



## GENERAL IMS LECTURE 4 – PIXELS AND FILTERS

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## WHAT WE WILL LEARN TODAY?

1. Image sampling and quantization
2. Image histograms
3. Images as functions
4. Linear systems (filters)
5. Convolution and correlation

Some background reading:

Forsyth and Ponce, Computer Vision, Chapter 7

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### Binary



### Binary



### Gray Scale



# TYPES OF IMAGES

## Binary



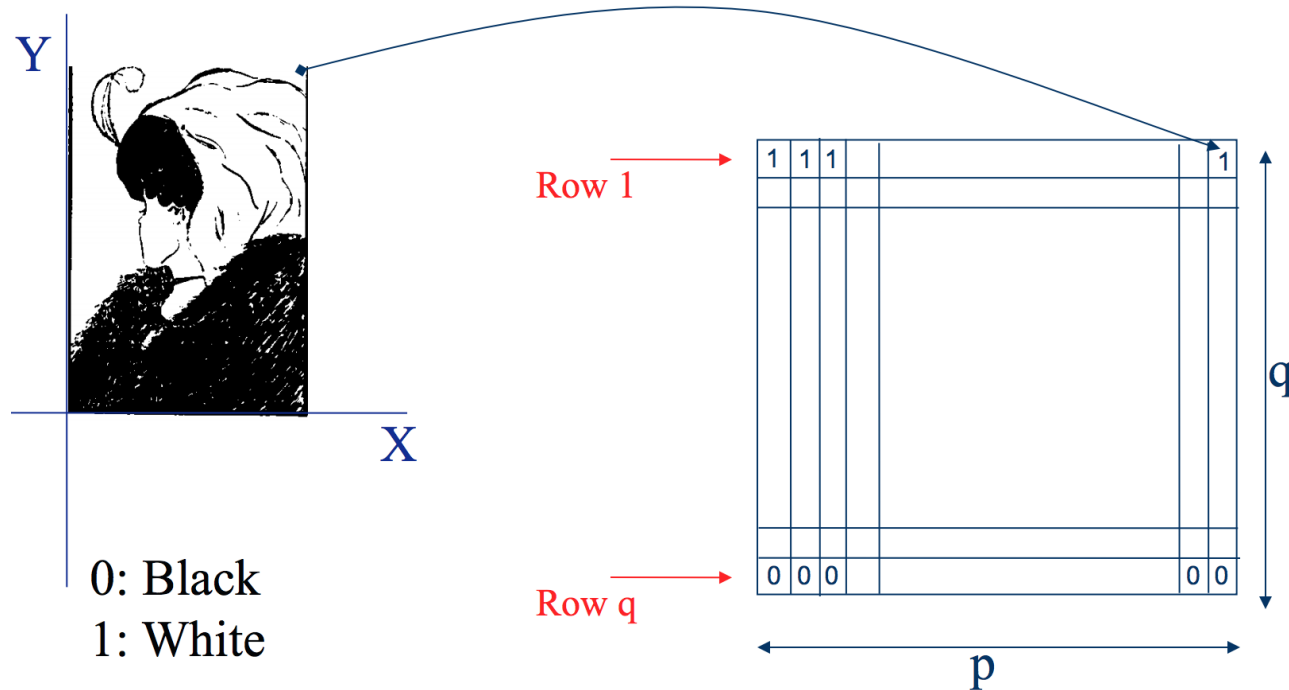
## Gray Scale



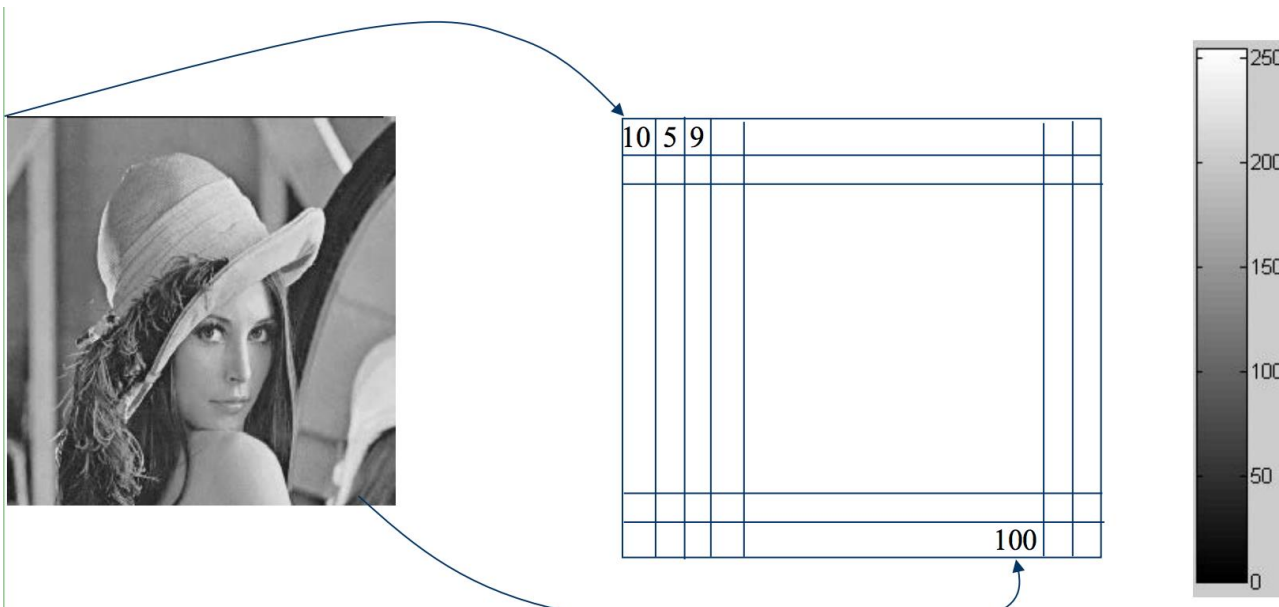
## Color



# BINARY IMAGE REPRESENTATION

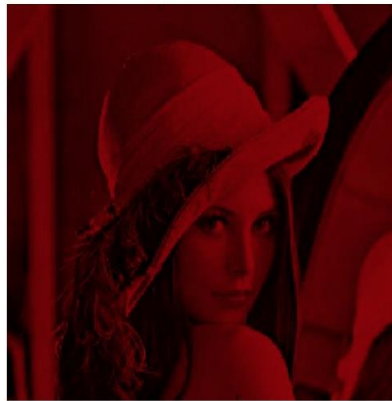


# GRayscale IMAGE REPRESENTATION





## COLOR IMAGE - ONE CHANNEL

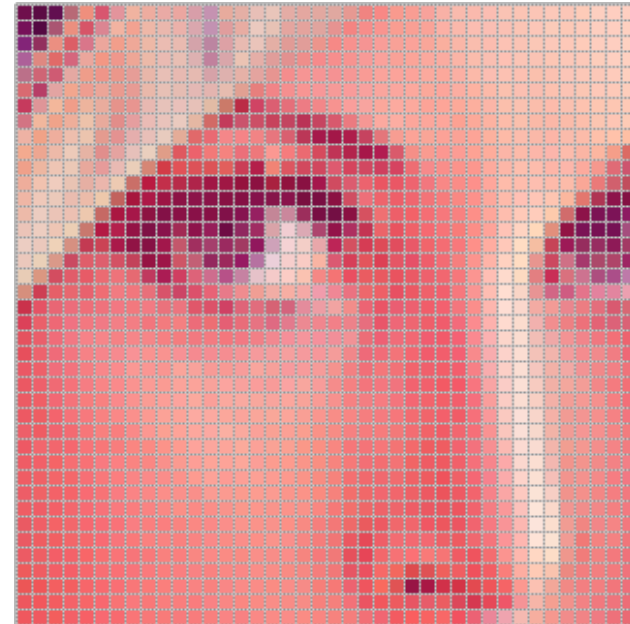
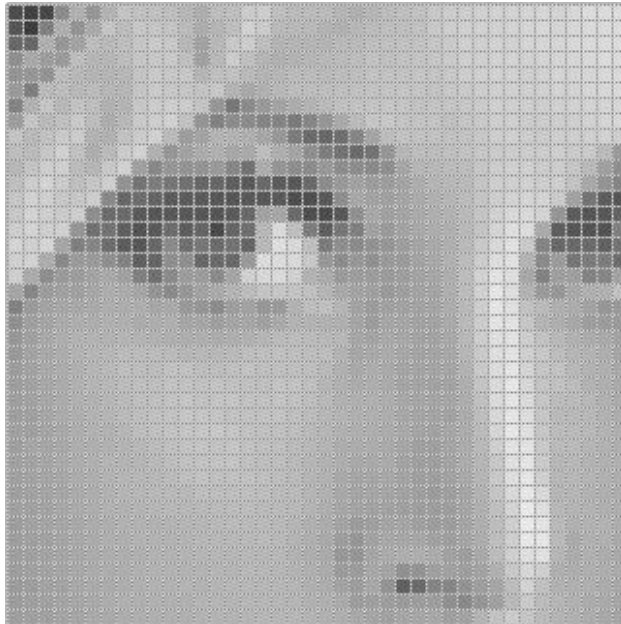


