

# Introduction to Image Processing

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# **Topic 07**

## **Image Transforms**

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## 1. Introduction

- In some cases, image **processing tasks** are best formulated by **transforming** the input images, carrying the specified task in a **transform** domain, and applying the **inverse transform** to return to the spatial domain.
- A particularly important class of 2-D linear transforms, can be expressed in the general form.

$$T(u, v) = \sum_{x=0}^{M-1} \sum_{y=0}^{N-1} f(x, y) r(x, y, u, v)$$

where  $f$  is the input image,  $r$  is called the **forward transformation** kernel, and the equation is evaluated for  $u = 0, 1, \dots, M-1$  and  $v = 0, 1, \dots, N-1$ .

## 1. Introduction

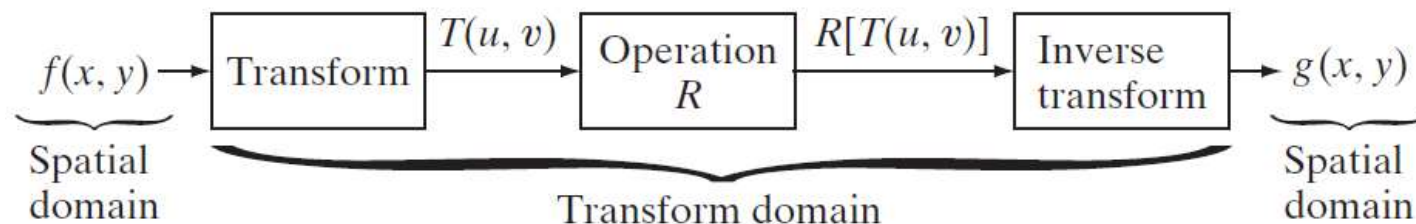
- $T$  is called the **forward transform** of  $f$ .
- Given  $T$  we can recover  $f$  using the **inverse transform**.

$$f(x, y) = \sum_{u=0}^{M-1} \sum_{v=0}^{N-1} T(u, v) s(x, y, u, v)$$

- The equation is evaluated for and  $x=0, 1, \dots, M-1$  and  $y=0, 1, \dots, N-1$ .
- And  $s$  is called the **inverse transformation** kernel.

## 1. Introduction

- By using these transforms, it is possible to express an image as a **combination** of a set **of basic signals**, known as the **basis functions**.
- The image output in the **transformed space** may be analyzed, interpreted, and further processed for implementing **diverse** image processing **tasks**.
- General approach for operating in the linear transform domain.



## 2. Discrete Fourier Transform

- Substituting the kernels below into the previous equations yields the **Discrete Fourier transform** pair

$$r(x, y, u, v) = e^{-j2\pi(ux+vy)/n}$$

$$s(x, y, u, v) = \frac{1}{n^2} e^{j2\pi(ux+vy)/n}$$

$$M = N = n$$

- The Discrete Fourier Transform was discussed in “**Topic 04** - Filtering in the Frequency Domain”.

## 2. Discrete Fourier Transform

- The 2-D Discrete Fourier Transform and its inverse.

$$F(u, v) = \sum_{x=0}^{M-1} \sum_{y=0}^{N-1} f(x, y) e^{-j2\pi(ux/M + vy/N)}$$

$$u = 0, 1, 2, \dots, M-1 \text{ and } v = 0, 1, 2, \dots, N-1.$$

$$f(x, y) = \frac{1}{MN} \sum_{u=0}^{M-1} \sum_{v=0}^{N-1} F(u, v) e^{j2\pi(ux/M + vy/N)}$$

$$x = 0, 1, 2, \dots, M-1 \text{ and } y = 0, 1, 2, \dots, N-1.$$

- DFT uses a set of complex exponential functions.
- Normally used for general spectral analysis applications.

### 3. Discrete Cosine Transform

- **Discrete Cosine Transform** (DCT) is the basis for many image and video **compression algorithms**, especially the baseline JPEG and MPEG standards for compression of **still** and **video** images respectively.

