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Texture classification using spline, wavelet decomposition and fractal dimension

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To cite this article:

Saad Al-Momen, Loay E. George, Raid K. Naji. Texture Classification Using Spline, Wavelet Decomposition and Fractal Dimension. *Applied and Computational Mathematics*. Vol. 4, No. 1, 2015, pp. 5-10. doi: 10.11648/j.acm.20150401.12

Abstract: Feature extraction is an important process for texture classification. This paper suggests two sets of features for texture analysis. In the first set of features, a set of fractal features is obtained from the eight wavelet sub-bands that are generated by applying Haar wavelet transform twice times according to dyadic architecture. The fractal features are determined using the differential box counting method. While for determining the second set of features, the cubic spline representation is applied to decompose the image signal into rough and smooth components; then applying the wavelet transform and finally compute the fractal dimension for all the sub-bands of both images. Each type of these two extracted feature sets is studied individually, and they are used together. Their overall performance is investigated. The proposed features set has been applied on two texture datasets, one consists of textures with directional properties, and the second set consists of textures samples that have directional attributes. The test results showed that the proposed methods give a high level of classification with images that have or do not have directional properties.

Keywords: Texture Classification, Texture Analysis, Fractal, Wavelet Features, Cubic Spline

1. Introduction

Texture is an important characteristic for analysis of many types of images. It is presented in many real as well as synthetic data (e.g.; clouds, trees, bricks, hair, fabric, etc). Despite its importance and ubiquity in image data, still a formal approach or definition of texture analysis does not exist [1]. Also, there is no formal definition of texture exists; different people define the texture depending upon the particular application. Some are perceptually motivated and others are driven completely by the application in which the definition will be used [2].

One immediate application of image texture analysis is the recognition of image regions using texture properties. Texture in this sense forms an important visual cue in identifying various types of homogeneous regions; this is known as texture classification. The goal of texture classification is to produce a classification map of the input image where each uniform textured region is identified with the texture class to which it belongs [2].

Texture classification techniques are grouped into five main groups, in general, namely: (i) structural, (ii) statistical,

(iii) signal processing, (iv) model-based stochastic and (v) morphology-based methods [3]. Most of them consist of two successive stages: feature extraction and feature-based classification [4]. For classification purpose different sets of texture features are obtained using different measures; and each can be used individually or in combination with each other.

1.1. Wavelet

Signal wavelet decomposition using Discrete Wavelet Transform (DWT) provides an alternative to the Discrete Fourier Transform (DFT) for signal analysis resulting in signal decomposition into two-dimensional functions of time and scale. The main benefit of DWT over DFT is in its multi-resolution time-scale analysis ability [5].

Haar wavelet transform (HWT) is the simplest decomposition process. For a specific image signal matrix (x) of the form

$$x = \begin{bmatrix} a & b \\ c & d \end{bmatrix} \quad (1)$$

Then, its Haar wavelet is:

$$y = \frac{1}{2} \begin{bmatrix} a+b+c+d & a-b+c-d \\ a+b-c-d & a-b-c+d \end{bmatrix} \quad (2)$$

These operations correspond to the following filtering processes:

LL: Top left: 2-D lowpass filter (Lo-Lo),

HL: Top right: horizontal highpass and vertical lowpass filter (Hi-Lo),

LH: Lower left: horizontal lowpass and vertical highpass filter (Lo-Hi),

HH: Lower right: 2-D highpass filter (Hi-Hi).

To apply this transform on the complete image, we group the pixels into 2×2 blocks and then apply Equation (1) on each block [6]. The LL-subband output from any stage can be decomposed further. Figure 1 below shows the result of one and two levels HWT based on the pyramid decomposition [7].

Wavelet transform had been very popularly used for classification. It is often used together with other methods to create a process that can best identify the required features [8]. Tou, Tay, and Lau [9] gave a review for the recent trends in texture classification and they showed that the information on the frequency domain is usually more stable than the spatial domain. Therefore, they often produce better features that lead to a higher accuracy despite being more complex and slower.

