Faber-Jackson)

$\sim D_h - \sigma$ relation D_h - radius within which mean surface brightness is $20.75 M_B$

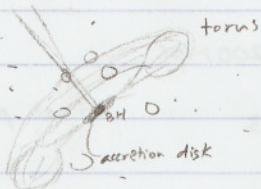
- Supernovae Type Ia $M_V \sim -19.3$ can use multiple colors to get better light curve (MLC)

$$H_0 = 72 \pm 3 \text{ (random)} \pm 7 \text{ (systematic)} \text{ km s}^{-1} \text{ Mpc}^{-1} \quad \text{in 2001}$$

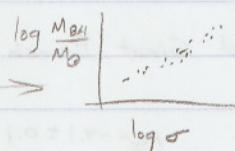
AGNs

presented by: Sarah Gallagher

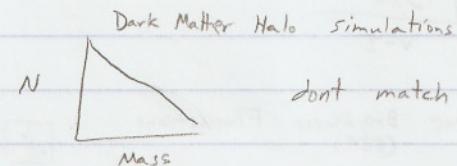
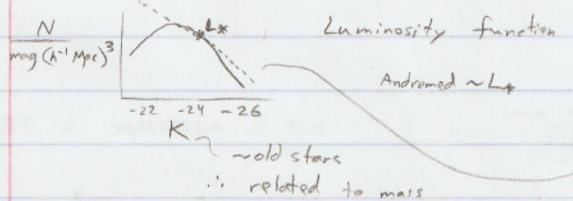
2/28/2007

jet - source of radio power ($\sim 10\%$ of quasars)

- Mass of local inactive BH are proportional velocity dispersions $M_{BH} \propto \sigma$
- Giant galaxies are not as massive as they should be

Sphere of influence of BH \sim light years

true also for active galaxies

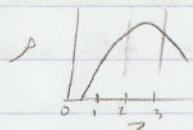
 $M-\sigma$ relationship $M \propto \sigma$ 

Quasar feedback: 1. Jet (injection of energy + matter as BH grows)
2. Winds

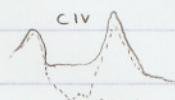
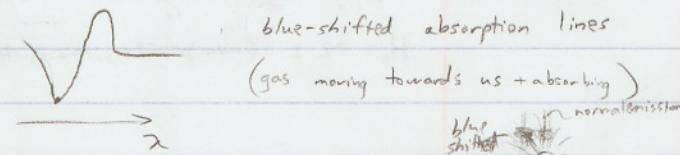
Assumptions:

- 1- All galaxies have BH
- 2- BH grows during quasar phase
- 3- $M_{BH} \propto M_{gal}$

} growth of BH
related to host galaxy growth

Grav collapse \rightarrow star forms, BH fueled \rightarrow quasar feedbacks clears gas \rightarrow stop SF.Quasar epoch: $z=2-3$ 

similar relationship for SFR

Outflows directly observed in $\sim 20\%$ $\text{Ly}\alpha$ - strongest line in Quasar spectrum $v \sim 25,000 \text{ km/s}$ up to $0.1-0.2c$ $(0.03-0.2)c$ broad absorption lines (BAL) \rightarrow BAL Quasars

Evolution (a phase) or Orientation?

