

## Question 6

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**proposition:** the only prime triple is 3, 5, 7.

**proof:** we prove by contradiction. and make use of the conclusion of last Question.

1. Assume there exists another prime triple, say,  $n, n + 2, n + 4$ . where  $n$  is odd and  $n \neq 3$ .

2. Using the conclusion of Q5, that means, at least one of  $n, n + 2, n + 4$  has factor 3.

3. As  $n \neq 3$ , therefore one of  $n, n + 2, n + 4$  has factor 3.

4. some number has a factor 3. means either it is not a prime or it is 3.

4.1. If this number is  $n$ .  $n = 3$  contradiction to  $n \neq 3$

4.2. If this number is  $n + 2$ . Either  $n + 2$  is not prime, contradiction, or  $n + 2 = 3 \Rightarrow n = 1$ , 1 is not prime. contradiction.

4.3. If this number is  $n + 4$ . Either  $n + 4$  is not prime, contradiction, or  $n + 4 = 3 \Rightarrow n = -1$ , -1 is not prime. contradiction.

5. That means under any circumstance, one of  $n, n + 2, n + 4$  will always not be prime number.

6. By contradiction there is not another prime triple other than 3, 5, 7.

**conclusion:** we proved that the only prime triple is 3, 5, 7 by contradiction.