Event-B Course

3. A Mechanical Press Controller

Jean-Raymond Abrial

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Outline

1. Informal presentation of the example
2. Presentation of some design patterns
3. Writing the requirement document
4. Proposing a refinement strategy
5. Development of the model using refinements and design patterns

1. Informal Presentation of the Example

Presentation of the Example

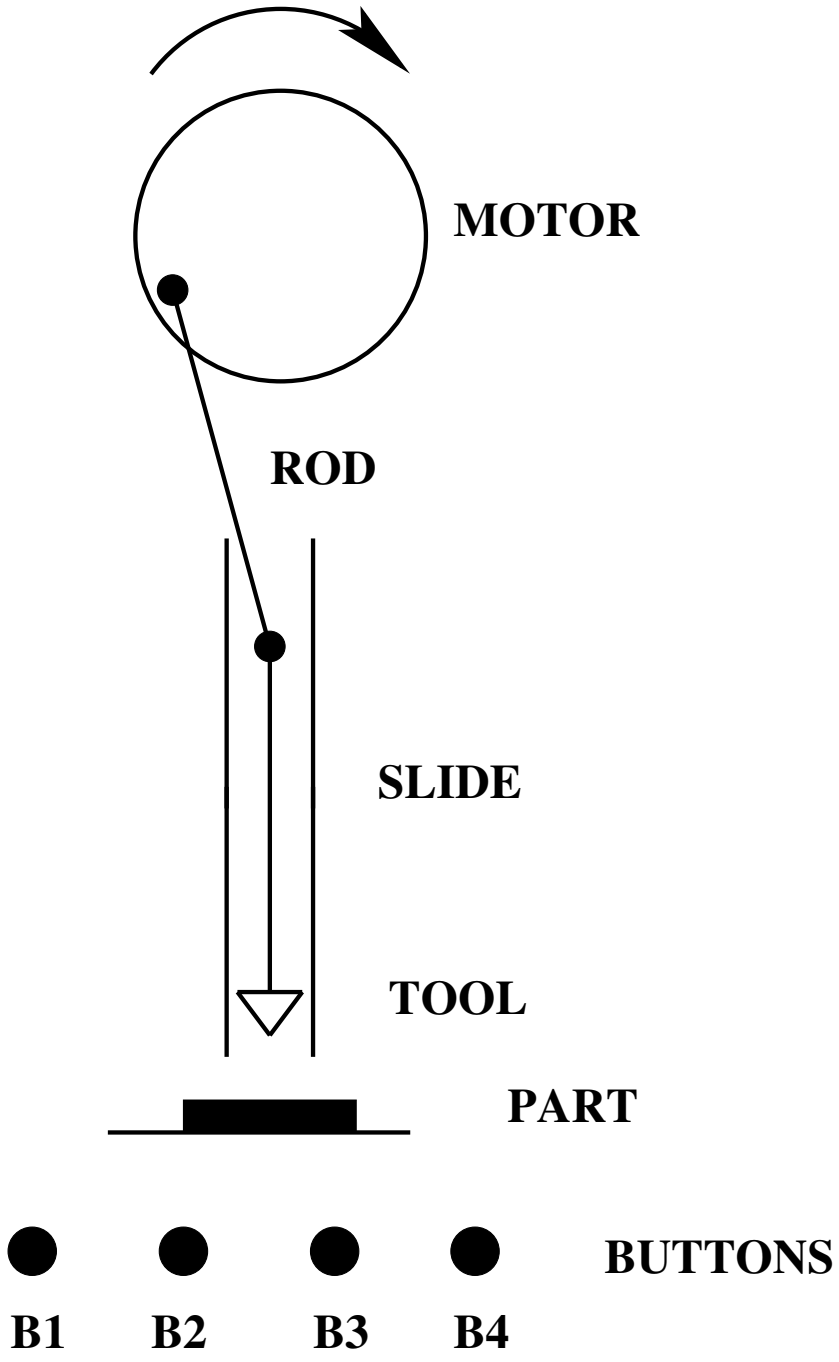
- A mechanical press controller

- Adapted from a real system

- The real system is coming from INRST:

  Institut National de la Recherche sur la Sécurité du Travail

Mechanical Press Schema



Basic Equipment

- A Vertical Slide with a tool at its lower extremity

- An electrical Rotating Motor

- A Rod connecting the motor to the slide.

- A Clutch engaging or disengaging the motor on the rod

- When the clutch is disengaged, the slide stops “immediately”

Basic Commands

- Button B1: start motor

- Button B2: stop motor

- Button B3: engage clutch

- Button B4: disengage clutch

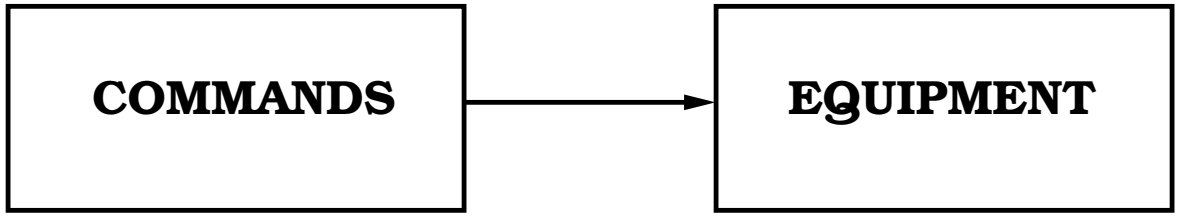
Basic User Actions

- Action 1: Change the tool at the lower extremity of the slide

- Action 2: Put a part to be treated under the slide

- Action 3: Remove the part

First Schematic View



A Typical User Session

1. start the motor (button B1)
2. change the tool (action 1)
3. put a part (action 2),
4. engage the clutch (button B3): the press now works,
5. disengage the clutch (button B4): the press does not work,
6. remove the part (action 3),
7. repeat zero or more times steps 3 to 6,
8. repeat zero or more times steps 2 to 7,
9. stop the motor (button B2).

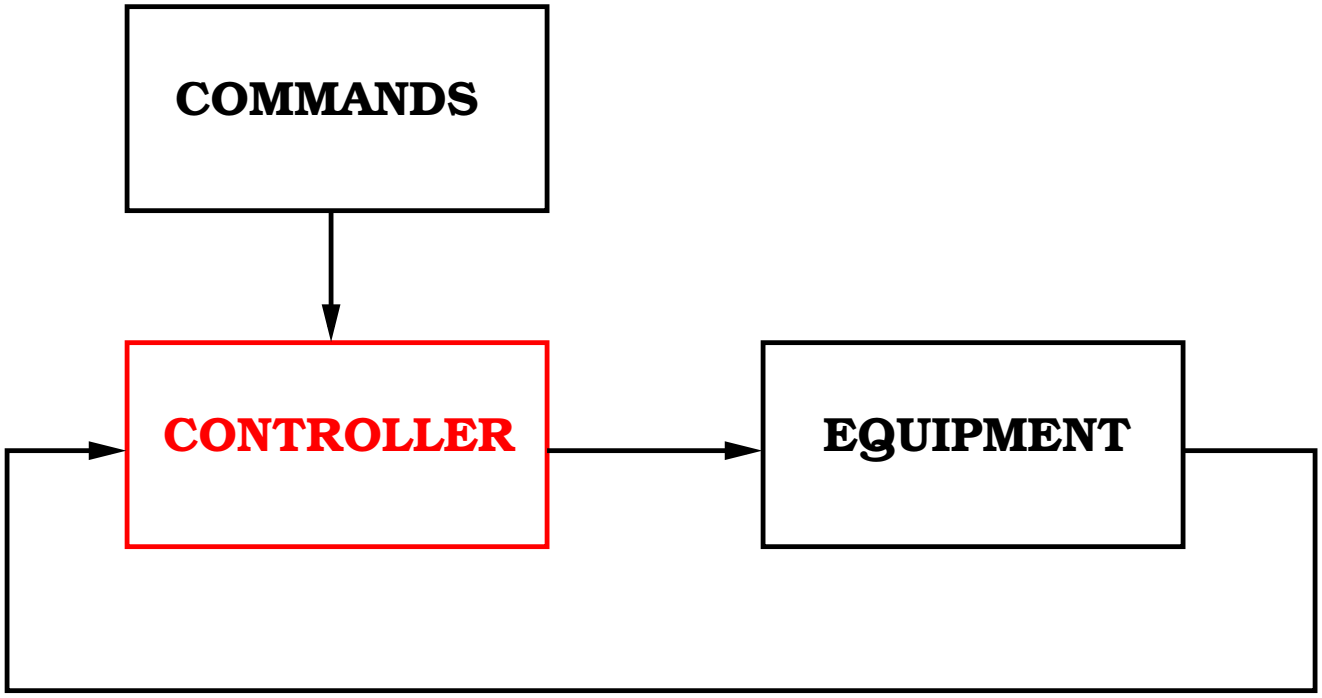
Danger: Necessity of a Controller

- step 2 (change the tool),

- step 3 (put a part),

- step 6 (remove the part) are all DANGEROUS

Second Schematic View

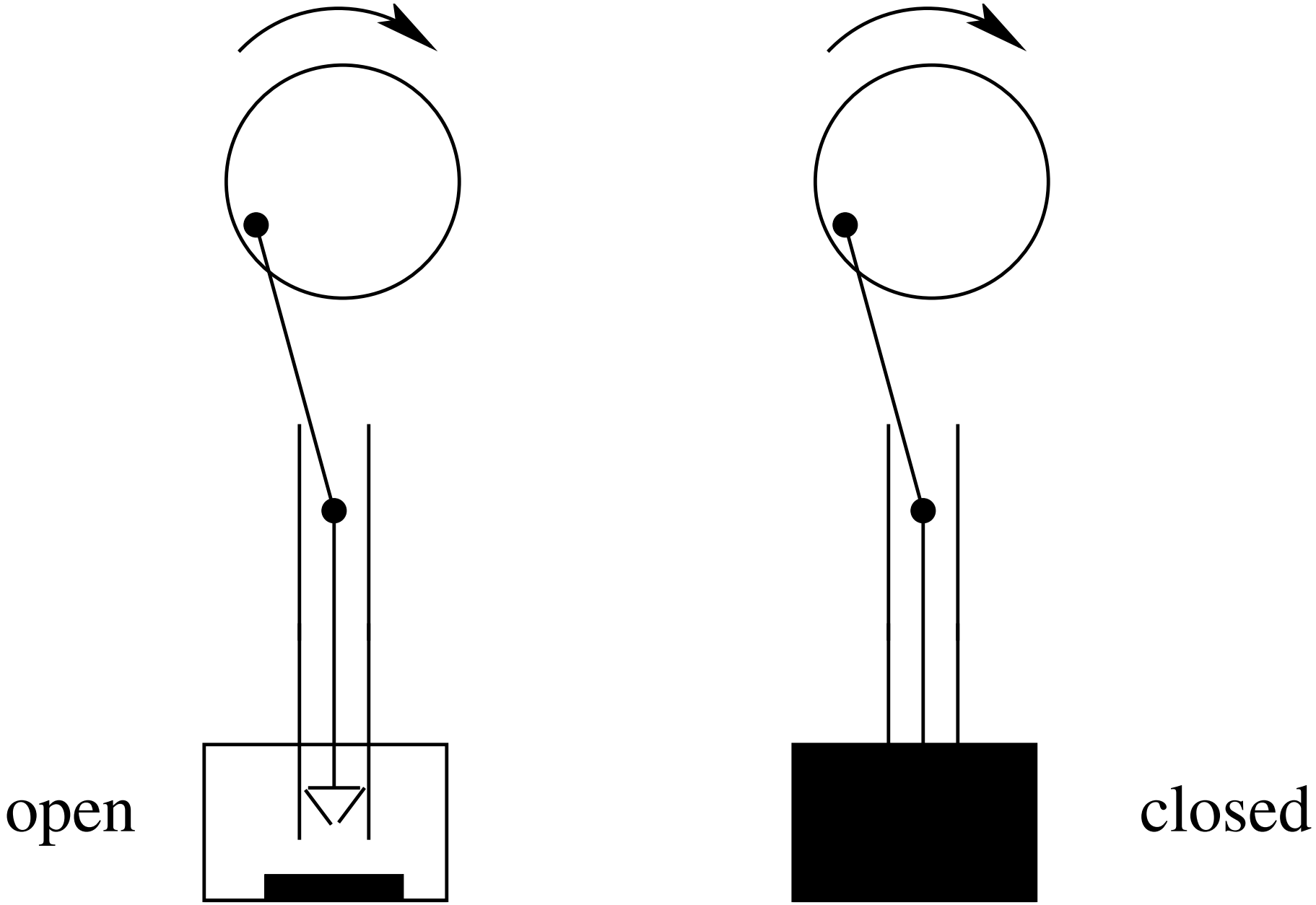


More Elaborate Commands for Protecting the User

- Controlling the way the clutch is engaged or disengaged

- Protection by means of a Front Door

The Front Door



The Front Door: Behavior

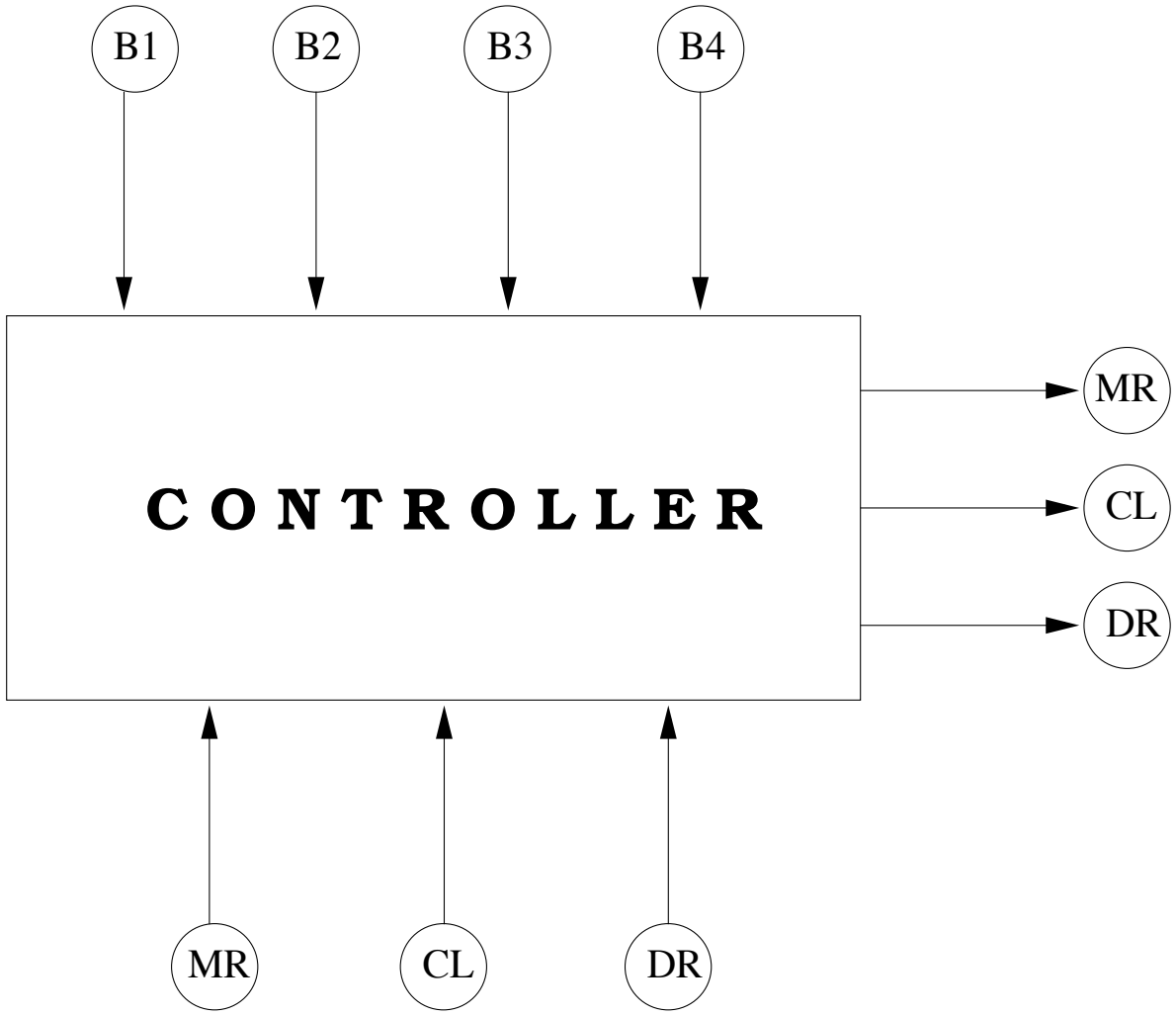
- Initially, the door is open

- When the user presses button B3 to engage the clutch,
  the door is first closed BEFORE engaging the clutch

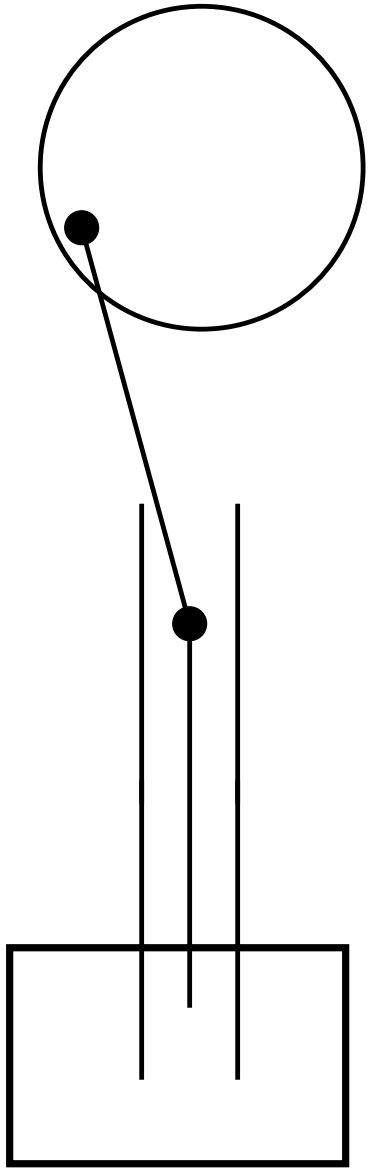
- When the user presses button B4 to disengage the clutch,
  the door is opened AFTER disengaging the clutch

- Notice: The door has no button.

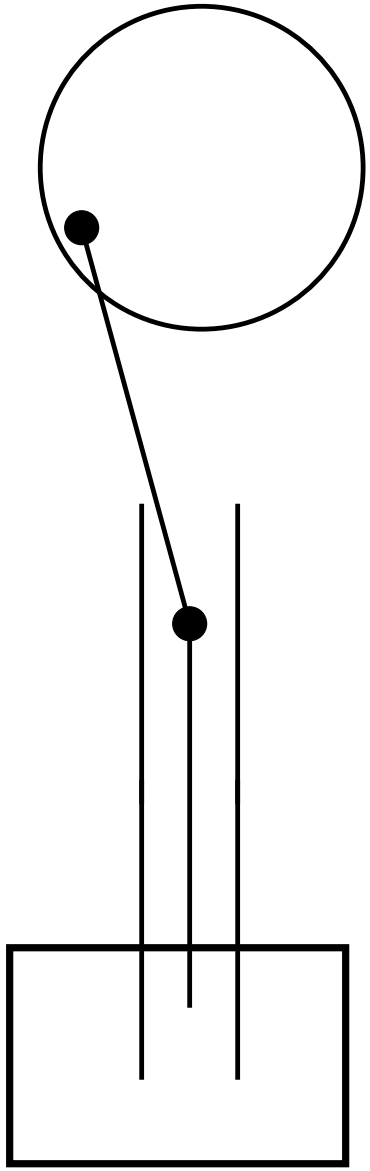
Summary of Connections



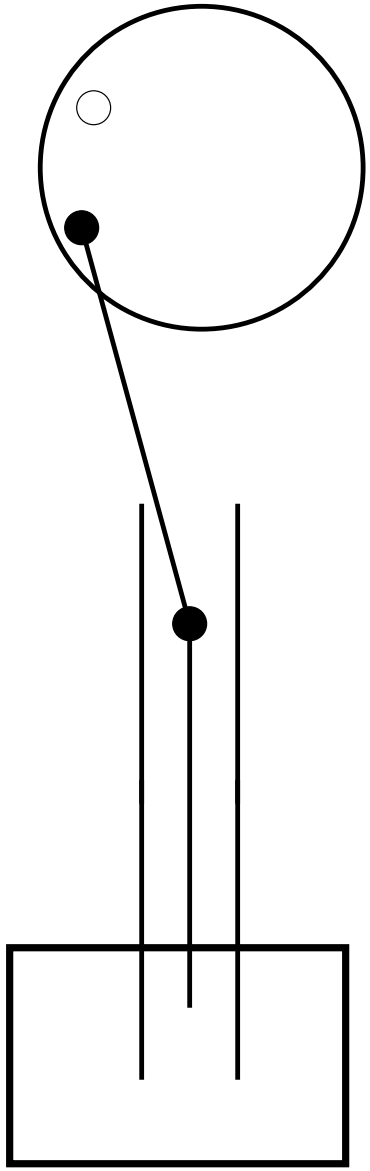
Initial Situation



Starting the Motor: Pressing Button B1



The Motor Works



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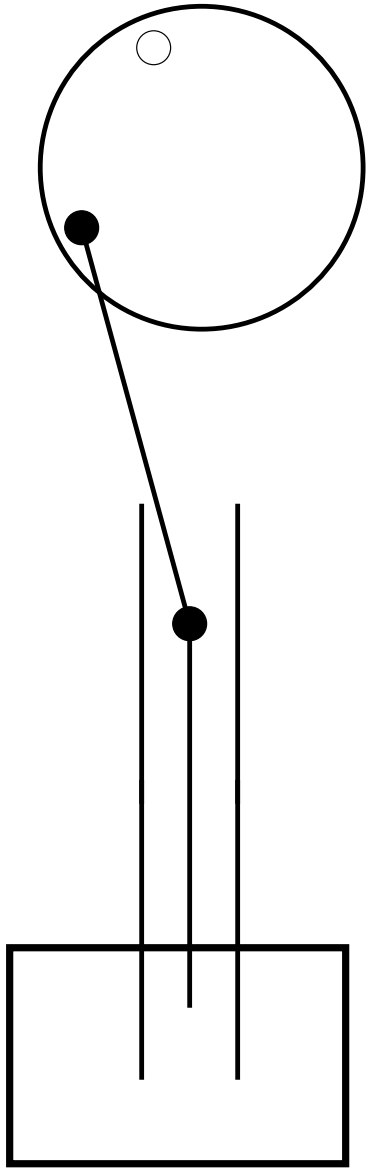

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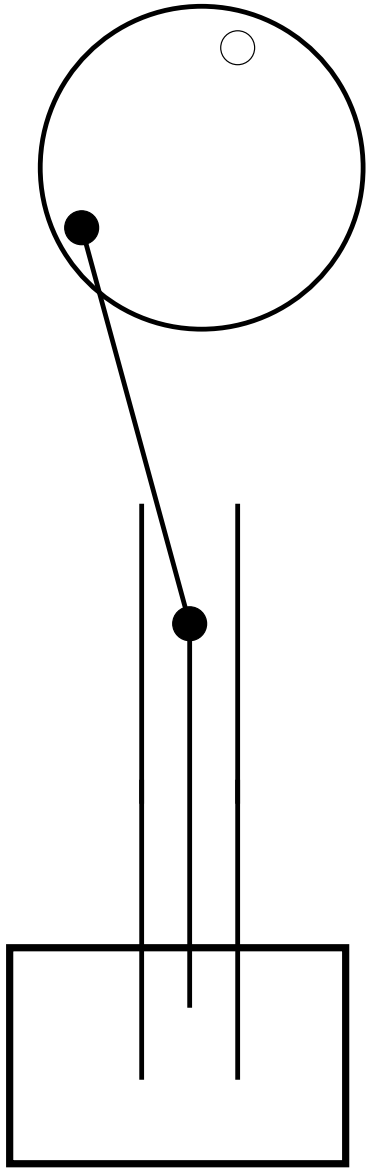
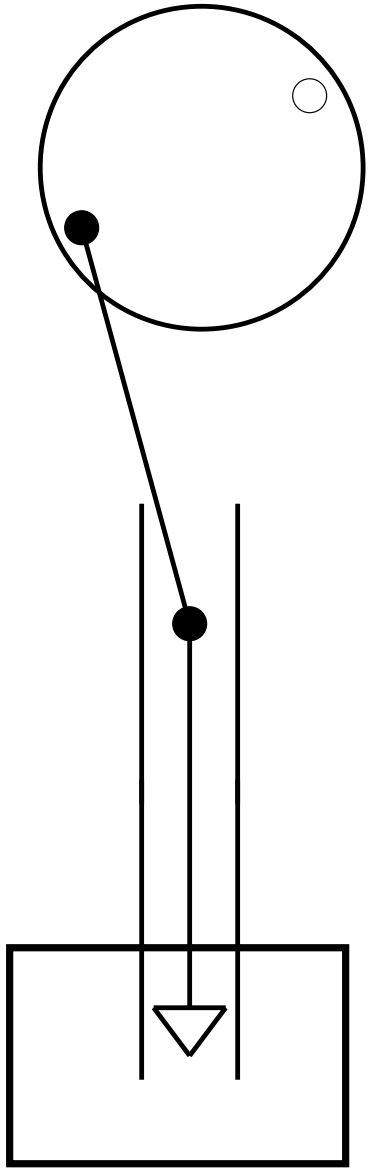


Adding a Tool



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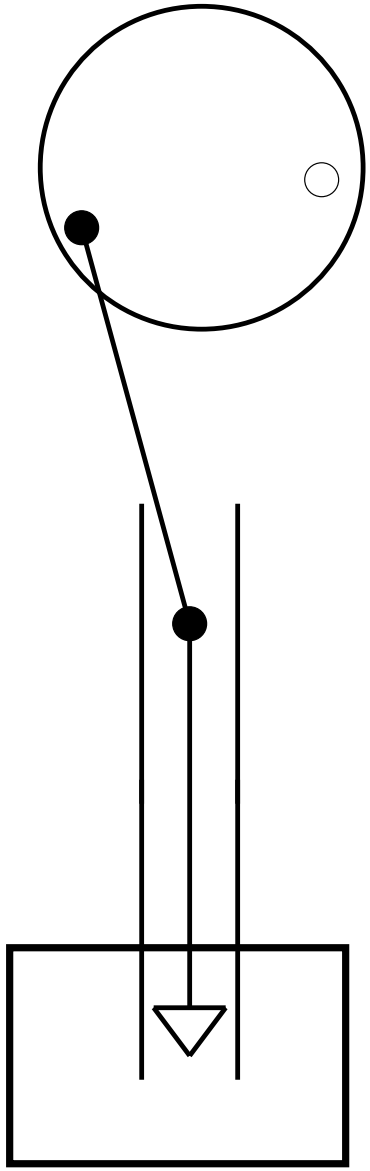
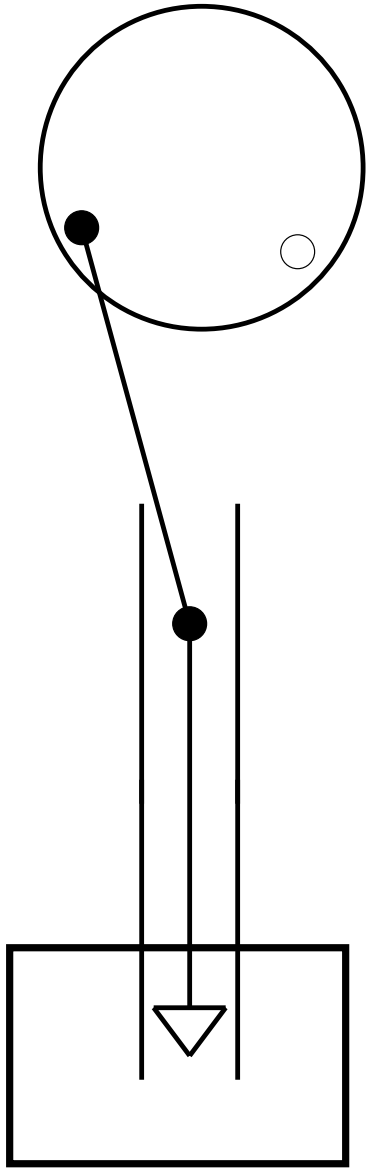
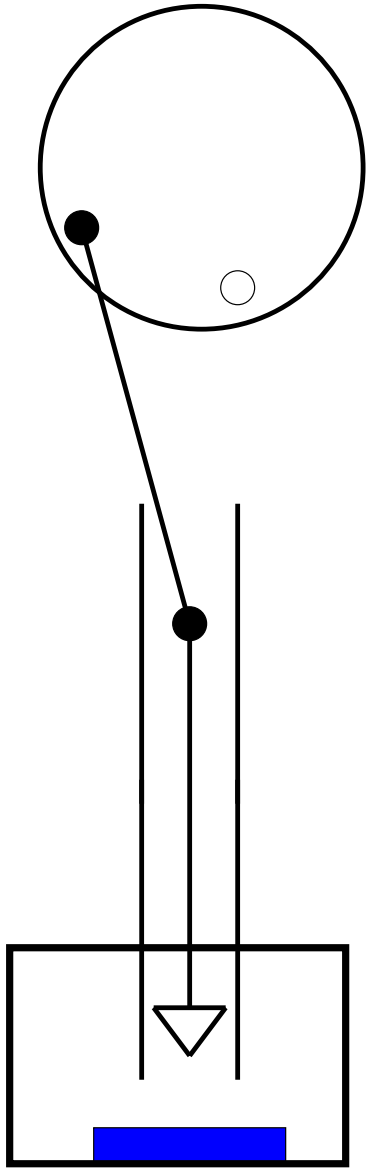




Putting a Part



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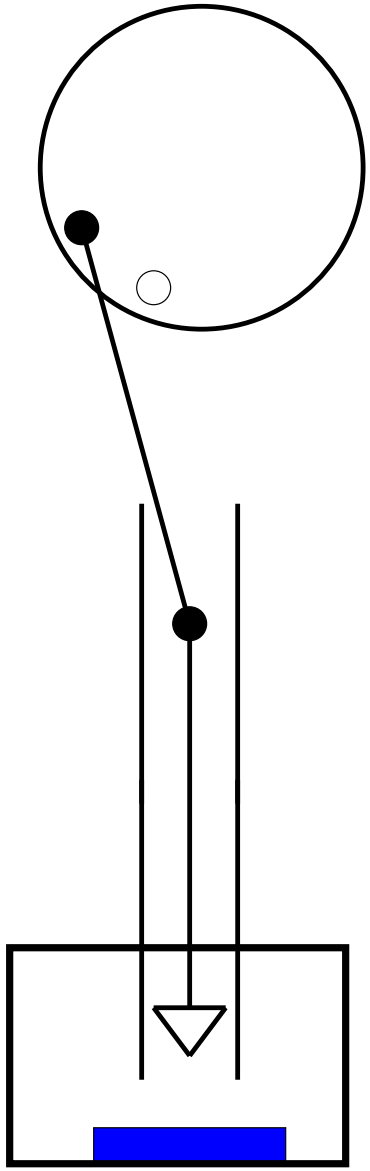

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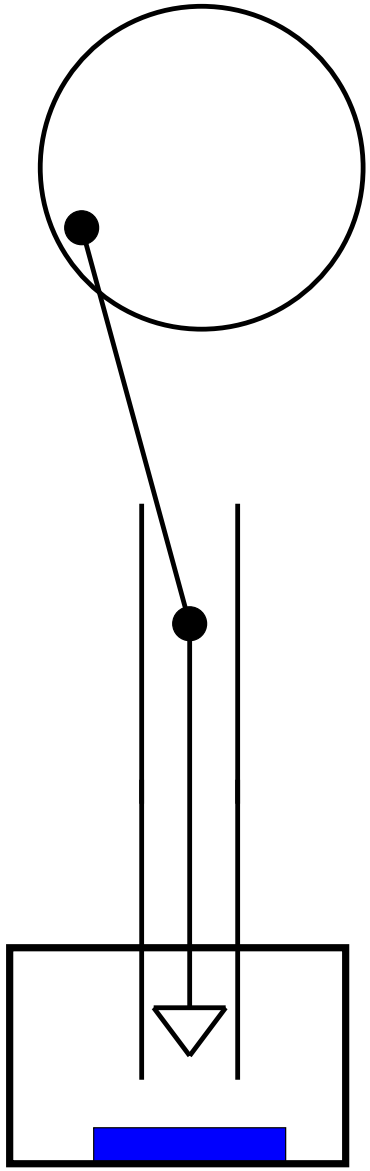

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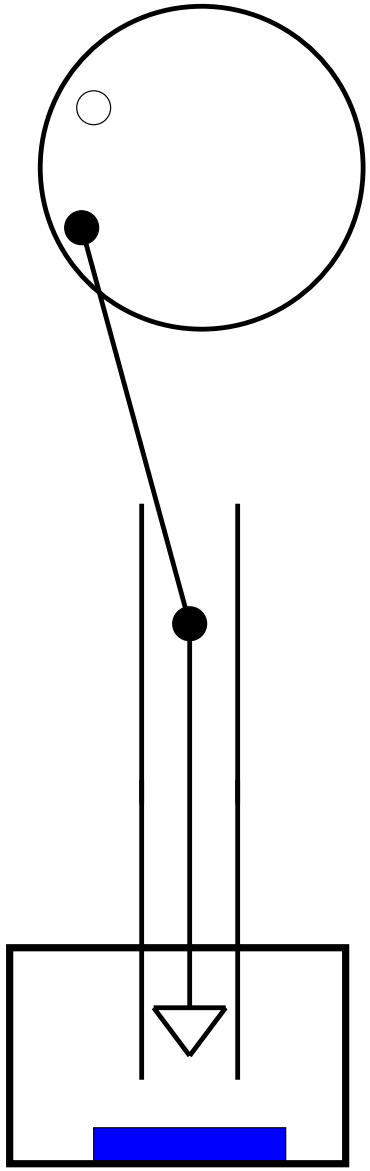

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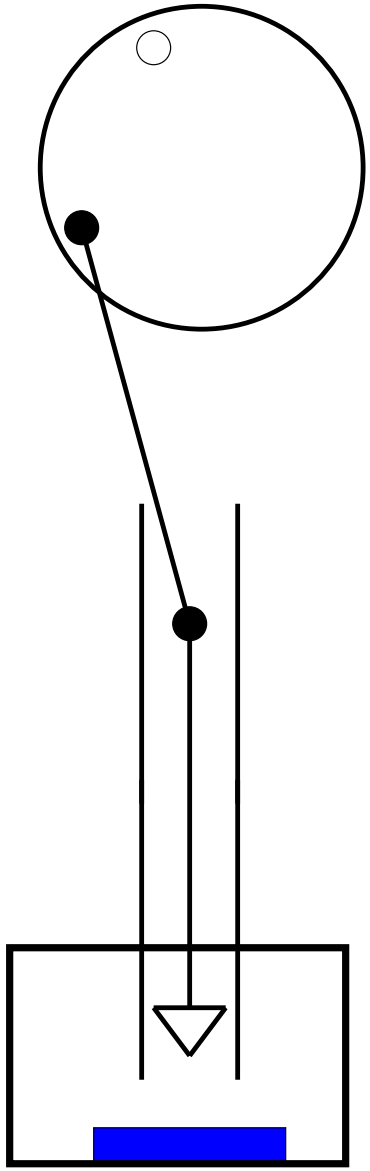

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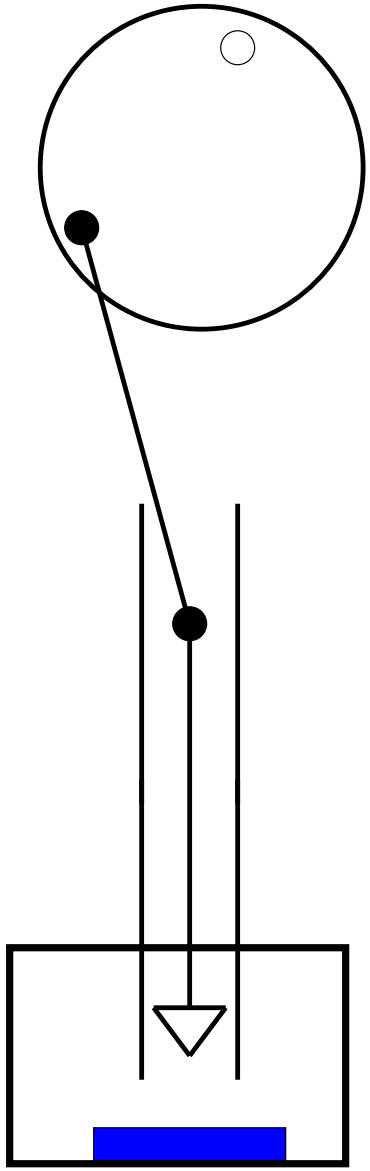

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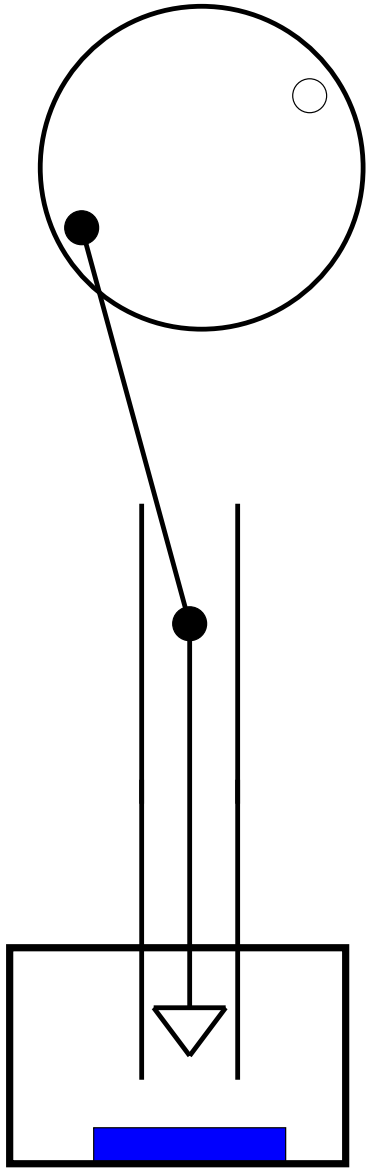

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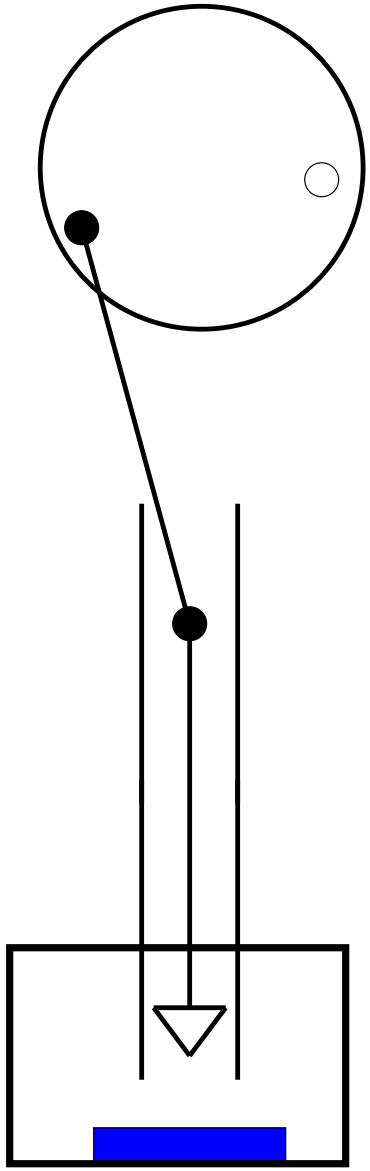

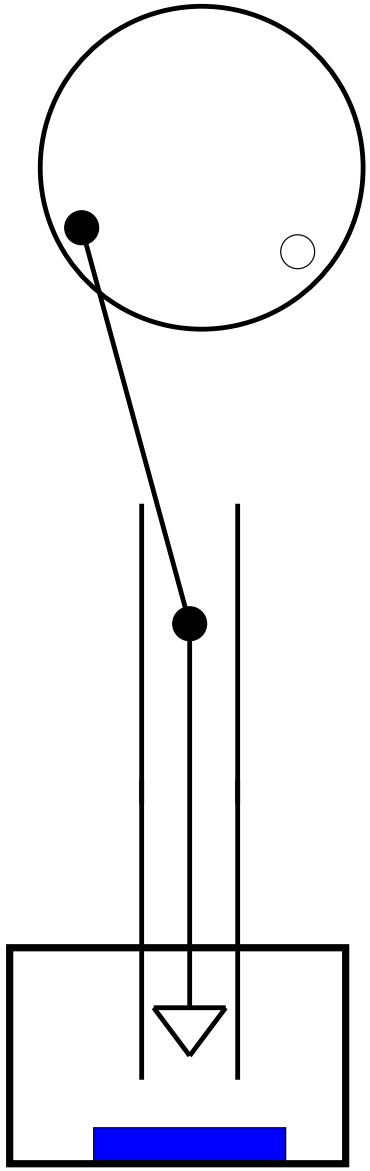

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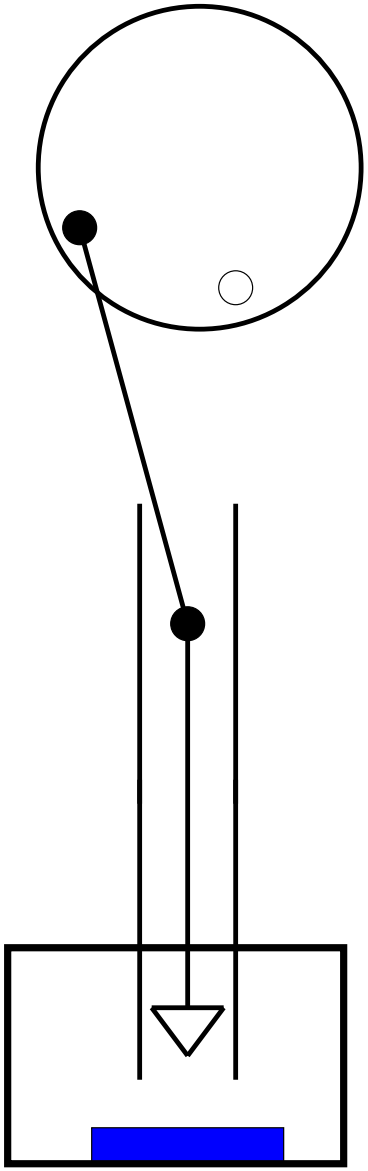

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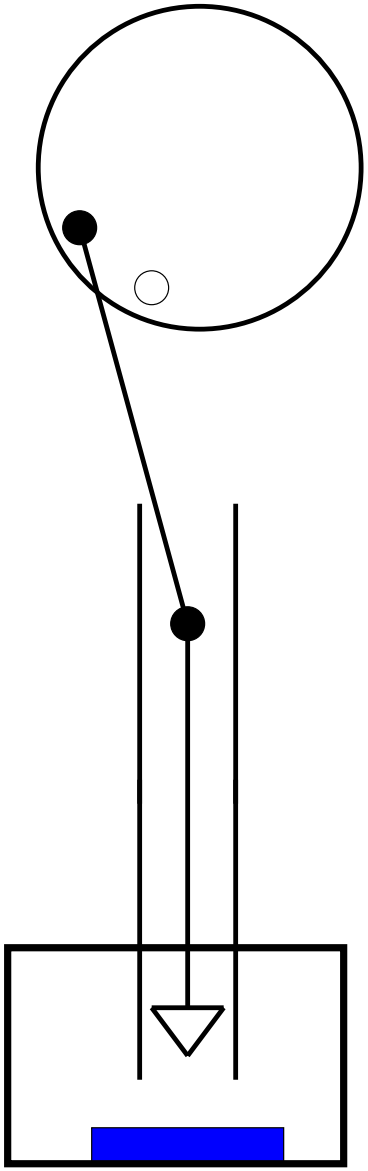
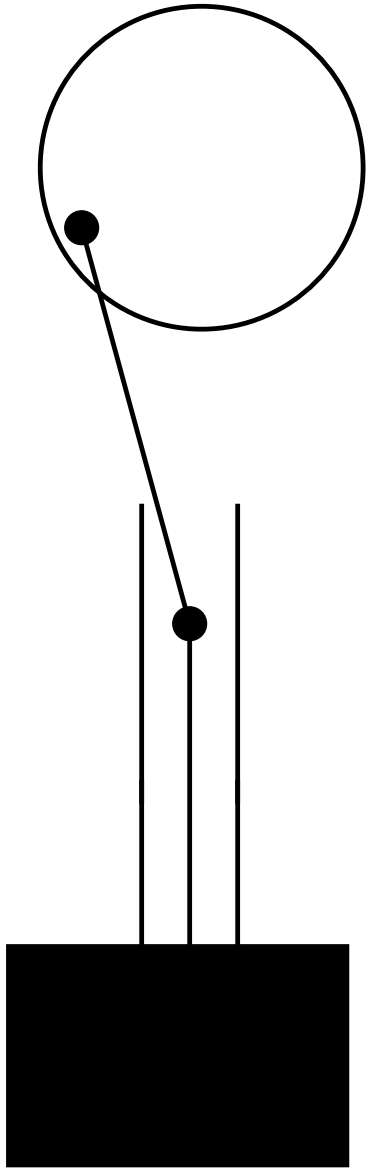