Extreme Explanations

Cocoon

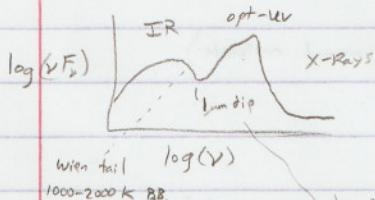
wind covers all
sky 20% of time

Disk-wind



wind covers 20%
of sky all the time

SED - spectral energy density



X-ray: ~Aus: close to BH

Opt-UV: (big blue bump): accretion disk < 1 pc

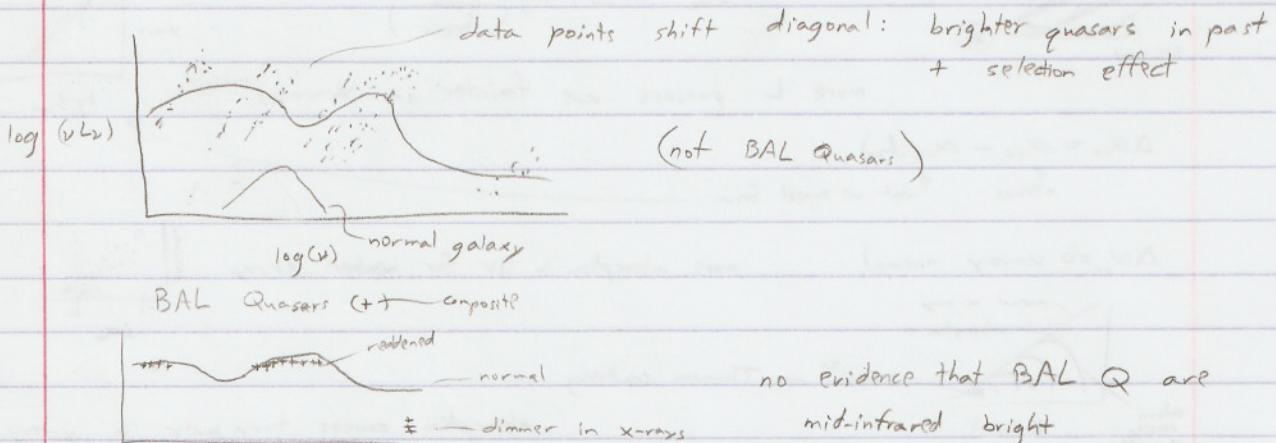
IR: "torus" 1-10 pc

transition from accretion to reprocessed light (torus)

dust can't exist close to accretion disk

Cocoon: BAL Quasars should be mid-IR bright relative to other quasars

cocoon has dust in more sky \Rightarrow captures more light and reprocesses it
also has more absorption



Starburst - dust is cooler (heated by OB stars)

not all BAL Q have high SF

Cocoon \rightarrow ruled out



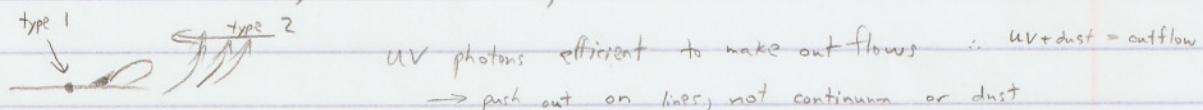
shielding gas \rightarrow to protect wind from ionizing x-rays (wind needs to be partially ionized only)
not completely

Torus must explain — ratio type 1 / type 2 1:(2-4)

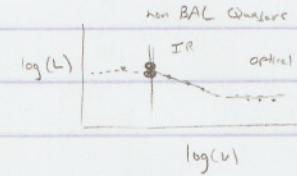
— mid-to-far IR SED

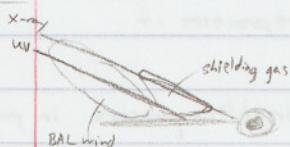
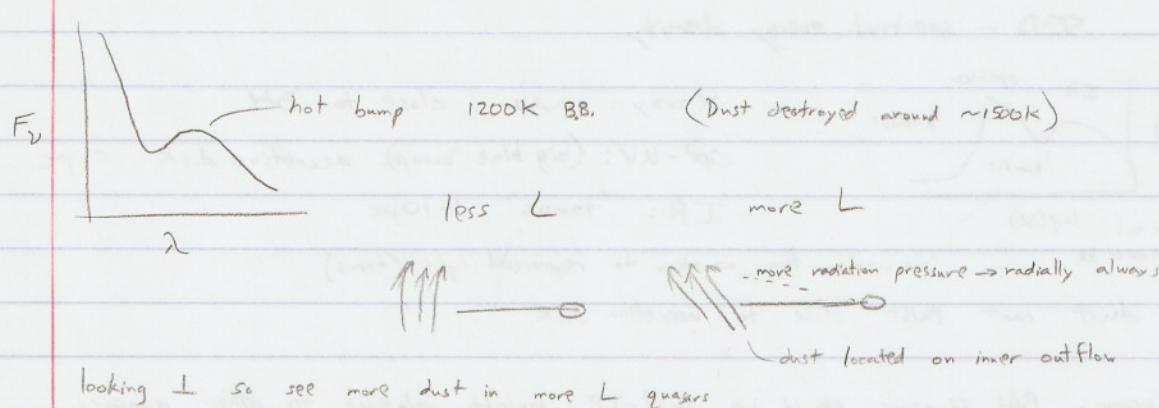
But: unstable