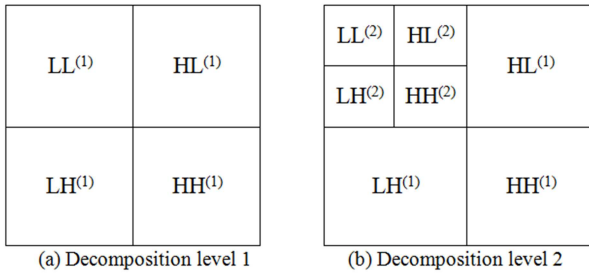


Fig 1. Pyramid decomposition using Haar wavelet filter

1.2. Fractal

Fractal dimension has the ability of distinguish texture by its roughness, different fractal texture classification and segmentation algorithms proposed during the last decades for many applications [4, 8, 10-15].

Several fractal models have been used to estimate the fractal dimension [16-21]. Differential Box Counting (DBC) method is one of the most popular methods that has been used widely to calculate the fractal dimension of images. Long and Peng [22] showed that, most of the existing box-counting methods for measuring fractal features are only applicable to square images or images with each dimension equal to the power of 2 and they require that the box at the top of the box stack of each image block is of the same height as that of other boxes in the same stack, which gives rise to inaccurate estimation of fractal dimension. They propose a more accurate box-counting method for images of arbitrary size, which allows the height of the box at the top of each grid block to be adaptable to the maximum and minimum gray-scales of that block so as to circumvent the

common limitations of existing box-counting methods.

1.3. Cubic Spline

Cubic Spline method relies on constructing a smooth polynomial surface of low degree between small set of known data points. The spline consists of weights attached to a flat surface at the points to be connected [23-24]. This technique is used widely in image processing for interpolating and resampling images.

Practically, the image is divided into $M \times N$ blocks, each of size $b \times b$, where b is an odd number. Then:

1. For each row of blocks the centers of the blocks ($m_{i1}, m_{i2}, \dots, m_{iN}$) are used to construct the cubic splines which are used to approximate the gray level of the pixels among these centers.
2. Backward interpolation is used to approximate the gray level of the pixels between the left border and the first center in the line (m_{i1}).
3. Forward interpolation is used to approximate the gray level of the pixels between the last center in the line (m_{iN}) and the right border.
4. Steps 1, 2, and 3 are repeated for each line of blocks to get M centerline with known gray level value; see Figure 2.
5. Steps 1, 2, 3, and 4 are repeated to each column of pixels until the whole image are interpolated.

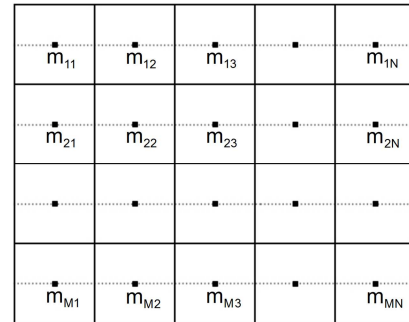


Fig 2. Image's blocked used for Cubic Spline interpolation

2. Features Extraction

Two set of features have been proposed to do classification of the images. The first classification feature set consists of the fractal dimensions of the multi-scale wavelet transform of the original image. While the second feature set consists of the fractal dimensions of the multi-scale wavelet transform of both the smooth and rough image components which are produced by decomposing the image signal into the smooth cubic spline surface and rough residue components.

2.1. Fractal-Wavelet Feature Set

Figure 3 shows that the original image, $I()$, is decomposed into 8 matrices using 2 levels Haar wavelet transform (HWT). Then the DBC method, suggested by Long and Peng [22], is used to calculate the fractal dimension FD of each one of these matrices in order to construct the feature vector F_1 .

$$F_1 = \{FD(LL_I^{(1)}), FD(HL_I^{(1)}), FD(LH_I^{(1)}), FD(HH_I^{(1)}), \\ FD(LL_I^{(2)}), FD(HL_I^{(2)}), FD(LH_I^{(2)}), FD(HH_I^{(2)})\} \quad (2)$$

So, F_1 consists of 8 values which represent the roughness of the texture at different frequencies and scales.