Engaging the Clutch: Pressing Button B3



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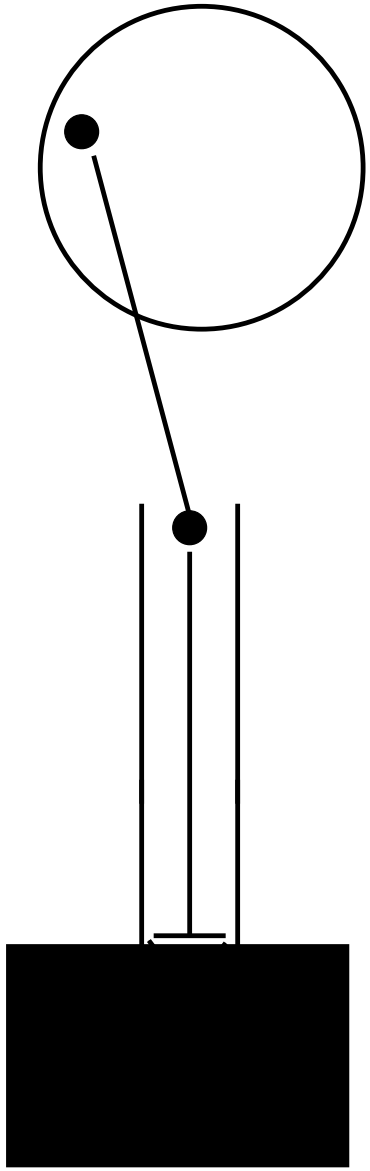

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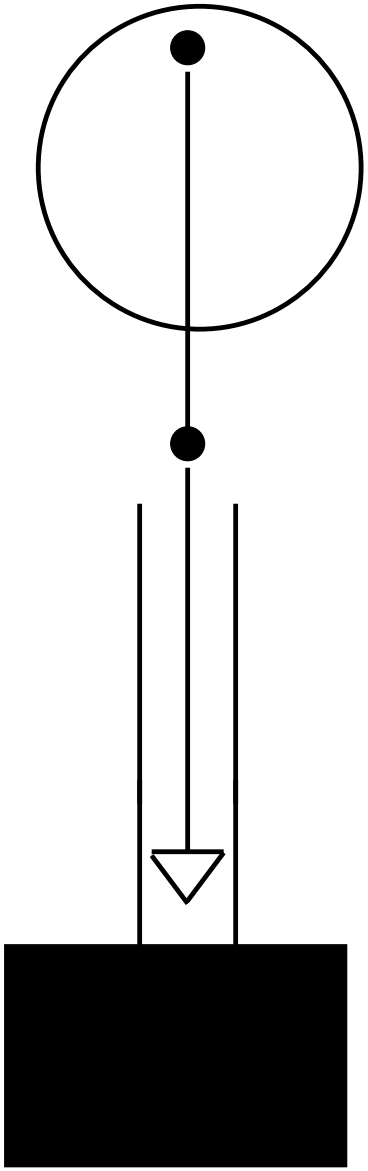

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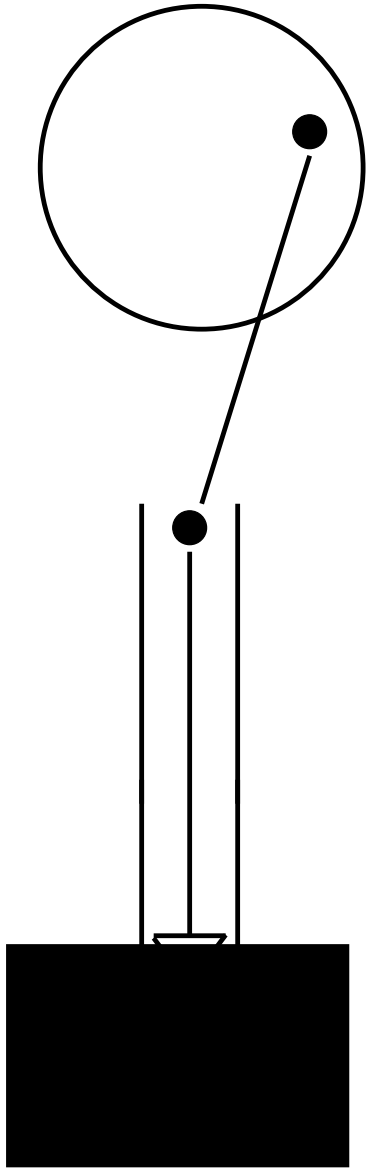

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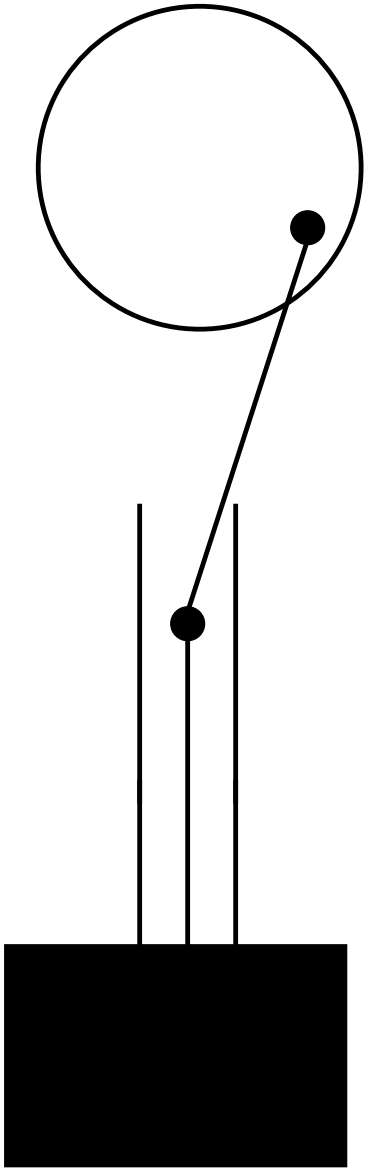

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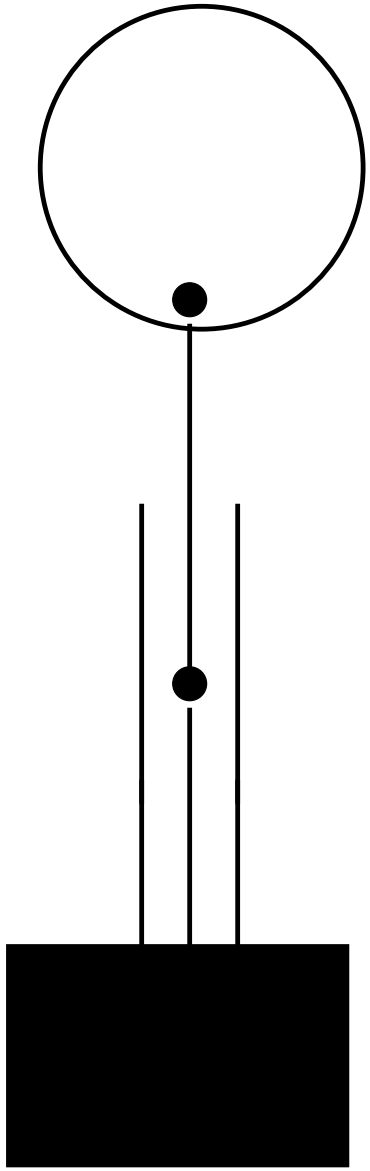

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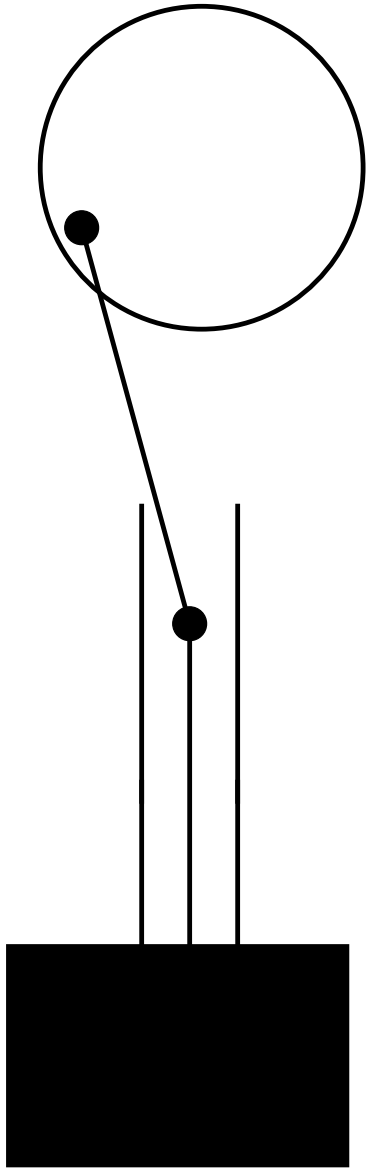

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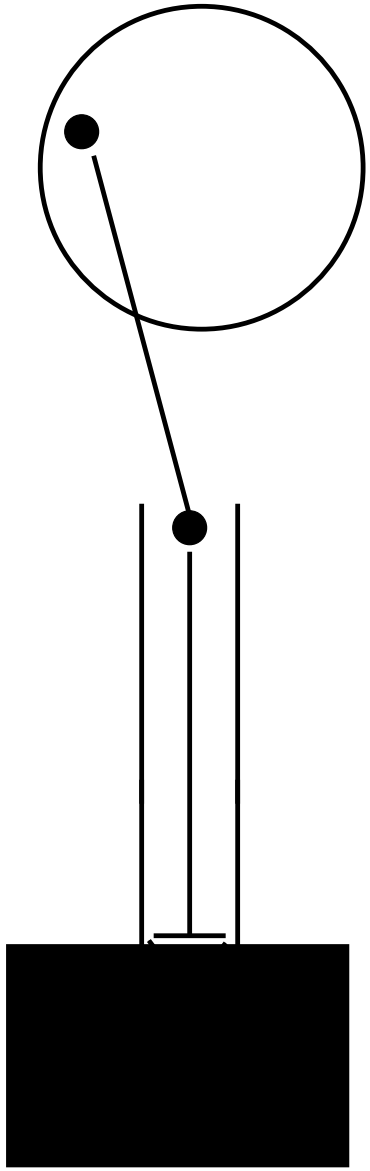

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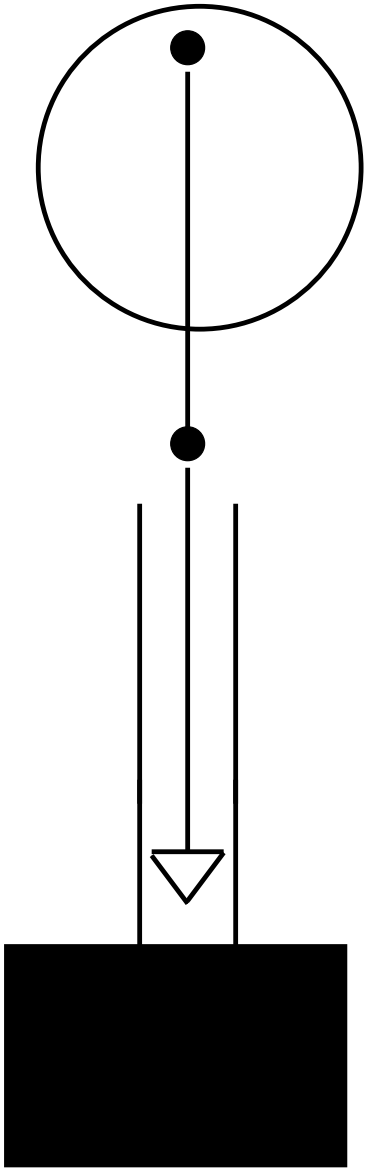

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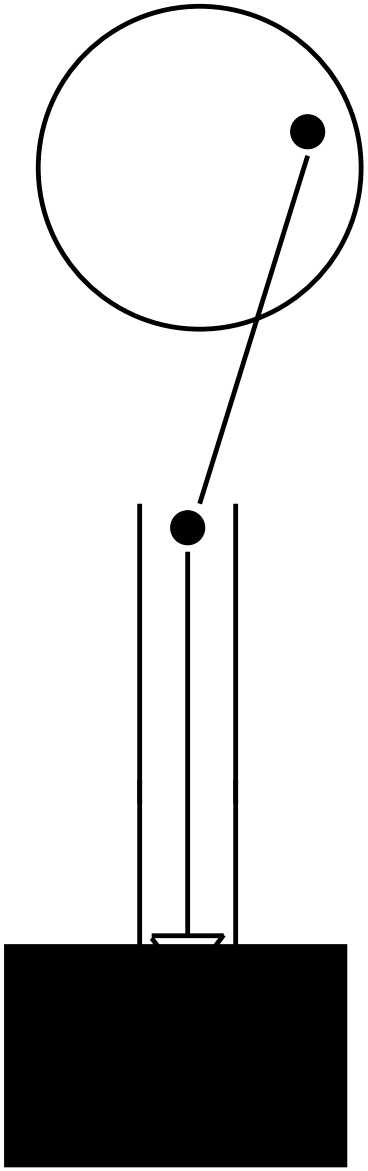

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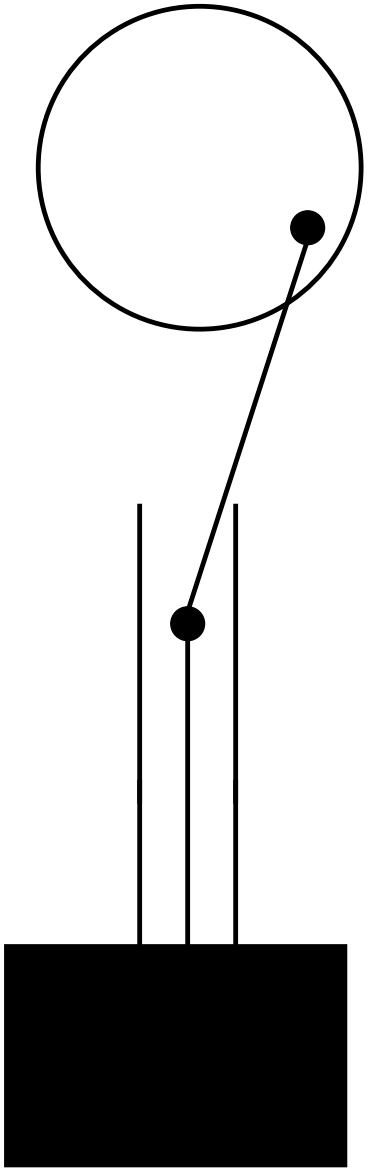

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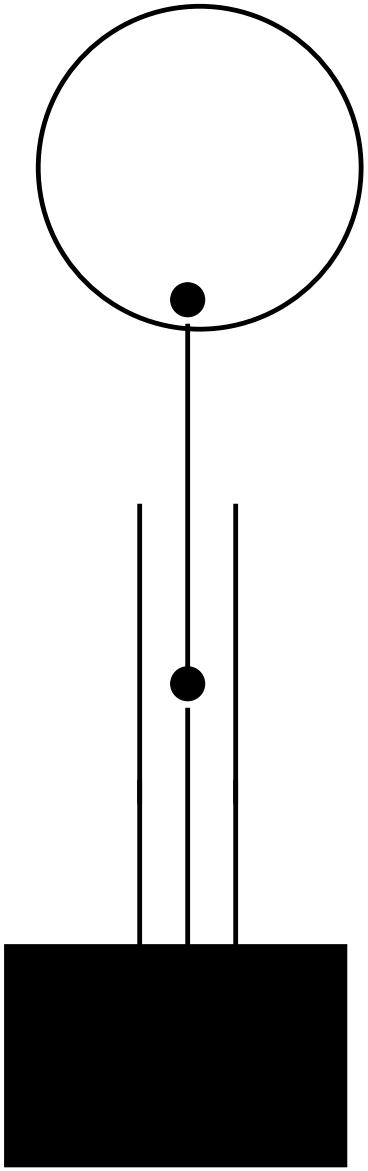

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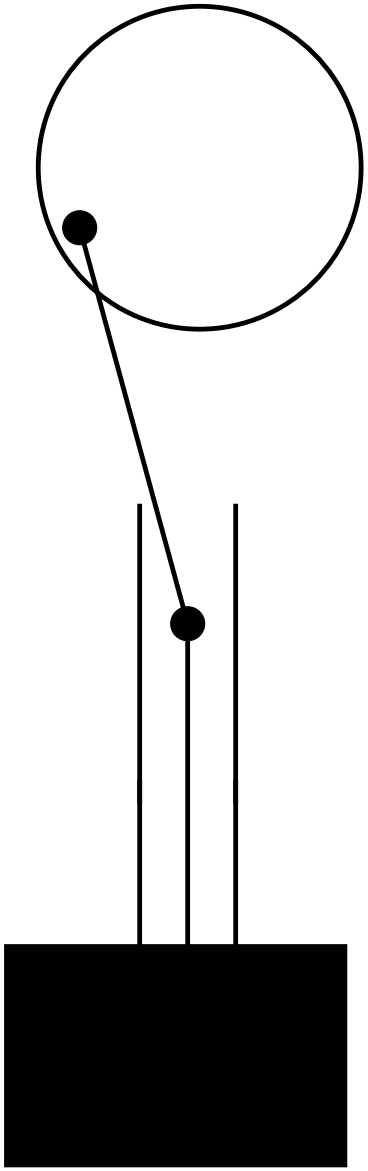

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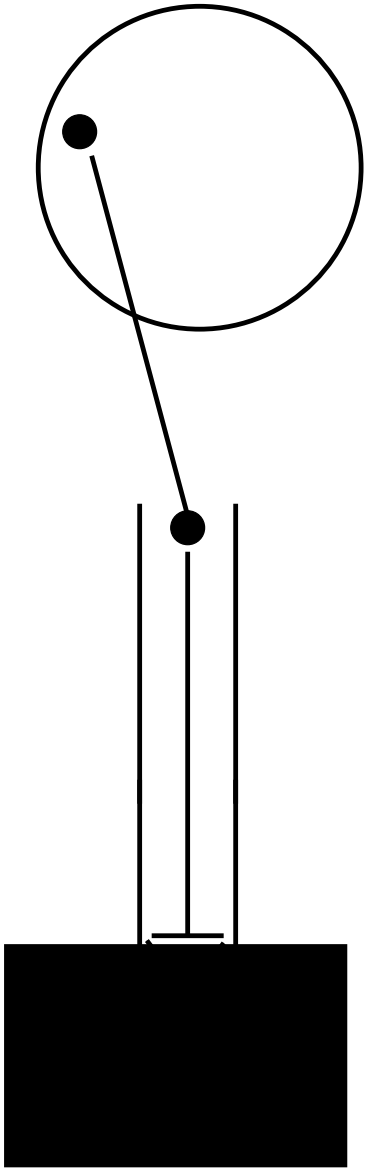

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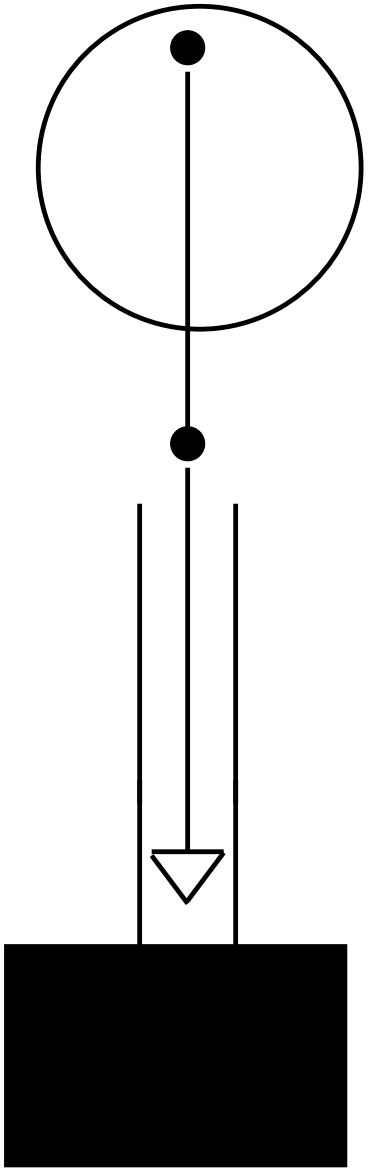

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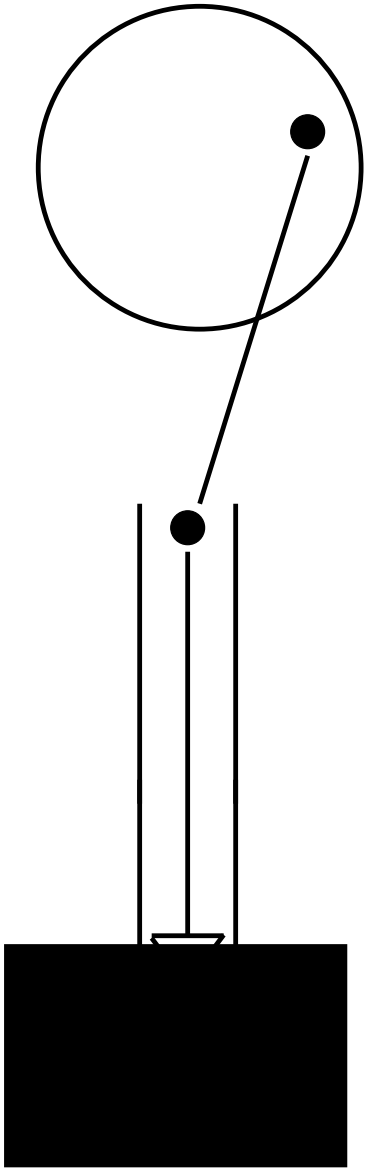

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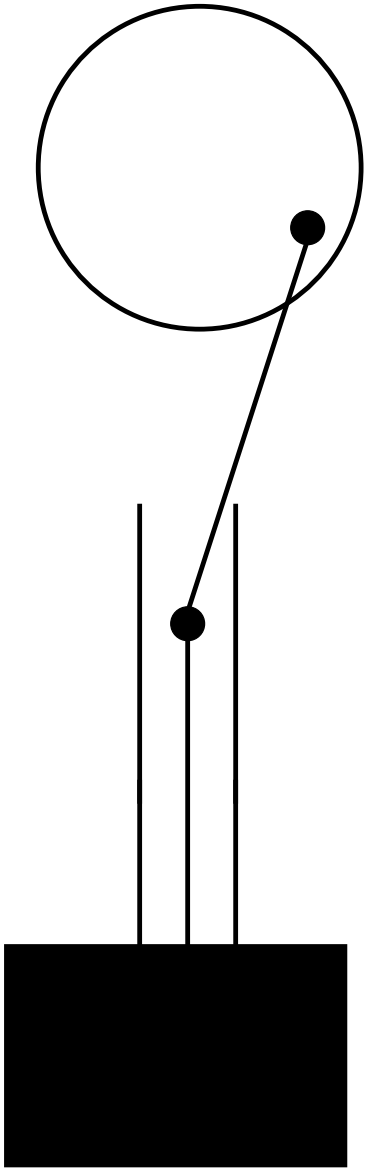
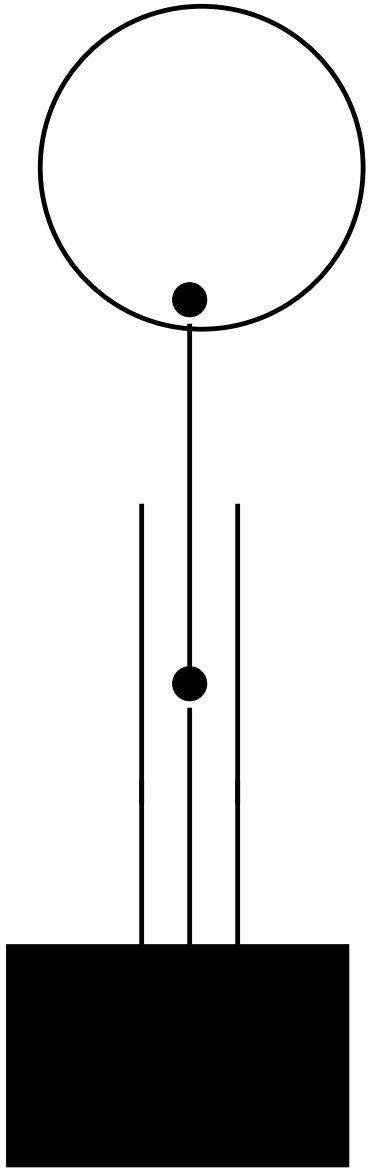
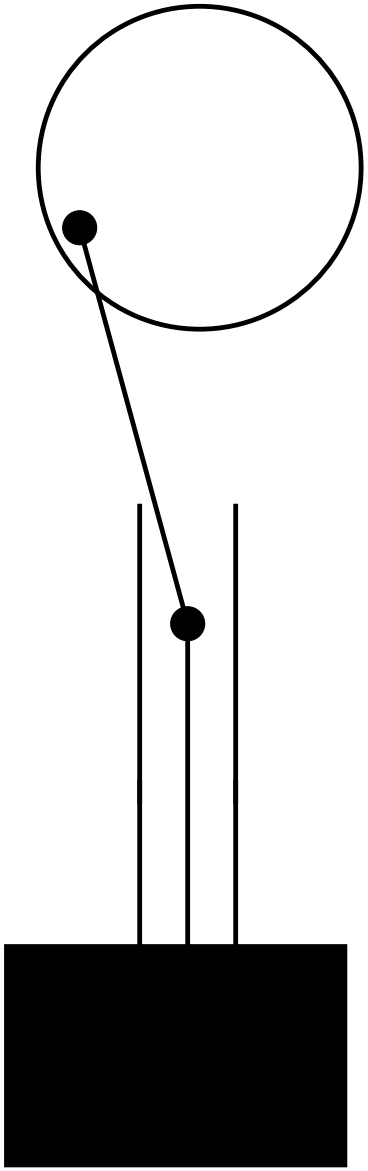
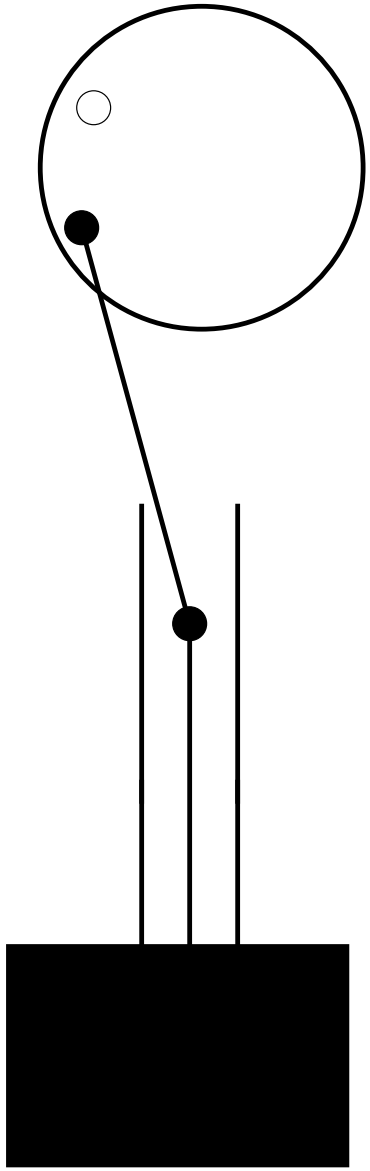
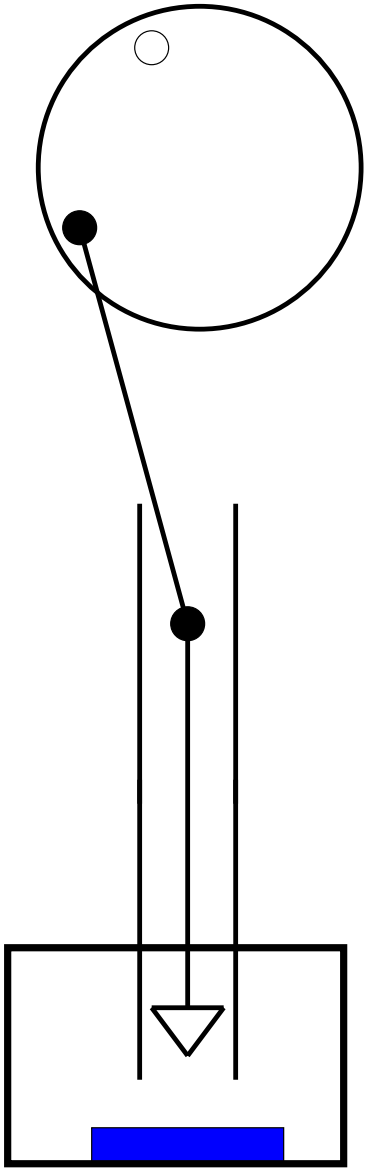
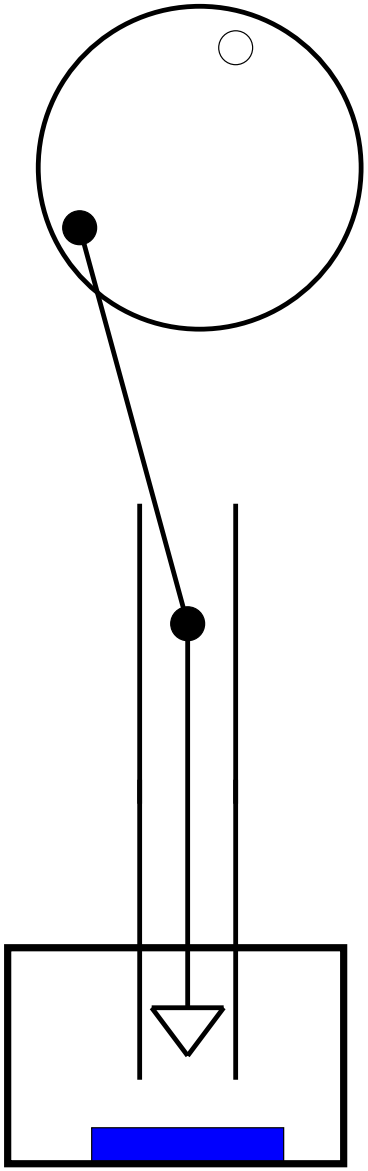


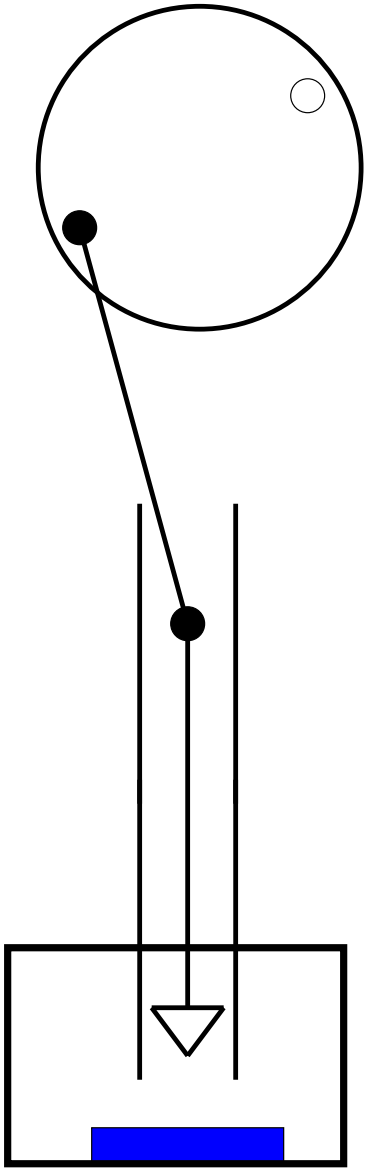




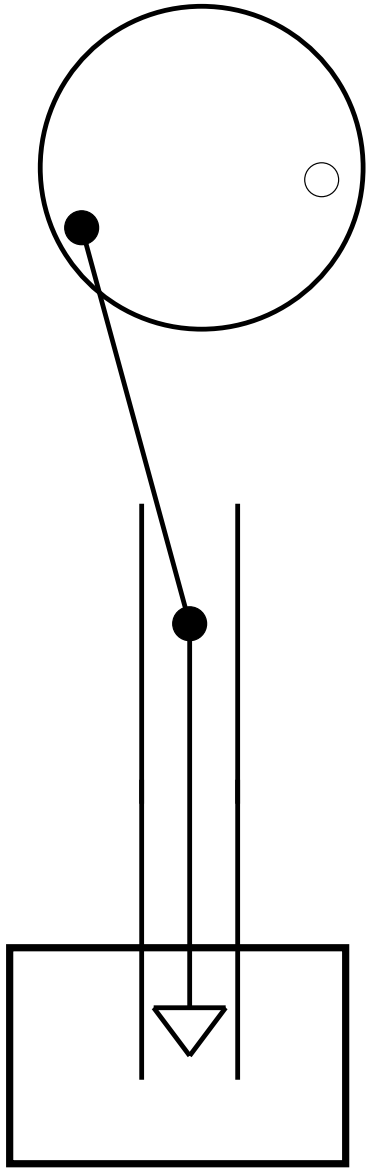


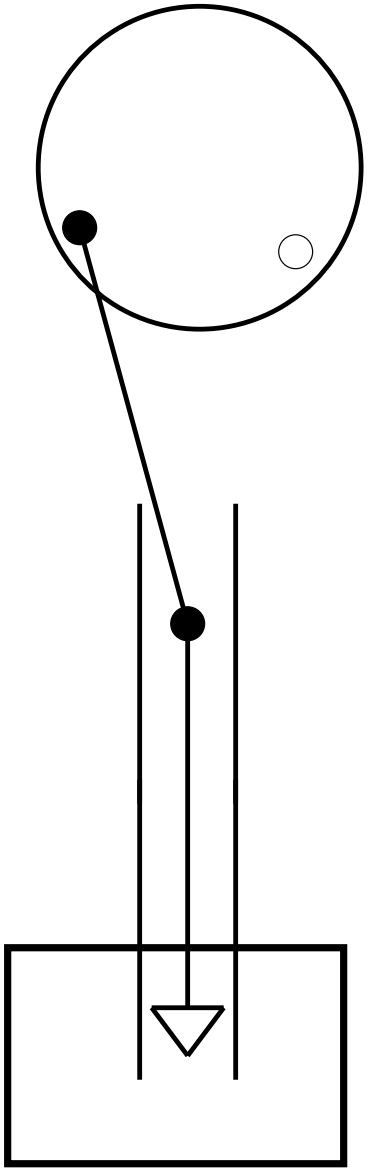


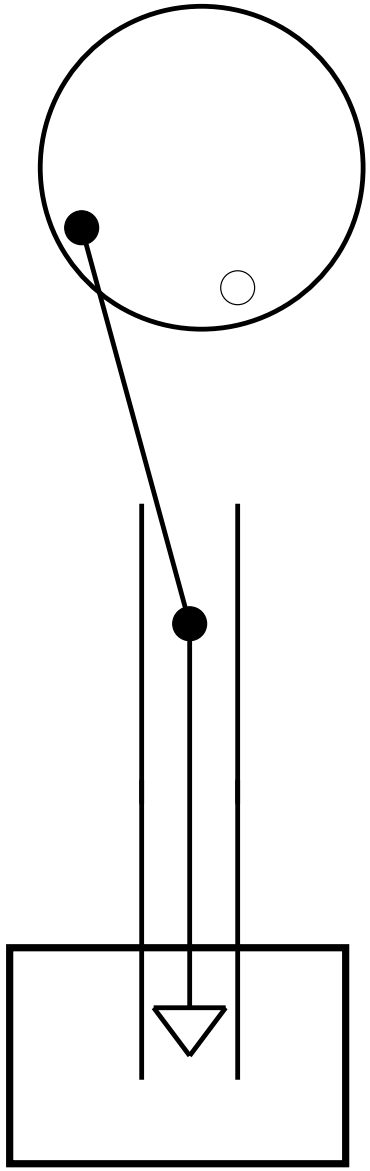




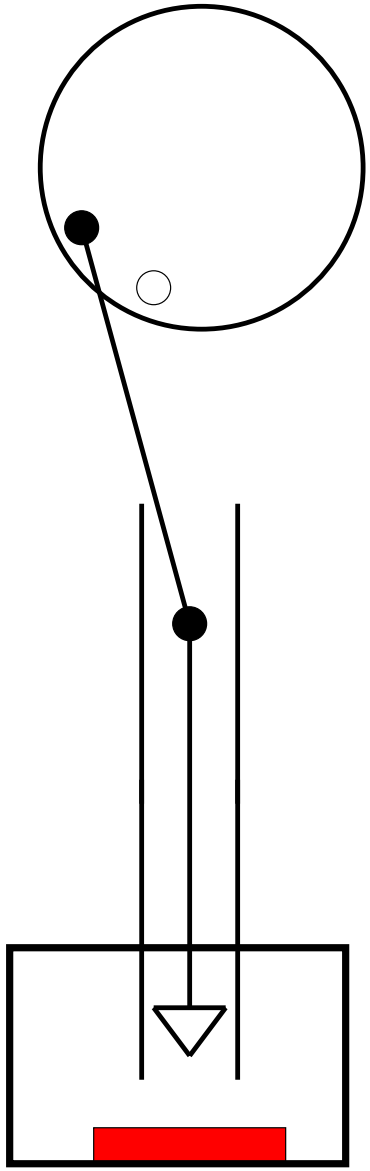
Removing the Part

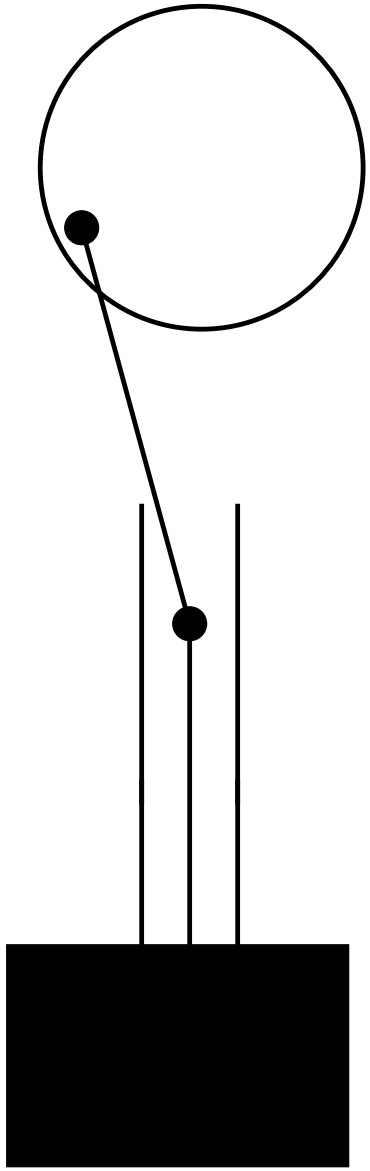






Putting a Part





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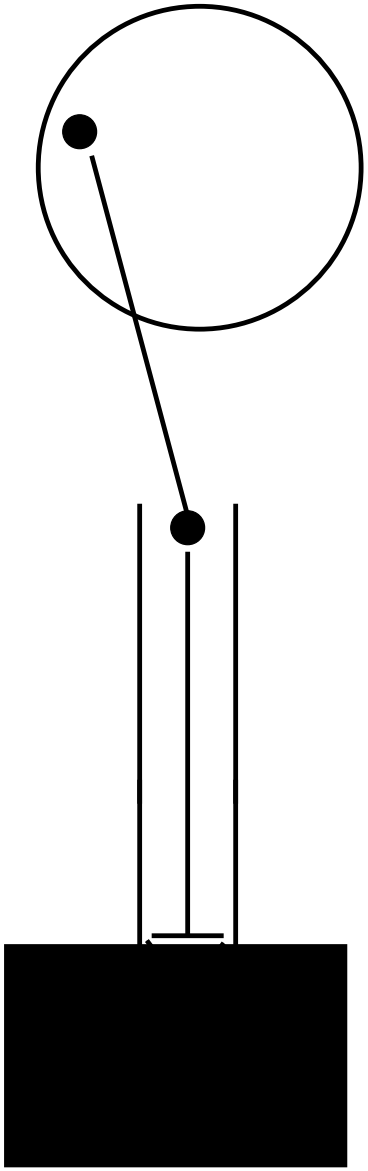

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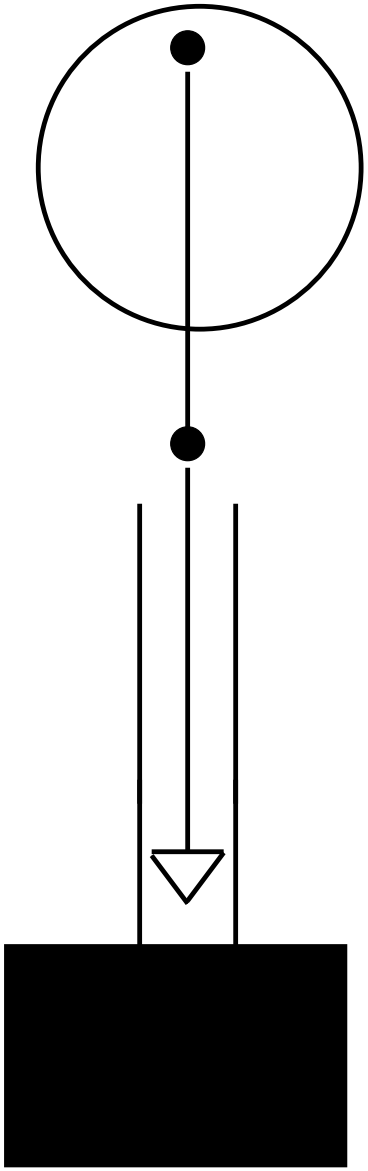

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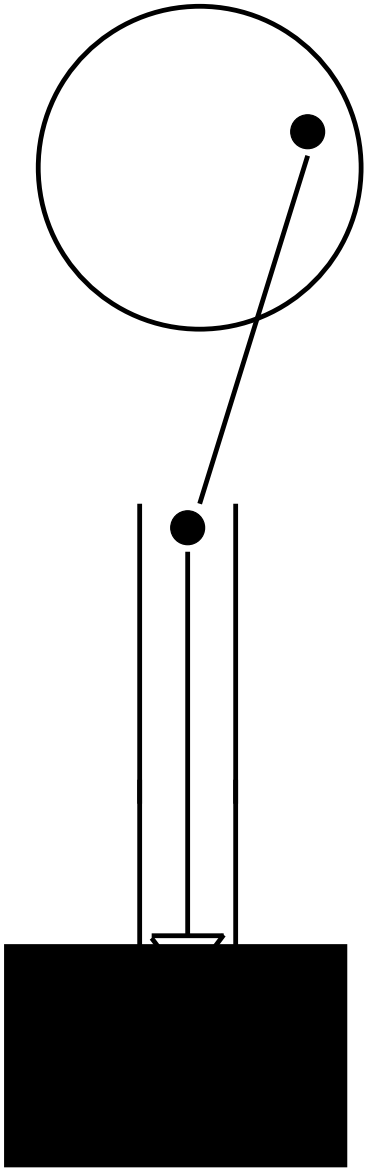

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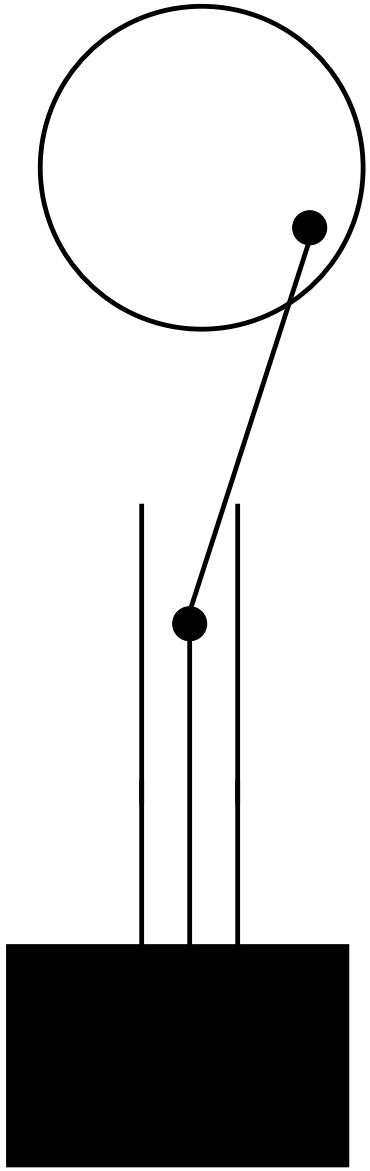