# COLOR IMAGE REPRESENTATION

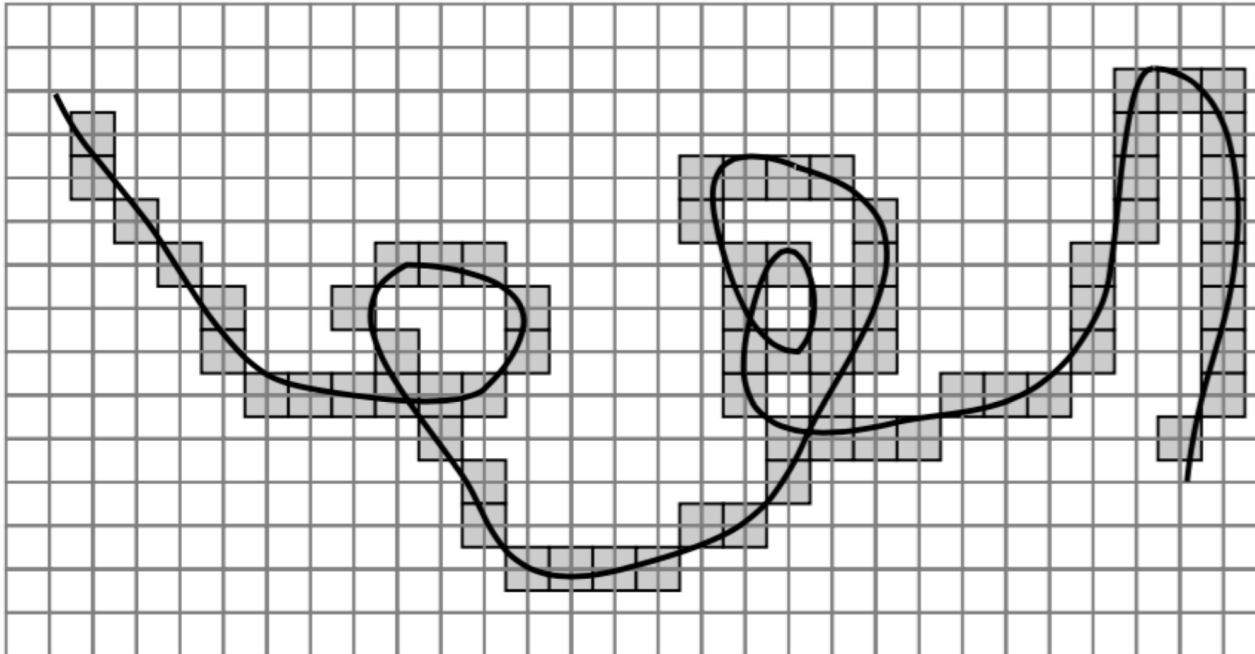


# IMAGES ARE SAMPLED

What happens when we zoom into the images we capture?



