```
function [DCdir midOrdDist midOrdX midOrdY midOrdZ chordAz] = findMidOrdDistance (chordLength,xStatic
 3
   % findMidOrdDistance.m - returns distance between a chord's mid ordinate
 4
   %
         and a series of line segments defined by data points.
 5
   %
 6
   %
       Input: search radius, chord and mid-ordinate X & Y coordinates,
 7
   %
           easting, northing of a set of ordered data points
 8
   %
 9
   %
       Output: distance between mid ordinate of a chord and the intersection
10
   %
            orthagonal with the chord at the mid ordinate, midOpt coords.
11
   %
   % Syntax:
12
13
   %
   14
15
   % Other m-files required: dist2pts.m, midOrd.m, pts2eqn.m,
16
   %
                              perp2line.m, intsct2lines.m
17
   %
18 % Subfunctions:
19
   %
20 % MAT-files required: none
21 | %
22
   8 See also: Route Location and Design, 5th ed. Thomas Hickerson, 1964
          chapter 14: "String-Lining Railroad Curves", pp 346-355
23
   %
24
   %
25
   % Author: Peter J Dailey, inspired by Doug Hull's (Doug.Hull@mathworks.com)
      Matlab Video Tutorial: Intersecting a circle with a line series.
26
27
   % email: daileypj@mac.com
28
   % Doug's website posting: http://blogs.mathworks.com/videos/2008/02/19/...
29 | %
        practical-example-intersecting-a-circle-with-a-line-series/
30 | % Last revision: 11-Aug-2009
32
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   45
46
47
   % find endpoint of chord, first is station, find second
48
   [xChord yChord zChord] = getIntLinesCircle(chordLength,xStation,yStation,zStation,x,y,z,lastXYZIndex)
49
50
   % direction of chord
51 chordAz = az2pts (xStation,yStation,xChord,yChord);
52
53
   % middle of chord coordinates
54 \% Calculate middle of chord coordinate given end point coordinates
55 dX
                = abs(xStation - xChord);
56 | dY
                = abs(yStation - yChord);
57 dZ
                = abs(zStation - zChord);
58 xMidOrd
                = min(xStation,xChord)+(dX/2);
59
   yMidOrd
                = min(yStation,yChord)+(dY/2);
60
   zMidOrd
                = min(zStation,zChord)+(dZ/2); %elev between chord end points
61
62 \% find closest point to the mid-ordinate
63
   [first]
                = closestPoint(xMidOrd,yMidOrd,zMidOrd,x,y,z);
64
65 % definition of the 2D chord line
   [aChord bChord cChord] = pts2eqn (xStation,yStation,xChord,yChord);
```

```
67
 68
    % definition of the line orthogonal to the chord passing through the mid ordinate
    [aPerChord bPerChord cPerChord] = perp2line (xMidOrd,yMidOrd,aChord,bChord,cChord);
 70
 71 | %
 72
    for i = 1:3 % three data points define two lines closest to MidOrdinate
 73
      % definition of each line
 74
       point
 75
       xx(i)
                     = x(point+i); % (the point one before closest - 1)
 76
       yy(i)
                     = y(point+i);
 77
    end
 78
    [a(1) b(1) c(1)] = pts2eqn (xx(1),yy(1),xx(2),yy(2));
 79
    [ a(2) b(2) c(2) ] = pts2eqn (xx(2),yy(2),xx(3),yy(3));
 80
 82
    % coordinates of the two intersections with the mid ordinate perpendicular
 83
    [xInt(1) yInt(1)] = intsct2lines (a(1),b(1),c(1),aPerChord,bPerChord,cPerChord);
 84
    [xInt(2) yInt(2)] = intsct2lines (a(2),b(2),c(2),aPerChord,bPerChord,cPerChord);
 85
    % distance from mid ordinate to each intersection
 87
    d = dist2pts (xMid0rd,yMid0rd,xInt,yInt);
 88
 89 % find the minimum distance to the two intersections
 90 minD
            = min(d);
    % index of intersection, use outside of loop
 91
    foundIdx = find(d == minD);
 93
    % If they are the same value then find has two index entries.