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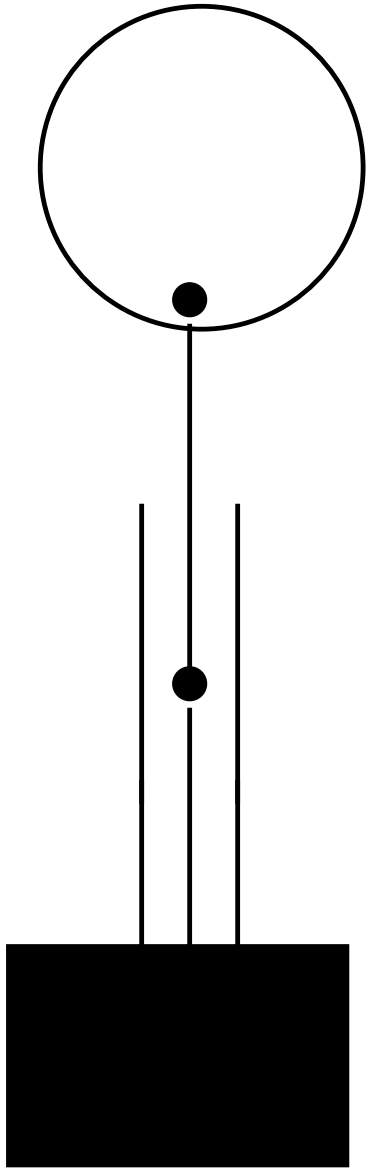

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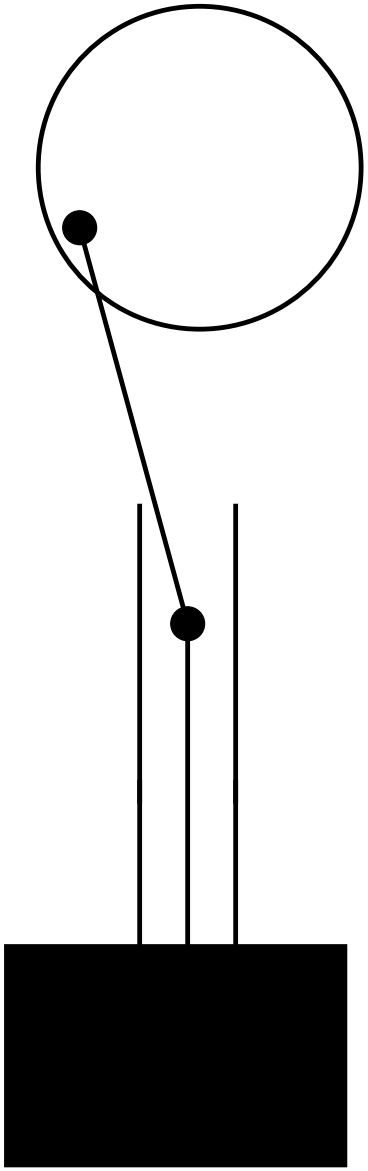

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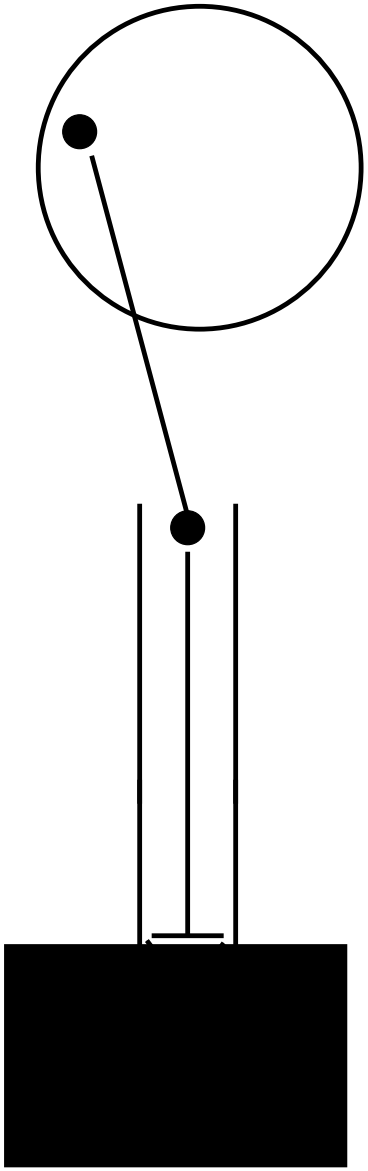

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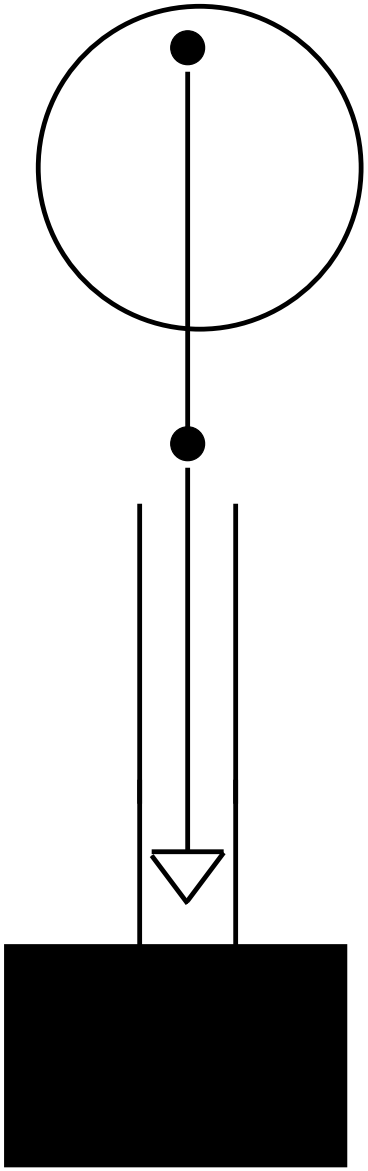

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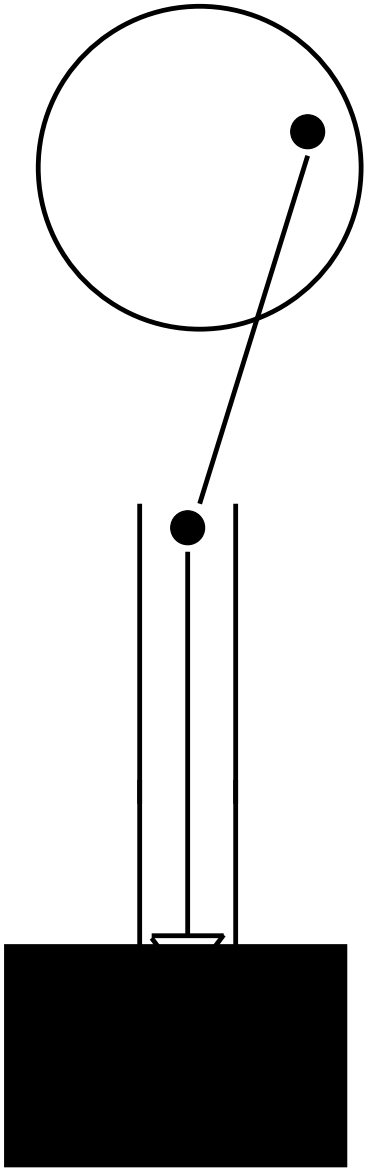

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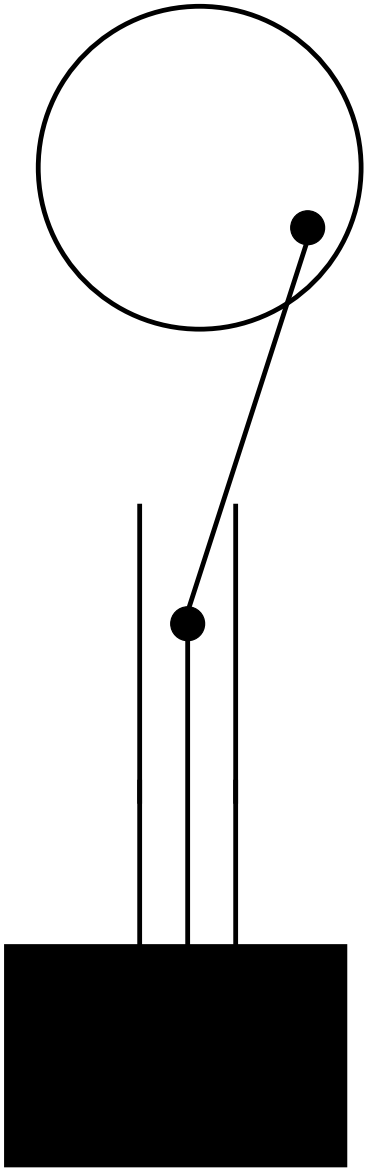

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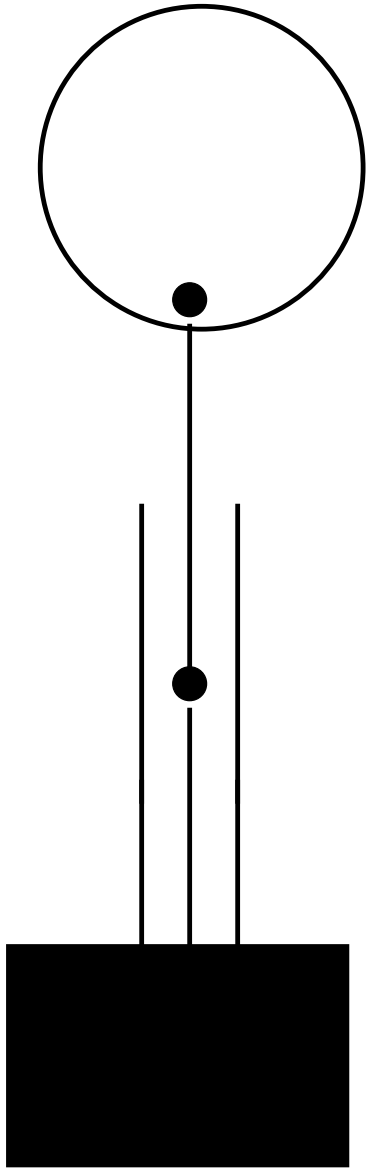

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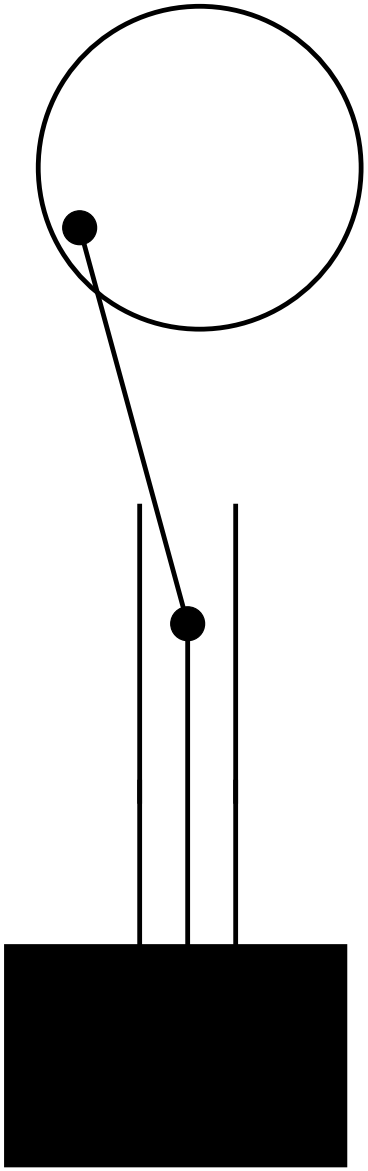

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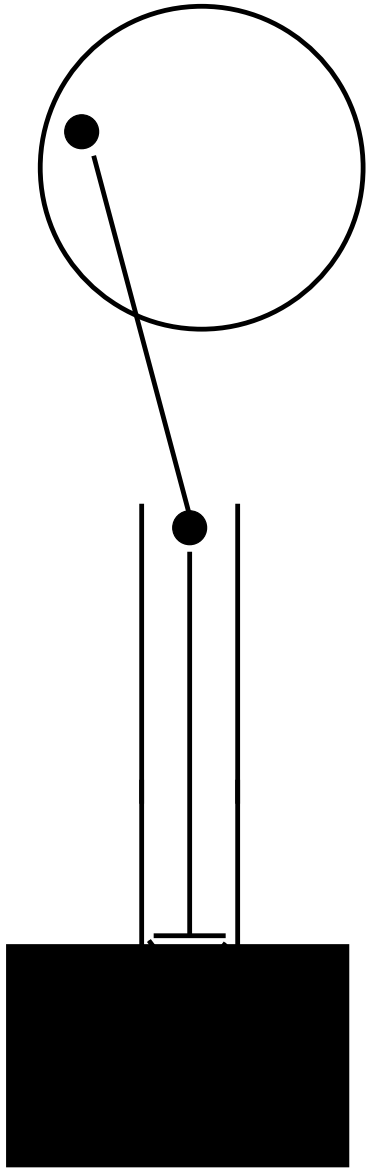

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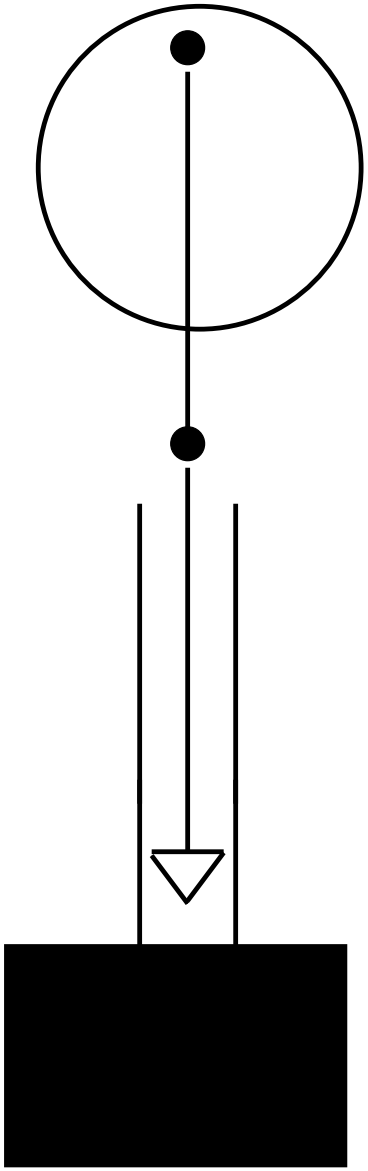

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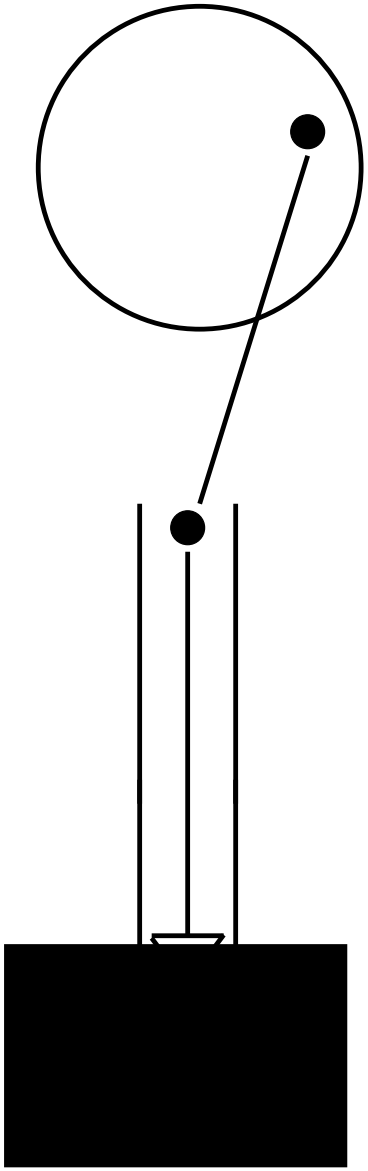

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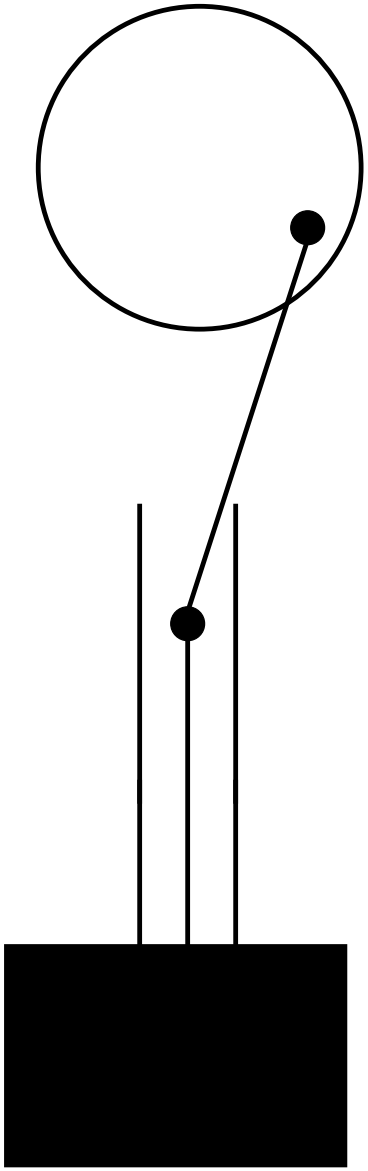

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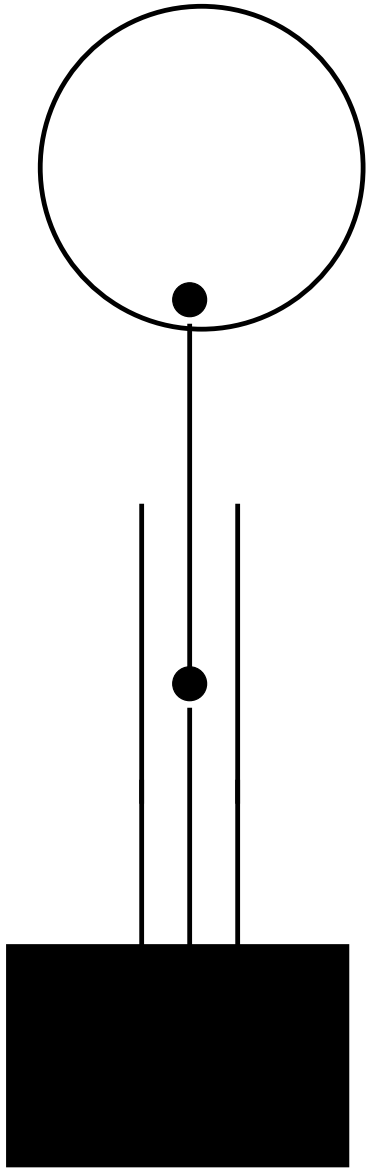

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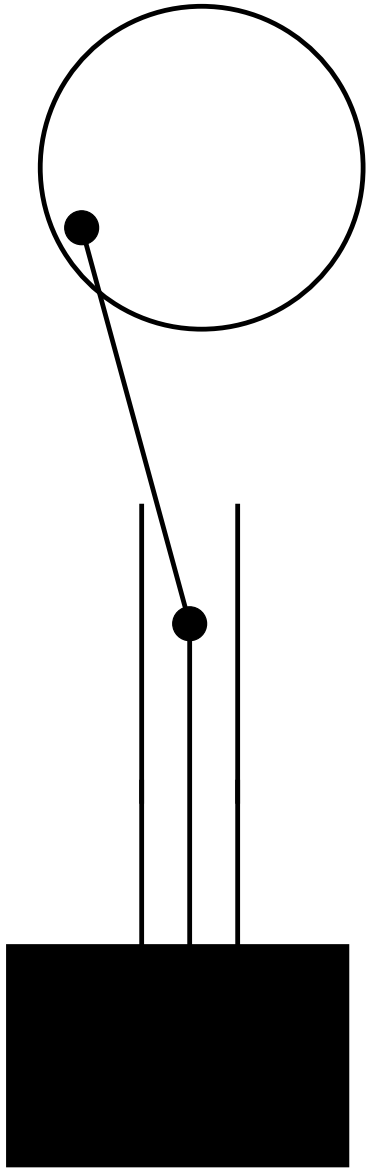
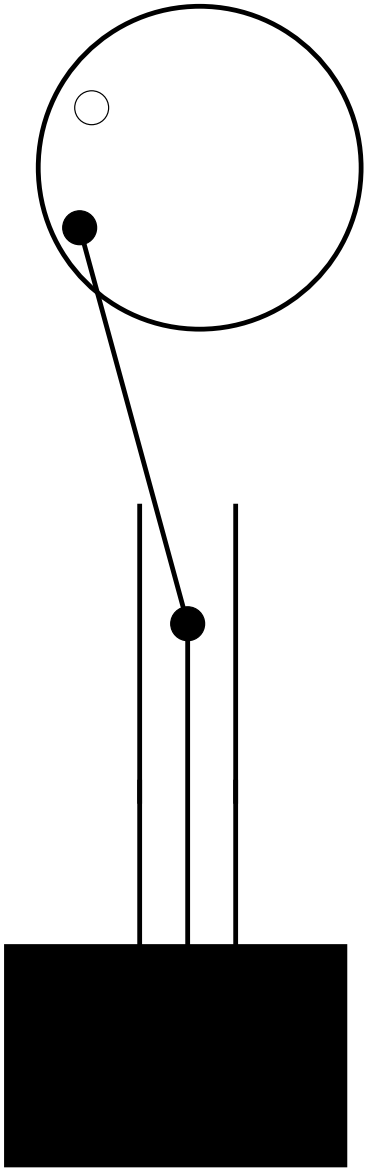
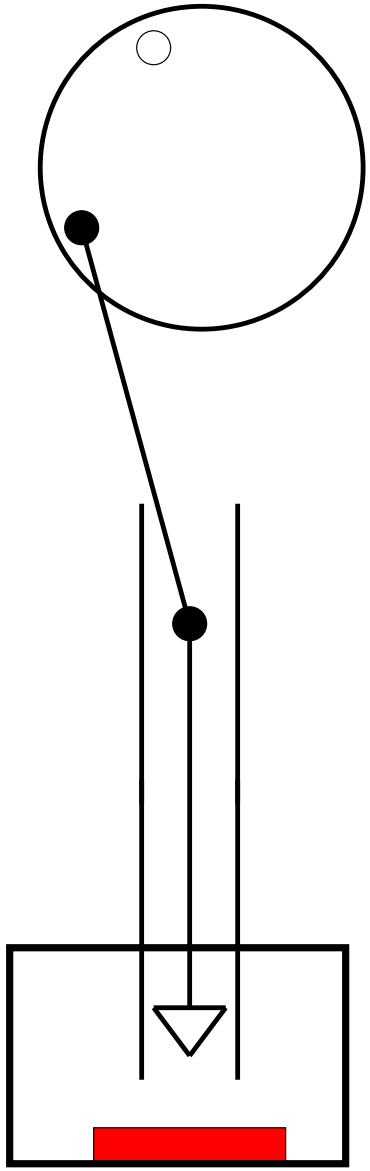
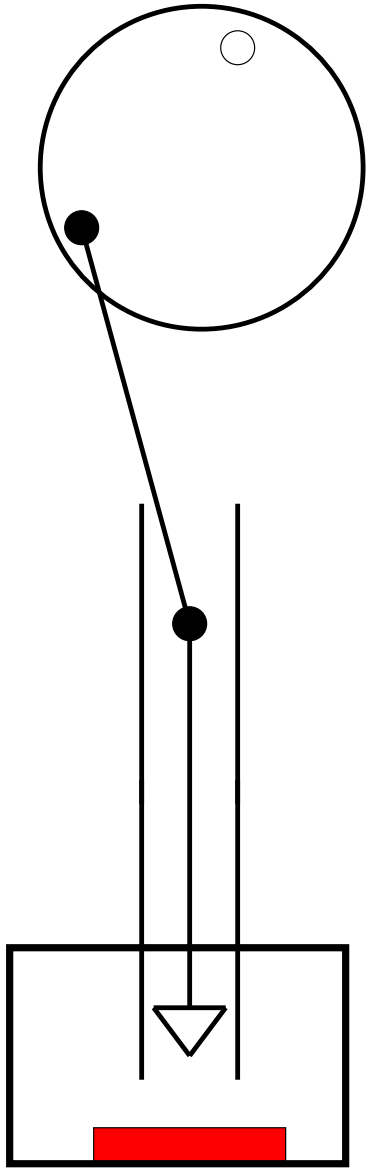
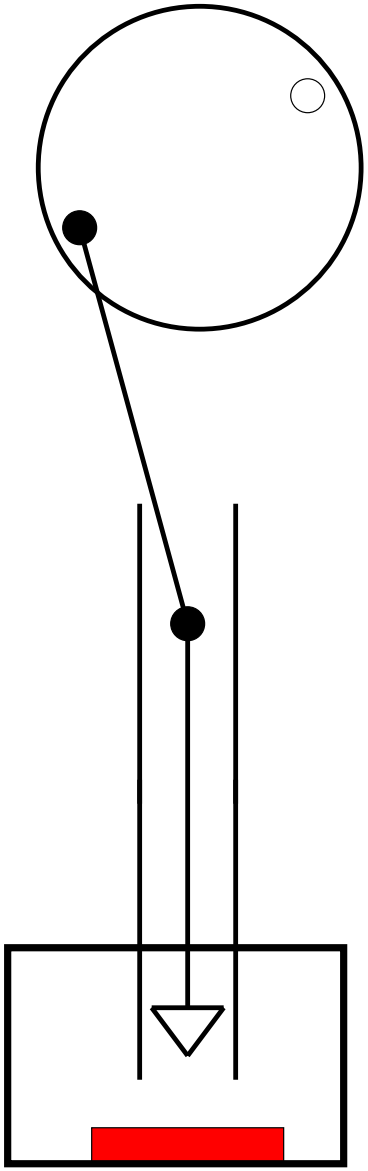


Disengaging the Clutch: Pressing Button B4

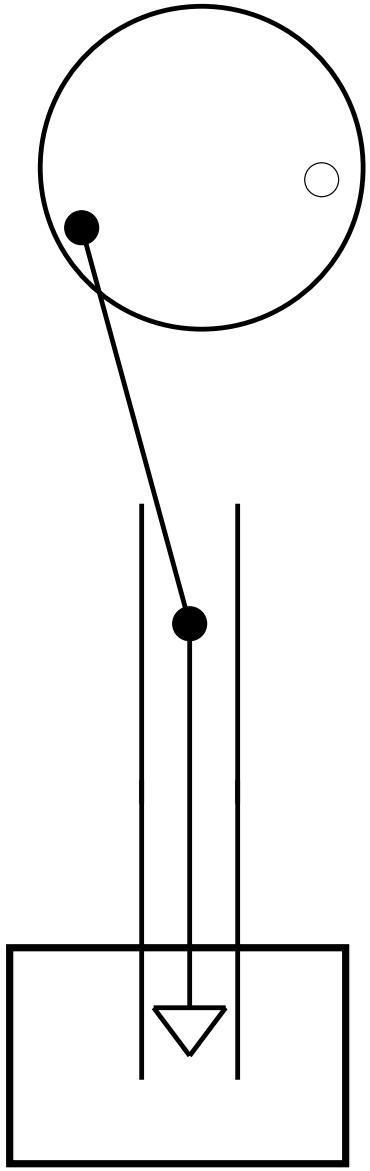


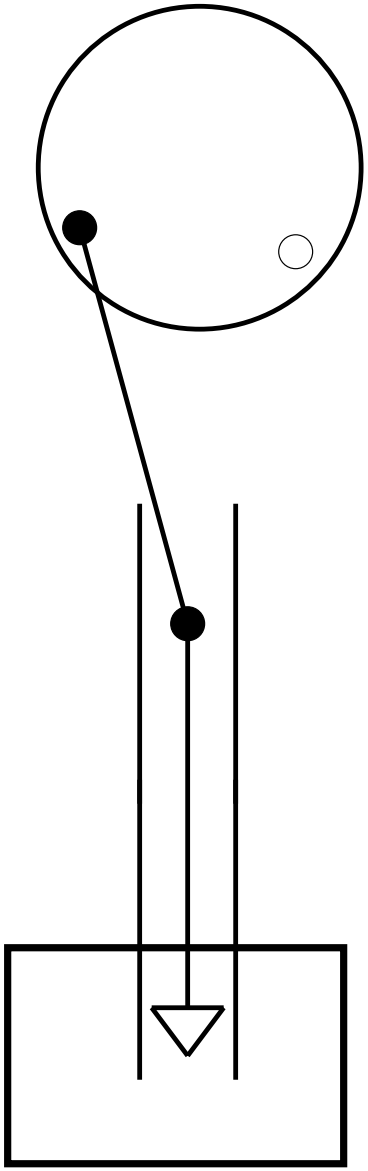


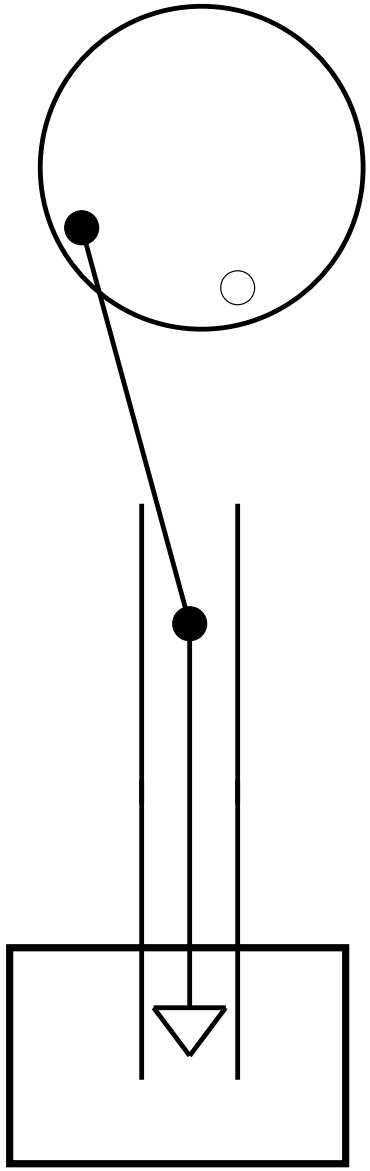




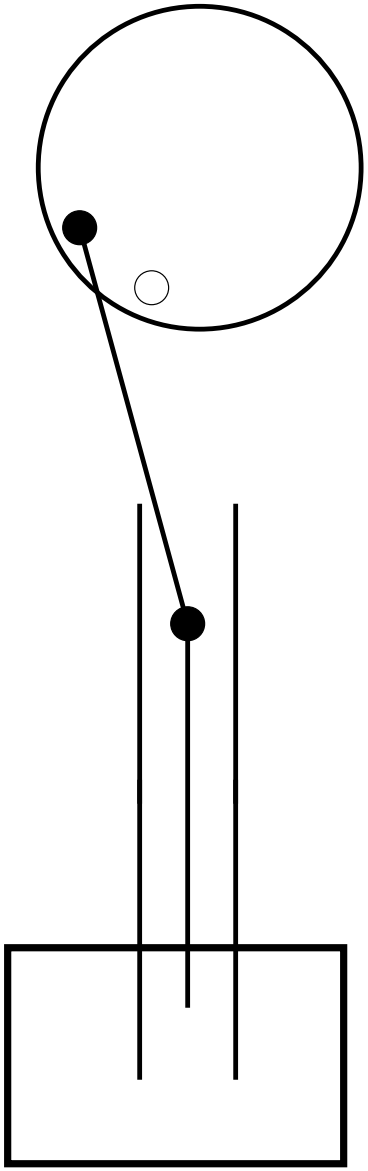
Removing the Part



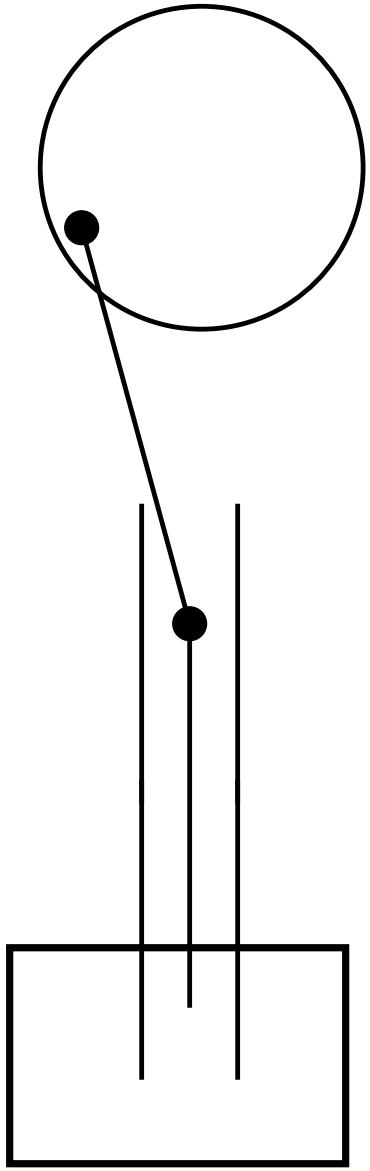




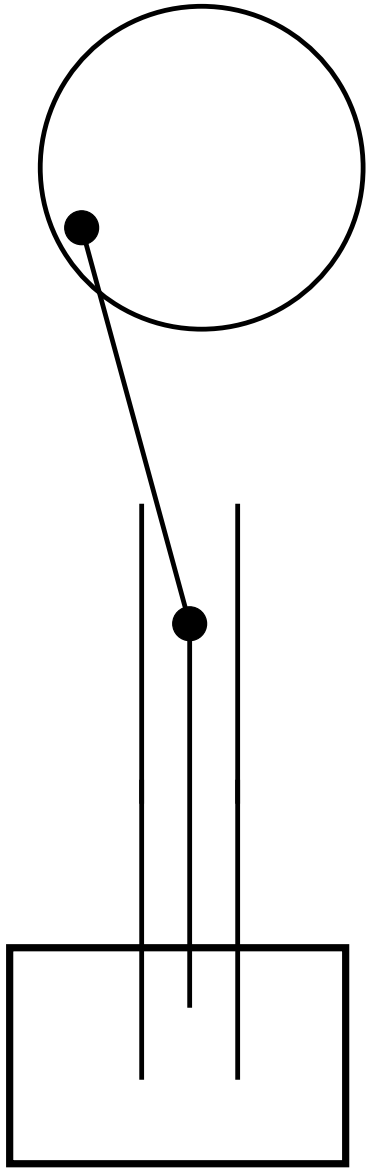
Removing the Tool

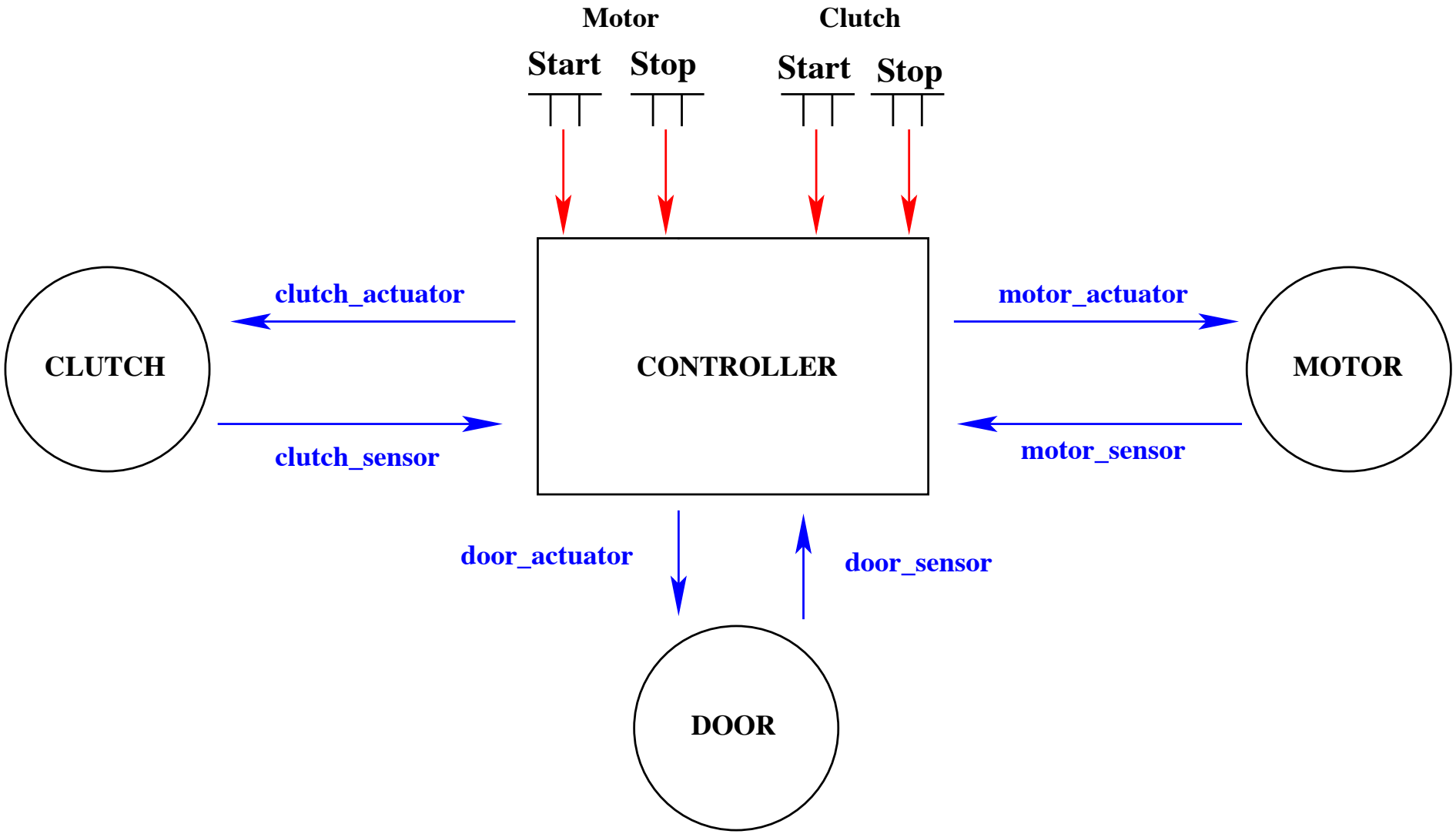


Stopping Motor: Pressing Button B2



Final Situation




Motor
Clutch
Start
Stop
Start
Stop
CLUTCH
clutch_actuator
clutch_sensor
CONTROLLER
motor_actuator
motor_sensor
MOTOR
door_actuator
door_sensor
DOOR

2. Presentation of some Design Patterns

Motivations

- A number of similar behaviors

- Some complex situations to handle

Similar Behavior (1)

- A specific action results eventually in having a specific reaction:
  - Pushing button B1 results eventually in starting the motor
  - Pushing button B4 results eventually in disengaging the clutch
  - ...

Similar Behavior (2)

- Correlating two pieces of equipment:
    - When the clutch is engaged then the motor must work
    - When the clutch is engaged then the door must be closed

Similar Behavior (3)

- Making an action dependent of another one:

- Engaging the clutch implies closing the door first

- Disengaging the clutch means opening the door afterwards

Motivation: Example of Some Complex Situation

- Here is a sequence of events:

  (1) User pushes button B1 (start motor)

  (1') User does not remove his finger from button B1

  (2) Controller sends the starting command to the motor

  (3) Motor starts and sends feedback to the controller

  (4) Controller is aware that the motor works

  (5) User pushes button B2 (stop motor)

  (6) Controller sends the stop command to the motor

  (7) Motor stops and sends feedback to the controller

  (8) Controller is aware that the motor does not work

  (9) Controller must not send the starting command to the motor

Motivation: Example of Some Complex Situation

- Here is a sequence of events:

  (1) User pushes button B1 (start motor)

  (2) Controller sends the starting command to the motor

  (3.1) Motor starts and sends feedback to the controller

  (3.2) User pushes button B2 (stop motor)

- (3.1) and (3.2) may occur simultaneously

- If controller treats (3.1) before (3.2): motor is stopped

- If controller treats (3.2) before (3.1): motor is not stopped

- We want to build systems which are correct by construction

- We want to have more methods for doing so

- "Design pattern" is an Object Oriented concept

- We would like to borrow this concept for doing formal developments

- A preliminary tentative with reactive system developments

- Advantage: systematic developments and also refinement of proofs

- This is an engineering concept

- It can be used outside OO

- The goal of each DP is to solve a certain category of problems

- But the design pattern has to be adapted to the problem at hand

- Is it compatible with formal developments?

- Let's apply this approach to the design of reactive systems

A Wikipedia View on Design Patterns (1)

- A design pattern isn't a finished design that can be transformed into code

- It is a template for how to solve a problem that can be used in many different situations

- Patterns originated as an architectural concept by Christopher Alexander

- "Design Patterns: Elements of Reusable Object-Oriented Software" published in 1994 (Gamma et al)

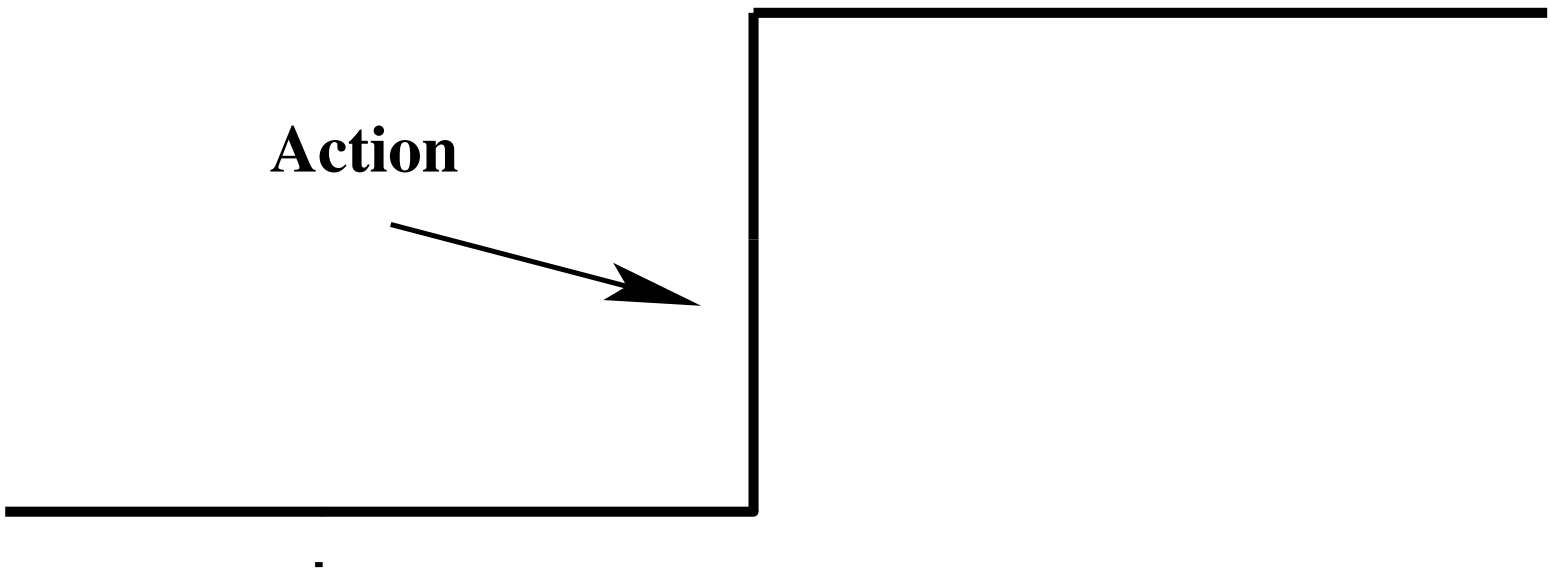
A Wikipedia View on Design Patterns (2)

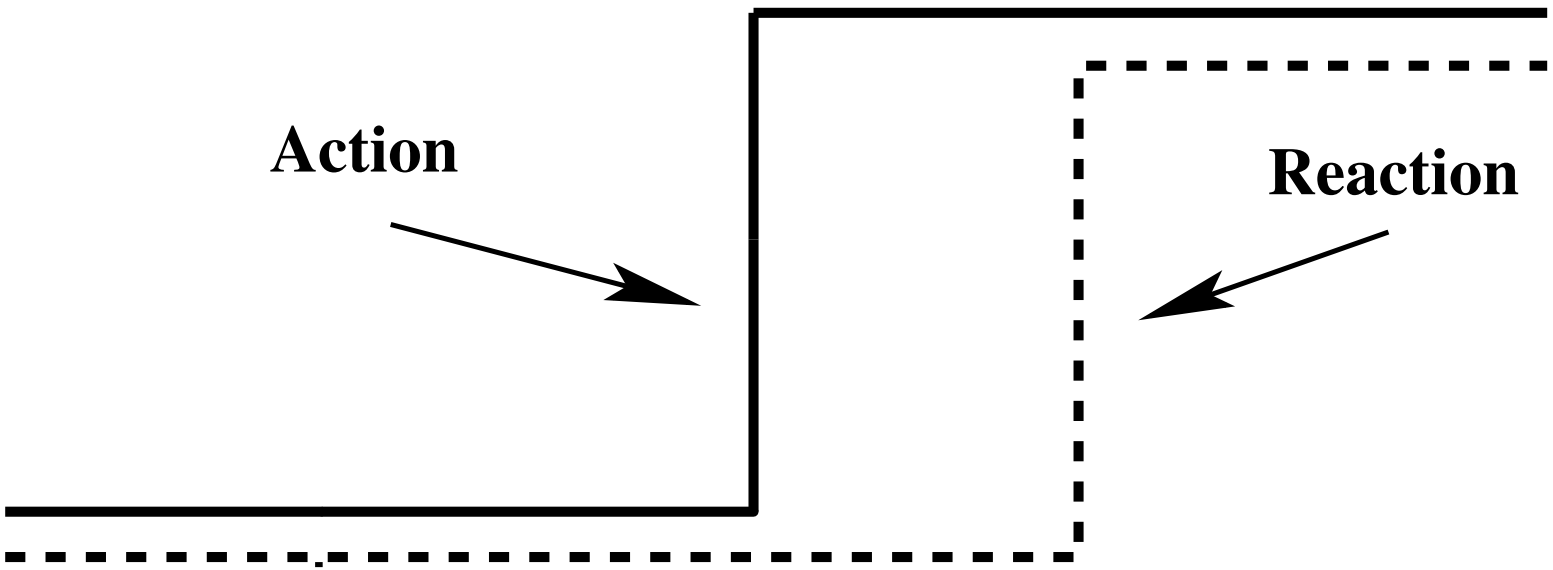
- Design pattern can speed up the development process by providing tested and proven development paradigms

- The documentation for a design pattern should contain enough information about the problem that the pattern addresses, the context in which it is used, and the suggested solution.