- It is obtained by using the following (equal) kernels:

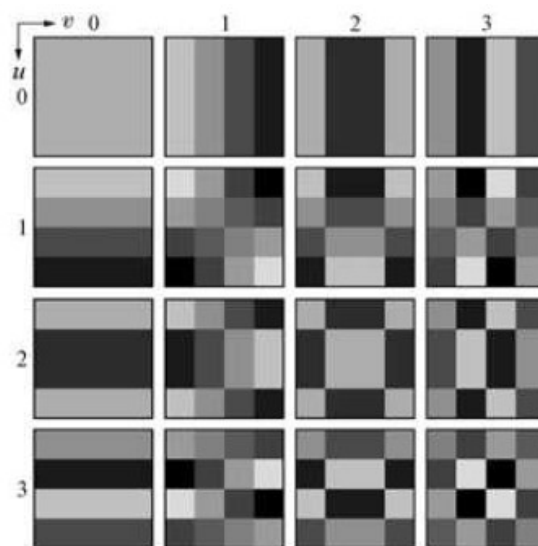
$$\begin{aligned} r(x, y, u, v) &= s(x, y, u, v) \\ &= \alpha(u)\alpha(v) \cos\left[\frac{(2x+1)u\pi}{2n}\right] \cos\left[\frac{(2y+1)v\pi}{2n}\right] \end{aligned}$$

$$\alpha(u) = \begin{cases} \sqrt{\frac{1}{n}} & \text{for } u = 0 \\ \sqrt{\frac{2}{n}} & \text{for } u = 1, 2, \dots, n-1 \end{cases}$$



### 3. Discrete Cosine Transform

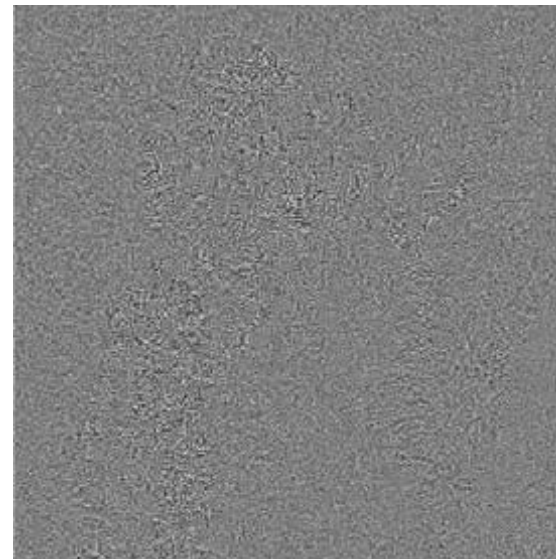
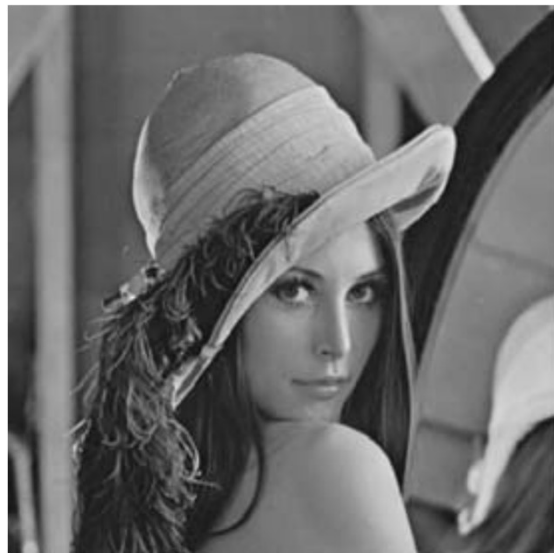
- DCT uses only (real-valued) cosine functions.
- It translates the correlated data to uncorrelated data.
- The DCT and inverse DCT can be computed using the DFT.
- Example: 8 basis functions of a 4-by-4 matrix.



**FIGURE 8.23**  
Discrete-cosine  
basis functions for  
 $n = 4$ . The origin  
of each block is at  
its top left.

### 3. Discrete Cosine Transform

- Example: approximations of the a monochrome image.
  - The result was obtained by **dividing** the original image into subimages of **size 8 x 8** using the DCT, **truncating** 50% of the resulting coefficients, and **taking the inverse transform** of the truncated coefficient arrays.



### 3. Discrete Cosine Transform

- **Mean-square** reconstruction **error** is related directly to the **energy** or **information** packing properties of the transform employed.
- An image  $g(x, y)$  can be expressed as a function of its 2-D transform

$$g(x, y) = \sum_{u=0}^{n-1} \sum_{v=0}^{n-1} T(u, v) s(x, y, u, v)$$

$$x, y = 0, 1, 2, \dots, n - 1$$

- The inverse kernel  $s$  can be viewed as defining a set of **basis functions** or **basis images**.