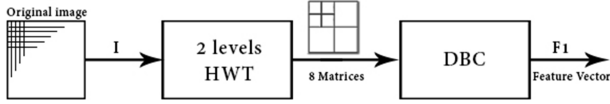


Fig 3. Fractal – wavelet technique

2.2. Rough – Smooth Technique

Figure 4 illustrates the scheme of determining the second feature set. Firstly, the cubic spline is applied on the original image, $I()$, to establish the smooth image component $S()$; then by subtracting the smooth image from the original one we will get the rough component $R()$, i.e.:

$$R(x,y) = S(x,y) - I(x,y) \quad \text{for } \forall x, y \quad (3)$$

The rough image component $R()$ contains all the coarse information of the texture image.

The 2D HWT is applied, separately, on both the smooth and the rough images to construct 16 matrices. Then the fractal dimension is calculated for each one of them using the DBC method suggested by Long and Peng [22]; to construct the feature vector F_2 ; so it consists of 16 features:

$$F_2 = \{FD(LL_S^{(1)}), FD(HL_S^{(1)}), FD(LH_S^{(1)}), FD(HH_S^{(1)}), \\ FD(LL_S^{(2)}), FD(HL_S^{(2)}), FD(LH_S^{(2)}), FD(HH_S^{(2)}), \\ FD(LL_R^{(1)}), FD(HL_R^{(1)}), FD(LH_R^{(1)}), FD(HH_R^{(1)}), \\ FD(LL_R^{(2)}), FD(HL_R^{(2)}), FD(LH_R^{(2)}), FD(HH_R^{(2)})\} \quad (4)$$

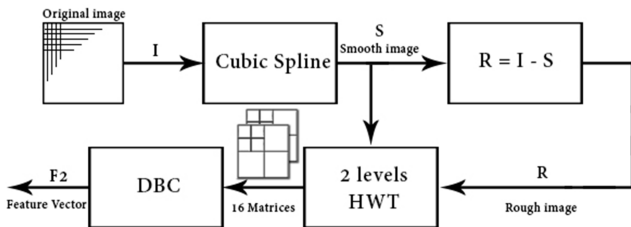


Fig 4. Rough – Smooth technique

3. Classifications

Classification is normally a two phase process. It requires an initial training phase during which the classifier is trained to recognize a class of reference feature vectors, and a testing (classification) phase during which unknown vectors are

classified according to a best match criterion, see Figure 5.

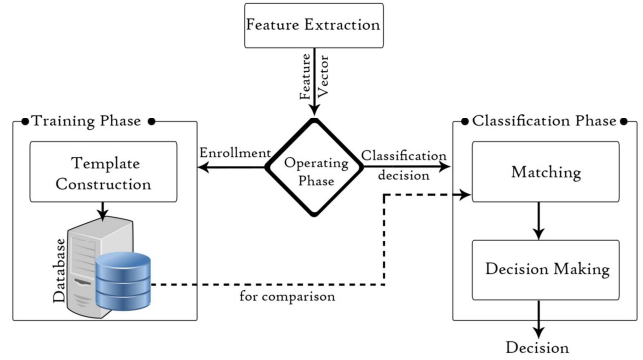


Fig 5. Training and classification phases

During the training phase, three templates are constructed for each class to cope over the variability of the images in each class. The conducted experiments showed that using one or two templates may not always enough for efficient classification. In this paper, three initial templates have been chosen as: (i) IC_1 , which is the mean feature vector of all the feature vectors extracted from the training samples belong to the class, (ii) IC_2 , the farthest feature vector to IC_1 , and (iii) IC_3 , the farthest feature vector to both IC_1 and IC_2 . Then the K-means algorithm is used to improve the values of these initial templates [25].