- Some feel that the need for patterns results from using computer languages or techniques with insufficient abstraction

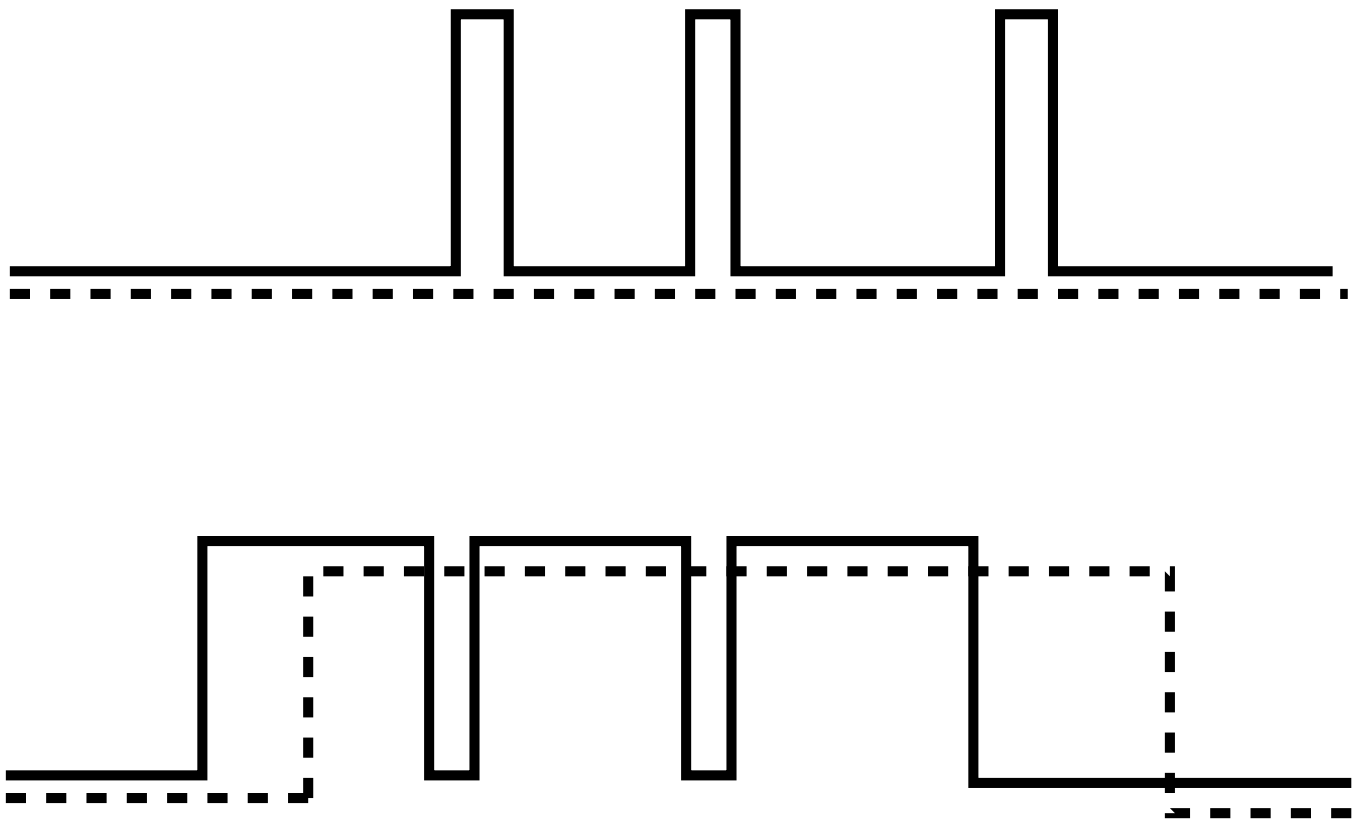
An Action Pattern




Action
Reaction

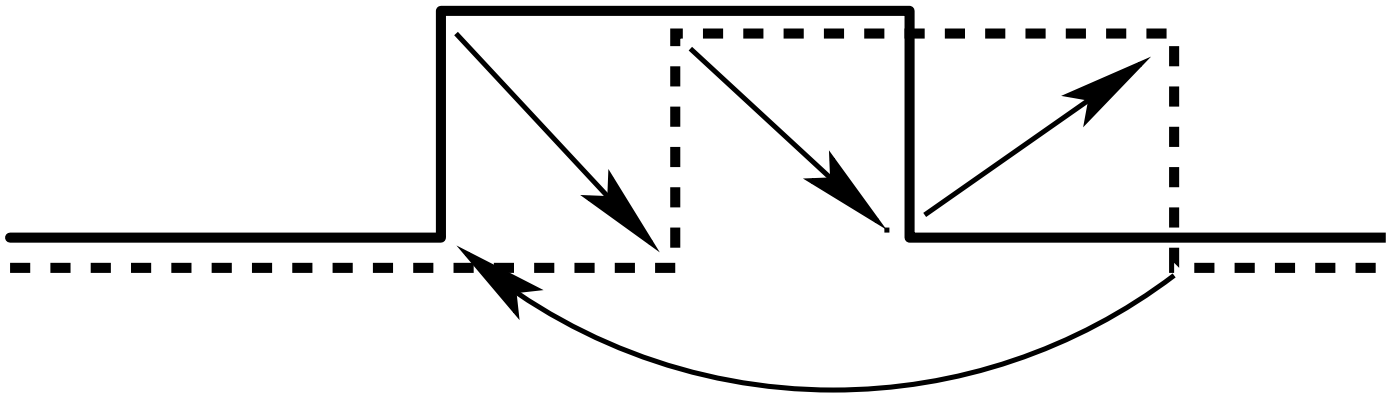
- Sometimes, the reaction has not enough time to react

- Because the action moves too quickly



- Sometimes, the reaction always follows the action

- They are both synchronized



- We built first a model of a weak reaction

- The strong reaction will be a refinement of the weak one

Model for weak action and reaction: the State

variables: a
r

pat0_1: $a \in \{0, 1\}$

pat0_2: $r \in \{0, 1\}$

- a denotes the action

- r denotes the reaction

Model for weak action and reaction: the State

variables: a, r, ca, cr

pat0_1: $a \in \{0, 1\}$

pat0_2: $r \in \{0, 1\}$

pat0_3: $ca \in \mathbb{N}$

pat0_4: $cr \in \mathbb{N}$

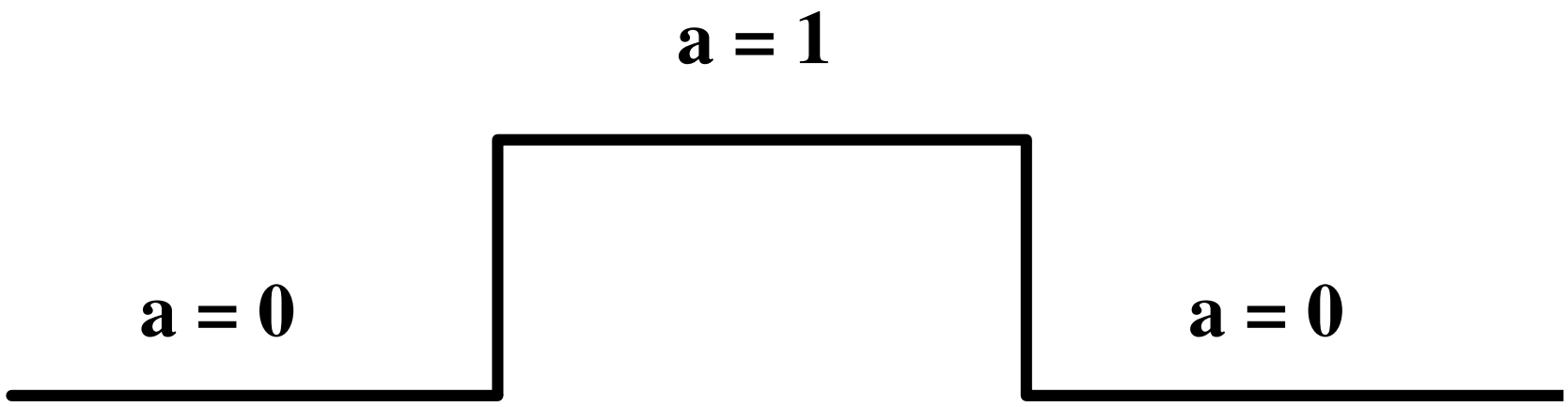
pat0_5: $cr \leq ca$

- ca and cr denote how many times a and r are set to 1
- **pat0_5** formalizes the weak reaction

Model for weak action and reaction: the Events (1)

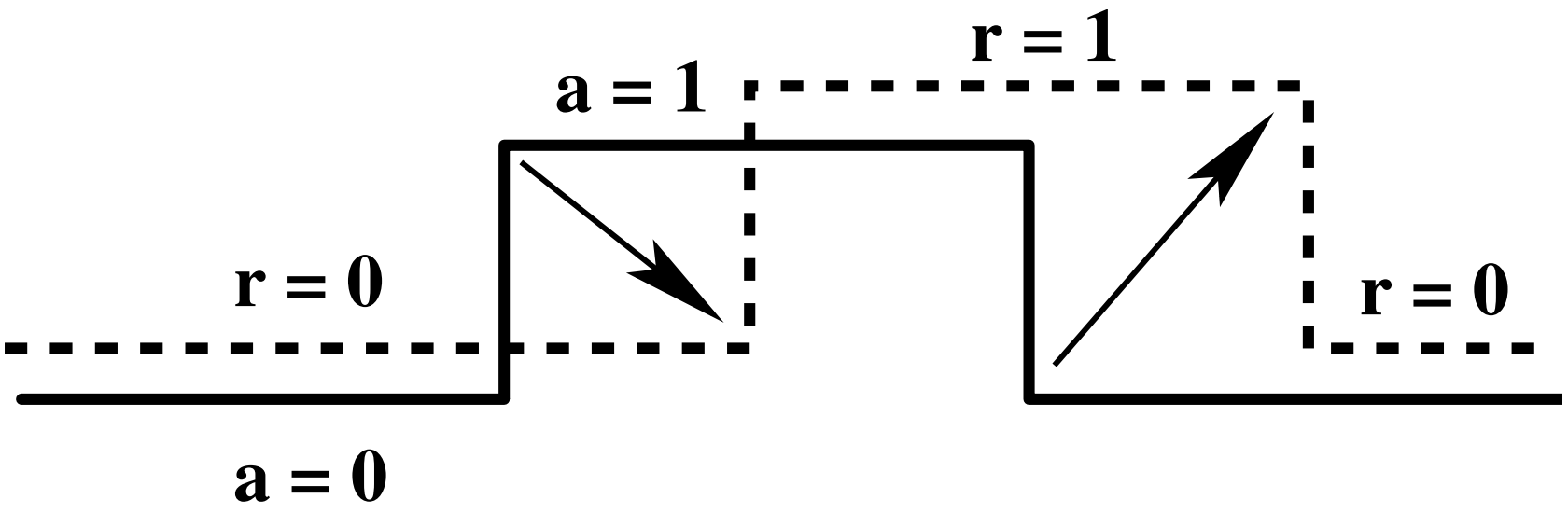
a_on
when
$a = 0$
then
$a := 1$
$ca := ca + 1$
end

a_off
when
$a = 1$
then
$a := 0$
end



r_on
when
$r = 0$
$a = 1$
then
$r := 1$
$cr := cr + 1$
end

r_off
when
$r = 1$
$a = 0$
then
$r := 0$
end



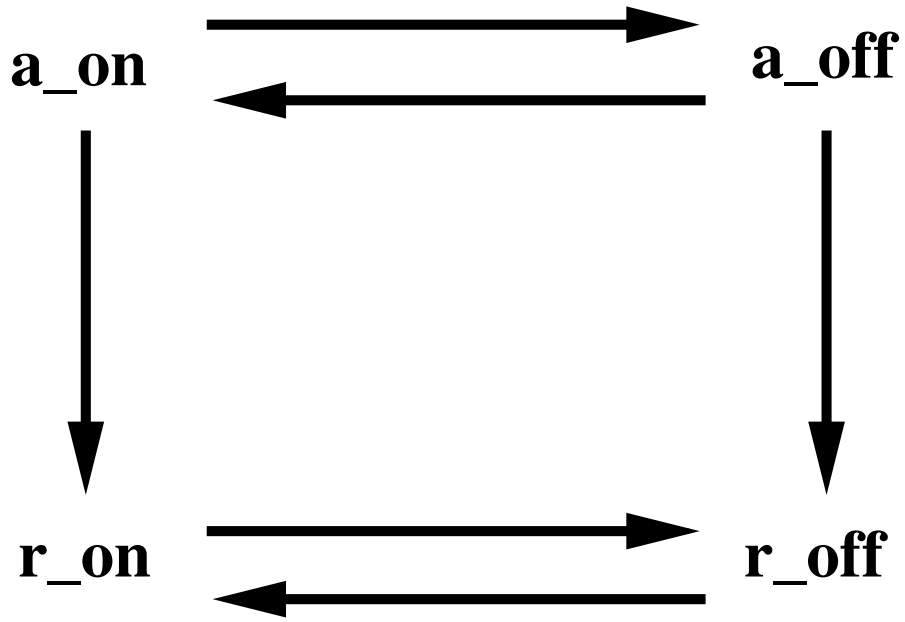
Summary of Events

a_on
when
$a = 0$
then
$a := 1$
$ca := ca + 1$
end

a_off
when
$a = 1$
then
$a := 0$
end

r_on
when
$r = 0$
$a = 1$
then
$r := 1$
$cr := cr + 1$
end

r_off
when
$r = 1$
$a = 0$
then
$r := 0$
end



Summary of Weak Synchronization

variables: a, r, ca, cr

pat0_1: $a \in \{0, 1\}$

pat0_2: $r \in \{0, 1\}$

pat0_3: $ca \in \mathbb{N}$

pat0_4: $cr \in \mathbb{N}$

pat0_5: $cr \leq ca$

init
$a := 0$
$r := 0$
$ca := 0$
$cr := 0$

a_on
when
$a = 0$
then
$a := 1$
$ca := ca + 1$
end

a_off
when
$a = 1$
then
$a := 0$
end

r_on
when
$r = 0$
$a = 1$
then
$r := 1$
$cr := cr + 1$
end

r_off
when
$r = 1$
$a = 0$
then
$r := 0$
end

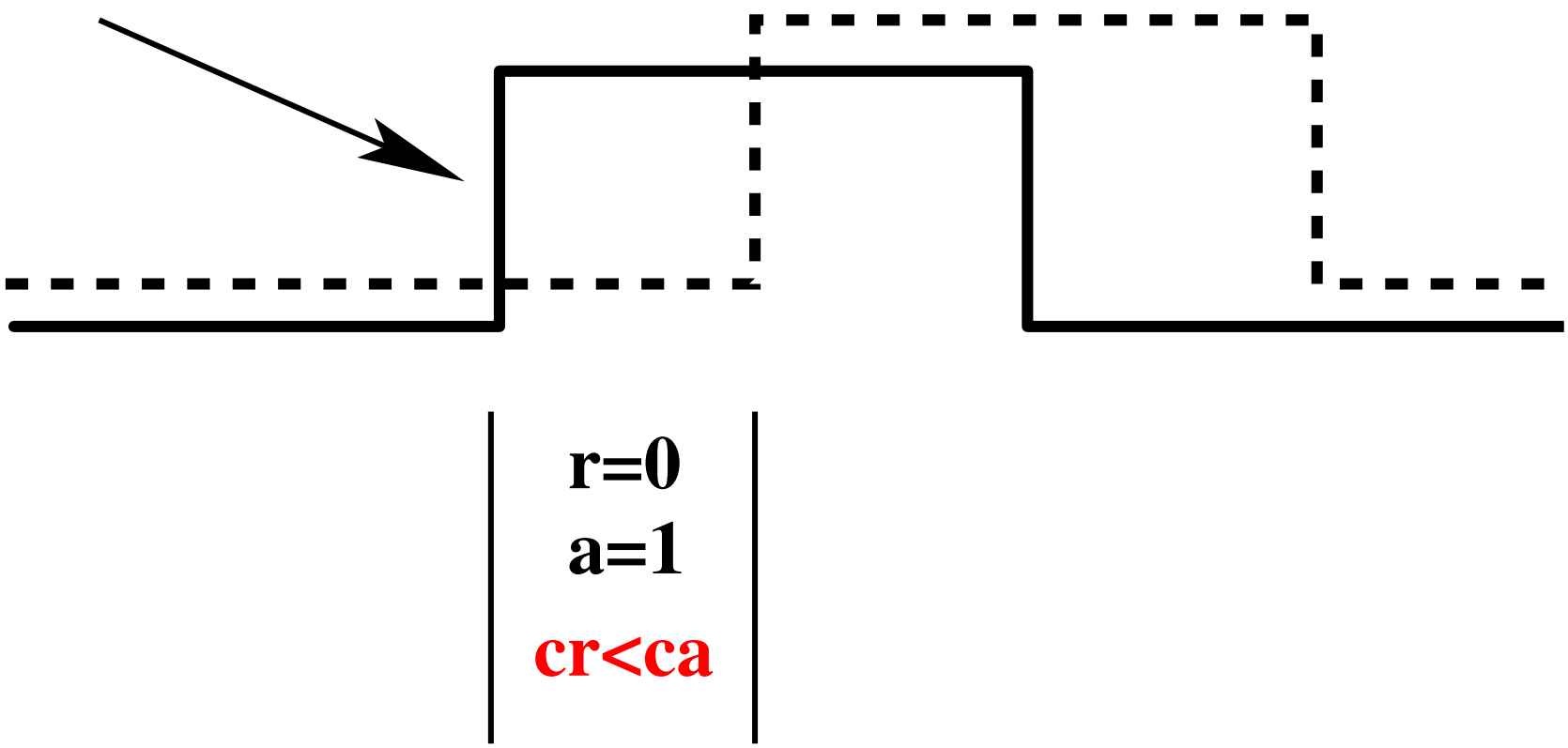
Nothing guarantees that the invariants are preserved

D E M 0 (Showing a Problem and Finding a Solution)

Intuition Behind the new Invariant

pat0_6: $r = 0 \ \wedge \ a = 1 \ \Rightarrow \ cr < ca$

ca is incremented



Summary of the State of the weak Reaction

pat0_1: $a \in \{0, 1\}$

pat0_2: $r \in \{0, 1\}$

pat0_3: $ca \in \mathbb{N}$

pat0_4: $cr \in \mathbb{N}$

pat0_5: $cr \leq ca$

pat0_6: $r = 0 \wedge a = 1 \Rightarrow cr < ca$

Summary of the Events of the weak Reaction

The counters have

been removed

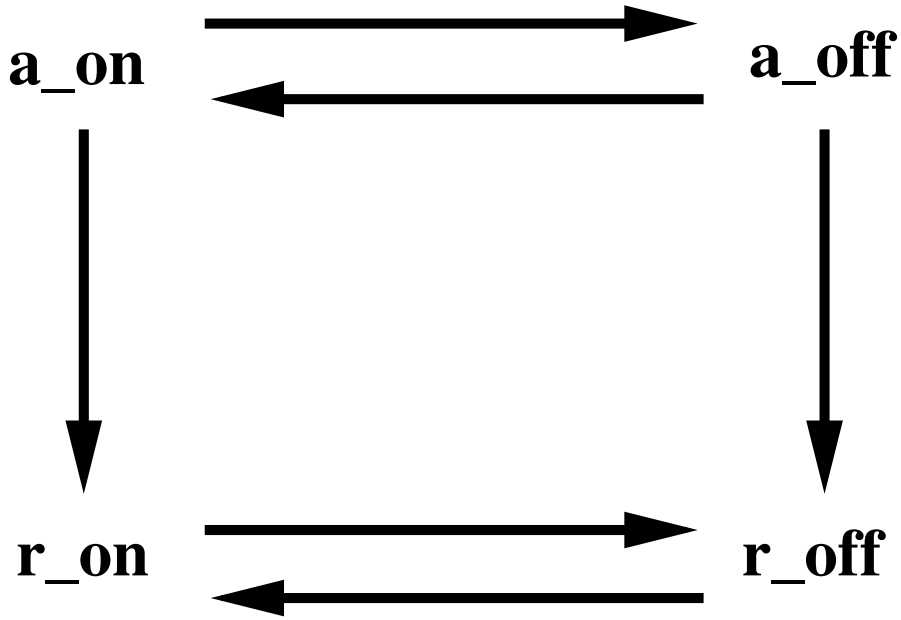
init
$a := 0$
$r := 0$

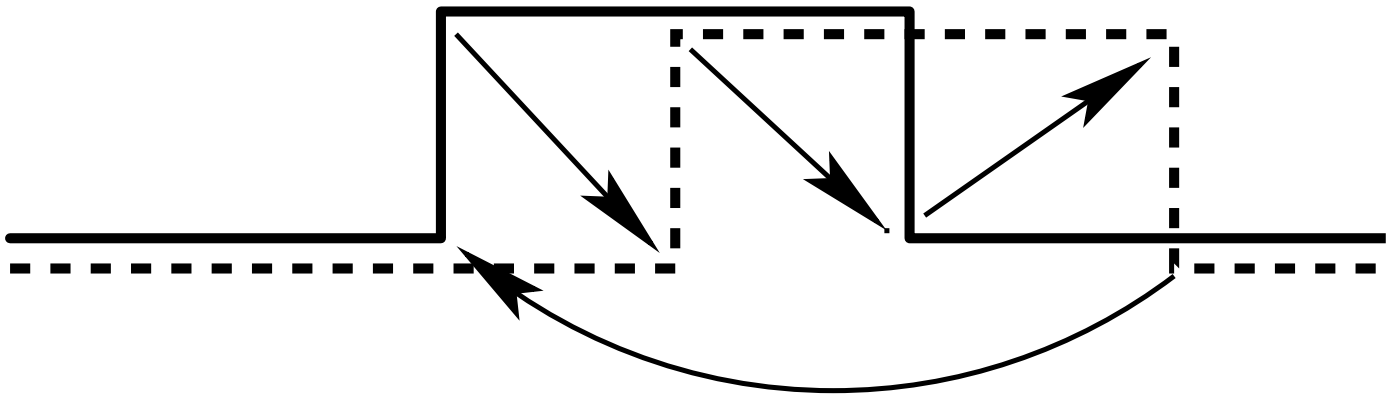
a_on
when
$a = 0$
then
$a := 1$
end

a_off
when
$a = 1$
then
$a := 0$
end

r_on
when
$r = 0$
$a = 1$
then
$r := 1$
end

r_off
when
$r = 1$
$a = 0$
then
$r := 0$
end


a_on
a_off
r_on
r_off



- We add the following invariant

pat1_1: $ca \leq cr + 1$

- Remember invariant **pat0_5**

pat0_5: $cr \leq ca$

We have thus: $ca = cr \ \vee \ ca = cr + 1$

Summary (so far) of the Strong Sncchronization

pat1_1: $ca \leq cr + 1$

a_on
when
$a = 0$
then
$a := 1$
$ca := ca + 1$
end

a_off
when
$a = 1$
then
$a := 0$
end

r_on
when
$r = 0$
$a = 1$
then
$r := 1$
$cr := cr + 1$
end

r_off
when
$r = 1$
$a = 0$
then
$r := 0$
end

Nothing guarantees that the invariant is preserved

D E M 0 (Showing Problems and Finding Solutions)

Merging the two invariants

- Putting together these two invariants

pat1_2: $a = 0 \Rightarrow ca = cr$

pat1_3: $a = 1 \wedge r = 1 \Rightarrow ca = cr$

- leads to the following

pat1_4: $a = 0 \vee r = 1 \Rightarrow ca = cr$

pat0_5: $cr \leq ca$

pat0_6: $a = 1 \ \wedge \ r = 0 \ \Rightarrow \ cr < ca$

pat1_1: $ca \leq cr + 1$

pat1_4: $a = 0 \ \vee \ r = 1 \ \Rightarrow \ ca = cr$

This can be simplified to

pat2_1: $a = 1 \ \wedge \ r = 0 \ \Rightarrow \ ca = cr + 1$

pat2_2: $a = 0 \ \vee \ r = 1 \ \Rightarrow \ ca = cr$

Summary of the State for the Strong Reaction

pat0_1: $a \in \{0, 1\}$

pat0_2: $r \in \{0, 1\}$

pat0_3: $ca \in \mathbb{N}$

pat0_4: $cr \in \mathbb{N}$

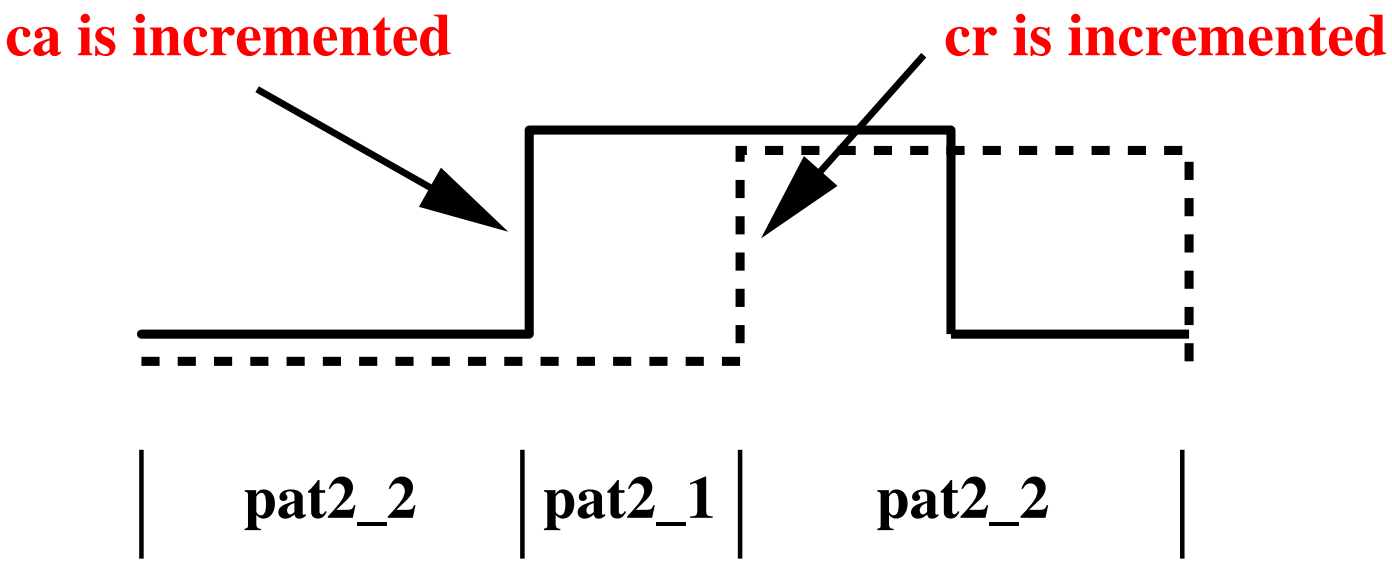
pat2_1: $a = 1 \wedge r = 0 \Rightarrow ca = cr + 1$

pat2_2: $a = 0 \vee r = 1 \Rightarrow ca = cr$

Intuition Behind the two Invariants

pat2_1: $a = 1 \ \wedge \ r = 0 \ \Rightarrow \ ca = cr + 1$

pat2_2: $a = 0 \ \vee \ r = 1 \ \Rightarrow \ ca = cr$



Summary of the Events for the Strong Reaction

The counters have

been removed

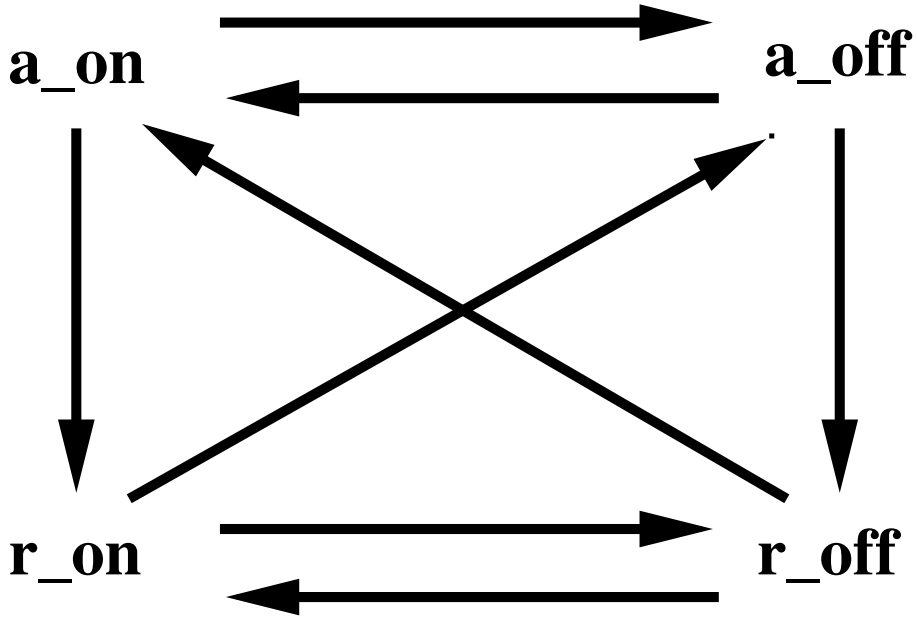
init
$a := 0$
$r := 0$

a_on
when
$a = 0$
$r = 0$
then
$a := 1$
end

a_off
when
$a = 1$
$r = 1$
then
$a := 0$
end

r_on
when
$r = 0$
$a = 1$
then
$r := 1$
end

r_off
when
$r = 1$
$a = 0$
then
$r := 0$
end


a_on
a_off
r_on
r_off

What we Have Learned

- Proof failures helped us improving our models

- When an invariant preservation proof fails on an event,
  there are two solutions:
    - adding a new invariant
    - strengthening the guard

- Modelling considerations helped us choosing one or the other

- At the end, we reached a stable situation (fixpoint)

3. Writing the Requirement Document

The system has got the following pieces of equipment: a Motor, a Clutch, and a Door	EQP_1

Four Buttons are used to start and stop the motor, and engage and disengage the clutch	EQP_2

A Controller is supposed to manage this equipment	EQP_3

Buttons and Controller are weakly synchronized	FUN_1

Controller are Equipment are strongly synchronized	FUN_2

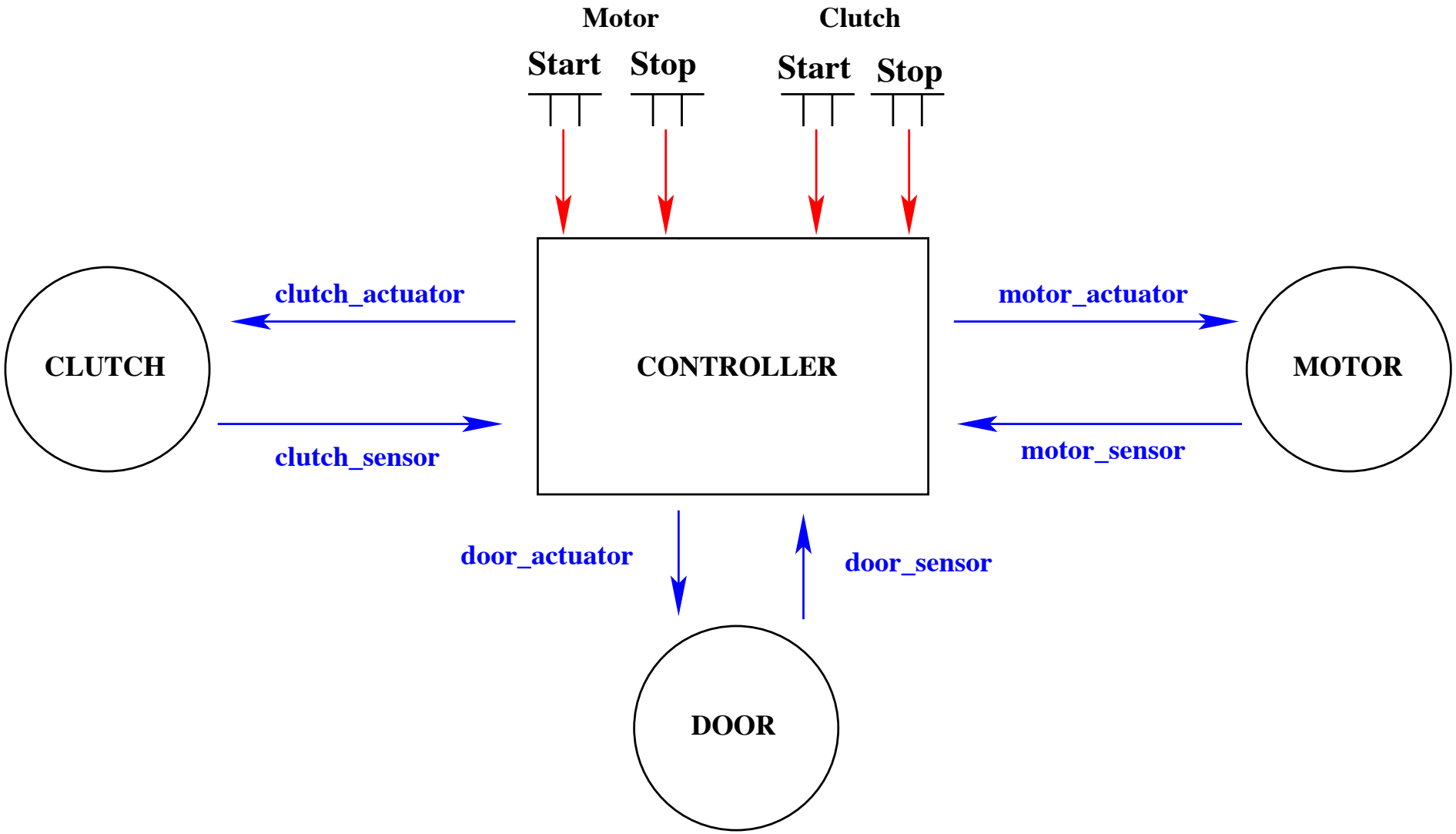
When the clutch is engaged, the motor must work	SAF_1

When the clutch is engaged, the door must be closed	SAF_2

When the clutch is engaged, the door cannot be closed several times, ONLY ONCE	FUN_3

When the door is closed, the clutch cannot be disengaged several times, ONLY ONCE	FUN_4

Opening and closing the door are not independent. It must be synchronized with disengaging and engaging the clutch	FUN_5


Motor
Clutch
Start
Stop
Start
Stop
CLUTCH
clutch_actuator
clutch_sensor
CONTROLLER
motor_actuator
motor_sensor
MOTOR
door_actuator
door_sensor
DOOR

4. Proposing a Refinement Strategy

Refinement Strategy

- Initial model: Connecting the controller to the motor

- 1st refinement: Connecting the motor buttons to the controller

- 2nd refinement: Connecting the controller to the clutch

- 3rd refinement: Constraining the clutch and the motor

Refinement Strategy (cont'd)

- 4th refinement: Connecting the controller to the door

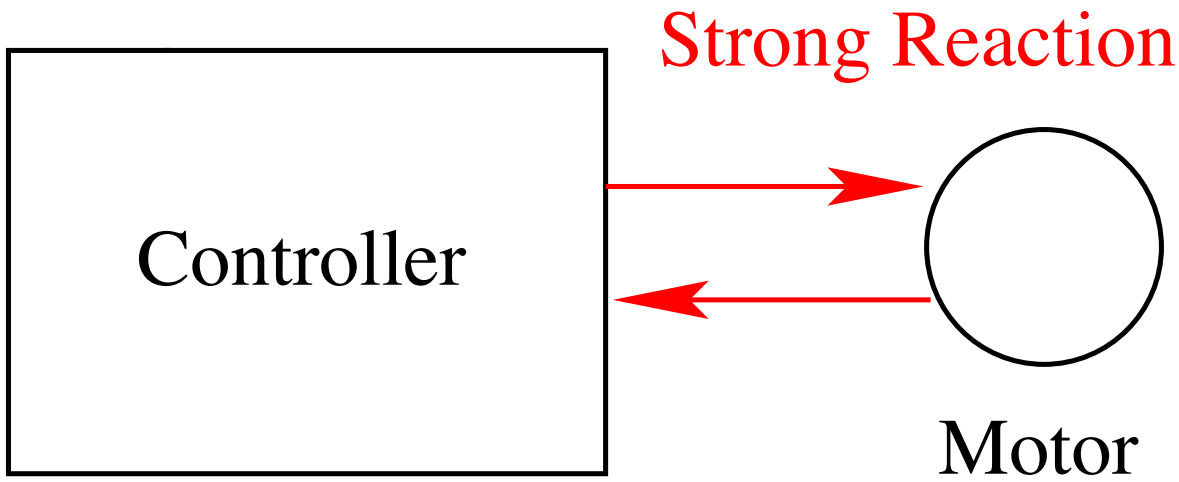
- 5th refinement: Constraining the clutch and the door

- 6th refinement: More constraints between clutch and door

- 7th refinement: Connecting the clutch buttons to the controller

5. Development of the Model using Refinements and Design Patterns

Initial Model: Connecting the Controller to the Motor



Controller are Equipment are strongly synchronized	FUN_2

The counters have

been removed

init
$a := 0$
$r := 0$

a_on
when
$a = 0$
$r = 0$
then
$a := 1$
end

a_off
when
$a = 1$
$r = 1$
then
$a := 0$
end

r_on
when
$r = 0$
$a = 1$
then
$r := 1$
end

r_off
when
$r = 1$
$a = 0$
then
$r := 0$
end

set: $STATUS$

constants: $stopped$, $working$

axm0_1: $STATUS = \{stopped, working\}$

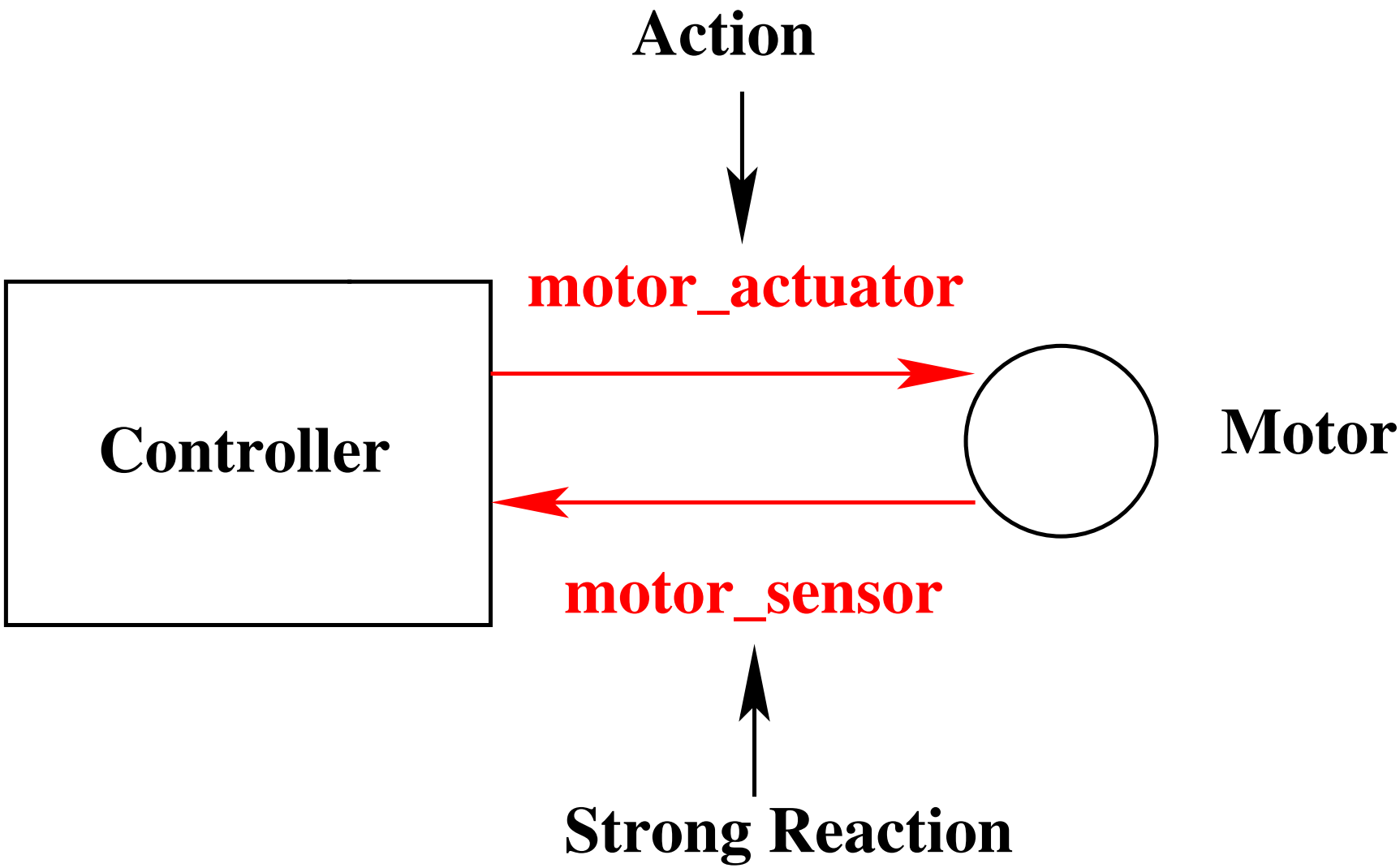
axm0_2: $stopped \neq working$

Initial Model: the State

variables: $motor\_actuator$
$motor\_sensor$

inv0_1: $motor\_sensor \in STATUS$

inv0_2: $motor\_actuator \in STATUS$


Action
motor_actuator
Controller
Motor
motor_sensor
Strong Reaction

Pattern Instantiation

- We instantiate the strong pattern as follows:

$$
\begin{array}{lcl}
a & \leadsto & motor\_actuator \\
r & \leadsto & motor\_sensor \\
0 & \leadsto & stopped \\
1 & \leadsto & working
\end{array}
$$

a_on	$\leadsto$	treat_start_motor
a_off	$\leadsto$	treat_stop_motor
r_on	$\leadsto$	Motor_start
r_off	$\leadsto$	Motor_stop