### 3. Discrete Cosine Transform

- This interpretation becomes clearer if we use the notation:

$$\mathbf{G} = \sum_{u=0}^{n-1} \sum_{v=0}^{n-1} T(u, v) \mathbf{S}_{uv}$$

$$\mathbf{S}_{uv} = \begin{bmatrix} s(0, 0, u, v) & s(0, 1, u, v) & \cdots & s(0, n-1, u, v) \\ s(1, 0, u, v) & \vdots & \cdots & \vdots \\ \vdots & \vdots & \cdots & \vdots \\ \vdots & \vdots & \cdots & \vdots \\ s(n-1, 0, u, v) & s(n-1, 1, u, v) & \cdots & s(n-1, n-1, u, v) \end{bmatrix}$$

- **G** contains the pixels of the image and is defined as a linear combination of  $n^2$  matrices of size  $n \times n$  that is, **S<sub>uv</sub>**, for  $u, v = 0, 1, 2, \dots, n-1$ .

### 3. Discrete Cosine Transform

- We can **define** a transform coefficient **masking function**  $\chi$  which is constructed to **eliminate** the **basis images** that make the smallest contribution to the total sum

$$\chi(u, v) = \begin{cases} 0 & \text{if } T(u, v) \text{ satisfies a specified truncation criterion} \\ 1 & \text{otherwise} \end{cases}$$

$$\hat{\mathbf{G}} = \sum_{u=0}^{n-1} \sum_{v=0}^{n-1} \chi(u, v) T(u, v) \mathbf{S}_{uv}$$

- The mean-square error between  $\mathbf{G}$  and  $\hat{\mathbf{G}}$  approximation is

$$e_{ms} = E \left\{ \|\mathbf{G} - \hat{\mathbf{G}}\|^2 \right\} = \sum_{u=0}^{n-1} \sum_{v=0}^{n-1} \sigma_{T(u,v)}^2 [1 - \chi(u, v)]$$

- The total mean-square approximation error thus is the sum of the variances of the discarded transform coefficients.

### **3. Discrete Cosine Transform**

- Transformations that redistribute or pack the most information into the fewest coefficients provide the smallest reconstruction errors.

## 4. Discrete Wavelet Transform

- Signal analysts already have at their disposal an impressive arsenal of tools. Perhaps the most well-known of these is **Fourier analysis**.



- Fourier analysis has a **serious drawback**. In transforming to the frequency domain, **time information is lost**.
- If a signal does not change much over time this drawback is not very important.

## 4. Discrete Wavelet Transform

- However, most **interesting signals** contain numerous non-stationary or **transitory characteristics**.
  - In an effort to **correct** this deficiency, Dennis Gabor (1946) adapted the Fourier transform to analyze only **a small section** of the signal at a **time**.
- Short-Time Fourier Transform (STFT)

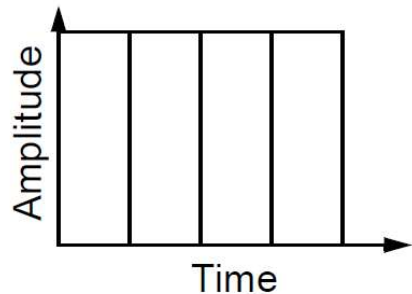


- Precision is determined by the size of the window.

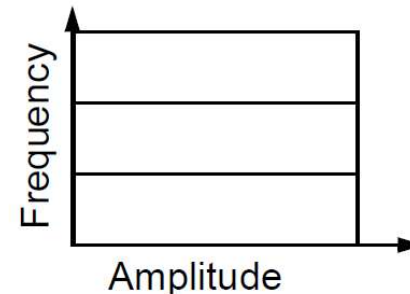


## 4. Discrete Wavelet Transform

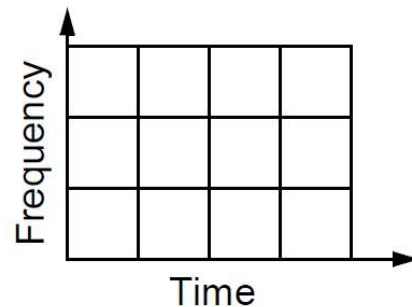
- **Wavelet analysis** represents the next logical step: a windowing technique with variable-sized regions.