    % Use the first one.
 95 if numel(foundIdx) > 1
 96
        index
               = foundIdx(1);
 97
    else
 98
        index
                = foundIdx;
 99
    end
100
102
    % This this was the original method to determine mid ordinate
103
    % Assign the closest intersection to the return value
104 % Return values in midOrdX and midOrdY
105 closeMidOrdDist
                     = d(index);
106 mid0rdX
                     = xInt(index);
107
    midOrdY
                     = yInt(index);
108 || % ************
109
111 \% This method determines the mid ordinate from the mean
112 % of the far and near intersections.
113 \% Find the coordinates between the two intersections,
114 % Return values in midOrdX and midOrdYs
115 xMidMean
                     = mean(xInt);
116 midOrdX
                     = xMidMean;
117 yMidMean
                    = mean(yInt);
118 midOrdY
                     = yMidMean;
                  = ymtumeun,
= dist2pts(xMid0rd,yMid0rd,xMidMean,yMidMean);
119 meanMidOrdDist
120 || % ***************
121 | %midOrdDist
                      = closeMidOrdDist;
122 midOrdDist
                     = meanMidOrdDist;
124
125 % calculate elevation at intersection
126 dist2Int
                    = dist2pts (x(first),y(first),xInt(index),yInt(index));
127
128 if index
                     == 1
129
      Xpt1
                     = x(first-1);
130
       Ypt1
                     = y(first-1);
131
       Zpt1
                     = z(first-1);
132
```

```
133
       Xpt2
                       = x(first);
134
        Ypt2
                       = y(first);
135
       Zpt2
                       = z(first);
    else
136
137
       Xpt1
                       = x(first);
138
       Ypt1
                       = y(first);
139
       Zpt1
                       = z(first);
140
141
       Xpt2
                       = x(first+1);
142
       Ypt2
                       = y(first+1);
143
                       = z(first+1);
       Zpt2
144 end
145
146 mid0rdZ
                       = getStaElev(dist2Int,Xpt1,Ypt1,Zpt1,Xpt2,Ypt2,Zpt2);
147 | % ****************
148 % find the direction from midordinate to intersection, (+ right) (- left)
149 moAz
                       = az2pts(xMidOrd,yMidOrd,xInt(index),yInt(index));
                       = round(moAz - chordAz);
150 DCdir
151 DCdirStr
                       = num2str(DCdir);
152
    switch DCdirStr
153
         % point to the right of the midordinate
154
         case '90'
155
              direction
                           = -1;
156
         case '-270'
157
              direction
                           = -1;
158
159
         % point to the left of the midordinate
         case '-90'
160
161
              direction
                           = 1;
162
         case '270'
163
              direction
                           = 1;
164 end
165 try
166 midOrdDist = midOrdDist * direction; % adj result left or right
167
    catch
         fprintf('MidOAz: %4.1f DCdir: %4.1f DCdirStr:%s\n',...
168
169
              moAz,DCdir,DCdirStr);
170
    end
171 end %function
172
173 % subfunction to find the point before the closest point to the midordinate
174 | function [first] = closestPoint(xMidOrd,yMidOrd,zMidOrd,x,y,z)
175 % Input: data set X & Y values; circle center x & y.
176 % Output: index of all points within radius
    deltaX = x - xMidOrd; % all X coord - circle origin X coord, Cx
178
    deltaY = y - yMidOrd; % all Y coord - circle origin Y coord, Cy
    deltaZ = z - zMidOrd; % all Z coord - circle origin Z coord, Cz
179
180
181
    % distance = pythagorus from center to point(s)
182 distance
                       = sqrt(deltaX.^2 + deltaY.^2 + deltaZ.^2);
183
184 % find the closest point
185 closest
                       = min(distance);
186 % get index of closest point
187 | index = find(distance == closest);
188 % return the index before the closest point
189 | first = index-1;
190 end
191
```