- Convention: Controller events start with "treat_"

Initial Model: Initialization

init
$a := 0$
$r := 0$

init
$motor\_actuator := stopped$
$motor\_sensor := stopped$

a_on
when
$a = 0$
$r = 0$
then
$a := 1$
end

treat_start_motor
when
$motor\_actuator = stopped$
$motor\_sensor = stopped$
then
$motor\_actuator := working$
end

r_on
when
$r = 0$
$a = 1$
then
$r := 1$
end

Motor_start
when
$motor\_sensor = stopped$
$motor\_actuator = working$
then
$motor\_sensor := working$
end

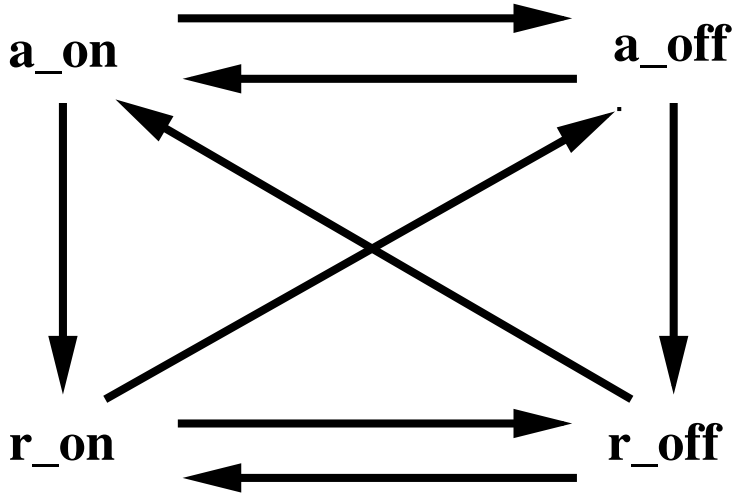
a_off
when
$a = 1$
$r = 1$
then
$a := 0$
end

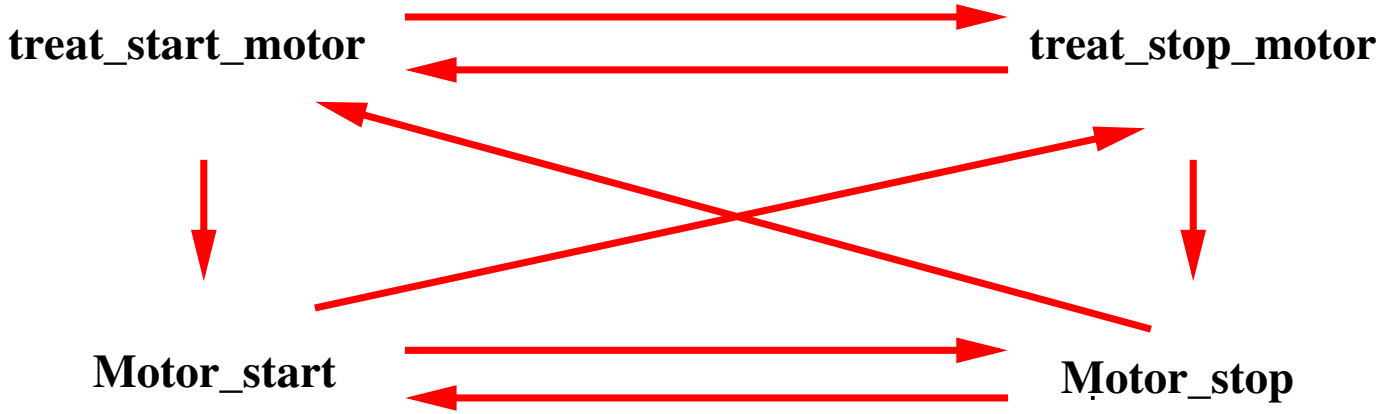
treat_stop_motor
when
$motor\_actuator = working$
$motor\_sensor = working$
then
$motor\_actuator := stopped$
end

Initial Model: Environment Event (2)

r_off
when
$r = 1$
$a = 0$
then
$r := 0$
end

Motor_stop
when
$motor\_sensor = working$
$motor\_actuator = stopped$
then
$motor\_sensor := stopped$
end

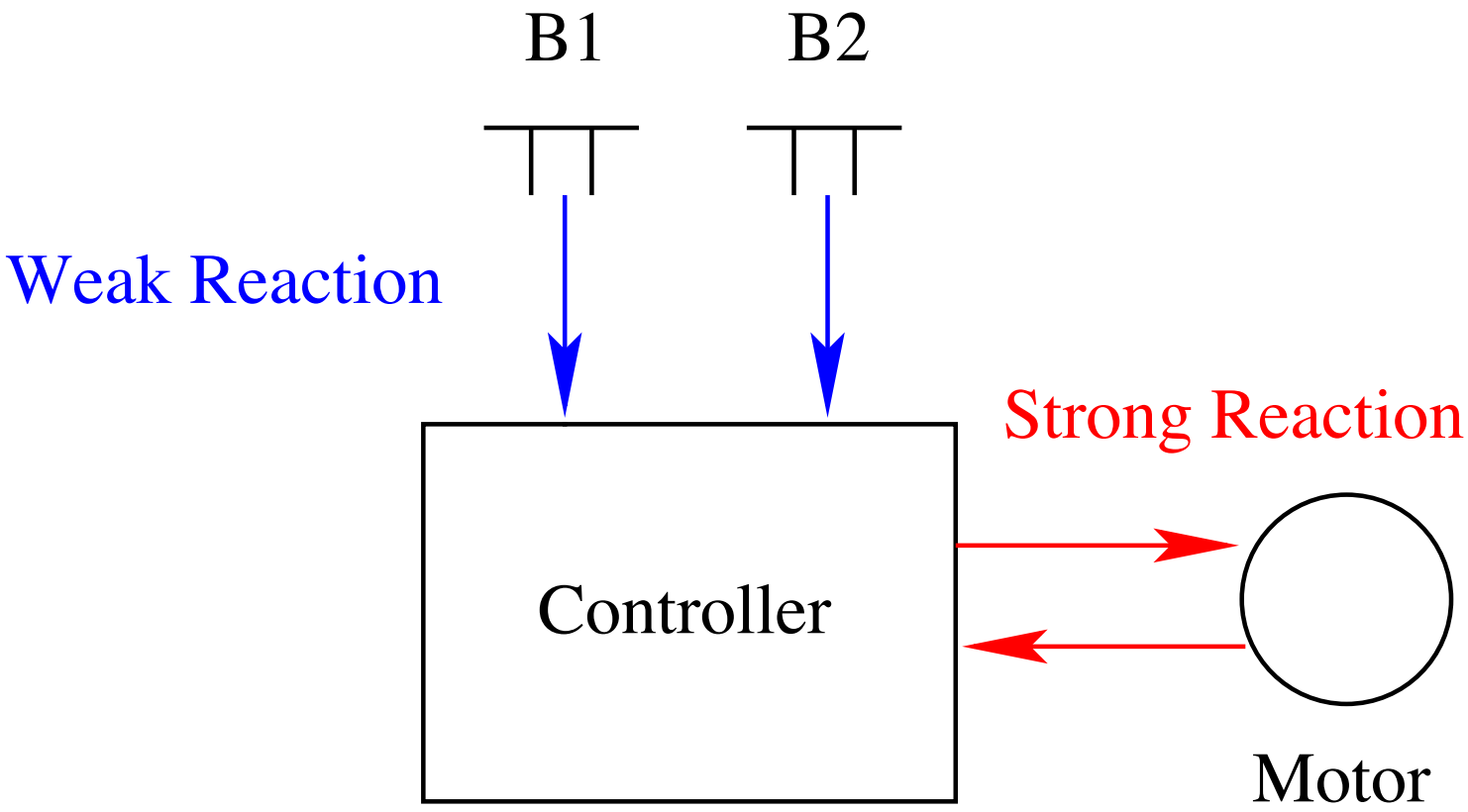

a_on
a_off
r_on
r_off


treat_start_motor
treat_stop_motor
Motor_start
Motor_stop

Initial Model: Summary of the Events

- Environment
    - motor_start
    - motor_stop

- Controller
    - treat_start_motor
    - treat_stop_motor



Buttons and Controller are weakly synchronized	FUN_1

The counters have

been removed

init
$a := 0$
$r := 0$

a_on
when
$a = 0$
then
$a := 1$
end

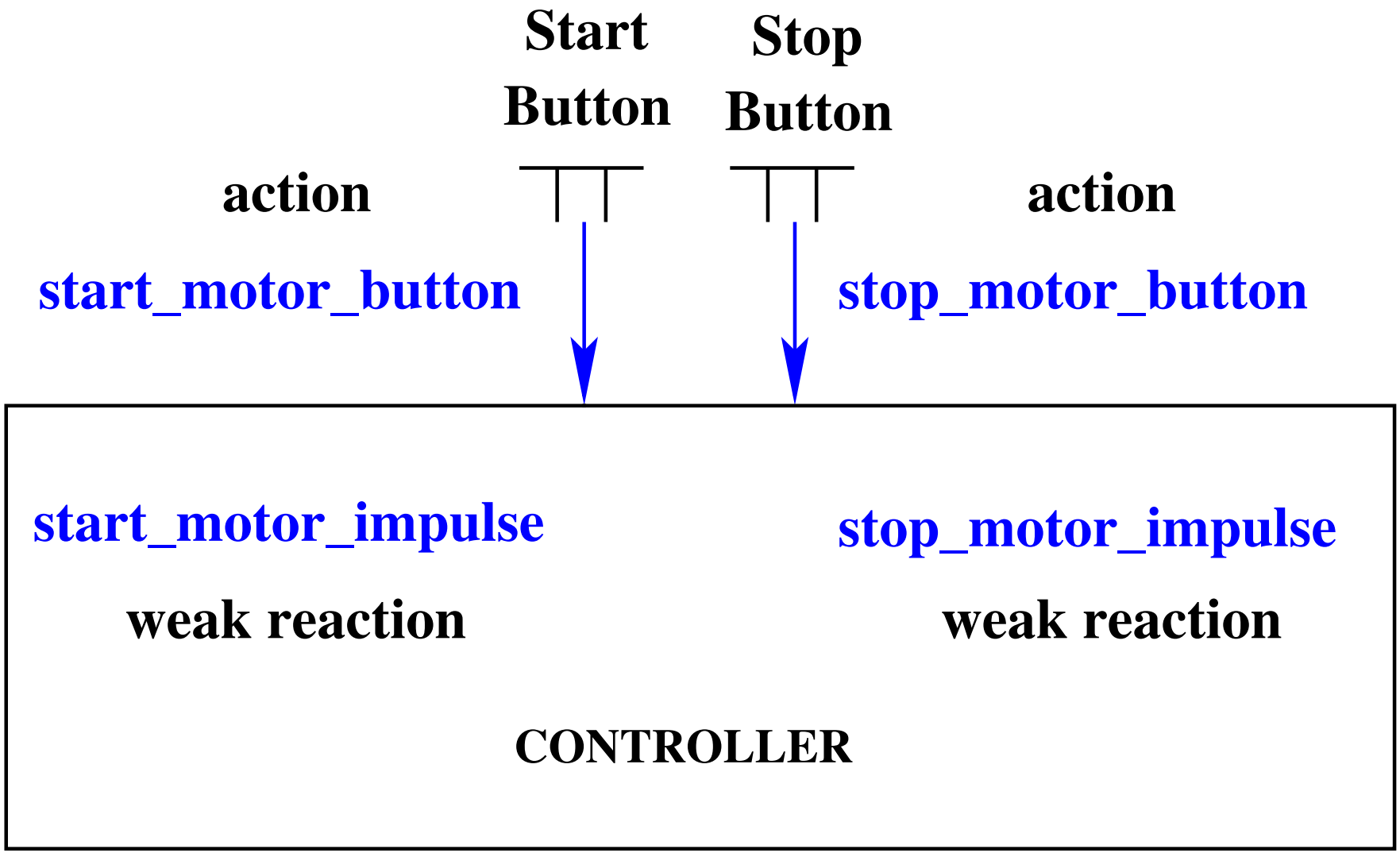
a_off
when
$a = 1$
then
$a := 0$
end

r_on
when
$r = 0$
$a = 1$
then
$r := 1$
end

r_off
when
$r = 1$
$a = 0$
then
$r := 0$
end

variables: ...
$start\_motor\_button$
$stop\_motor\_button$
$start\_motor\_impulse$
$stop\_motor\_impulse$

inv1_1: $stop\_motor\_button \in \mathrm{BOOL}$
inv1_2: $start\_motor\_button \in \mathrm{BOOL}$
inv1_3: $stop\_motor\_impulse \in \mathrm{BOOL}$
inv1_4: $start\_motor\_impulse \in \mathrm{BOOL}$


Start
Button
Stop
Button
action
action
start_motor_button
stop_motor_button
start_motor_impulse
stop_motor_impulse
weak reaction
weak reaction
CONTROLLER

Pattern Instantiation

- We instantiate the pattern as follows:

$$
\begin{array}{lcl}
a & \leadsto & start\_motor\_button \\
r & \leadsto & start\_motor\_impulse \\
0 & \leadsto & \mathbf{FALSE} \\
1 & \leadsto & \mathbf{TRUE}
\end{array}
$$

a_on	$\leadsto$	push_start_motor_button
a_off	$\leadsto$	release_stop_motor_button
r_on	$\leadsto$	treat_push_start_motor_button
r_off	$\leadsto$	treat_release_start_motor_button

- We rename treat_start_motor as treat_push_start_motor_button

init

$a := 0$
$r := 0$

init

$motor\_actuator := stopped$
$motor\_sensor := stopped$
$start\_motor\_button := \mathrm{FALSE}$
$start\_motor\_impulse := \mathrm{FALSE}$

First Refinement: New Environment Events (1)

a_on
when
$a = 0$
then
$a := 1$
end

push_start_motor_button
when
$start\_motor\_button = \mathrm{FALSE}$
then
$start\_motor\_button := \mathrm{TRUE}$
end

a_off
when
$a = 1$
then
$a := 0$
end

release_start_motor_button
when
$start\_motor\_button = \mathrm{TRUE}$
then
$start\_motor\_button := \mathrm{FALSE}$
end

First Refinement: Refining Controller Events (1)

r_on

when
$r = 0$
$a = 1$

then
$r := 1$

end

treat_push_start_motor_button
refines
treat_start_motor
when
$start\_motor\_impulse = \mathrm{FALSE}$
$start\_motor\_button = \mathrm{TRUE}$
$motor\_actuator = stopped$
$motor\_sensor = stopped$
then
$start\_motor\_impulse := \mathrm{TRUE}$
$motor\_actuator := working$
end

- This is the most important slide of the talk
- We can see how patterns can be superposed

a_on

when

$a = 0$

$r = 0$

then

$a := 1$

end

treat_start_motor

when

$motor\_actuator = stopped$

$motor\_sensor = stopped$

then

$motor\_actuator := working$

end

r_on

when

r = 0

a = 1

then

r := 1

end

treat_push_start_motor_button

when

$start\_motor\_impulse = \mathrm{FALSE}$

$start\_motor\_button = \mathrm{TRUE}$

$motor\_actuator = stopped$

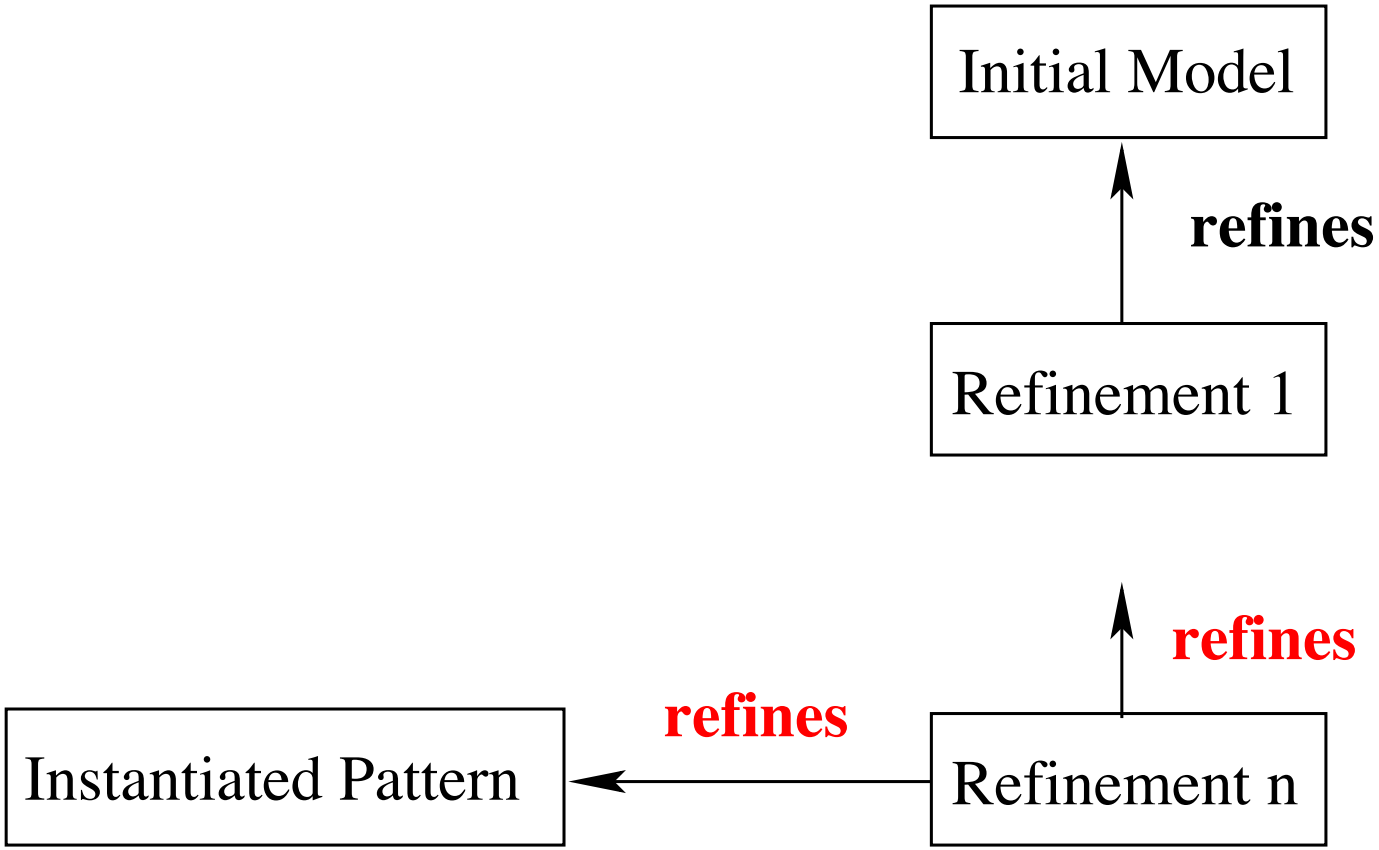
$motor\_sensor = stopped$

then

$start\_motor\_impulse := \mathrm{TRUE}$

$motor\_actuator := working$

end


Initial Model
refines
Refinement 1
refines
refines
Instantiated Pattern
Refinement n

r_off
when
$r = 1$
$a = 0$
then
$r := 0$
end

treat_release_start_motor_button
when
$start\_motor\_impulse = \mathrm{TRUE}$
$start\_motor\_button = \mathrm{FALSE}$
then
$start\_motor\_impulse := \mathrm{FALSE}$
end

Pattern Instantiation

- We instantiate the pattern as follows:

$$
\begin{array}{lcl}
a & \leadsto & \mathit{stop\_motor\_button} \\
r & \leadsto & \mathit{stop\_motor\_impulse} \\
\mathbf{0} & \leadsto & \mathbf{FALSE} \\
\mathbf{1} & \leadsto & \mathbf{TRUE}
\end{array}
$$

a_on	$\leadsto$	push_stop_motor_button
a_off	$\leadsto$	release_stop_motor_button
r_on	$\leadsto$	treat_push_stop_motor_button
r_off	$\leadsto$	treat_release_stop_motor_button

init

$a := 0$
$r := 0$

init

$motor\_actuator := stopped$
$motor\_sensor := stopped$
$start\_motor\_button := \mathbf{FALSE}$
$start\_motor\_impulse := \mathbf{FALSE}$
$stop\_motor\_button := \mathbf{FALSE}$
$stop\_motor\_impulse := \mathbf{FALSE}$

First Refinement: New Environment Events

a_on
when
$a = 0$
then
$a := 1$
end

push_stop_motor_button
when
$stop\_motor\_button = \mathrm{FALSE}$
then
$stop\_motor\_button := \mathrm{TRUE}$
end

a_off
when
$a = 1$
then
$a := 0$
end

release_stop_motor_button
when
$stop\_motor\_button = \mathrm{TRUE}$
then
$stop\_motor\_button := \mathrm{FALSE}$
end

First Refinement: Refining Controller Events (2)

r_on

when
$r = 0$
$a = 1$

then
$r := 1$

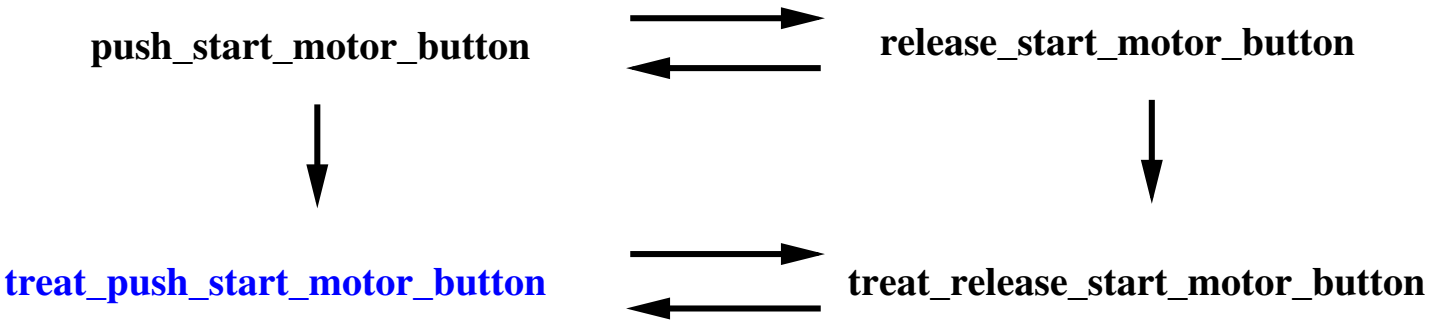
end

treat_push_stop_motor_button
refines
treat_stop_motor
when
$stop\_motor\_impulse = \mathrm{FALSE}$
$stop\_motor\_button = \mathrm{TRUE}$
$motor\_sensor = working$
$motor\_actuator = working$
then
$stop\_motor\_impulse := \mathrm{TRUE}$
$motor\_actuator := stopped$
end

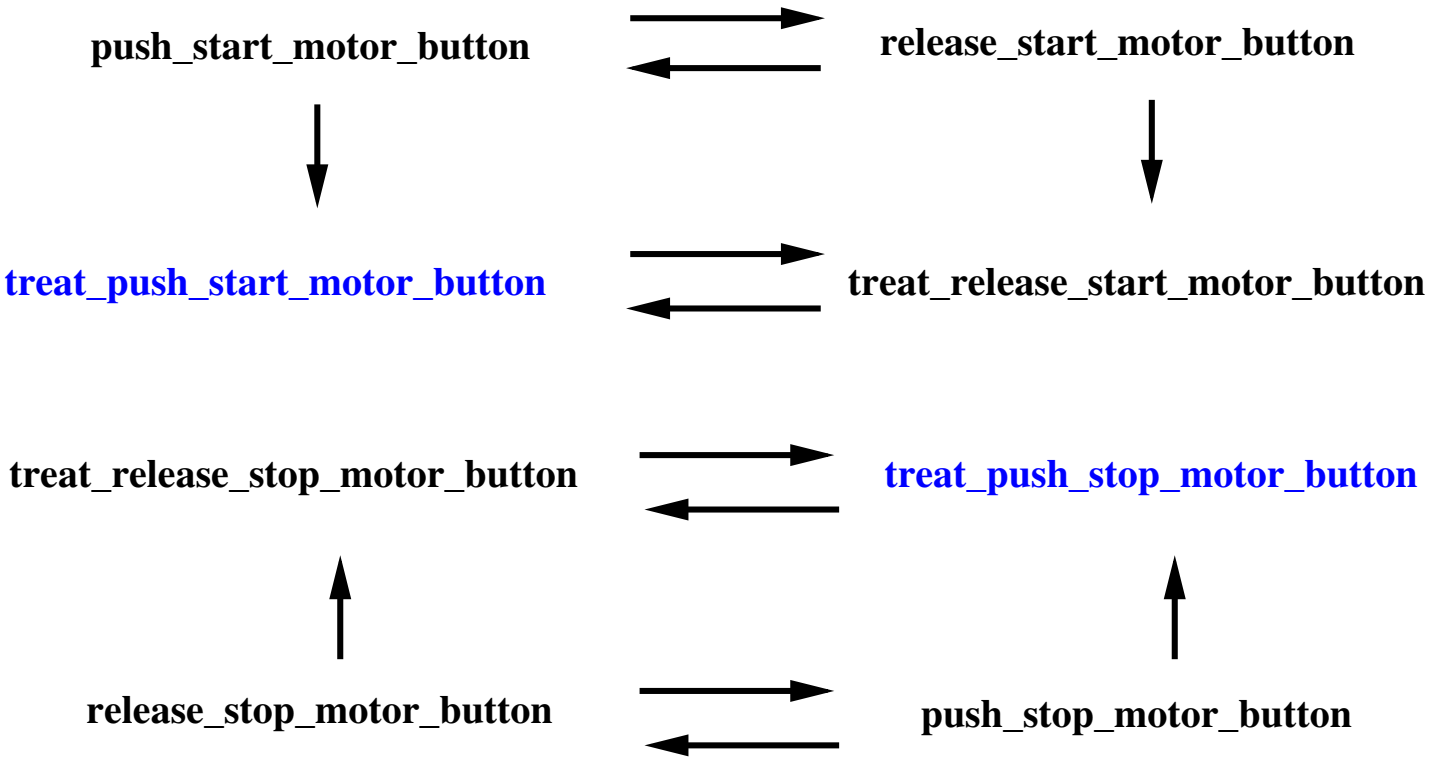
r_off
when
$r = 1$
$a = 0$
then
$r := 0$
end

treat_release_stop_motor_button
when
$stop\_motor\_impulse = \mathrm{TRUE}$
$stop\_motor\_button = \mathrm{FALSE}$
then
$stop\_motor\_impulse := \mathrm{FALSE}$
end

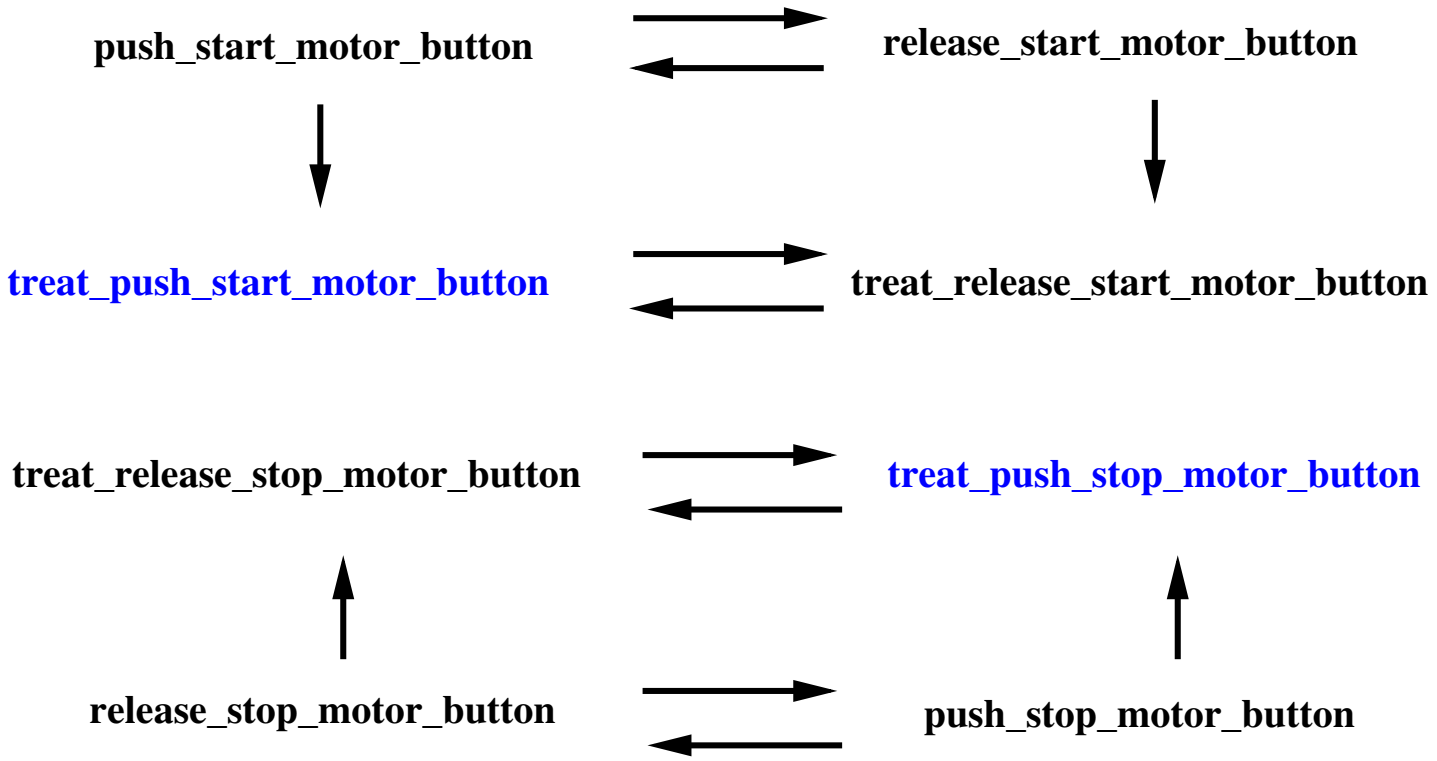
Independent Synchronizations

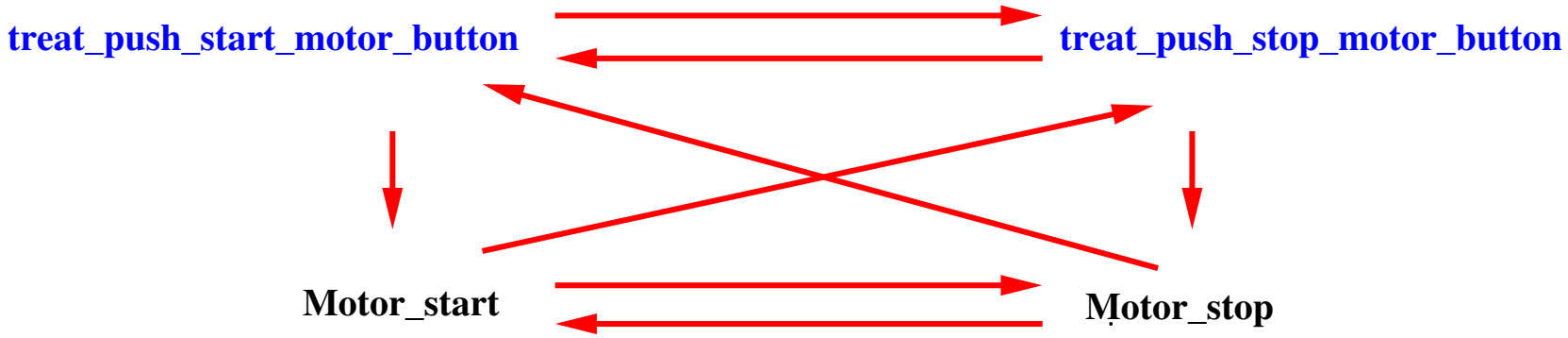


Independent Synchronizations

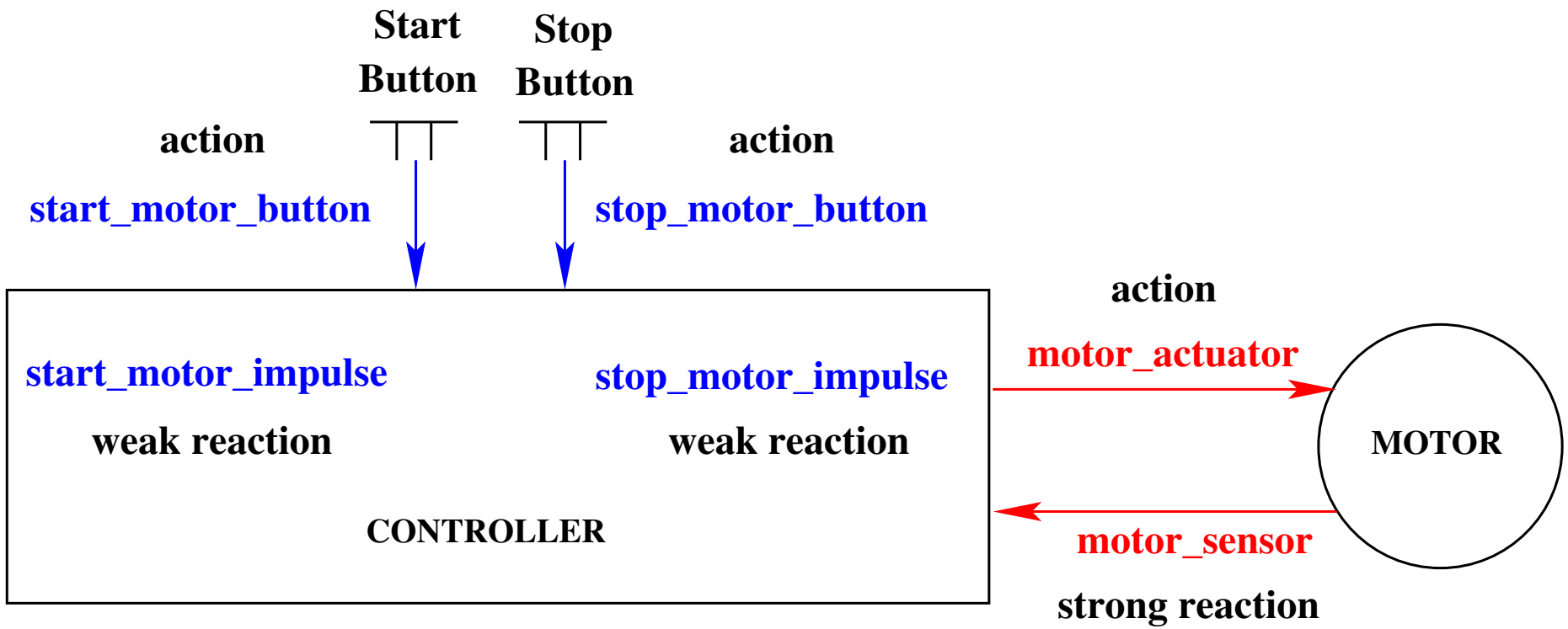


Independent Synchronizations

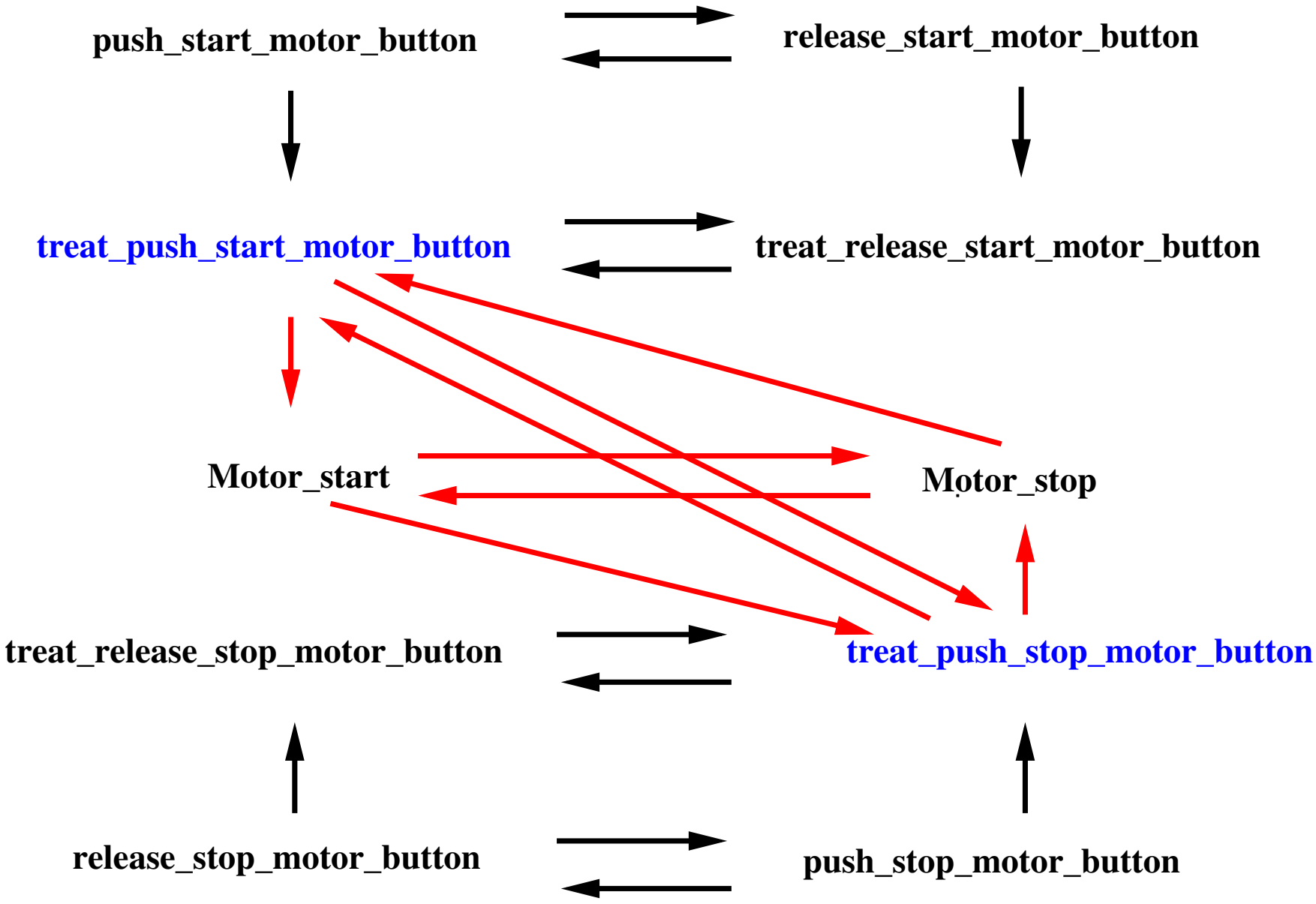




Weak and Strong Reactions Together



Combined Synchronizations



treat_push_start_motor_button
refines
treat_start_motor
when
$start\_motor\_impulse = \mathrm{FALSE}$
$start\_motor\_button = \mathrm{TRUE}$
$motor\_actuator = stopped$
$motor\_sensor = stopped$
then
$start\_motor\_impulse := \mathrm{TRUE}$
$motor\_actuator := working$
end

- What happens when the following hold

$$\neg\,(motor\_actuator = stopped \;\wedge\; motor\_sensor = stopped)$$

- We need another event

Problems with treat_push_start_motor_button

treat_push_start_motor_button
refines
treat_start_motor
when
$start\_motor\_impulse = \text{FALSE}$
$start\_motor\_button = \text{TRUE}$
$motor\_actuator = stopped$
$motor\_sensor = stopped$
then
$start\_motor\_impulse := \text{TRUE}$
$motor\_actuator := working$
end

treat_push_start_motor_button_false
when
$start\_motor\_impulse = \text{FALSE}$
$start\_motor\_button = \text{TRUE}$
$\neg\ (motor\_actuator = stopped\ \wedge$
$motor\_sensor = stopped)$
then
$start\_motor\_impulse := \text{TRUE}$
end

- In the second case, the button has been pushed but the internal conditions are not met

- However, we need to record that the button has been pushed:

$$start\_motor\_impulse := \text{TRUE}$$

Problems with treat_push_stop_motor_button

treat_push_stop_motor_button
refines
treat_stop_motor
when
$stop\_motor\_impulse = \text{FALSE}$
$stop\_motor\_button = \text{TRUE}$
$motor\_sensor = working$
$motor\_actuator = working$
then
$stop\_motor\_impulse := \text{TRUE}$
$motor\_actuator := stopped$
end

treat_push_stop_motor_button_false
when
$stop\_motor\_impulse = \text{FALSE}$
$stop\_motor\_button = \text{TRUE}$
$\neg (motor\_sensor = working \ \wedge$
$motor\_actuator = working)$
then
$stop\_motor\_impulse := \text{TRUE}$
end

- In the second case, the button has been pushed but the internal conditions are not met

- However, we need to record that the button has been pushed:

$$stop\_motor\_impulse := \text{TRUE}$$

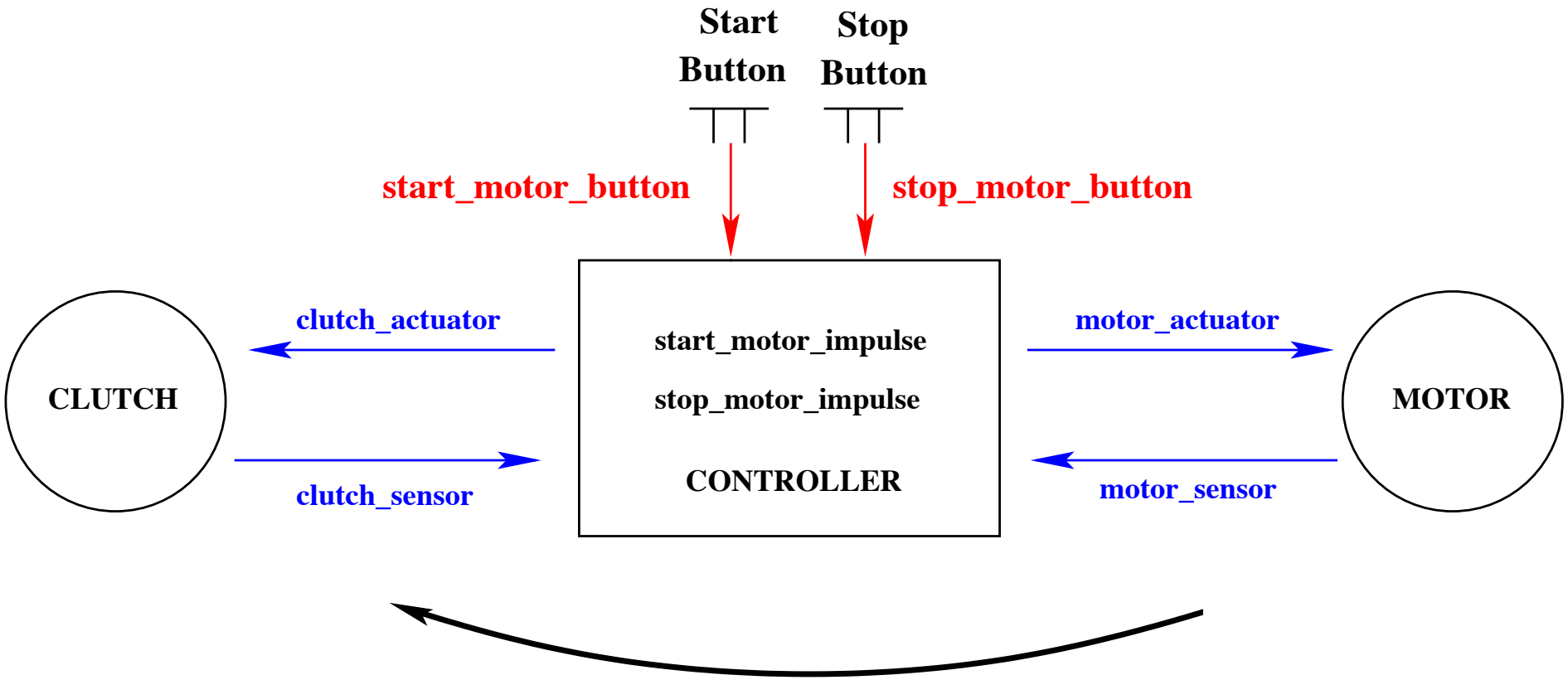
First Refinement: Summary of the Events (1)