Maybe its a radially wind

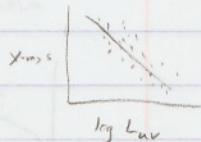


IR-Luminous Quasars typically have steeper SED show spectral curvature





$$\alpha_{ox} = 0.384 \log \left(\frac{f_{2600}}{f_{2800}} \right)$$



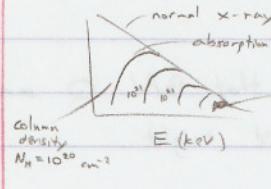
more L quasars are fainter in X-rays

$$\Delta \alpha_{ox} = \alpha_{ox} - \alpha_{ox}(L_{\text{bd}})$$

measured what we expect from

$$\Delta \alpha_{ox} = 0 \text{ X-ray normal}$$

more absorption in UV for weaker X-ray

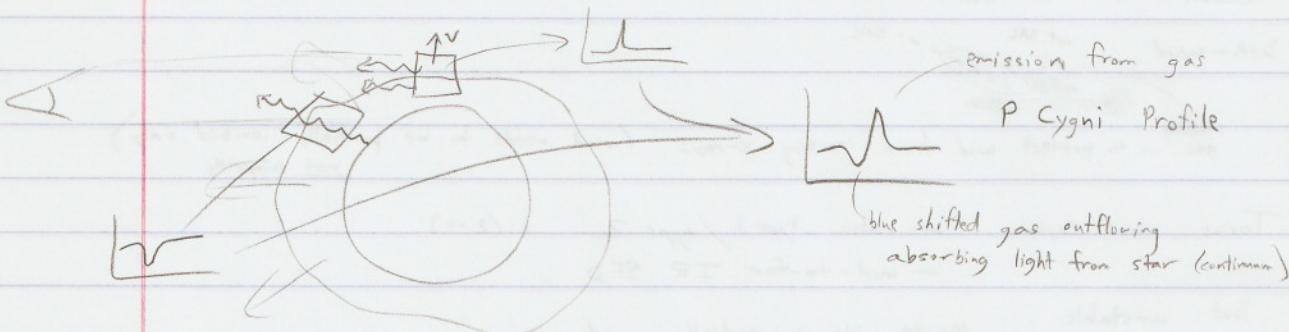


absorption causes turn over in x-ray

normal underlying X-ray continua

significant absorption $N_H = (0.1 - 5.0) \times 10^{23} \text{ cm}^{-2}$

($10^{23} \text{ cm}^{-2} \rightarrow$ your hand)

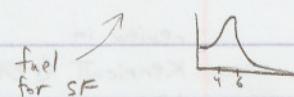


presented by: Nate McCrady

3/5/2007

Starburst Galaxiesglobal star formation rate $\dot{M}_* \sim 4 M_\odot \text{ yr}^{-1}$ for MW.low rate for disk galaxies
mostmolecular gas: $2 \times 10^9 M_\odot$ star formation can last $\sim 10^9 \text{ yrs}$ local SFR $\dot{m}_*(R)$ near Sun: $\dot{m}_*(R) \sim 3 \times 10^{-9} M_\odot \text{ yr}^{-1} \text{ pc}^{-2}$
(per unit area)rises as you move inward to $\sim 4-5 \text{ kpc}$ then falls \rightarrow same as H₂ distribution

