## Question 3

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**proposition:** For any integer n, the number  $n^2 + n + 1$  is odd.

**proof:** we prove by the fact that multiply an odd integer by an even integer results a even number.

1. the proposition is equal to –For any integer n, the number  $n^2 + n$  is even (as an even number plus one equal to an odd number)

- 2.  $n^2 + n = n(n+1)$
- 3. for any integer n, and n + 1. If n is odd, then n + 1 is even. if n is even then n + 1is odd. there is no other situation.
  - 4. multiply an odd number by an even number give an even number.
  - 5. therefore  $n(n+1) = n^2 + n$  is even 6. **conclusion:**  $n^2 + n + 1$  is odd.