- Environment
  - motor_start
  - motor_stop
  - push_start_motor_button
  - release_start_motor_button
  - push_stop_motor_button
  - release_stop_motor_button

First Refinement: Summary of the Events (2)

- Controller
  - treat_push_start_motor_button
  - treat_push_start_motor_button_false
  - treat_push_stop_motor_button
  - treat_push_stop_motor_button_false
  - treat_release_start_motor_button
  - treat_release_stop_motor_button

2nd Refinement: Connecting the Controller to the Clutch



- We introduce the set in a new context:

$$CLUTCH = \{engaged, disengaged\}$$

- We copy the initial model where we instantiate:

$$\begin{array}{lcl} motor & \leadsto & clutch \\ STATUS & \leadsto & CLUTCH \\ working & \leadsto & engaged \\ stopped & \leadsto & disengaged \end{array}$$

Second Refinement: Summary of the Events (1)

- Environment
    - motor_start
    - motor_stop
    - clutch_start
    - clutch_stop
    - push_start_motor_button
    - release_start_motor_button
    - push_stop_motor_button
    - release_stop_motor_button

Second Refinement: Summary of the Events (2)

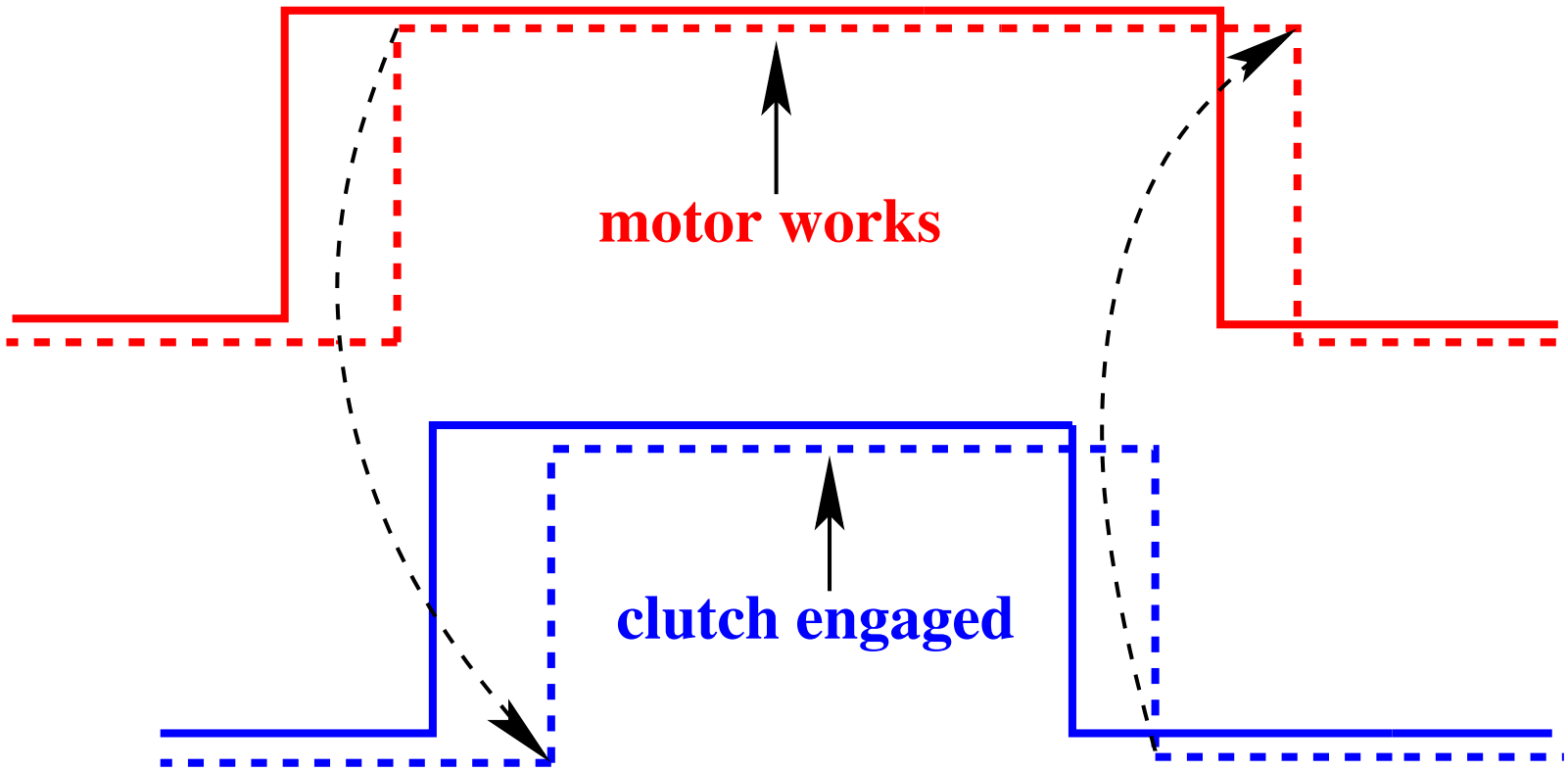
- Controller
    - treat_push_start_motor_button
    - treat_push_start_motor_button_false
    - treat_push_stop_motor_button
    - treat_push_stop_motor_button_false
    - treat_release_start_motor_button
    - treat_release_stop_motor_button
    - treat_start_clutch
    - treat_stop_clutch

- An additional safety constraint

When the clutch is engaged, the motor must work	SAF_1

- For this we develop ANOTHER DESIGN PATTERN

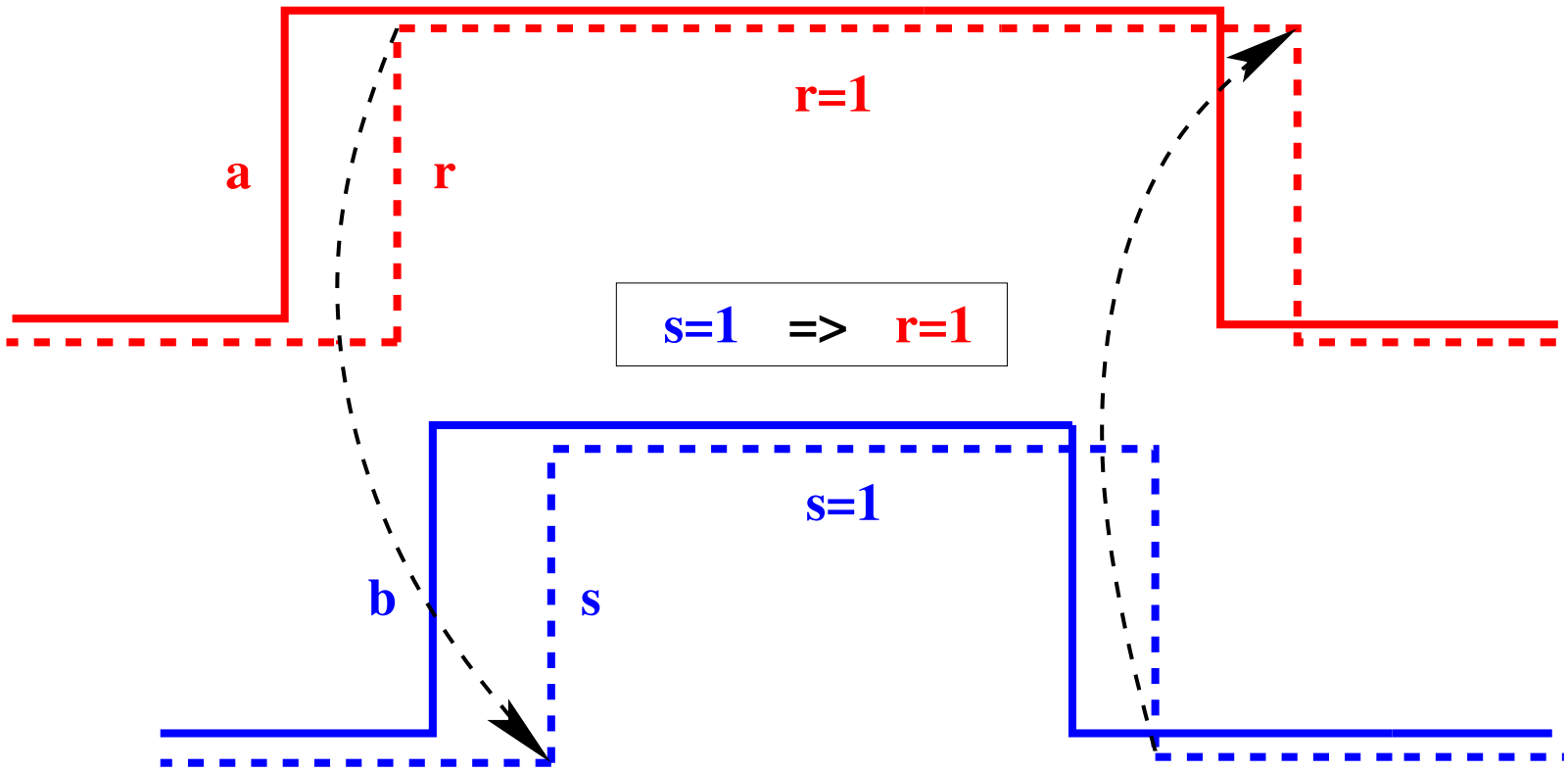
- It is called: Weak synchronization of two Strong Reactions



When the clutch is engaged

then

the motor must work

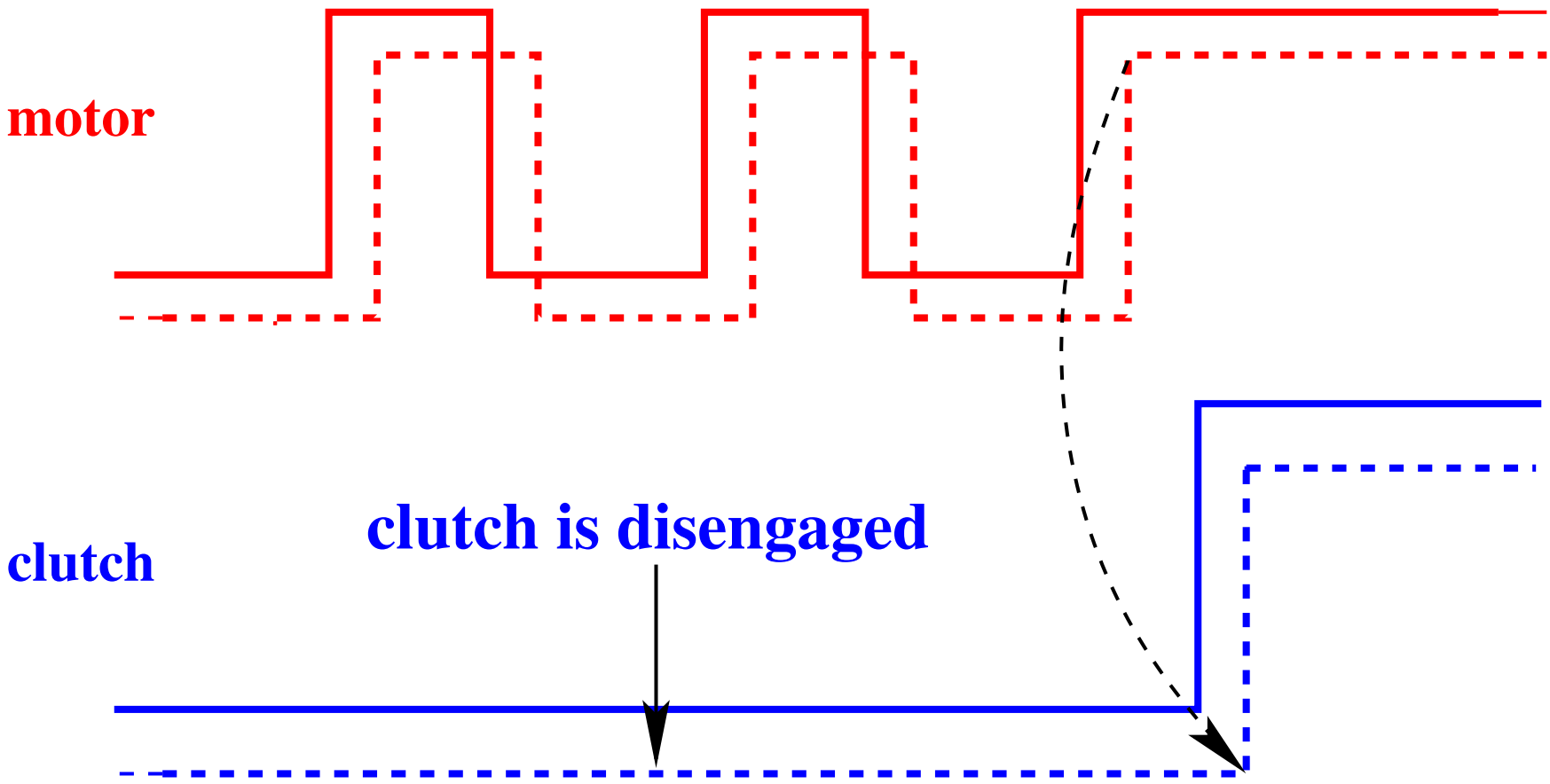


When the clutch is engaged

then

the motor must work

The Synchronization is Weak (1)

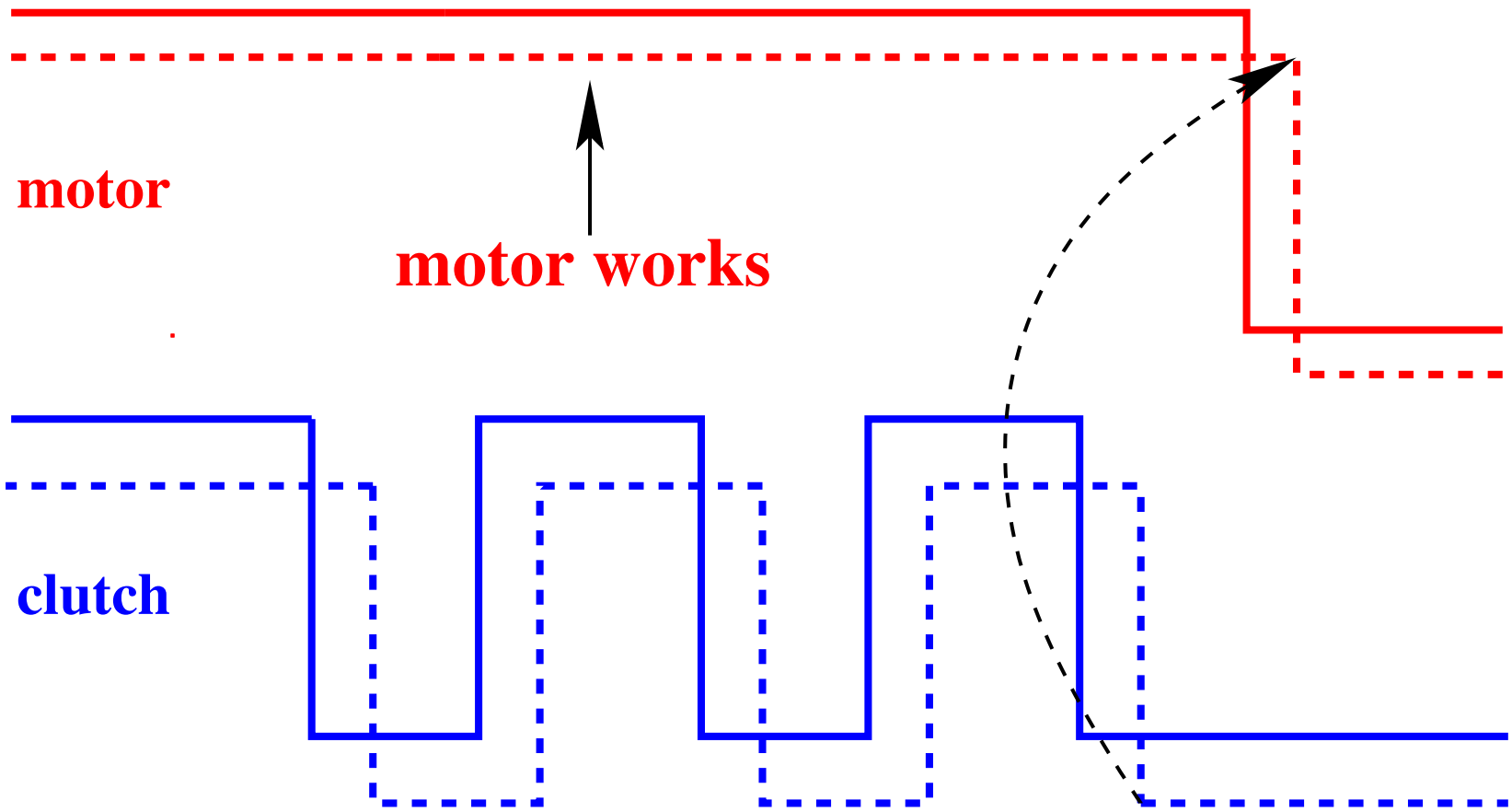


When the clutch is disengaged,

then

the motor can be started and stopped several times

The Synchronization is Weak (2)

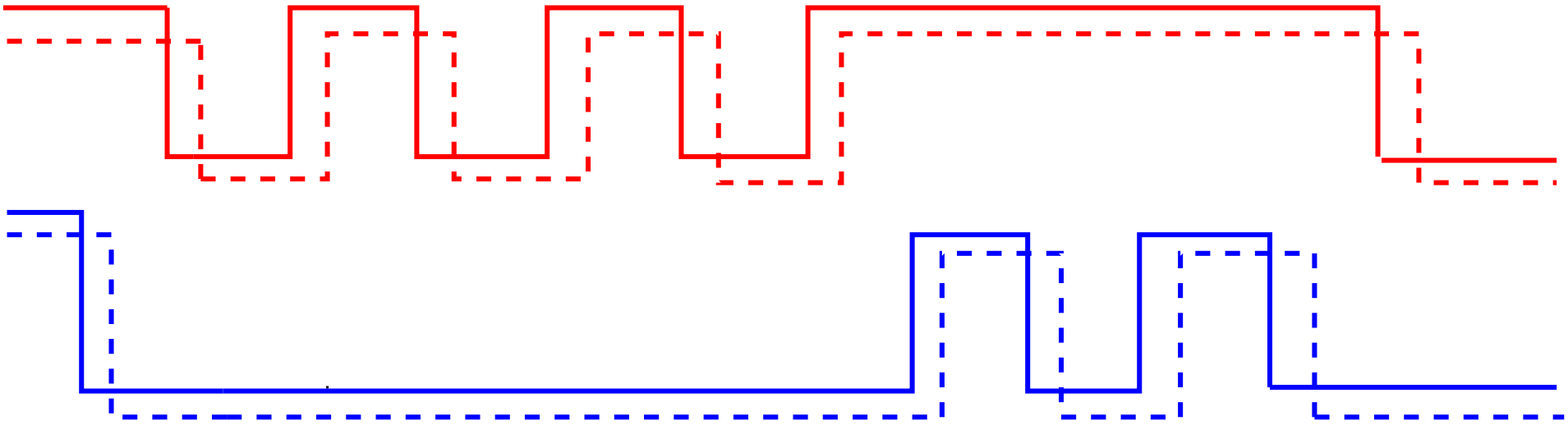


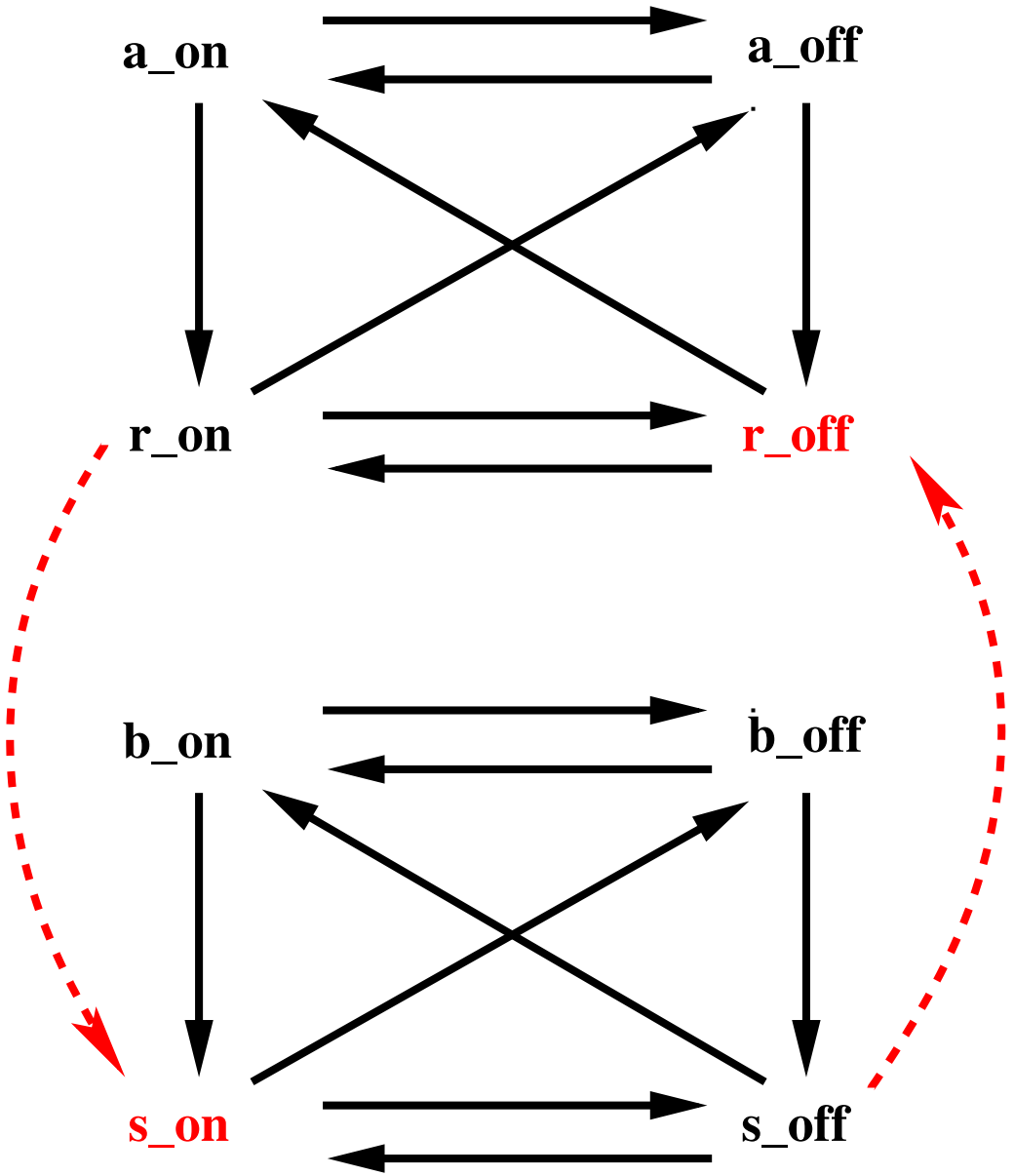
When the motor works,

then

the clutch can be engaged and disengaged several times

Putting the Two Together




a_on
a_off
r_on
r_off
b_on
b_off
s_on
s_off

dbl0_1: $a \in \{0,1\}$
dbl0_2: $r \in \{0,1\}$
dbl0_3: $ca \in \mathbb{N}$
dbl0_4: $cr \in \mathbb{N}$
dbl0_5: $a = 1 \wedge r = 0 \Rightarrow ca = cr + 1$
dbl0_6: $a = 0 \vee r = 1 \Rightarrow ca = cr$

dbl0_7: $b \in \{0,1\}$
dbl0_8: $s \in \{0,1\}$
dbl0_9: $cb \in \mathbb{N}$
dbl0_10: $cs \in \mathbb{N}$
dbl0_11: $b = 1 \wedge s = 0 \Rightarrow cb = cs + 1$
dbl0_12: $b = 0 \vee s = 1 \Rightarrow cb = cs$

The Initial Event Situation (1)

a_on
when
$a = 0$
$r = 0$
then
$a := 1$
$ca := ca + 1$
end

r_on
when
$r = 0$
$a = 1$
then
$r := 1$
$cr := cr + 1$
end

a_off
when
$a = 1$
$r = 1$
then
$a := 0$
end

r_off
when
$r = 1$
$a = 0$
then
$r := 0$
end

The Initial Event Situation (2)

b_on
when
$b = 0$
$s = 0$
then
$b := 1$
$cb := cb + 1$
end

s_on
when
$s = 0$
$b = 1$
then
$s := 1$
$cs := cs + 1$
end

b_off
when
$b = 1$
$s = 1$
then
$b := 0$
end

s_off
when
$s = 1$
$b = 0$
then
$s := 0$
end

The Synchronizing Invariant

dbl1_1: $s = 1 \Rightarrow r = 1$

- It seems sufficient to add the following guards

s_on
when
$s = 0$
$b = 1$
$r = 1$
then
$s := 1$
$cs := cs + 1$
end

r_off
when
$r = 1$
$a = 0$
$s = 0$
then
$r := 0$
end

- But we do not want to touch these events

s_on
when
$s = 0$
$b = 1$
$r = 1$
then
$s := 1$
$cs := cs + 1$
end

r_off
when
$r = 1$
$a = 0$
$s = 0$
then
$r := 0$
end

- We introduce the following additional invariants

dbl1_2: $b = 1 \Rightarrow r = 1$

dbl1_3: $a = 0 \Rightarrow s = 0$

Maintaining Invariant dbl1_2 (1)

dbl1_2: $b = 1 \Rightarrow r = 1$

In order to maintain this invariant, we have to refine b_on

b_on
when
$b = 0$
$s = 0$
then
$b := 1$
$cb := cb + 1$
end

$\rightsquigarrow$

b_on
when
$b = 0$
$s = 0$
$r = 1$
then
$b := 1$
$cb := cb + 1$
end

Maintaining (Contraposition of) Invariant dbl1_2 (2)

dbl1_2: $b = 1 \Rightarrow r = 1 \qquad (r = 0 \Rightarrow b = 0)$

In order to maintain this invariant, we have to refine r_off

r_off
when
$r = 1$
$a = 0$
then
$r := 0$
end

$\rightsquigarrow$

r_off
when
$r = 1$
$a = 0$
$b = 0$
then
$r := 0$
end

- But, again, we do not want to touch this event

r_off
when
$r = 1$
$a = 0$
$b = 0$
then
$r := 0$
end

- We introduce the following invariant

dbl1_4: $a = 0 \Rightarrow b = 0$

Maintaining Invariant dbl1_3 (1)

dbl1_3: $a = 0 \Rightarrow s = 0$

In order to maintain this invariant, we have to refine a_off

a_off
when
$a = 1$
$r = 1$
then
$a := 0$
end

$\rightsquigarrow$

a_off
when
$a = 1$
$r = 1$
$s = 0$
then
$a := 0$
end

Maintaining (Contraposition of) Invariant dbl1_3 (2)

dbl1_3: $a = 0 \Rightarrow s = 0 \qquad (s = 1 \Rightarrow a = 1)$

In order to maintain this invariant, we have to refine s_on

s_on
when
$s = 0$
$b = 1$
then
$s := 1$
$cs := cs + 1$
end

$\leadsto$

s_on
when
$s = 0$
$b = 1$
$a = 1$
then
$s := 1$
$cs := cs + 1$
end

- But, again, we do not want to touch this event

s_on
when
$s = 0$
$b = 1$
$a = 1$
then
$s := 1$
$cs := cs + 1$
end

- We have to introduce the following invariant

$$b = 1 \Rightarrow a = 1$$

- Fortunately, this is **dbl1_4** ($a = 0 \Rightarrow b = 0$) contraposed

Maintaining Invariant dbl1_4 (1)

dbl1_4: $a = 0 \Rightarrow b = 0$

In order to maintain this invariant, we have to refine a_off again

a_off
when
$a = 1$
$r = 1$
$s = 0$
then
$a := 0$
end

$\rightsquigarrow$

a_off
when
$a = 1$
$r = 1$
$s = 0$
$b = 0$
then
$a := 0$
end

Maintaining (Contraposition of) Invariant dbl1_4 (2)

dbl1_4: $a = 0 \Rightarrow b = 0 \qquad (b = 1 \Rightarrow a = 1)$

In order to maintain this invariant, we have to refine b_on again

b_on
when
$b = 0$
$s = 0$
$r = 1$
then
$b, cb := 1, cb + 1$
end

$\rightsquigarrow$

b_on
when
$b = 0$
$s = 0$
$r = 1$
$a = 1$
then
$b, cb := 1, cb + 1$
end

Summary of Refinement: Reactions have not been Touched

dbl1_1:	$s = 1$	$\Rightarrow$	$r = 1$
dbl1_2:	$b = 1$	$\Rightarrow$	$r = 1$
dbl1_3:	$a = 0$	$\Rightarrow$	$s = 0$
dbl1_4:	$a = 0$	$\Rightarrow$	$b = 0$

b_on
when
$b = 0$
$s = 0$
$r = 1$
$a = 1$
then
$b, cb := 1, cb + 1$
end

a_off
when
$a = 1$
$r = 1$
$s = 0$
$b = 0$
then
$a := 0$
end

Intuition about the Invariants

dbl1_1: $s = 1 \Rightarrow r = 1$
dbl1_2: $b = 1 \Rightarrow r = 1$
dbl1_3: $a = 0 \Rightarrow s = 0$
dbl1_4: $a = 0 \Rightarrow b = 0$

$(s = 1 \Rightarrow a = 1)$
$(b = 1 \Rightarrow a = 1)$

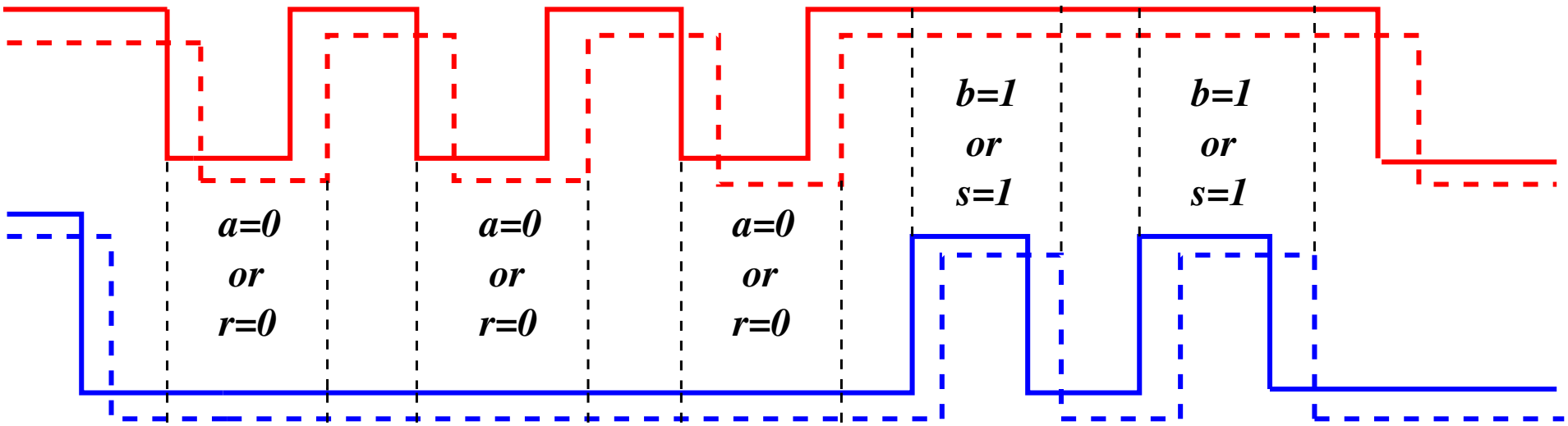
This can be put into a single invariant

dbl1_5: $b = 1 \lor s = 1 \Rightarrow a = 1 \land r = 1$

with the following contraposed form

dbl1_6: $a = 0 \lor r = 0 \Rightarrow b = 0 \land s = 0$

Intuition about the Invariants

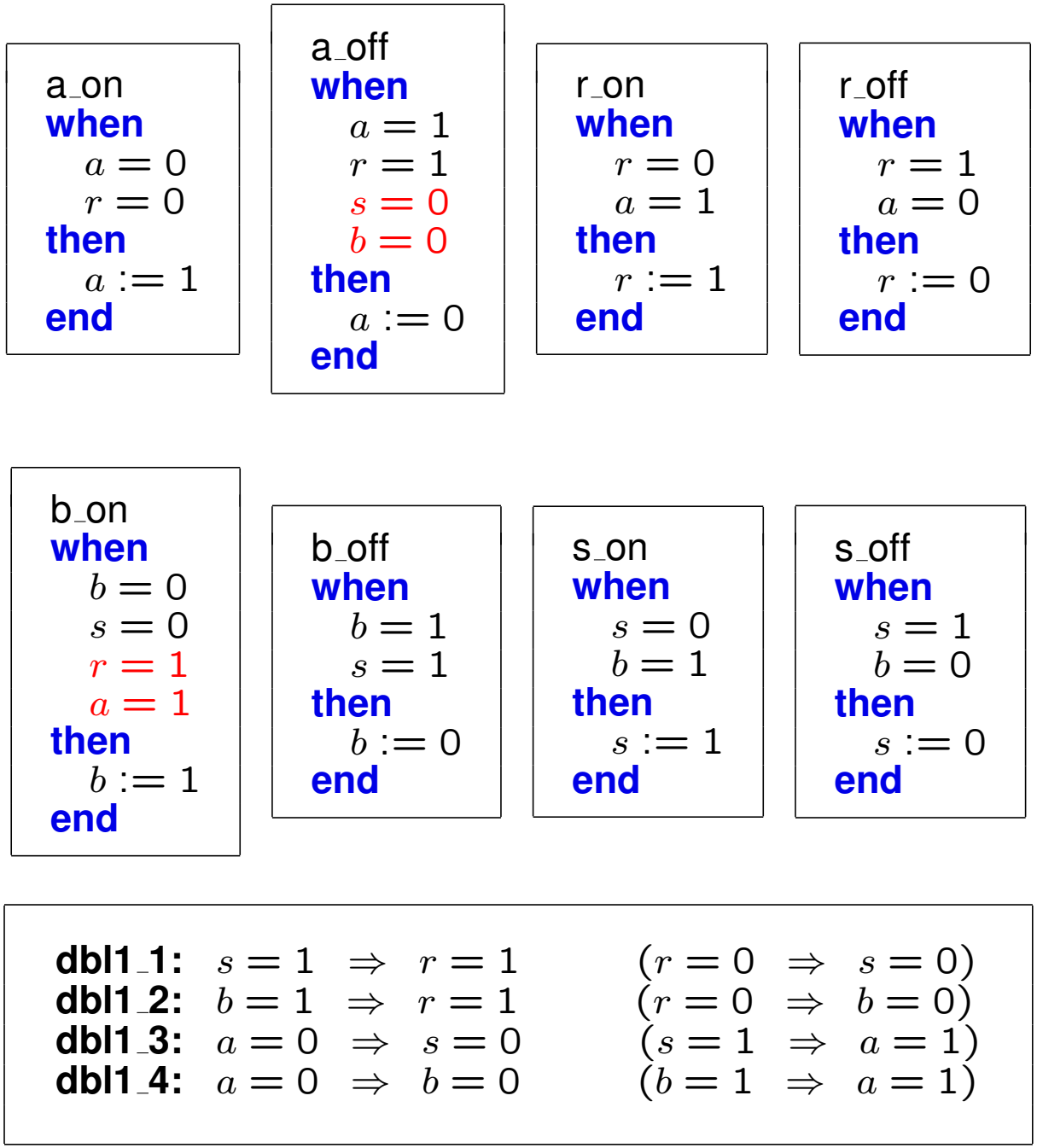


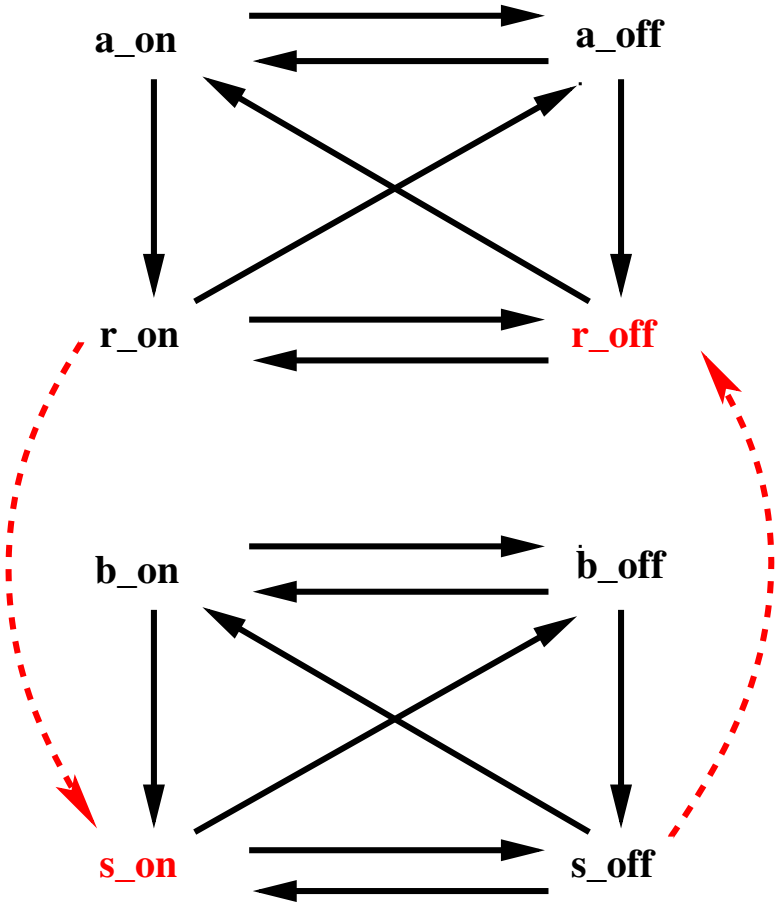
Reminder: - - - is the motor and - - - is the clutch

dbl1_5: $b = 1 \ \vee \ s = 1 \ \Rightarrow \ a = 1 \ \wedge \ r = 1$

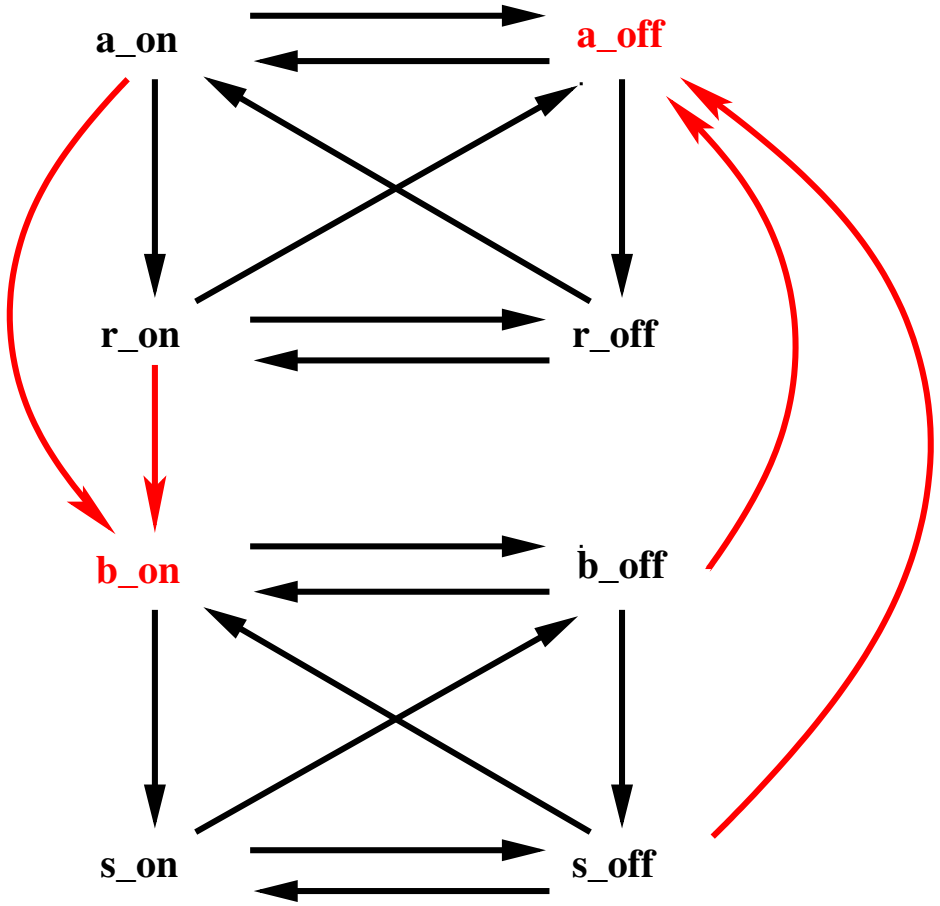
dbl1_6: $a = 0 \ \vee \ r = 0 \ \Rightarrow \ b = 0 \ \wedge \ s = 0$

Looking at the Result





dbl1_1: $s = 1 \Rightarrow r = 1 \qquad (r = 0 \Rightarrow s = 0)$



b_on
when
$b = 0$
$s = 0$
$r = 1$
$a = 1$
then
$b := 1$
end

a_off
when
$a = 1$
$r = 1$
$s = 0$
$b = 0$
then
$a := 0$
end

Back to 3rd Reft.: Constraining the Clutch and the Motor

When the clutch is engaged, the motor must work	SAF_1

inv3_1: $$clutch\_sensor = engaged \Rightarrow motor\_sensor = working$$

- This is an instance of the previous design pattern

Pattern Instantiation

- We instantiate the pattern as follows:

a	$\rightsquigarrow$	$motor\_actuator$	a_on	$\rightsquigarrow$	treat_push_start_motor_button
r	$\rightsquigarrow$	$motor\_sensor$	a_off	$\rightsquigarrow$	treat_push_stop_motor_button
0	$\rightsquigarrow$	$stopped$	r_on	$\rightsquigarrow$	Motor_start
1	$\rightsquigarrow$	$working$	r_off	$\rightsquigarrow$	Motor_stop

b	$\rightsquigarrow$	$clutch\_actuator$	b_on	$\rightsquigarrow$	treat_start_clutch
s	$\rightsquigarrow$	$clutch\_sensor$	b_off	$\rightsquigarrow$	treat_stop_clutch
0	$\rightsquigarrow$	$disengaged$	s_on	$\rightsquigarrow$	Clutch_start
1	$\rightsquigarrow$	$engaged$	s_off	$\rightsquigarrow$	Clutch_stop

Translating the pattern invariants (1)

dbl1_1: $s = 1 \Rightarrow r = 1$

dbl1_2: $b = 1 \Rightarrow r = 1$

inv3_1:
$$clutch\_sensor = engaged \Rightarrow motor\_sensor = working$$

inv3_2:
$$clutch\_actuator = engaged \Rightarrow motor\_sensor = working$$

Translating the pattern invariants (2)

dbl1_3: $a = 0 \Rightarrow s = 0$

dbl1_4: $a = 0 \Rightarrow b = 0$

inv3_3:
$$motor\_actuator = stopped \Rightarrow clutch\_sensor = disengaged$$

inv3_4:
$$motor\_actuator = stopped \Rightarrow clutch\_actuator = disengaged$$

Adapting the Events of the Pattern (1)

b_on
when
$b = 0$
$s = 0$
$r = 1$
$a = 1$
then
$b := 1$
end

treat_start_clutch
when
$clutch\_actuator = disengaged$
$clutch\_sensor = disengaged$
$motor\_sensor = working$
$motor\_actuator = working$
then
$clutch\_actuator := engaged$
end

Adapting the events of the pattern (2)

a_off
when

$a = 1$
$r = 1$
$s = 0$
$b = 0$

then

$a := 0$

end

treat_push_stop_motor_button
when

$stop\_motor\_impulse = \mathrm{FALSE}$
$stop\_motor\_button = \mathrm{TRUE}$
$motor\_actuator = working$
$motor\_sensor = working$
$clutch\_sensor = disengaged$
$clutch\_actuator = disengaged$

then

$motor\_actuator := stopped$
$stop\_motor\_impulse := \mathrm{TRUE}$

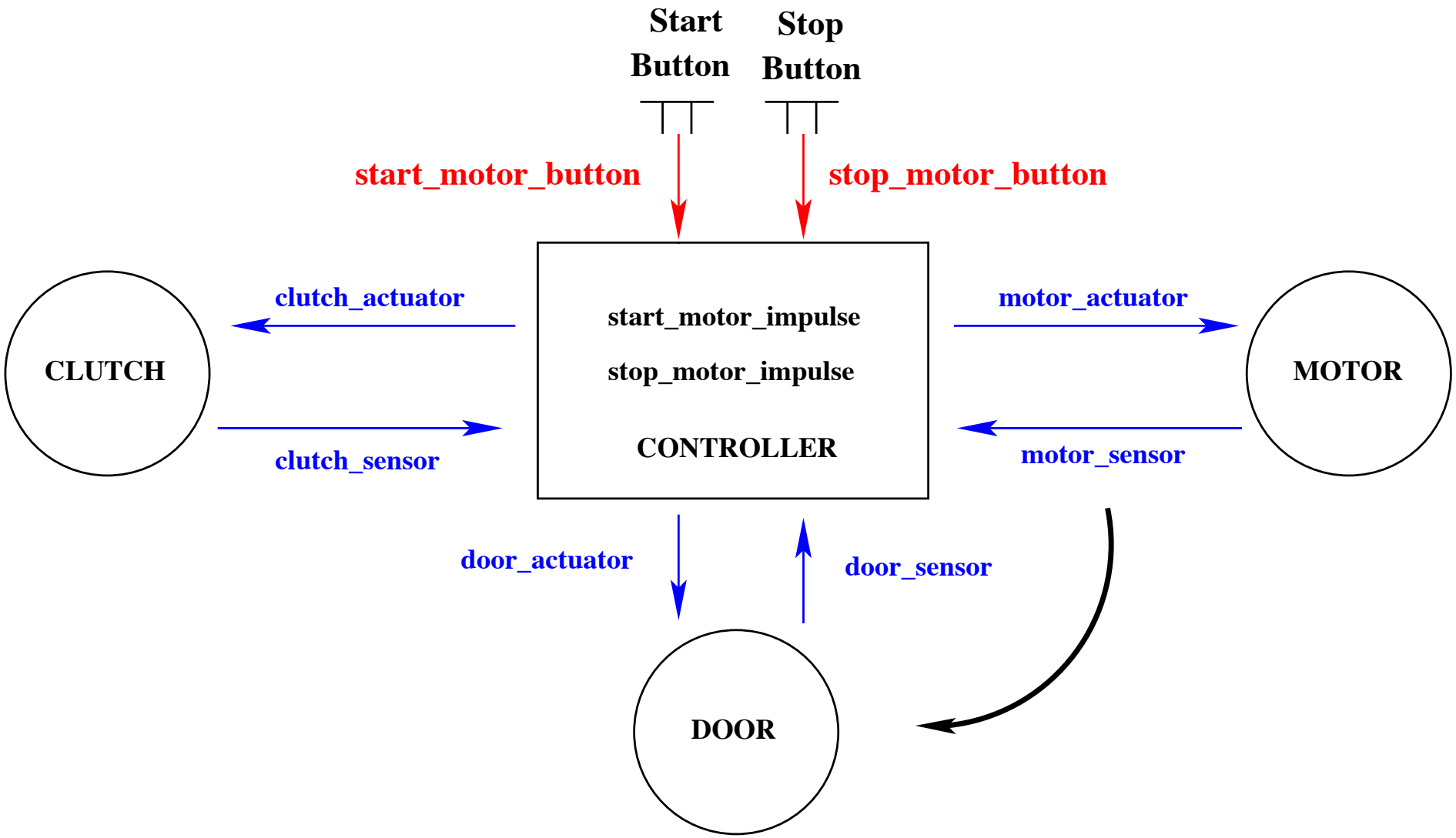
end

Third Refinement: Summary of the Events (1)

- Environment (no new events)
    - motor_start
    - motor_stop
    - clutch_start
    - clutch_stop
    - push_start_motor_button
    - release_start_motor_button
    - push_stop_motor_button
    - release_stop_motor_button

Third Refinement: Summary of the Events (2)

- Controller (no new events)
    - treat_push_start_motor_button
    - treat_push_start_motor_button_false
    - treat_push_stop_motor_button
    - treat_push_stop_motor_button_false
    - treat_release_start_motor_button
    - treat_release_stop_motor_button
    - treat_start_clutch
    - treat_stop_clutch



- We copy (after renaming "motor" to "door") what has been done in the initial model

- We introduce the set in a new context:

$$DOOR = \{open, closed\}$$

- We copy the initial model where we instantiate:

$$\begin{array}{lcl} motor & \leadsto & door \\ STATUS & \leadsto & DOOR \\ working & \leadsto & closed \\ stopped & \leadsto & open \end{array}$$

Fourth Refinement: Summary of the Events (1)

- Environment
    - motor_start
    - motor_stop
    - clutch_start
    - clutch_stop
    - door_close
    - door_open
    - push_start_motor_button
    - release_start_motor_button
    - push_stop_motor_button
    - release_stop_motor_button

Fourth Refinement: Summary of the Events (2)

- Controller
  - treat_push_start_motor_button
  - treat_push_start_motor_button_false
  - treat_push_stop_motor_button
  - treat_push_stop_motor_button_false
  - treat_release_start_motor_button
  - treat_release_stop_motor_button
  - treat_start_clutch
  - treat_stop_clutch
  - treat_close_door
  - treat_open_door

- An additional safety constraint

When the clutch is engaged, the door must be closed	SAF_2

- We copy (after renaming "motor" to "door") what has been done in the third model:

When the clutch is engaged, the motor must work	SAF_1

- Can you guess it?