## ERRORS DUE SAMPLING



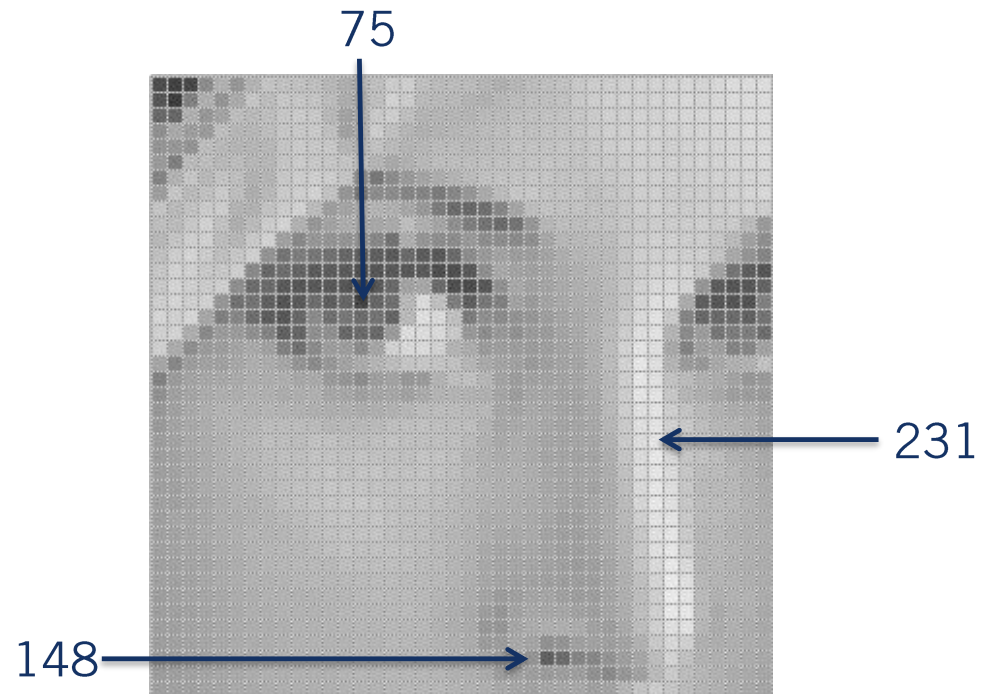
is a **sampling** parameter, defined in dots per inch (DPI) or equivalent measures of spatial pixel density, and its standard value for recent screen technologies is 72 dpi



# IMAGES ARE SAMPLED AND QUANTIZED

## 1. An image contains discrete number of pixels

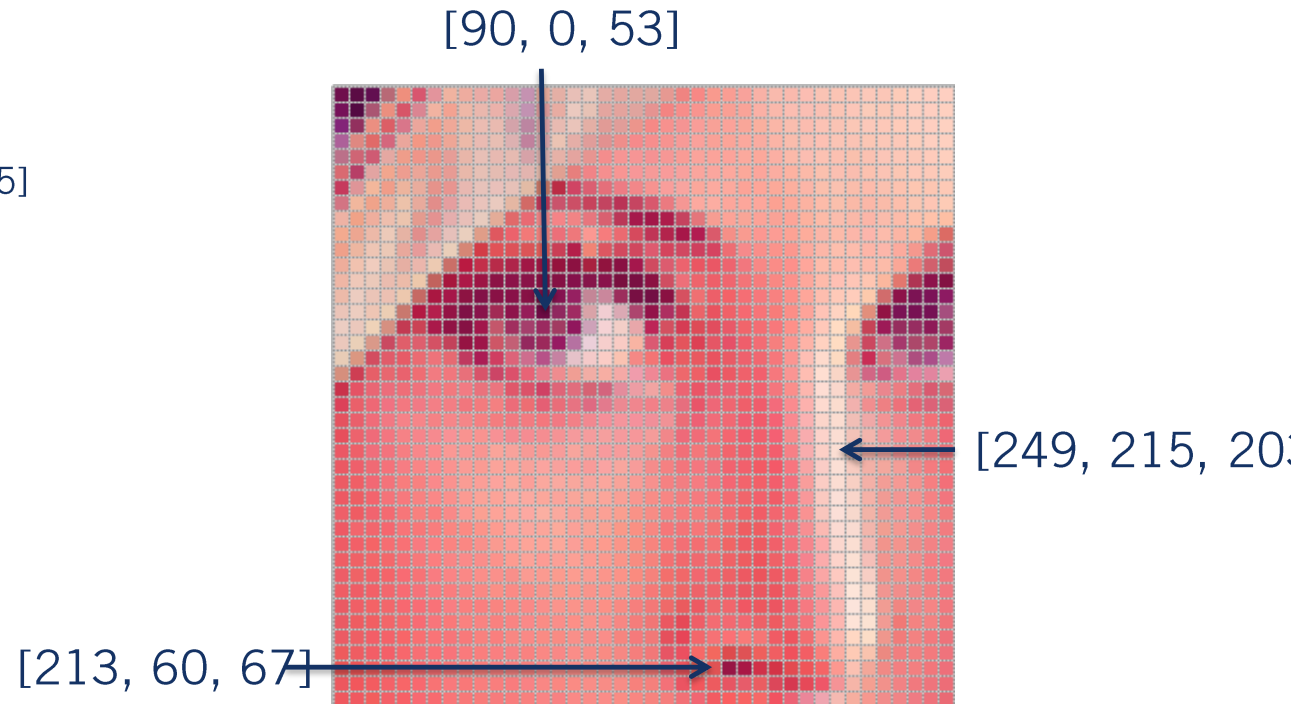
- A simple example
- Pixel value:
  - “grayscale”  
(or “intensity”):  $[0, 255]$