Schmidt Law



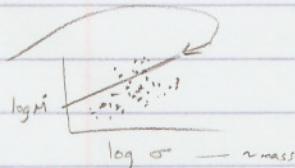
$$\langle \dot{m}_* \rangle \propto \langle \Sigma_{\text{gas}} \rangle^N \quad N \approx 1.4 \quad (\text{empirical law})$$

(surface density of all diffuse gas)

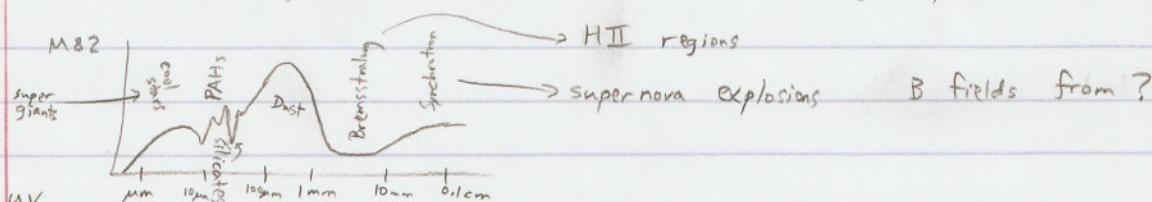
Starburst: $\dot{M}_* > 10^2 M_\odot \text{ yr}^{-1}$ \rightarrow only in inner few hundred pcM82 $\dot{M}_* \sim 10^2 M_\odot \text{ yr}^{-1}$ $M_{\text{dyn}} \sim 10^{10} M_\odot$ (MW: $10^{12} M_\odot$) $L_{\text{IR}} = 3 \times 10^{10} L_\odot$ $\sim 30\%$ in molecular gas
 $L_{\text{bol}} > L_{\text{bol}}$ of M31

Operational Definitions: (for starburst)

- At current SFR, gas reservoir would be exhausted in less than Hubble time
- SFR per unit area is much higher than normal galaxies
- SFR approaches limit set by causality

OB stars' radiation can stop star formation \rightarrow Eddington limitStarbursts are powered by high mass ($M > 8 M_\odot$) stars

Wolf-Rayet stars are associated with starburst

 $\sim 30 M_\odot$, high winds, lots of emission, P Cygni profile

Dust reprocesses UV light from OB stars

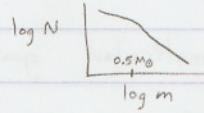
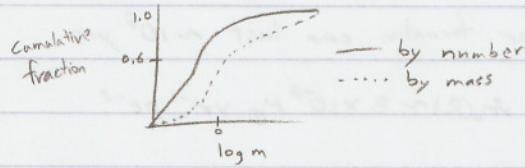
Initial Mass function

$$N(m, t) = \phi(m) \psi(t) dm dt$$

coeval population (constant age) $\psi(t) = \delta(t)$ $dN = m^{-\alpha} dm$

Saltz peter $\alpha = 2.35$ for high mass stars

$$\alpha = 1.3 \quad 0.1 \leq m/M_{\odot} < 0.5 \quad \alpha = 2.3 \quad 0.5 \leq m/M_{\odot} \leq 100 \quad \text{Kroupa IMF} \rightarrow \text{flatter at low masses}$$



How to measure SFR?

UV: stellar continuum 125–250 nm problem: dust

review in

Kennicutt (1998)

ARA&A 36: 189

Optical: Balmer emission, [OII] doublet

Infrared: Paschen, Brackett series Brackett $\gamma \rightarrow K$ band
(atin window)
Far-IR dust continuum 10–300 μm

Starbursts: supernova factories $0.05 - 5 \text{ SNe yr}^{-1}$

morphological evidence for mergers or interacting galaxies

near M82: M81 \leftarrow massive spiral galaxies connected in HI

collisions transfer angular momentum from gas to stars allowing gas to fall to bottom of potential well

Super star clusters $\sim 10^6 M_{\odot}$ bright, dense, young, massive

star formation rate $\sim 10^4 M_{\odot} \text{ pc}^{-3}$

if they have old stars \rightarrow might turn into globular clusters?
(controversial)