Commonly, Euclidean distance measure is used to match the similarity. But, one weakness of the basic Euclidean distance function is that if one of the input features has a relatively large range, then it can overpower the other features. Since the problem here is the used features are not isotropic; that is, every feature may not have similar behaviors. So, the normalized Euclidean distance has been used to evaluate the similarity degree between the extracted feature vector of the tested sample, and the templates representing certain class [26]:

$$d(T^i, F^j) = \sum_{k=1}^K \frac{(T_k^i - F_k^j)^2}{\sigma_k} \quad (5)$$

where T_k^i is the template value of k^{th} feature that belong to i^{th} class; F_k^j is the value of k^{th} feature extracted from j^{th} sample; σ_k is the standard deviation over the sample set.

As mentioned above, the matching process uses three templates per class, in order to maximize the probability of true match classification and minimize the misclassification. The efficiency of classification is calculated for each distance using the following equation [1]:

$$\eta(\%) = \frac{\text{Total no. of samples} - \text{No. of misclassified samples}}{\text{Total no. of samples}} \times 100\% \quad (6)$$

4. Experimental Results

To demonstrate the efficiency of the proposed classification system, two different dataset are used, where both of them were selected from the Brodatz album [27]. The

first dataset is that used by Al-Momen, George, and Naji [25], which consists of different types of woven fabrics as shown in Figure 6. Twenty two different texture images having size of 512 x 512 with 8-bit grey levels were selected to define twenty two classes. While the second dataset is that used by Al-Kadi [10], consists of eight classes as shown in Figure 7.

For each dataset, each image defines a separate class; and

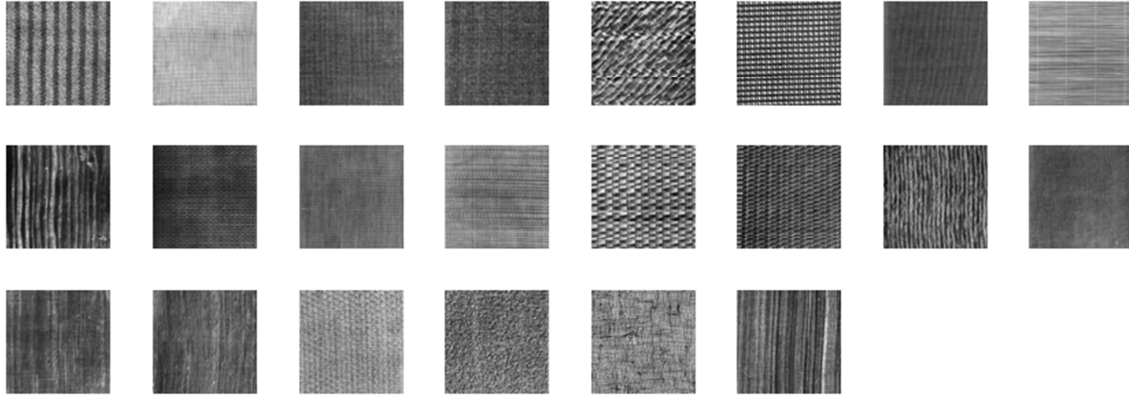


Fig 6. Dataset #1: Twenty two different Brodatz texture showing up to bottom and from left to right: D11, D14, D16, D17, D18, D20, D21, D49, D50, D52, D53, D55, D56, D65, D76, D77, D78, D79, D82, D84, D104 and D105.

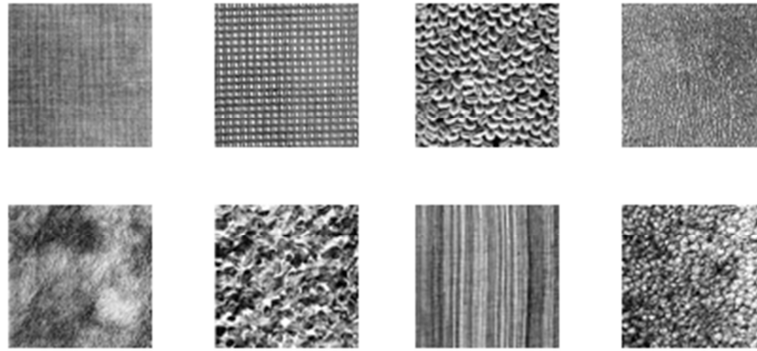


Fig 7. Dataset #2: Eight different Brodatz texture images showing from up to bottom and from left to right: herringbone cloth (D16), canvas (D20), coffee beans (D74), calf leather (D24), fur (D93), quartz (D98), cheese cloth (D106) and plastic bubbles (D112).