# IMAGES ARE SAMPLED AND QUANTIZED

## 1. An image contains discrete number of pixels

- A simple example
- Pixel value:
  - “grayscale”  
(or “intensity”):  $[0, 255]$
  - “color”
    - RGB:  $[R, G, B]$
    - Lab:  $[L, a, b]$
    - HSV:  $[H, S, V]$



## WHAT WE WILL LEARN TODAY?

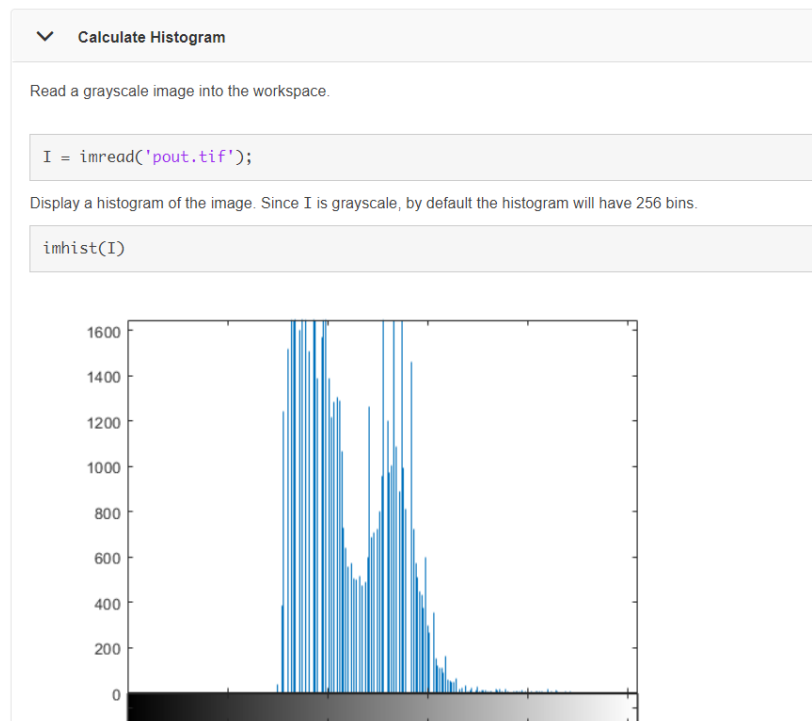
1. Image sampling and quantization
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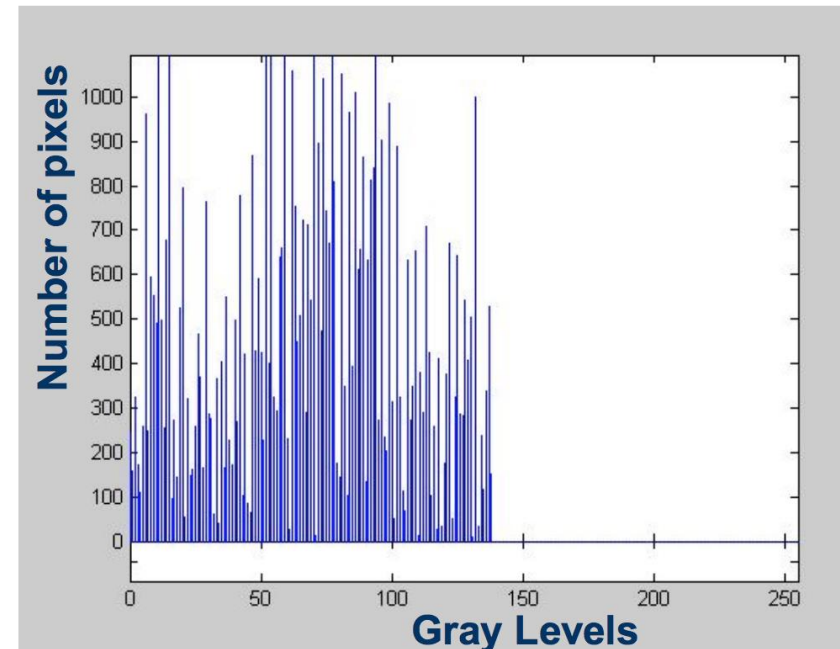