- Can you guess it?

- When the motor is not working, we must allow users:
    - to change the tool
    - to replace the part to be treated

- Can you guess it?

- When the motor is not working, we must allow users:
  - to change the tool
  - to replace the part to be treated

- Hence the following additional requirement (which was forgotten)

When the motor is stopped, the door must be open	SAF_3

- Can you guess it?

- When the motor is not working, we must allow users:
  - to change the tool
  - to replace the part to be treated

- Hence the following additional requirement (which was forgotten)

When the door is closed, the motor must work	SAF_3'

- SAF_3' is the contraposed form of SAF_3

- Additional safety constraint

When the door is closed, the motor must work	SAF_3’

- We copy (after renaming "clutch" to "door") what has been done in the third model:

When the clutch is engaged, the motor must work	SAF_1

Fifth Reft.: Summary of the Safety Requirements

When the clutch is engaged, the motor must work	SAF_1

When the clutch is engaged, the door must be closed	SAF_2

When the door is closed, the motor must work	SAF_3'

- Requirement SAF_1 is now redundant: SAF_2 $\wedge$ SAF_3' $\Rightarrow$ SAF_1

Possible New Refinement Strategy

- Initial model: Connecting the controller to the motor

- 1st refinement: Connecting the motor button to the controller

- 2nd refinement: Connecting the controller to the clutch

- 3rd (4th) refinement: Connecting the controller to the door

Possible New Refinement Strategy (cont'd)

- 4th (5th) refinement: Constraining the clutch and the door

  Constraining the motor and the door

- 5th (6th) refinement: More constraints between clutch and door

- 6th (7th) refinement: Connecting the clutch button to the controller

Fifth Refinement: Summary of the Events (1)

- Environment (no new events)
    - motor_start
    - motor_stop
    - clutch_start
    - clutch_stop
    - door_close
    - door_open
    - push_start_motor_button
    - release_start_motor_button
    - push_stop_motor_button
    - release_stop_motor_button

Fifth Refinement: Summary of the Events (2)

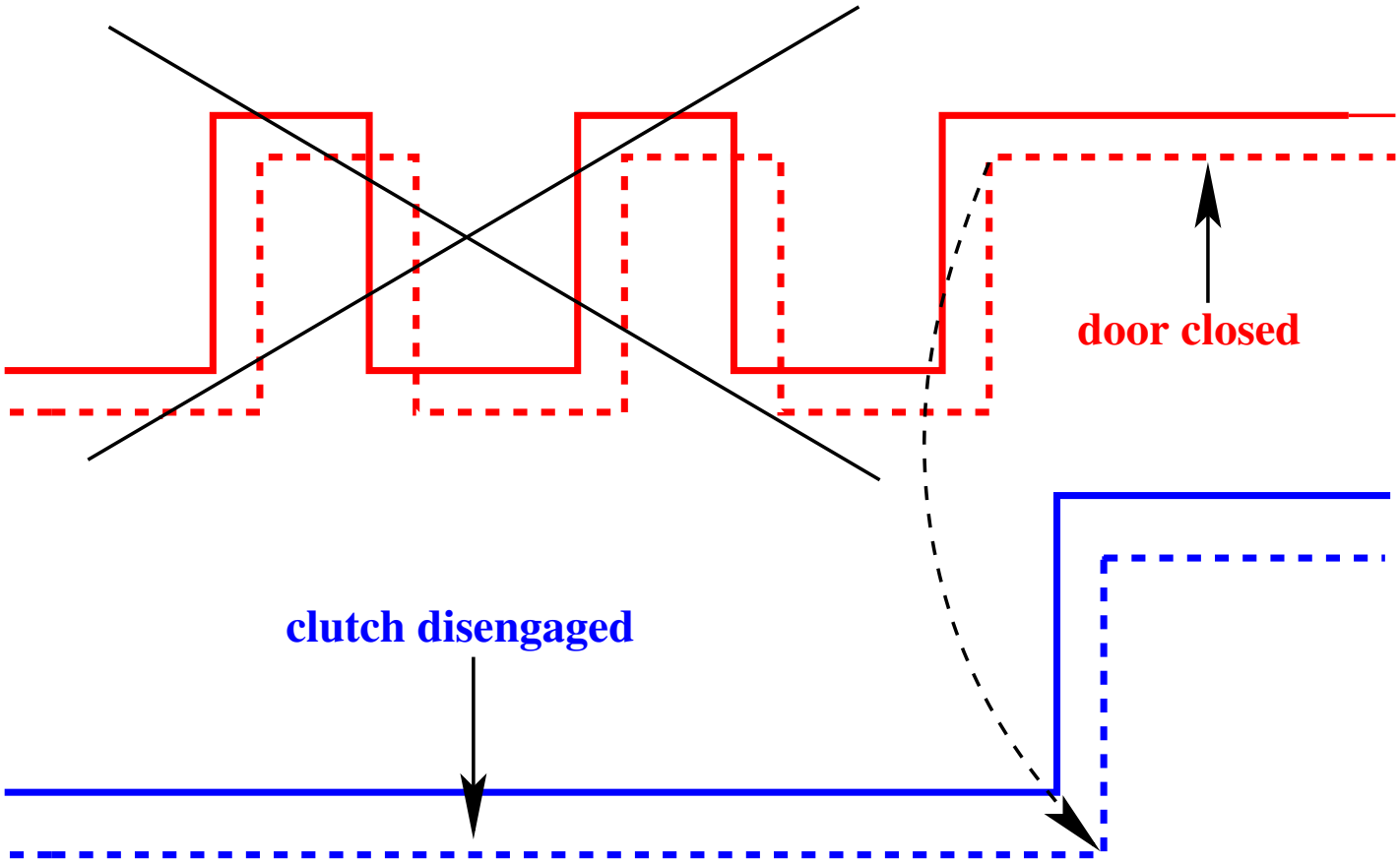
- Controller (no new events)
    - treat_push_start_motor_button
    - treat_push_start_motor_button_false
    - treat_push_stop_motor_button
    - treat_push_stop_motor_button_false
    - treat_release_start_motor_button
    - treat_release_stop_motor_button
    - treat_start_clutch
    - treat_stop_clutch
    - treat_close_door
    - treat_open_door

- Adding two functional constraints

When the clutch is disengaged, the door cannot be closed several times, ONLY ONCE	FUN_3

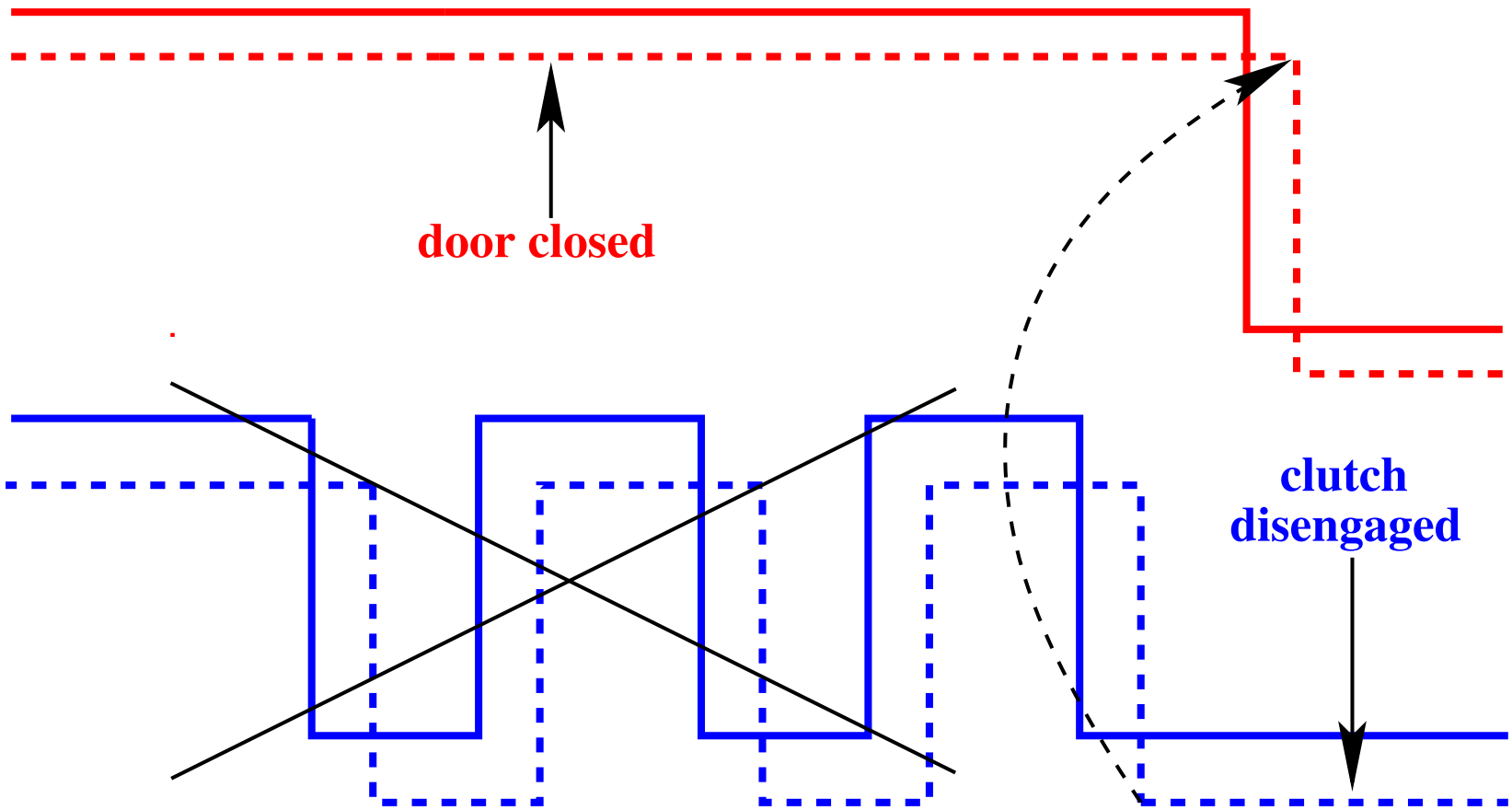
When the door is closed, the clutch cannot be disengaged several times, ONLY ONCE	FUN_4

Problem with the Weak Synchronization of Strong Reactions



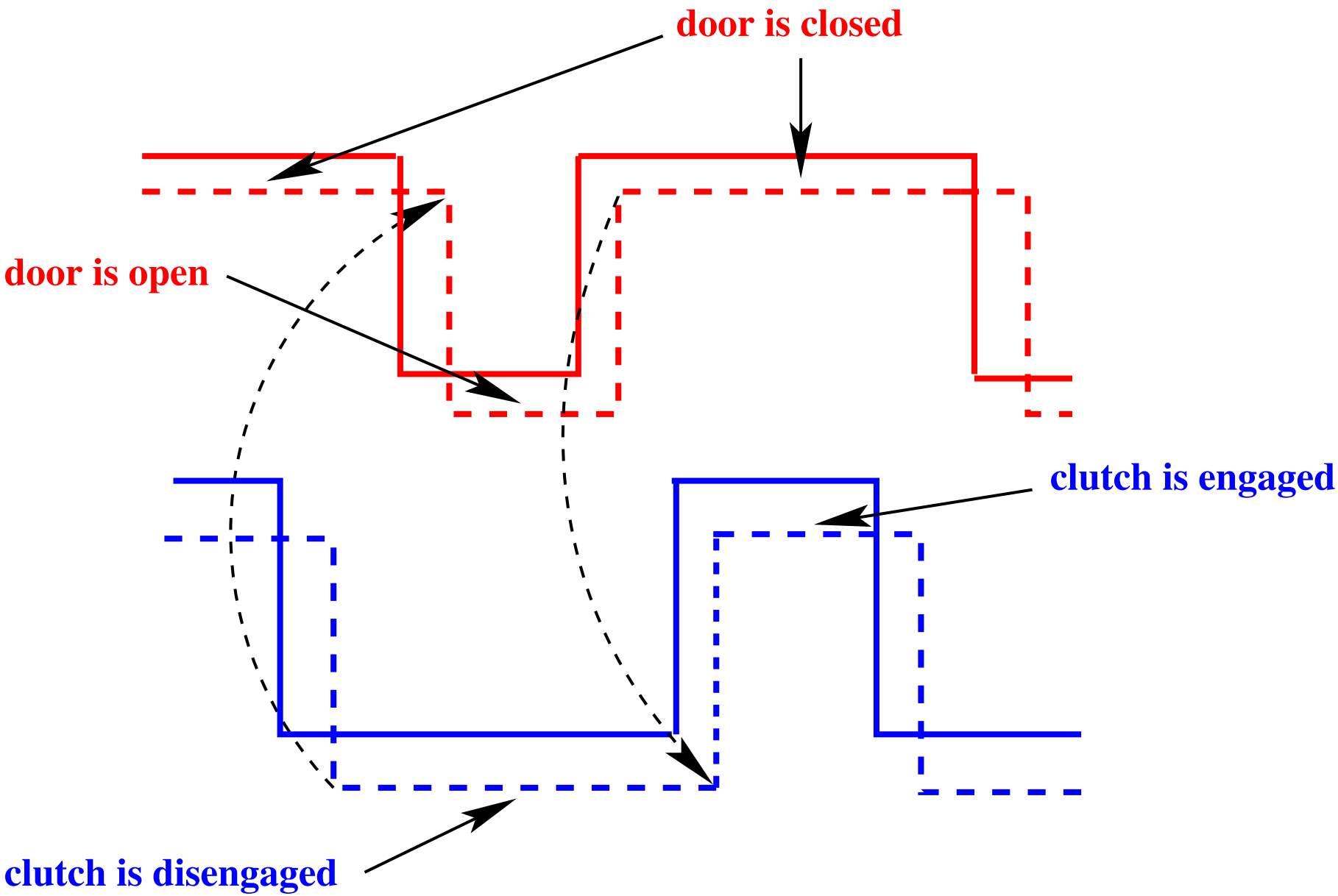
- When the clutch is disengaged, the door cannot be closed several times

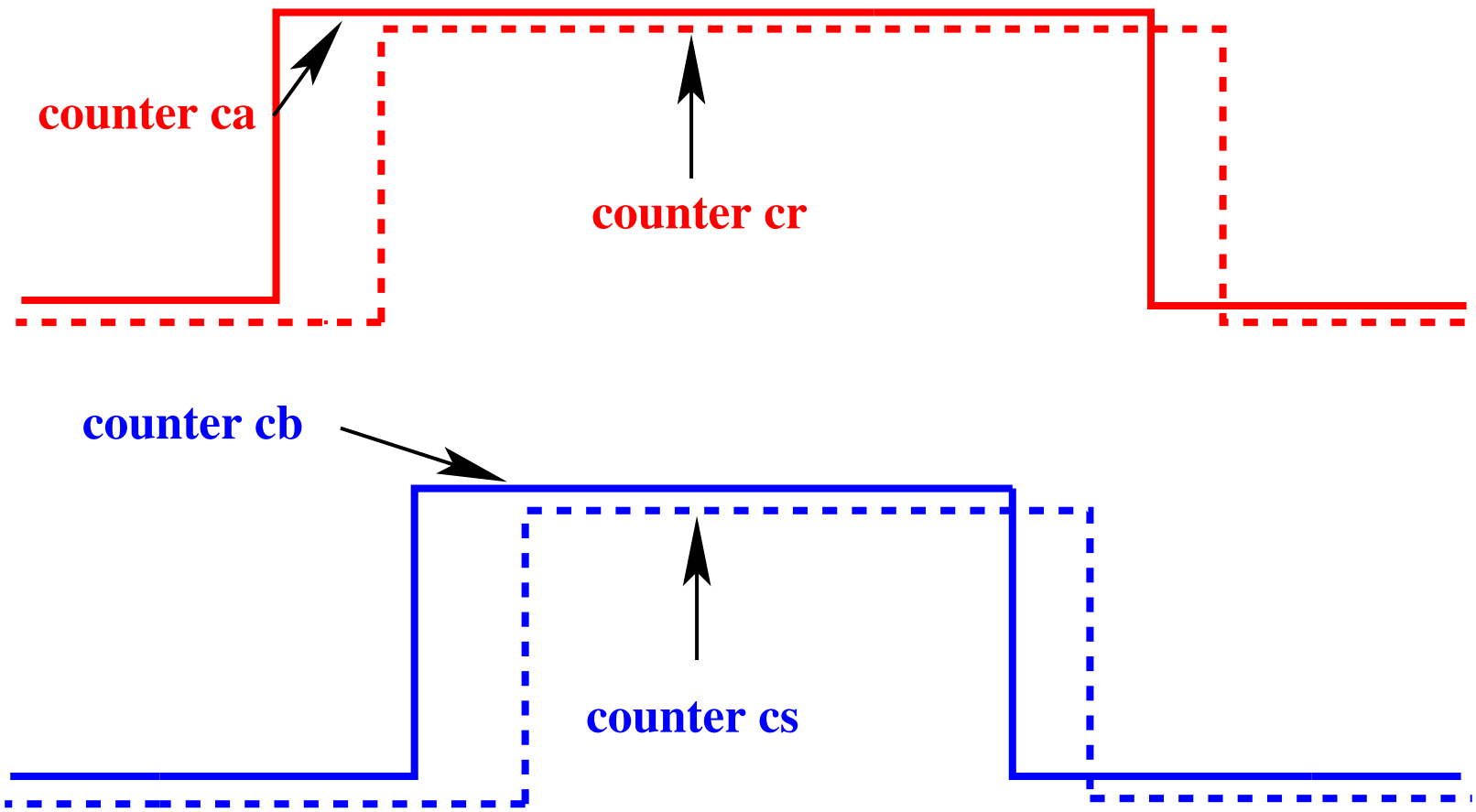
Problem with the Weak Synchronization of Strong Reactions



- When the door is closed, the clutch cannot be disengaged several times

The Full Picture



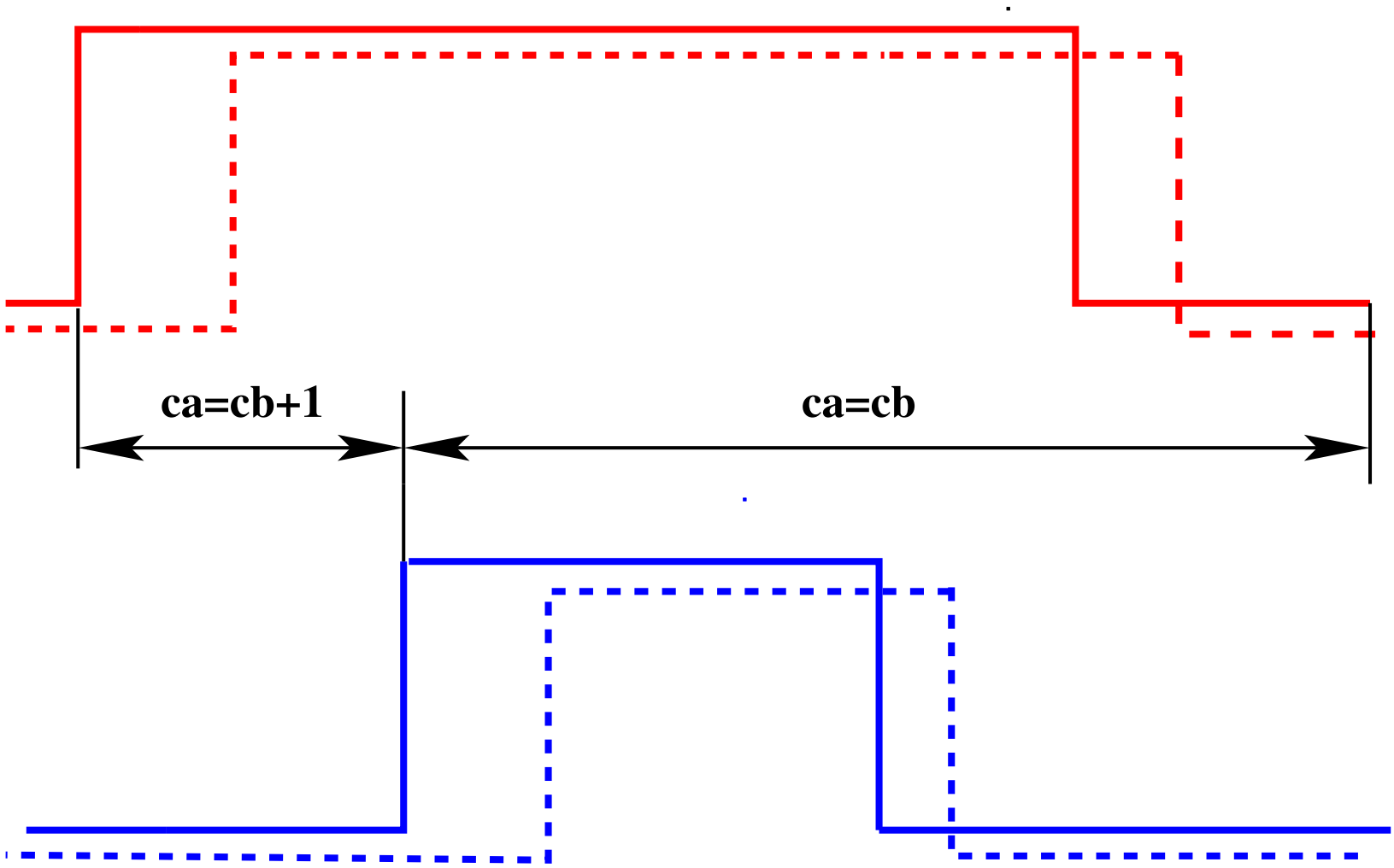


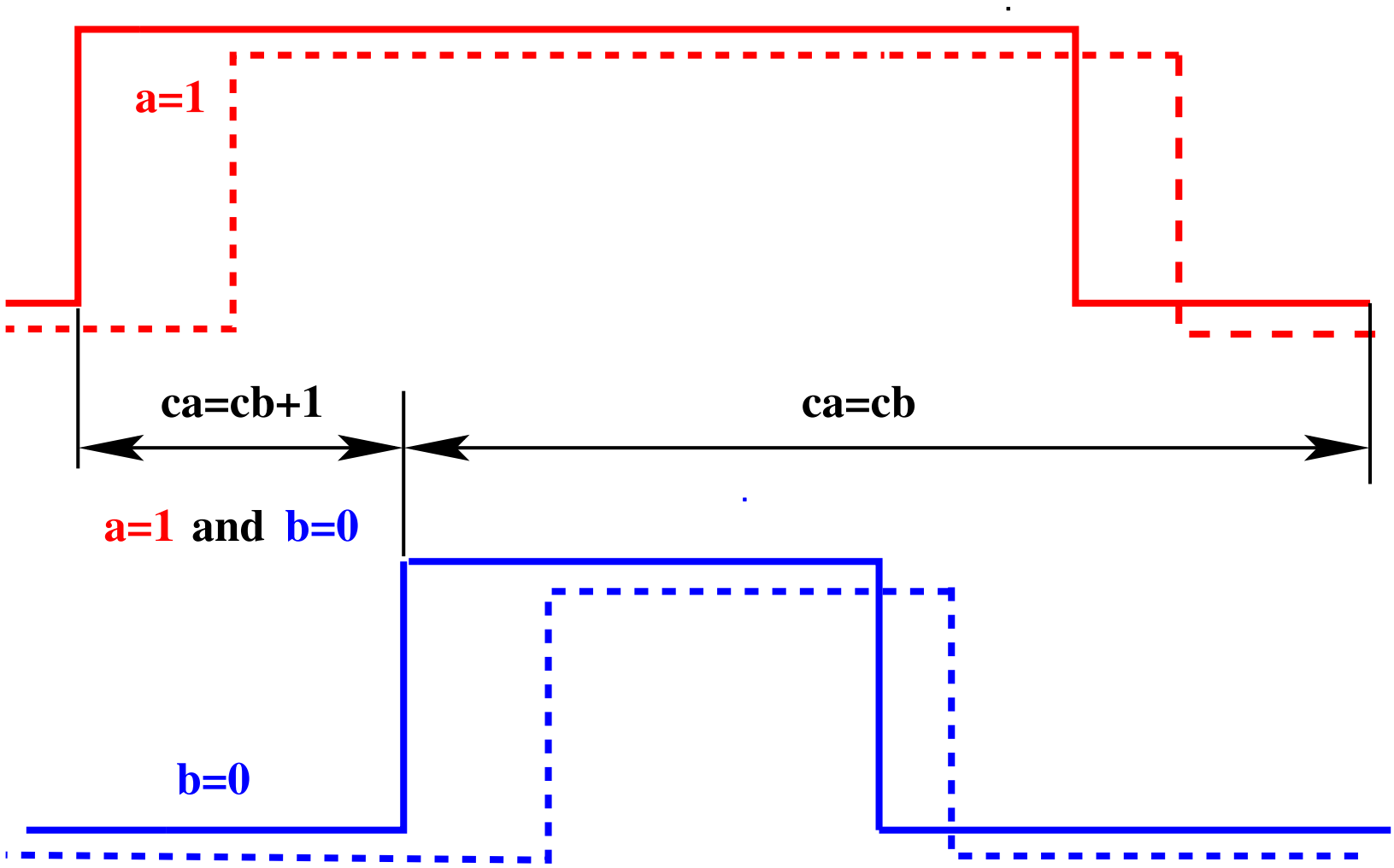
What we want:

$$ca = cb \;\vee\; ca = cb + 1$$

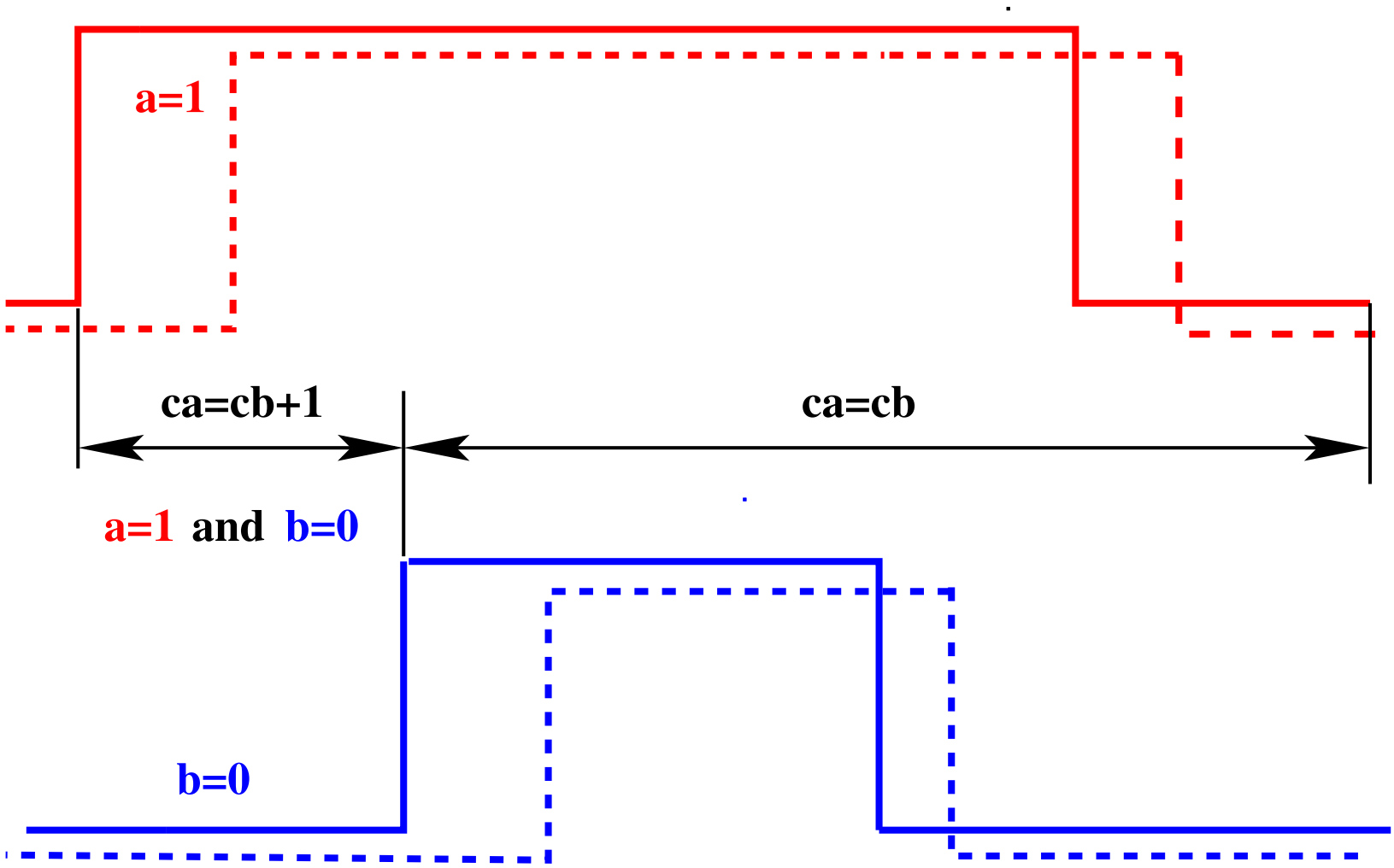
$$cr = cs \;\vee\; cr = cs + 1$$

How about counters ca and cb?



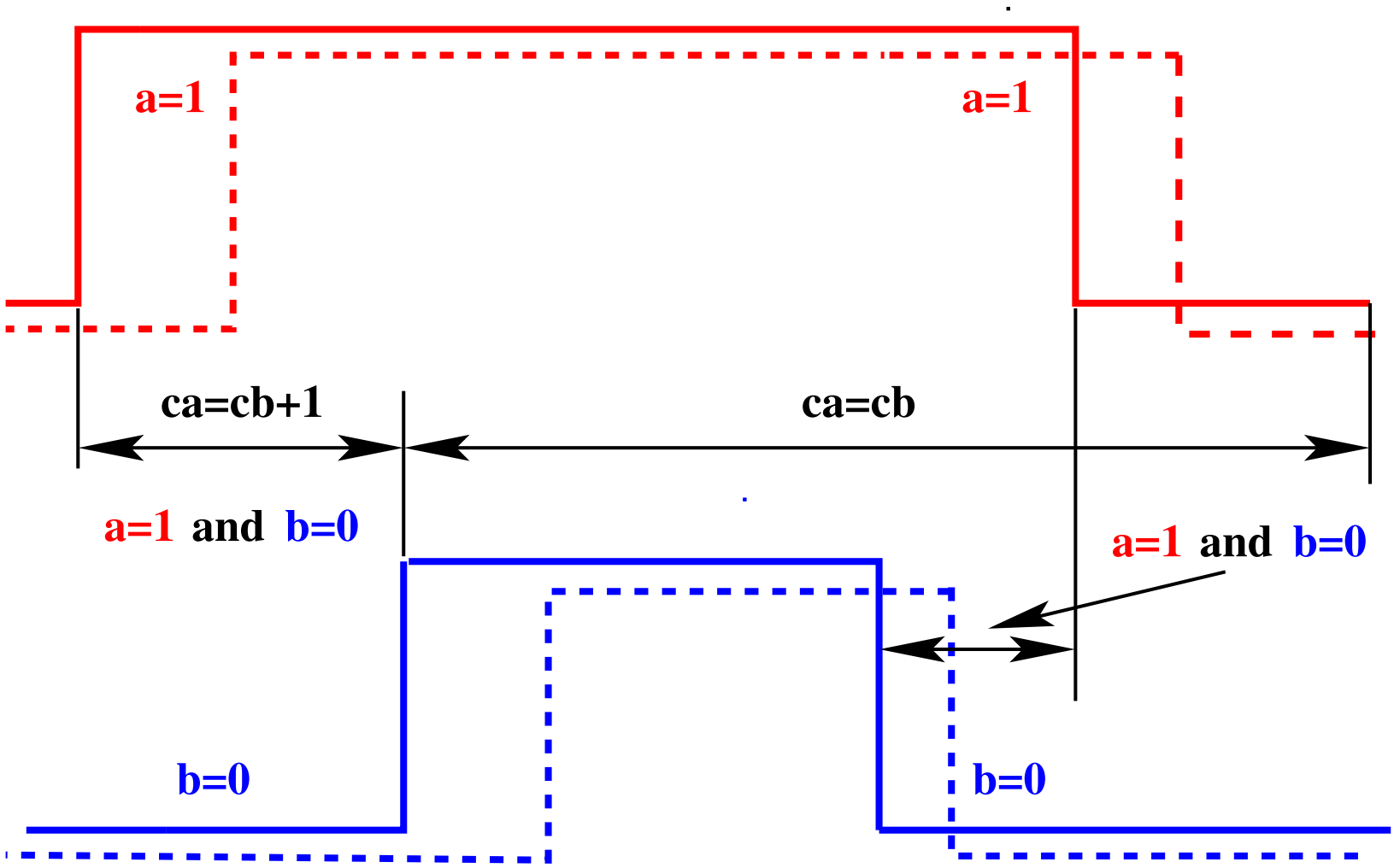

a=1
ca=cb+1
ca=cb
a=1 and b=0
b=0

In Search of a Solution

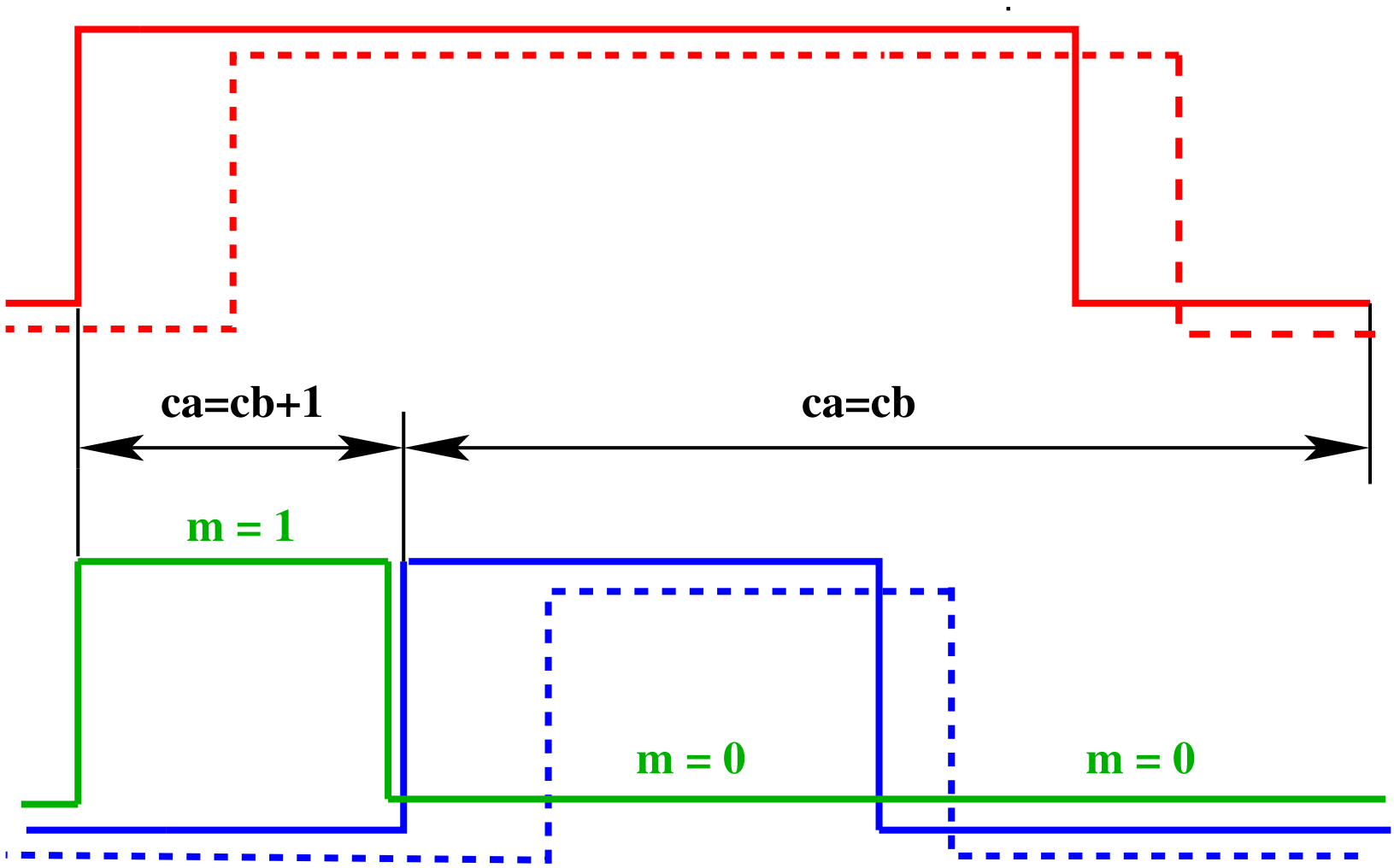


$$a = 1 \ \wedge \ b = 0 \ \Rightarrow \ ca = cb + 1 \qquad ?$$

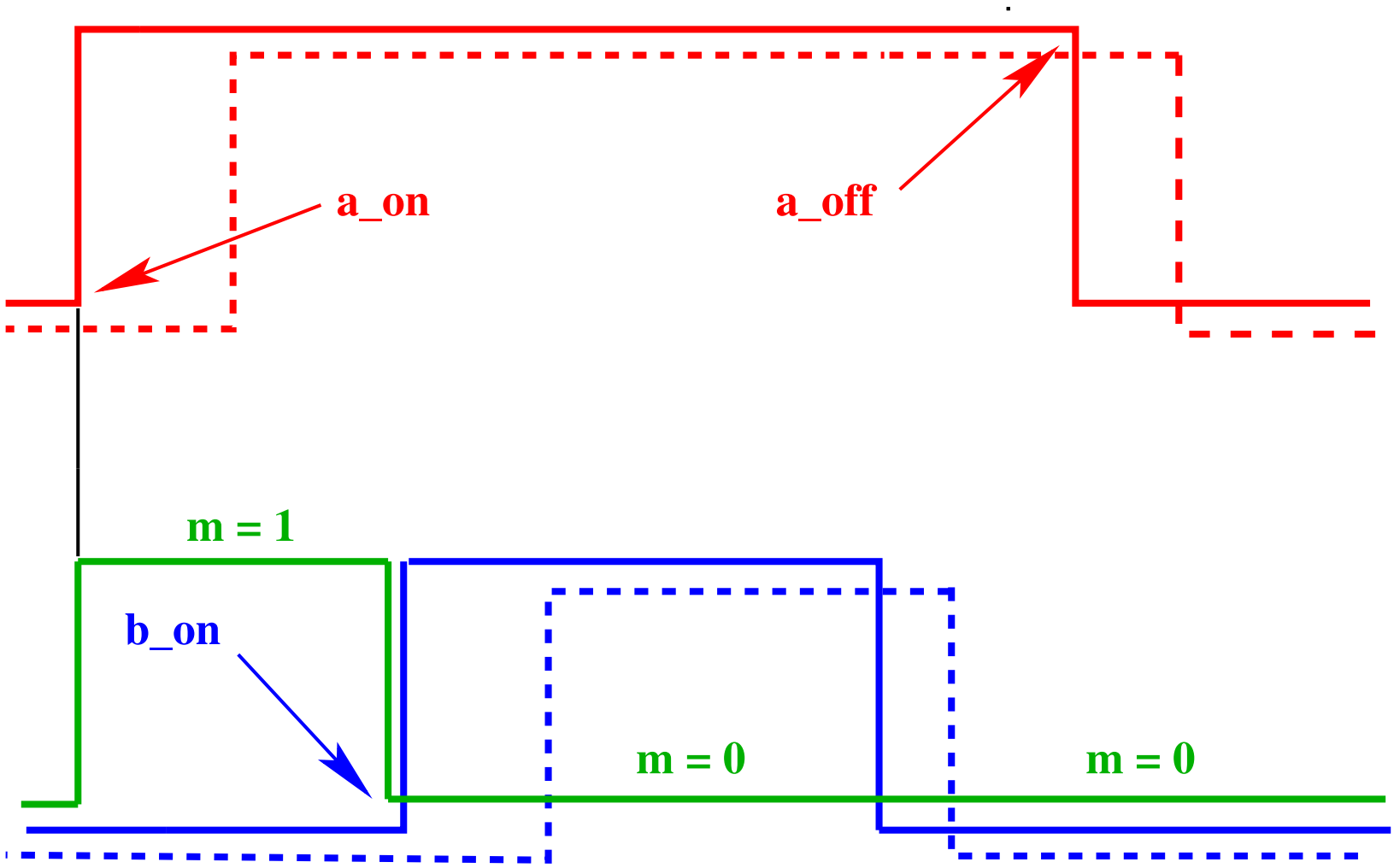
This Solution Does not Work



The Solution: an Additional Variable m



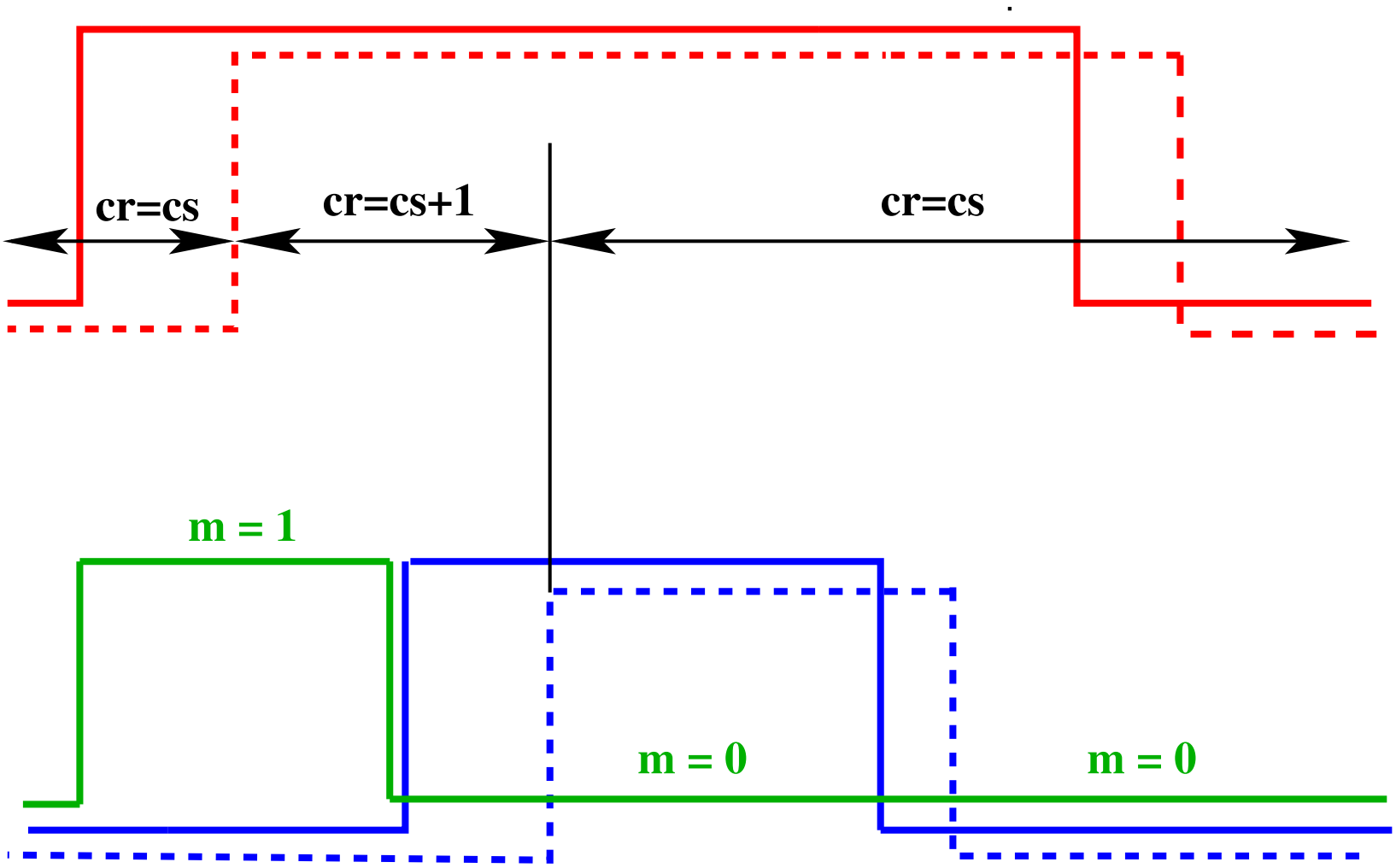
$$m = 1 \quad \Rightarrow \quad ca = cb + 1$$
$$m = 0 \quad \Rightarrow \quad ca = cb$$