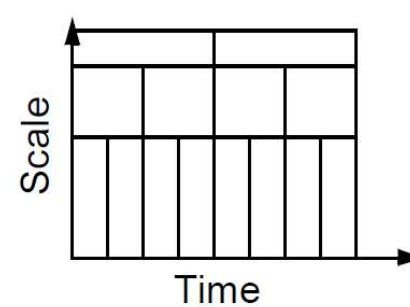
Time Domain (Shannon)



Frequency Domain (Fourier)



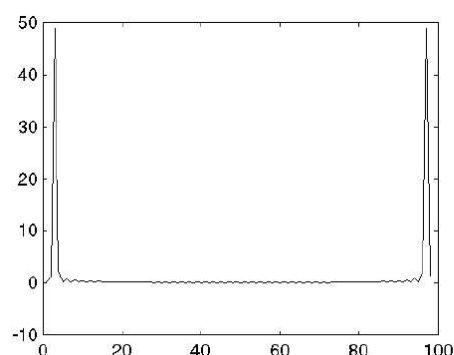
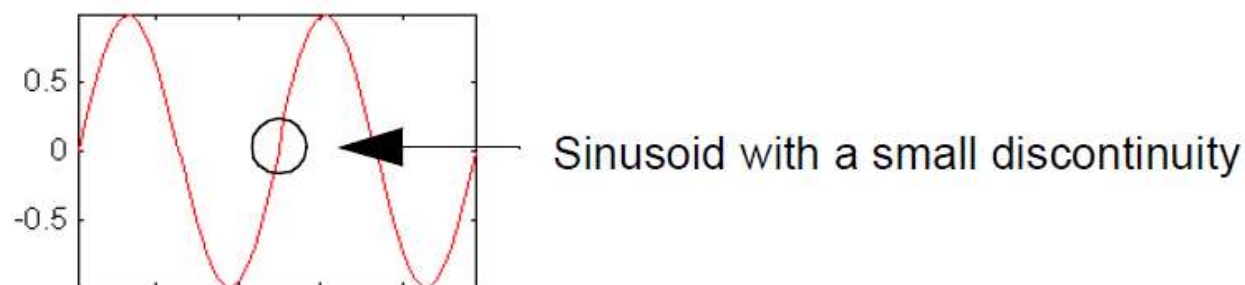
STFT (Gabor)



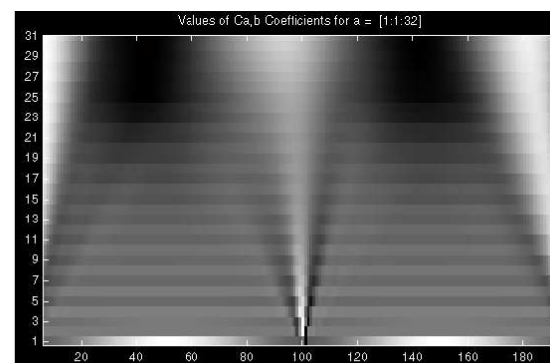
Wavelet Analysis

## 4. Discrete Wavelet Transform

- One major **advantage** afforded by wavelets is the ability to perform **local analysis** — that is, to analyze a localized area of a larger signal.



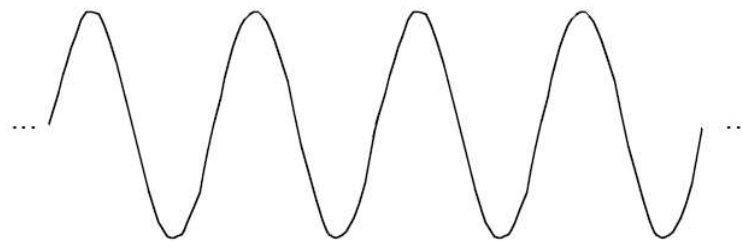
Fourier Coefficients



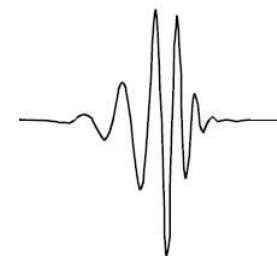
Wavelet Coefficients

## 4. Discrete Wavelet Transform

- A wavelet is a waveform of effectively **limited duration** that has an **average** value of **zero**.
- Compare wavelets with sine waves, which are the basis of Fourier analysis:
  - Sinusoids do not have limited duration.
  - Sinusoids are smooth and predictable.
  - Wavelets tend to be irregular and asymmetric.