1. Histogram of an image provides the frequency of the brightness (intensity) value in the image.

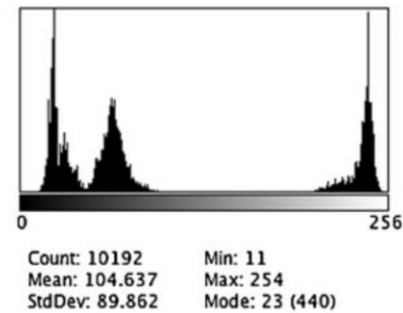
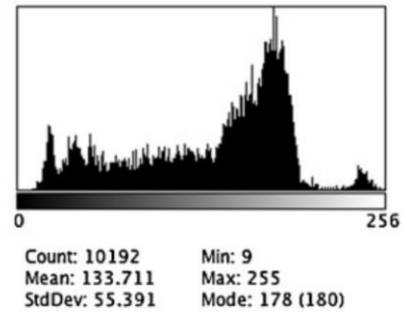


# HISTOGRAM

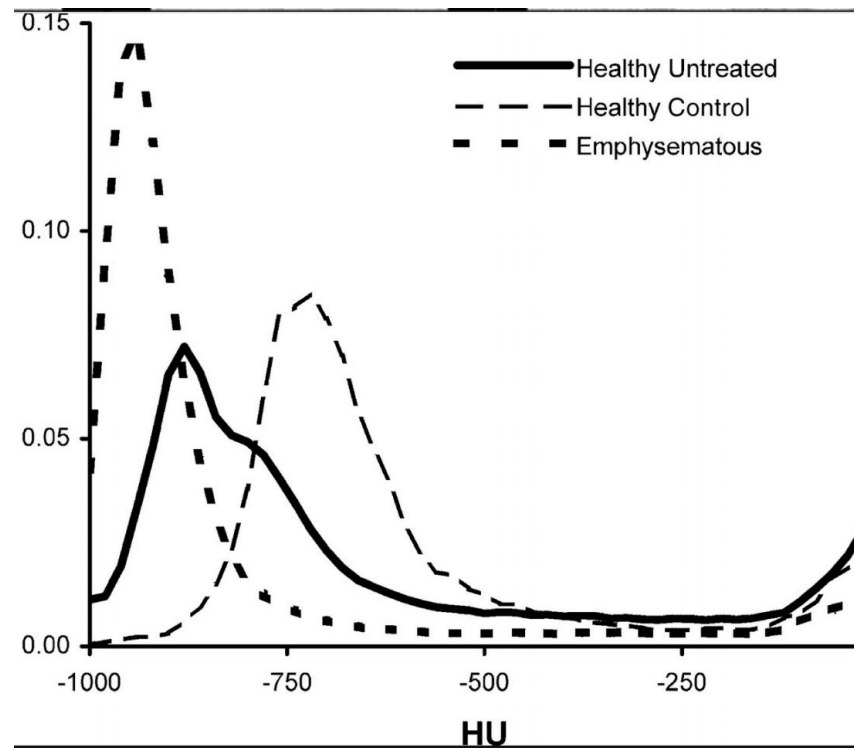
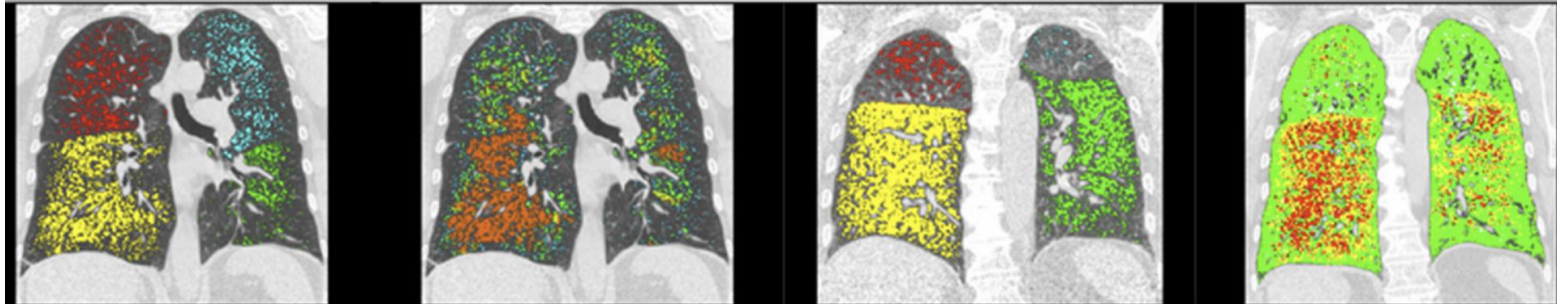
1. Histogram captures the distribution of gray levels in the image.
2. How frequently each gray level occurs in the image