a_on
a_off
m = 1
b_on
m = 0
m = 0

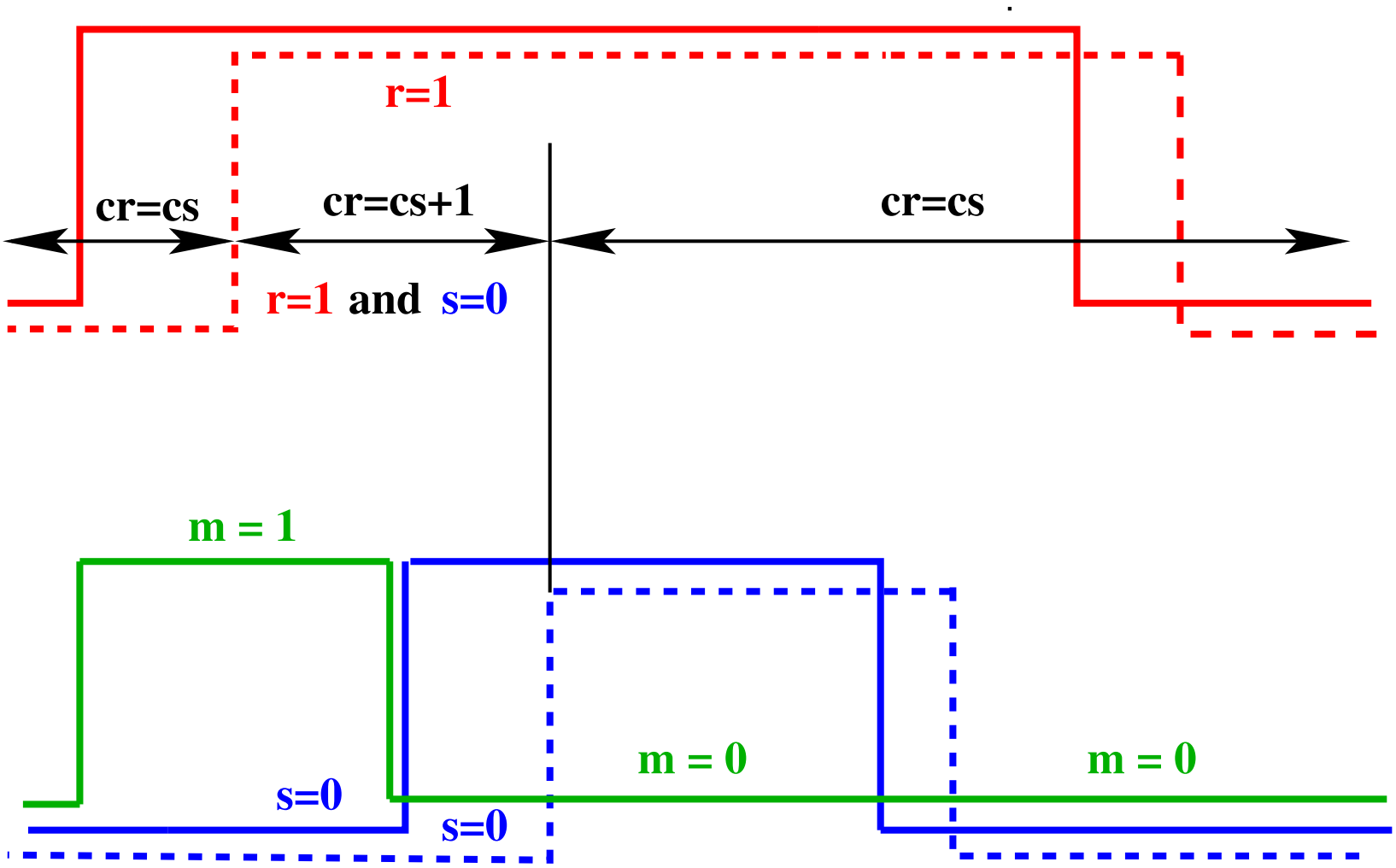
a_on
when
$a = 0$
$r = 0$
then
$a := 1$
$ca := ca + 1$
$m := 1$
end

b_on
when
$r = 1$
$a = 1$
$b = 0$
$s = 0$
$m = 1$
then
$b := 1$
$cb := cb + 1$
$m := 0$
end

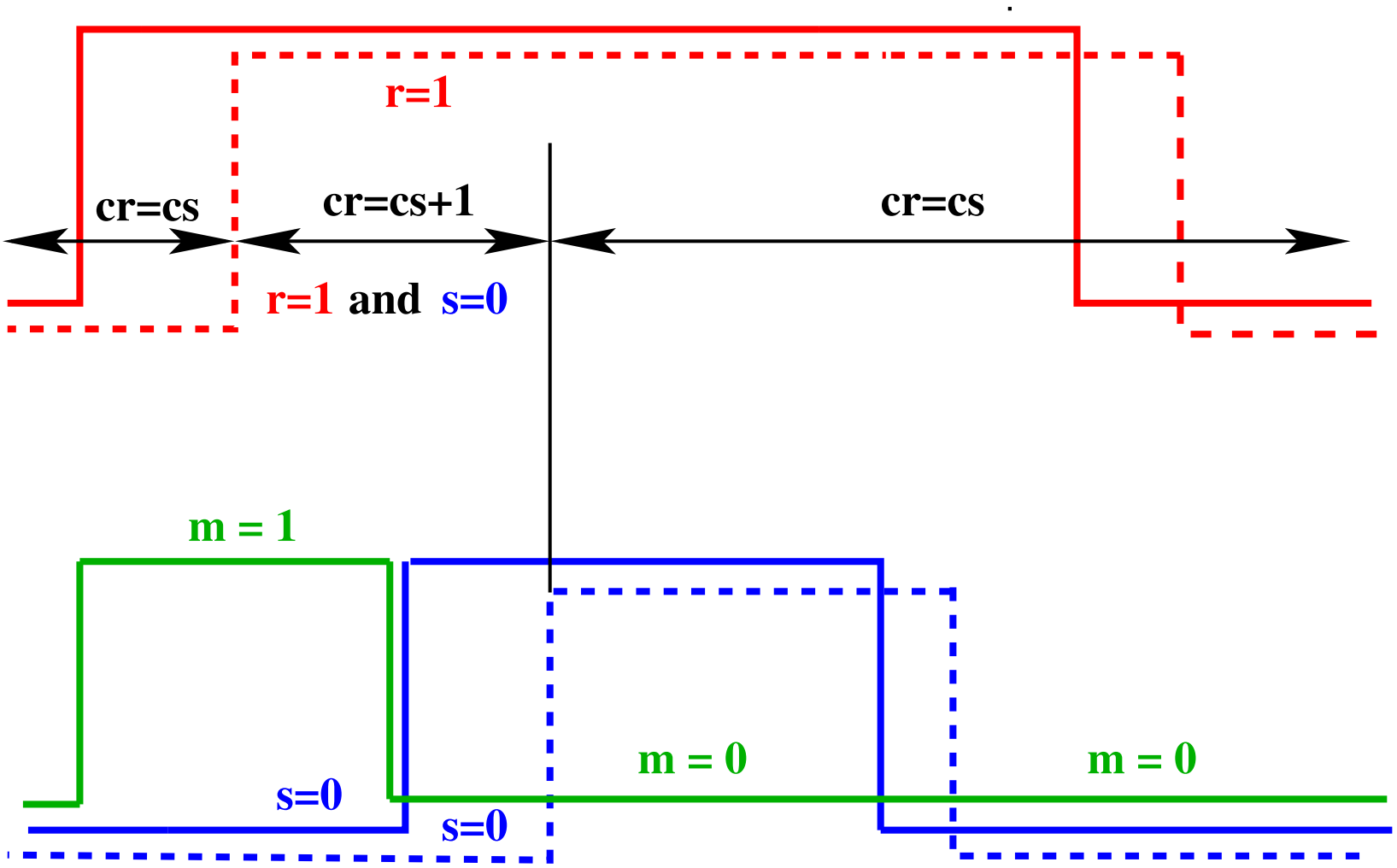
How about counters cr and cs



In Search of a Solution

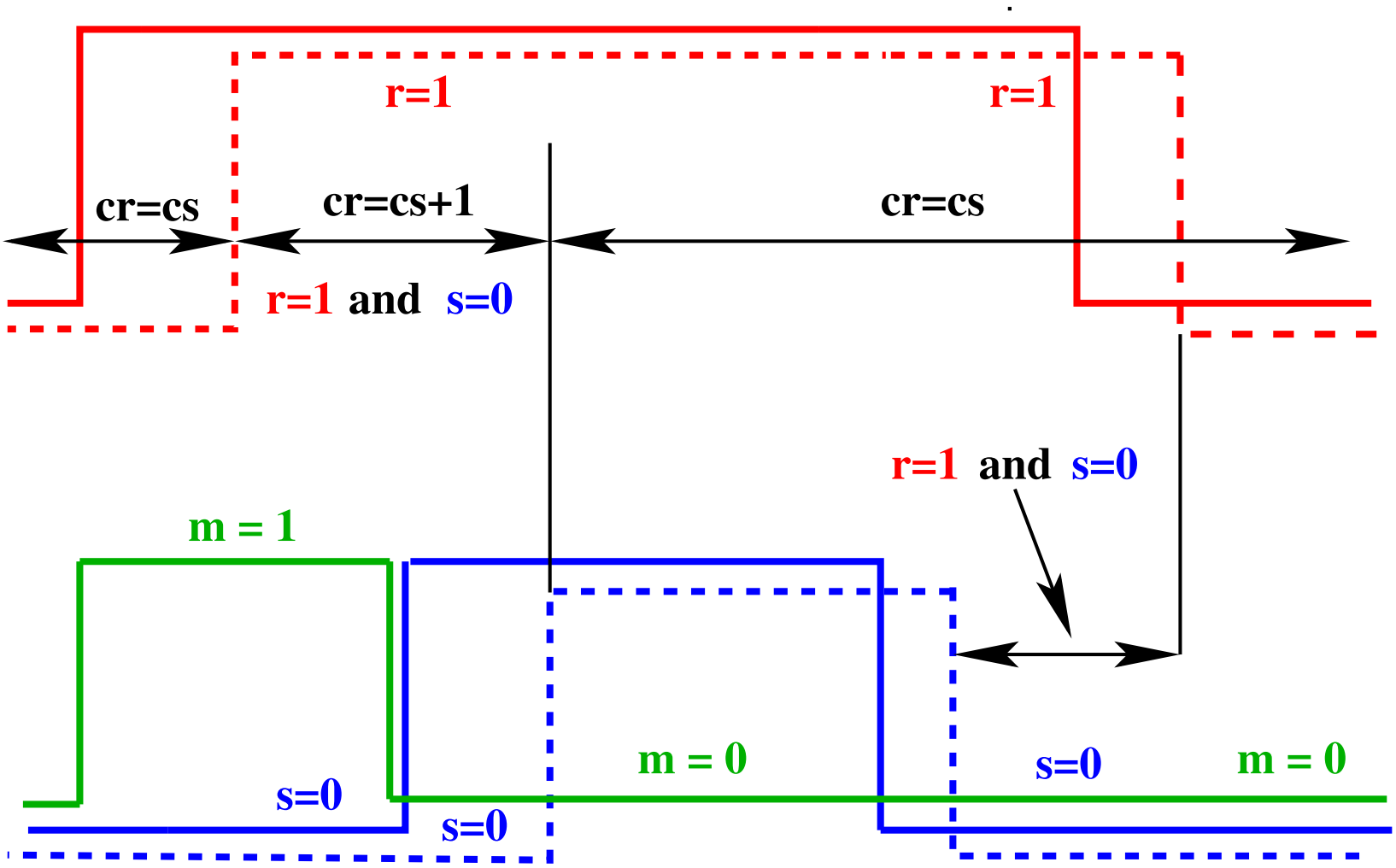


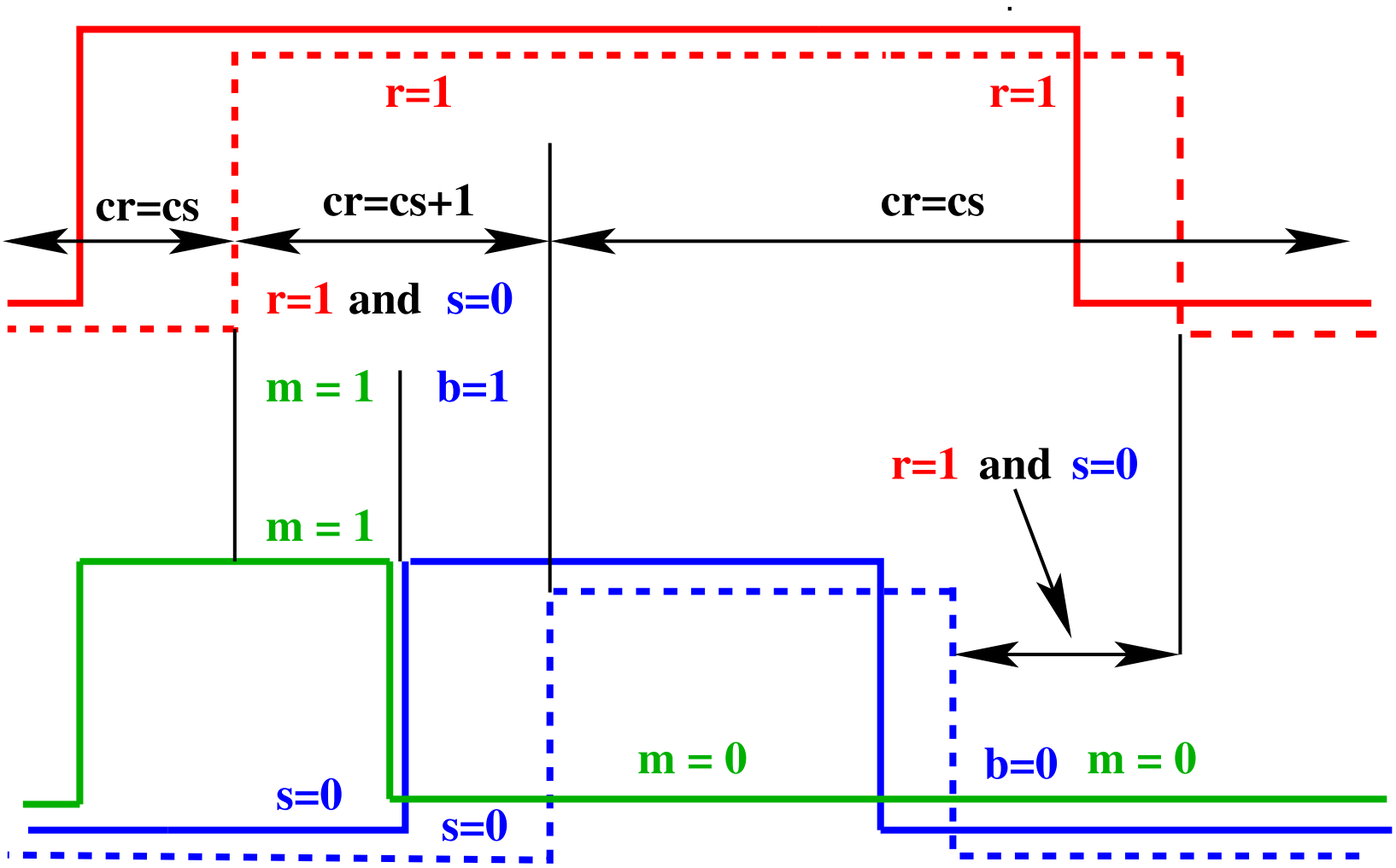
In Search of a Solution

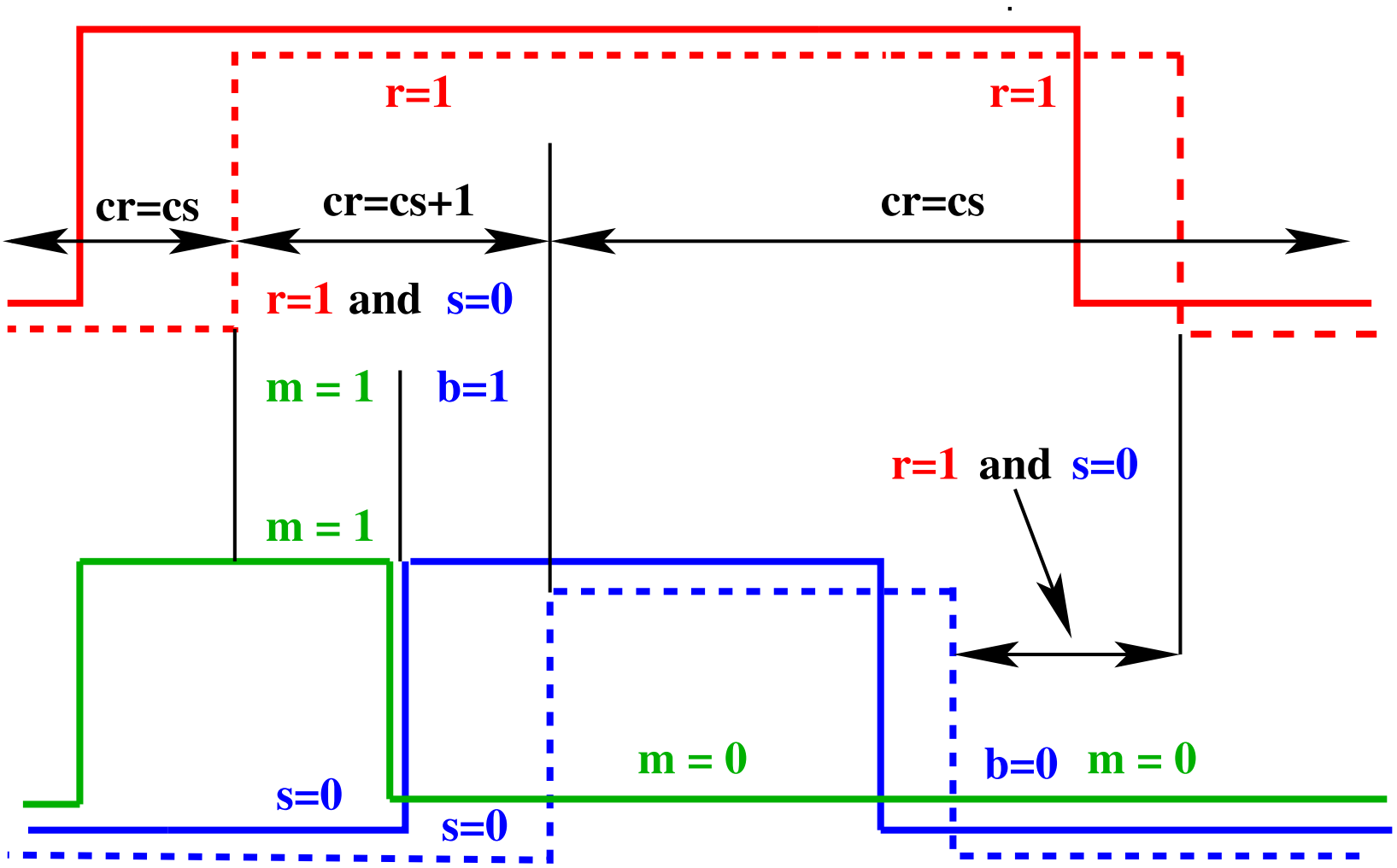


$$r = 1 \ \wedge \ s = 0 \ \Rightarrow \ cr = cs + 1 \qquad ?$$

This Solution Does not Work




r=1
r=1
cr=cs
cr=cs+1
cr=cs
r=1 and s=0
m = 1
b=1
r=1 and s=0
m = 1
m = 0
b=0 m = 0
s=0
s=0



$$r = 1 \ \wedge \ s = 0 \ \wedge \ (m = 1 \ \vee \ b = 1) \ \Rightarrow \ cr = cs + 1$$

$$r = 0 \ \vee \ s = 1 \ \vee \ (m = 0 \ \wedge \ b = 0) \ \Rightarrow \ cr = cs$$

Summary of Refinement: the state

dbl2_1: $m \in \{0, 1\}$

dbl2_2: $m = 1 \Rightarrow ca = cb + 1$

dbl2_3: $m = 0 \Rightarrow ca = cb$

dbl2_4: $r = 1 \wedge s = 0 \wedge (m = 1 \vee b = 1) \Rightarrow cr = cs + 1$

dbl2_5: $r = 0 \vee s = 1 \vee (m = 0 \wedge b = 0) \Rightarrow cr = cs$

Summary of Refinement: the state

dbl2_1: $m \in \{0, 1\}$

dbl2_2: $m = 1 \Rightarrow ca = cb + 1$

dbl2_3: $m = 0 \Rightarrow ca = cb$

dbl2_4: $r = 1 \wedge s = 0 \wedge (m = 1 \vee b = 1) \Rightarrow cr = cs + 1$

dbl2_5: $r = 0 \vee s = 1 \vee (m = 0 \wedge b = 0) \Rightarrow cr = cs$

- The following theorems are easy to prove

thm2_1: $ca = cb \vee ca = cb + 1$

thm2_2: $cr = cs \vee cr = cs + 1$

More Invariant

dbl2_1: $m \in \{0, 1\}$

dbl2_2: $m = 1 \Rightarrow ca = cb + 1$

dbl2_3: $m = 0 \Rightarrow ca = cb$

dbl2_4: $r = 1 \wedge s = 0 \wedge (m = 1 \vee b = 1) \Rightarrow cr = cs + 1$

dbl2_5: $r = 0 \vee s = 1 \vee (m = 0 \wedge b = 0) \Rightarrow cr = cs$

dbl2_6: $a = 0 \Rightarrow m = 0$

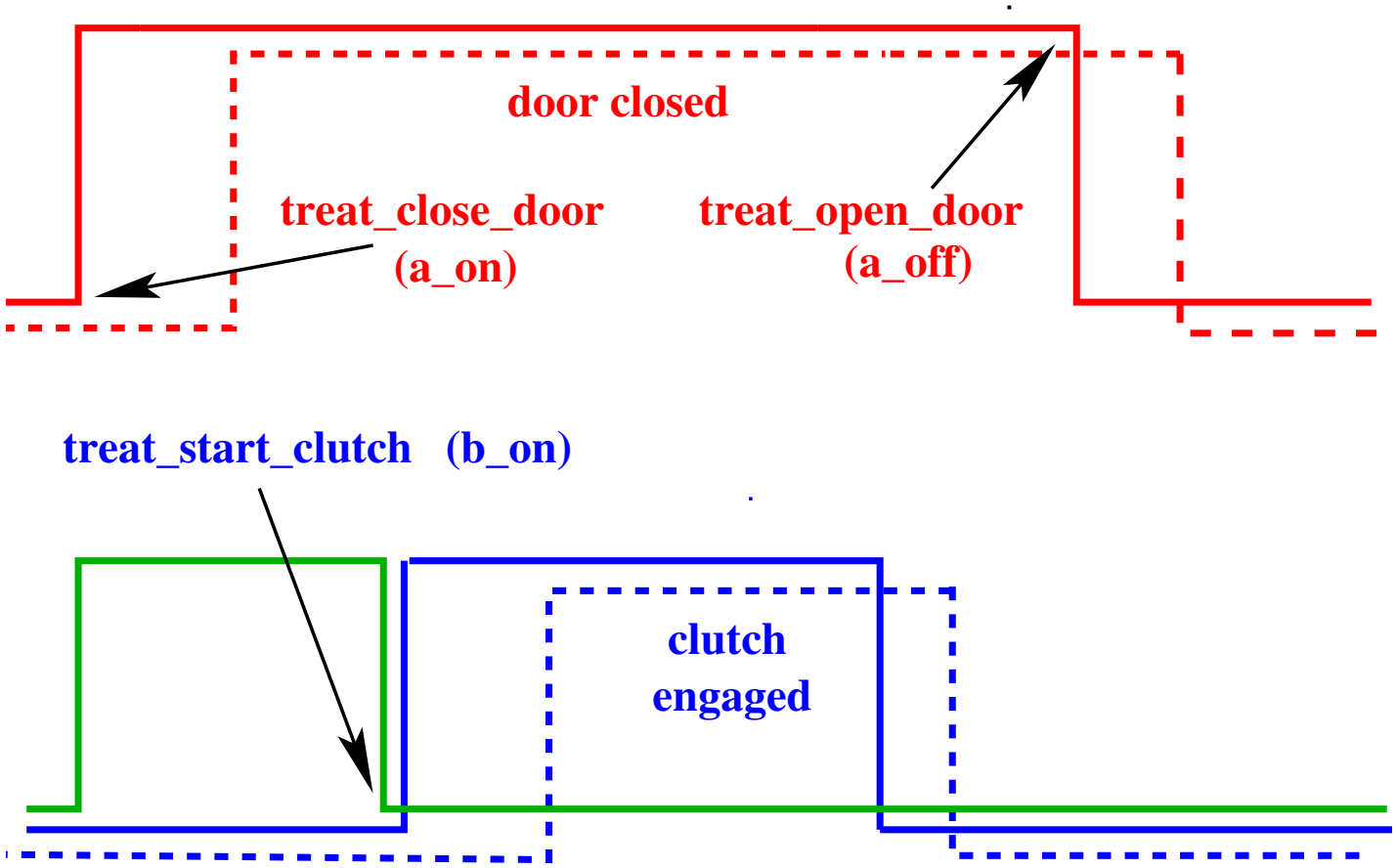
- The last new invariants was discovered while doing the proof
- It requires adding the guard $m = 0$ in event a_off
- The proofs are now completely automatic

The Final Modified Events

a_on
when
$a = 0$
$r = 0$
then
$a := 1$
$ca := ca + 1$
$m := 1$
end

b_on
when
$r = 1$
$a = 1$
$b = 0$
$s = 0$
$m = 1$
then
$b := 1$
$cb := cb + 1$
$m := 0$
end

a_off
when
$a = 1$
$r = 1$
$b = 0$
$s = 0$
$m = 0$
then
$a := 0$
end


door closed
treat_close_door
(a_on)
treat_open_door
(a_off)
treat_start_clutch (b_on)
clutch
engaged

Pattern Instantiation for the 6th Refinement

- We instantiate the pattern as follows:

$$
\begin{array}{lcl@{\qquad}lcl}
a & \leadsto & door\_actuator & b & \leadsto & clutch\_actuator \\
r & \leadsto & door\_sensor & s & \leadsto & clutch\_sensor \\
0 & \leadsto & open & 0 & \leadsto & disengaged \\
1 & \leadsto & closed & 1 & \leadsto & engaged
\end{array}
$$

$$
\begin{array}{lcl}
\text{a\_on} & \leadsto & \text{treat\_close\_door} \\
\text{a\_off} & \leadsto & \text{treat\_open\_door} \\
\text{b\_on} & \leadsto & \text{treat\_start\_clutch}
\end{array}
$$

6th Refinement: Adapting the events of the pattern (2)

a_on
when
$a = 0$
$r = 0$

then
$a := 1$
$m := 1$
end

treat_close_door
when
$door\_actuator = open$
$door\_sensor = open$
$motor\_actuator = working$
$motor\_sensor = working$
then
$door\_actuator := closed$
$m := 1$
end

b_on
when
$b = 0$
$s = 0$
$r = 1$
$a = 1$
$m = 1$
then
$b := 1$
$m := 0$
end

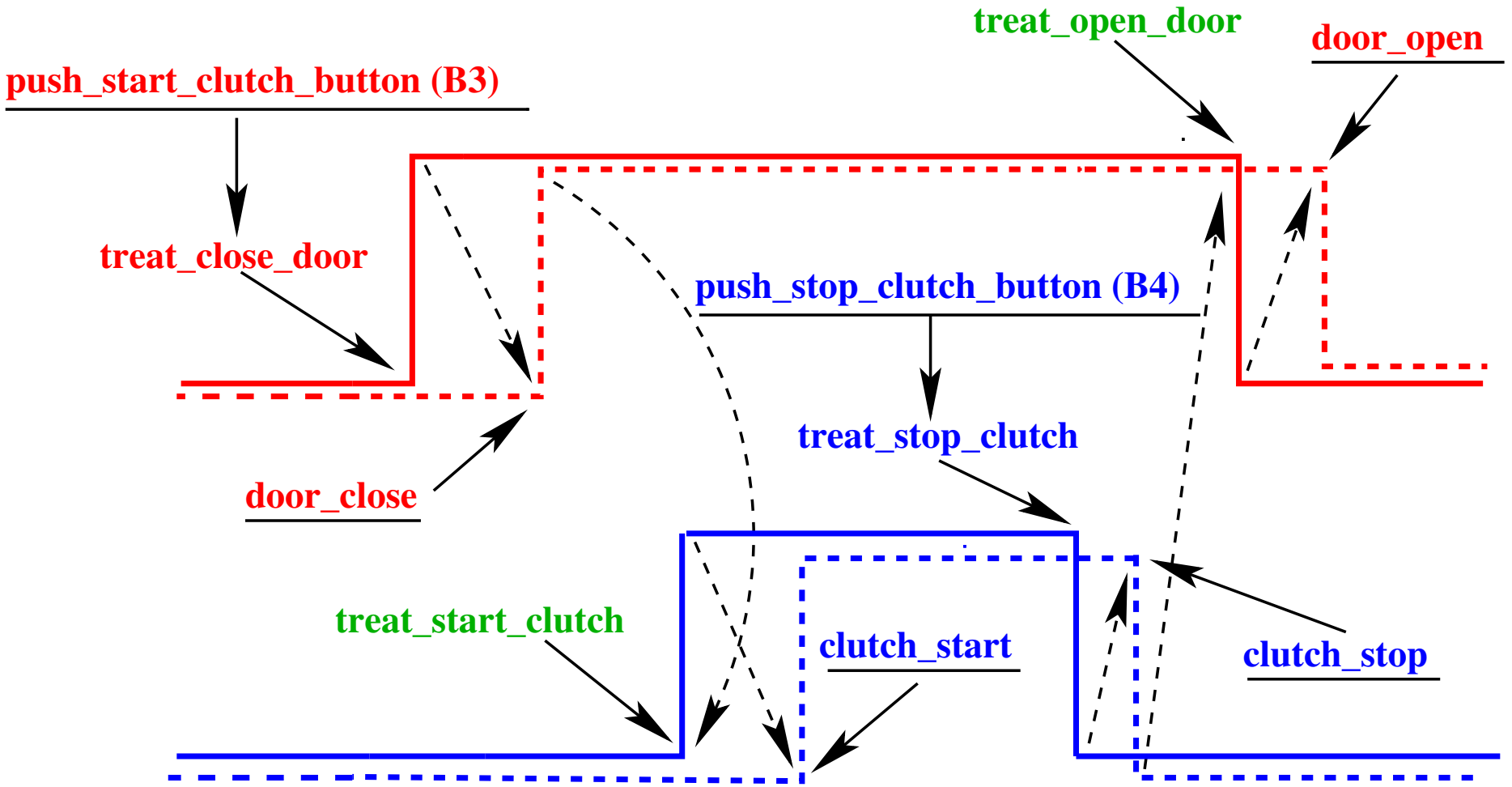
treat_start_clutch
when
$motor\_actuator = working$
$motor\_sensor = working$
$clutch\_actuator = disengaged$
$clutch\_sensor = disengaged$
$door\_sensor = closed$
$door\_actuator = closed$
$m = 1$
then
$clutch\_actuator := engaged$
$m := 0$
end

6th Refinement: Adapting the events of the pattern (3)

a_off
when
$a = 1$
$r = 1$
$s = 0$
$b = 0$
$m = 0$
then
$a := 0$
end

treat_open_door
when
$door\_actuator = closed$
$door\_sensor = closed$
$clutch\_sensor = disengaged$
$clutch\_actuator = disengaged$
$m = 0$
then
$door\_actuator := open$
end

The Complete Synchronization of Door and Clutch



- treat_close_door is the result of depressing button B3
- treat_stop_clutch is the result of depressing button B4
- treat_start_clutch and treat_open_door are automatic

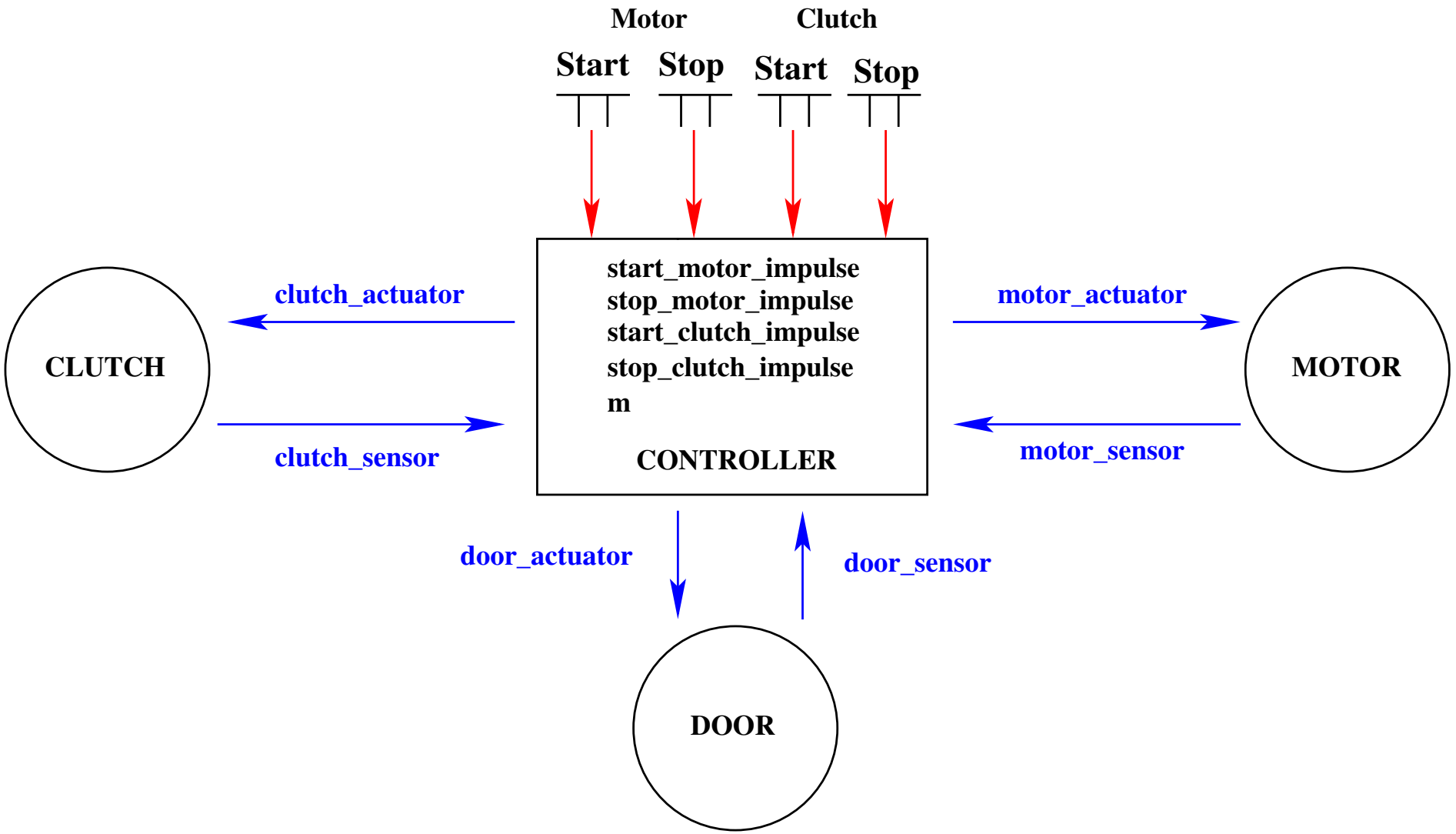
Sixth Refinement: Summary of the Events (1)

- Environment (no new events)
    - motor_start
    - motor_stop
    - clutch_start
    - clutch_stop
    - door_close
    - door_open
    - push_start_motor_button
    - release_start_motor_button
    - push_stop_motor_button
    - release_stop_motor_button

Sixth Refinement: Summary of the Events (2)

- Controller (no new events)
    - treat_push_start_motor_button
    - treat_push_start_motor_button_false
    - treat_push_stop_motor_button
    - treat_push_stop_motor_button_false
    - treat_release_start_motor_button
    - treat_release_stop_motor_button
    - treat_start_clutch
    - treat_stop_clutch
    - treat_close_door
    - treat_open_door

7th Reft.: Connecting the Controller to the Clutch Buttons



Reminder: Synchronizing Door and Clutch

- There are no door buttons

- The door must be closed before engaging the clutch

- The door must be opened after disengaging the clutch

- It is sufficient to connect:
    - button B3 to the door (closing the door)
    - button B4 to the clutch (disengaging the clutch)

- motor_start
- motor_stop
- clutch_start
- clutch_stop
- door_close
- door_open
- push_start_motor_button
- release_start_motor_button
- push_stop_motor_button
- release_stop_motor_button
- push_start_clutch_button
- release_start_clutch_button
- push_stop_clutch_button
- release_stop_clutch_button

- treat_push_start_motor_button
- treat_push_start_motor_button_false
- treat_push_stop_motor_button
- treat_push_stop_motor_button_false
- treat_release_start_motor_button
- treat_release_stop_motor_button
- treat_start_clutch
- treat_stop_clutch
- treat_close_door
- treat_open_door
- treat_close_door_false
- treat_stop_clutch_false
- treat_release_start_clutch_button
- treat_release_stop_clutch_button

Decomposing the Final Model: Environment

- The environment events

- The environment variables modified by environment events

- The sensor variables modified by environment events

- The actuator variables read by environment events

- The controller variables not seen by environment events

- No environment variables in this model

Decomposing the Final Model: Controller

- The controller events

- The controller variables modified by controller events

- The sensor variables read by controller events

- The actuator variables modified by controller events

- The environment variables not seen by controller events

- No environment variables in this model

Summary: Variables of the Last Refinement (1)

- 7 sensor variables:
  - $motor\_sensor$
  - $clutch\_sensor$
  - $door\_sensor$
  - $start\_motor\_button$
  - $stop\_motor\_button$
  - $start\_clutch\_button$
  - $stop\_clutch\_button$

Summary: Variables of the Last Refinement (2)

- 3 actuator variables:
  - $motor\_actuator$
  - $clutch\_actuator$
  - $door\_actuator$
- 5 controller variables (without the counter variables):
  - $start\_motor\_impulse$
  - $stop\_motor\_impulse$
  - $start\_clutch\_impulse$
  - $stop\_clutch\_impulse$
  - m

Summary: Events of the Last Refinement

- 14 environment events,

- 14 controller events,

- 130 lines for environment events,

- 180 lines for controller events.

Summary: Usage of the Design Patterns

- 4 weak reactions: 4 buttons (B1, B2, B3, B4)

- 3 strong reactions: 3 devices (motor, clutch, door)

- 3 strong-weak reactions: motor-clutch, clutch-door, motor-door

- 1 strong-strong reaction: clutch-door

Summary: Number of Invariants

- Weak reaction: 6
- Strong reaction: 3
- Strong-weak reaction: 16
- Strong-strong reaction: 6
- Total: 31

- Press (typing): 15
- Total: 15

Summary: Number of Proof Obligations

- Weak reaction: 18
- Strong reaction: 12
- Strong-weak reaction: 61
- Strong-strong reaction: 35
- Total: 126

- Press: 0

- PO saving: 4x18 + 3x12 + 3x61 + 35 = 326

Summary: Proofs

- Design patterns: 126 (all automatic)

- Press: 0

Conclusion

- This design pattern approach is very fruitful

- It results in a very systematic formal development

- Many other patterns have to be developed

- More automation has to be provided (plug-in)