Table 1 shows the percentage of correctly classified samples of all the tested samples for dataset #1 under the use of the fractal – wavelet technique (F_1), the rough–smooth technique (F_2), and the two features sets together $\{F_1, F_2\}$. While, Table 2 shows the same results for the eight classes of

dataset #2.

By using the two features sets together, i.e. $\{F_1, F_2\}$, the overall classification for dataset #1 is slightly lower than that obtained by Al-Momen, George, and Naji [25], but it is higher than that obtained by Al-Kadi [10].

Table 1. The percentage of correctly classified samples under F_1 , F_2 , and $\{F_1, F_2\}$ for dataset #1

Class no.	Class Name	Fractal – Wavelet Technique F_1		Rough –Smooth Technique F_2		The two techniques together $\{F_1, F_2\}$	
		Training	Testing	Training	Testing	Training	Testing
01	D11	98	91.4286	100	97.1429	100	99.4286
02	D14	92	84	100	94.8571	100	98.2857
03	D16	100	100	86	100	100	100
04	D17	100	100	98	98.8571	100	100
05	D18	90	86.2857	100	86.8571	98	91.4286
06	D20	100	99.4286	100	96.5714	100	100
07	D21	100	100	90	99.4286	100	100
08	D49	100	100	98	100	100	100
09	D50	84	76.5714	92	71.4286	90	87.4286
10	D52	100	97.7143	100	100	100	100
11	D53	100	98.2857	96	99.4286	100	98.8571

Class no.	Class Name	Fractal – Wavelet Technique F_1		Rough –Smooth Technique F_2		The two techniques together $\{F_1, F_2\}$	
		Training	Testing	Training	Testing	Training	Testing
12	D55	88	90.8571	100	91.4286	98	97.1429
13	D56	98	95.4286	100	87.4286	98	98.8571
14	D65	100	96	98	92.5714	100	100
15	D76	98	95.4286	92	89.7143	100	97.1429
16	D77	100	100	100	100	100	100
17	D78	94	96.5714	100	97.7143	96	98.8571
18	D79	100	98.8571	100	98.2857	100	99.4286
19	D82	100	99.4286	86	98.2857	100	100
20	D84	82	89.7143	98	86.2857	96	97.1429
21	D104	100	94.8571	100	97.7143	100	98.8571
22	D105	100	100	100	100	100	100
Overall		96.5455	95.0390	96.7273	94.7273	98.9091	98.3117

Table 2. The percentage of correctly classified samples under F_1 , F_2 , and $\{F_1, F_2\}$ for dataset #2

Class no.	Class name	Fractal – Wavelet Technique F_1		Rough –Smooth Technique F_2		The two techniques together $\{F_1, F_2\}$	
		Training	Testing	Training	Testing	Training	Testing
01	D16	100	99.4286	100	100	100	100
02	D20	100	99.4286	100	100	100	99.4286
03	D74	100	100	94	97.7143	100	100
04	D24	98	96	94	83.4286	100	97.7143
05	D93	98	95.4286	96	95.4286	100	100
06	D98	98	93.7143	94	78.2857	96	91.4286
07	D106	98	100	100	97.7143	100	100
08	D112	92	94.2857	98	93.7143	100	98.8571
Overall		98	97.2857	97	93.2857	99.5	98.4286

5. Conclusion

In this paper, the fractal based features are extracted from the 2-level decompositions of the original image, in addition to that of the rough and smooth images produced by the cubic spline method. The combined features improved the overall classification accuracy.

The experimental results showed the suitability of the proposed system for the texture with or without directional properties.

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