# HISTOGRAM



## HISTOGRAM – USE CASE



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- Images are usually **digital (discrete)**:
  - **Sample** the 2D space on a regular grid
- Represented as a matrix of integer values

pixel



	$j$								
		62	79	23	119	120	05	4	0
$i$		10	10	9	62	12	78	34	0
		10	58	197	46	46	0	0	48
		176	135	5	188	191	68	0	49
		2	1	1	29	26	37	0	77
		0	89	144	147	187	102	62	206
		255	252	0	166	123	62	0	31
		166	63	127	17	1	0	99	30

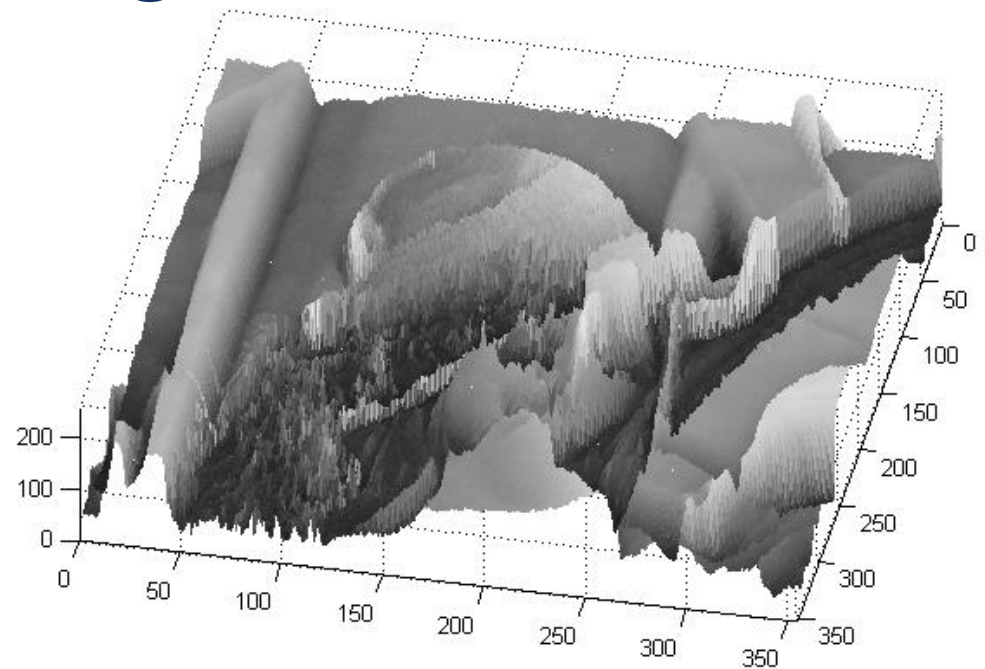
# Cartesian coordinates

$f[n, m] =$

↑  
 Notation for  
 discrete  
 functions

$$\begin{bmatrix}
 \ddots & & \vdots & & \\
 & f[-1, -1] & f[0, -1] & f[1, -1] & \\
 \dots & f[-1, 0] & \underline{f[0, 0]} & f[1, 0] & \dots \\
 & f[-1, 1] & f[0, 1] & f[1, 1] & \\
 & & \vdots & & \ddots
 \end{bmatrix}$$

- **An Image** as a function  $f$  from  $\mathbb{R}^2$  to  $\mathbb{R}^M$ :
  - $f(x, y)$  gives the **intensity** at position  $(x, y)$
  - Defined over a rectangle, with a finite  $r$





- **An Image** as a function  $f$  from  $\mathbb{R}^2$  to  $\mathbb{R}^M$ :
  - $f(x, y)$  gives the **intensity** at position  $(x, y)$
  - Defined over a rectangle, with a finite range:

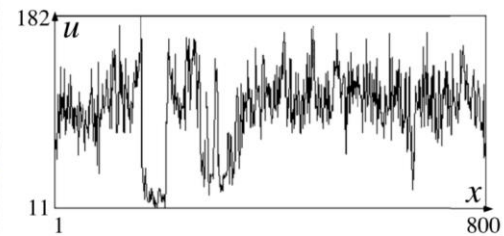
