Solution for (i),  $p = a \land (\neg b \lor c)$ 

## Solution (Instructor only):

- (a) Clauses are a, b, c.
- $(b) p_a = \neg b \lor c$   $p_b = a \land \neg c$   $p_c = a \land b$
- (c) Note: Blank cells represent values of 'F'.

	a	b	c	$\mid p \mid$	$p_a$	$p_b$	$p_c$
1	T	T	T	$\mid T \mid$	T		T
2	T	T	F			T	T
3	T	F	T	T	T		
4	T	F	F	T	T	T	
5	F	T	T		T		
6	F	T	F				
$\gamma$	F	F	T		T		
8	F	F	F		T		

- (d) GACC pairs for clause a are:  $\{1,3,4\} \times \{5,7,8\}$ . There is only one GACC pair for clause b: (2,4). There is only one GACC pair for clause c: (1,2).
- (e) CACC pairs for clauses a, b, and c are the same as GACC pairs.
- (f) RACC pairs for clause a are: (1,5), (3,7)(4,8).

  RACC pairs for clauses b and c are the same as CACC pairs.
- (g) GICC tuples for a are: (2,6) for p=F; no feasible pair for p=T. GICC tuples for b are:  $\{5,6\} \times \{7,8\}$  for p=F; (1,3) for p=T. GICC tuples for c are:  $\{5,7\} \times \{6,8\}$  for p=F; (3,4) for p=T.
- (h) RICC tuples for a are same as GICC. RICC tuples for b are: (5,7), (6,8) for p=F; (1,3) for p=T. RICC tuples for c are: (5,6), (7,8) for p=F; (3,4) for p=T.

Solution for (ix),  $p = a \lor b \lor (c \land d)$ 

## Solution (Instructor only):

(a) Clauses are a, b, c, d.

(b) 
$$p_a = \neg b \land (\neg c \lor \neg d)$$
  
 $p_b = \neg a \land (\neg c \lor \neg d)$   
 $p_c = \neg a \land \neg b \land d$   
 $p_d = \neg a \land \neg b \land c$ 

		a	b	c	d	p	$p_a$	$p_b$	$p_c$	$p_d$
	1	T	T	T	T	T				
	2	T	T	T	F	T				
	3	T	T	F	T	T				
	4	T	T	F	F	T				
	5	T	F	T	T	T				
	6	T	F	T	F	T	T			
	7	T	F	F	T	T	T			
(c)	8	T	$\overline{F}$	F	F	T	T			
	9	$\overline{F}$	T	T	T	T				
	10	F	T	T	F	T		T		
	11	F	T	F	T	T		T		
	12	F	T	F	F	T		T		
	13	$\overline{F}$	$\overline{F}$	T	T	T			T	T
	14	F	F	T	F		T	T		T
	15	F	F	F	T		T	T	T	
	16	F	F	F	F		T	T		

- (d) GACC pairs for clause a are:  $\{6,7,8\} \times \{14,15,16\}$ . GACC pairs for clause b are:  $\{10,11,12\} \times \{14,15,16\}$ . GACC pair for clause c is: (13,15). GACC pair for clause d is: (13,14).
- (e) CACC pairs for clauses a, b, c, and d are the same as GACC pairs.
- (f) RACC pairs for clause b are: (6, 14), (7, 15), (8, 16). RACC pairs for clause b are: (10, 14), (11, 15), (12, 16). RACC pairs for clauses c and d are the same as CACC pairs.
- (g) GICC tuples for clause a are: no feasible pair for p = F;  $\{1, 2, 3, 4, 5\} \times \{9, 10, 11, 12, 13\}$  for p = T. GICC tuples for clause b are: no feasible pair for p = F;  $\{1, 2, 3, 4, 9\} \times \{5, 6, 7, 8, 13\}$  for p = T. GICC tuples for clause c are: (14,16) for p = F;  $\{1, 2, 5, 6, 9, 10\} \times \{3, 4, 7, 8, 11, 12\}$  for p = T. GICC tuples for clause d are: (15,16) for p = F;  $\{1, 3, 5, 7, 9, 11\} \times \{2, 4, 6, 8, 10, 12\}$  for p = T.

(h) RICC tuples for clause a are: no feasible pair for p = F; (1,9), (2,10), (3,11), (4,12), (5,13) for p = T. RICC tuples for clause b are: no feasible pair for p = F; (1,5), (2,6), (3,7), (4,8), (9,13) for p = T. RICC tuples for clause c are: (14,16) for p = F; (1,3), (2,4), (5,7), (6,8), (9,11), (10,12) for p = T. RICC tuples for clause d are: (14,16) for p = F; (1,2), (3,4), (5,6), (7,8), (9,10), (11,12) for p = T.

Solution for (x),  $p = (a \wedge b) \vee (b \wedge c) \vee (a \wedge c)$ 

## Solution (Instructor only):

- (a) Clauses are a, b, c.
- (b) All three answers are equivalent and can be expressed in a couple of different ways:

$$p_a = b \wedge \neg c \vee \neg b \wedge c$$

$$p_b = a \land \neg c \lor \neg a \land c$$

$$p_c = a \wedge \neg b \vee \neg a \wedge b$$

or with an exclusive or:

$$p_a = b \oplus c$$

$$p_b = a \oplus c$$

$$p_c = a \oplus b$$

(c) Note: Blank cells represent values of 'F'.

	a	b	$\mid c \mid$	p	$p_a$	$p_b$	$p_c$
1	T	T	T	T			
2	T	T	F	T	T	T	
3	T	F	T	$\mid T \mid$	T		T
4	T	$\overline{F}$	F			T	T
5	F	T	T	T		T	T
6	F	T	F		T		T
$\gamma$	F	F	T		T	T	
8	F	F	F				

- (d) GACC pairs for clause a are:  $\{2,3\} \times \{6,7\}$ .
  - GACC pairs for clause b are:  $\{2,5\} \times \{4,7\}$ .
  - GACC pairs for clause c are:  $\{3,5\} \times \{4,6\}$ .
- (e) CACC pairs for clauses a, b, and c are the same as GACC pairs.
- (f) RACC pairs for clause a are: (2,6), (3,7).
  - RACC pairs for clause b are: (2,4),(5,7).
  - RACC pairs for clause c are: (3,4), (5,6).
- (g) GICC tuples for clause a are: (4,8) p = F; (1,5) for p = T.
  - GICC tuples for clause b are: (6,8) p = F; (1,3) for p = T.
  - GICC tuples for clause c are: (7,8) p = F; (1,2) for p = T.
- (h) RICC tuples for a, b, and c are same as GICC tuples.