Sine Wave

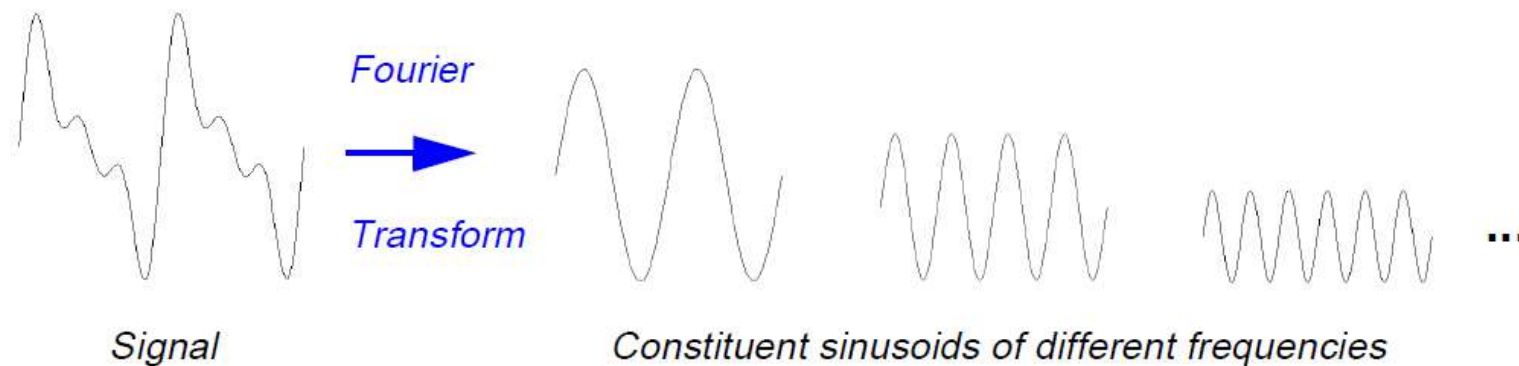


Wavelet (db10)

## 4. Discrete Wavelet Transform

- Fourier analysis consists of breaking up a signal into sine waves of various frequencies.

$$F(\omega) = \int_{-\infty}^{\infty} f(t) e^{-j\omega t} dt$$



## 4. Discrete Wavelet Transform

- The **Continuous Wavelet Transform** (CWT) of a continuous function  $f(x)$ , relative to a real-valued wavelet,  $\psi(x)$ , is defined as

$$W_{\psi}(s, \tau) = \int_{-\infty}^{\infty} f(x) \psi_{s,\tau}(x) dx$$

$$\psi_{s,\tau}(x) = \frac{1}{\sqrt{s}} \psi\left(\frac{x - \tau}{s}\right)$$

where  $s$  and  $\tau$  are called **scale** and **translation** parameters, respectively.

## 4. Discrete Wavelet Transform

- The function  $f(x)$  can be obtained using the **inverse** Continuous Wavelet Transform,

$$f(x) = \frac{1}{C_\psi} \int_0^\infty \int_{-\infty}^\infty W_\psi(s, \tau) \frac{\psi_{s,\tau}(x)}{s^2} d\tau ds$$

$$C_\psi = \int_{-\infty}^\infty \frac{|\Psi(\mu)|^2}{|\mu|} d\mu$$

where  $\Psi(\mu)$  is the Fourier transform of  $\psi(x)$ .

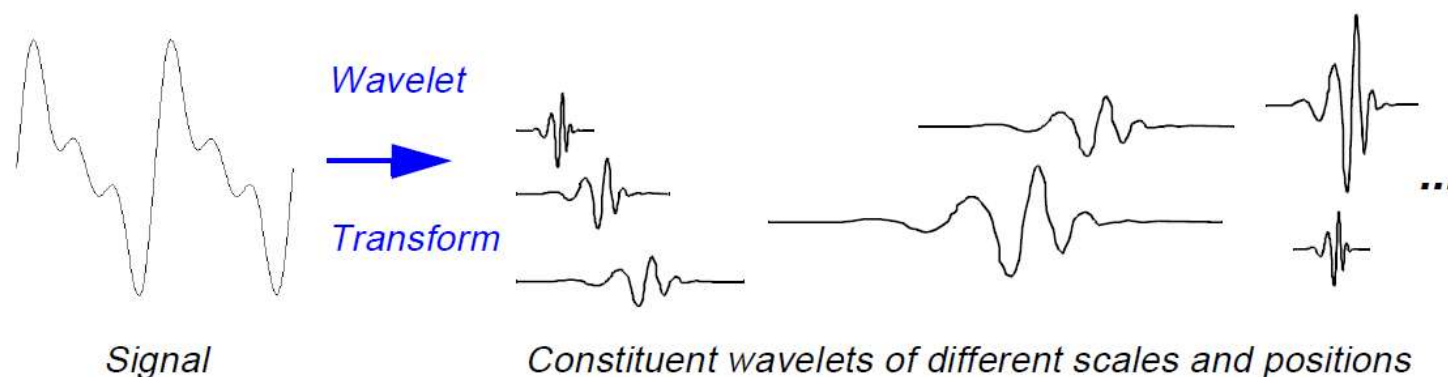
- The previous equations define a reversible transformation as long as the so-called admissibility criterion is satisfied,