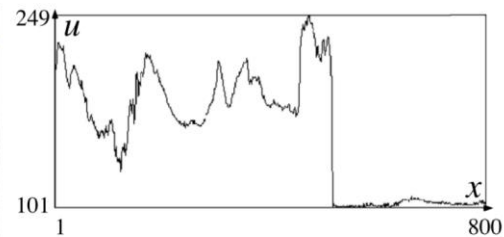
$$f: [a, b] \times [c, d] \rightarrow [0, 255]$$

Domain  
support

range

- A color image:  $f(x, y) = \begin{bmatrix} r(x, y) \\ g(x, y) \\ b(x, y) \end{bmatrix}$

# HISTOGRAMS ARE A TYPE OF IMAGE FUNCTION



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# Filtering:

- Forming a new image whose pixel values are transformed from original pixel values

## Goals:

- Goal is to extract useful information from images, or transform images into another domain where we can modify/enhance image properties
  - Features (edges, corners, blobs...)
  - super-resolution; in-painting; de-noising

1. we define a system as a unit that converts an input function  $f[n,m]$  into an output (or response) function  $g[n,m]$ , where  $(n,m)$  are the independent variables.
  - In the case for images,  $(n,m)$  represents the **spatial position in the image**.

$$f[n, m] \rightarrow \boxed{\text{System } \mathcal{S}} \rightarrow g[n, m]$$

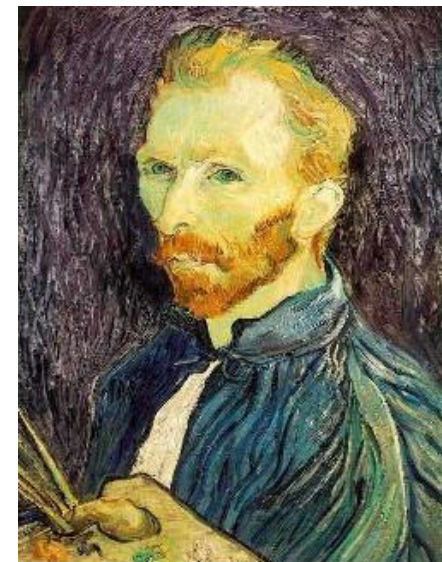
## DE-NOISING



Salt and pepper noise



## Super-resolution



## In-painting



*Image Inpainting*, M. Bertalmio et al.

<http://www.iua.upf.es/~mbertalmio/restoration.html>

ANY QUESTIONS?