$$C_\psi < \infty$$

## 4. Discrete Wavelet Transform

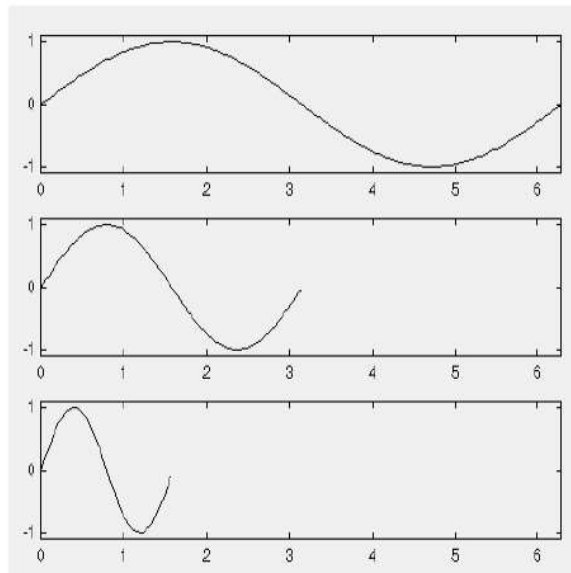
- Similarly, wavelet analysis is the breaking up of a signal into **shifted** and **scaled** versions of the original (or **mother**) wavelet.

$$C(\text{scale}, \text{position}) = \int_{-\infty}^{\infty} f(t) \psi(\text{scale}, \text{position}, t) dt$$



## 4. Discrete Wavelet Transform

- Scaling a wavelet simply means **stretching** (or compressing) it.



$$f(t) = \sin(t) \quad ; \quad a = 1$$

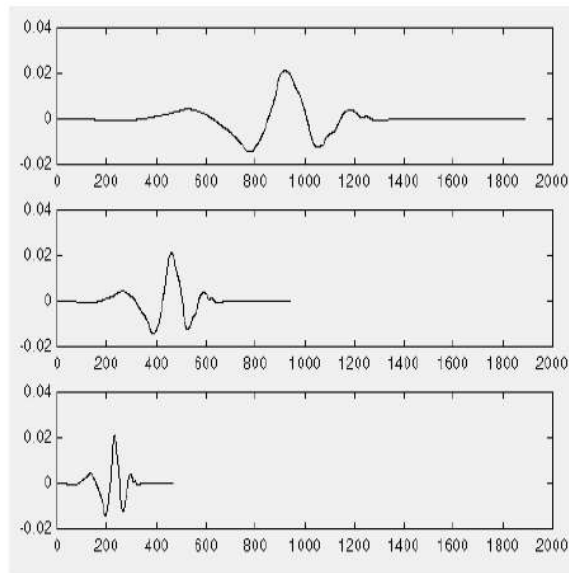
$$f(t) = \sin(2t) \quad ; \quad a = \frac{1}{2}$$

$$f(t) = \sin(4t) \quad ; \quad a = \frac{1}{4}$$



## 4. Discrete Wavelet Transform

- The scale factor works exactly the same with wavelets.



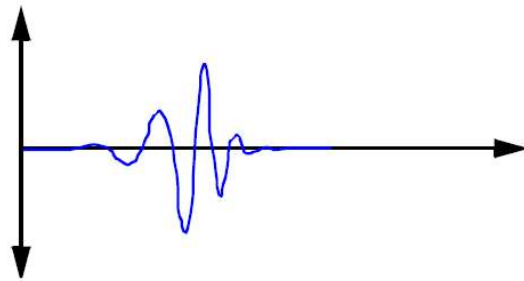
$$f(t) = \psi(t) \quad ; \quad a = 1$$

$$f(t) = \psi(2t) \quad ; \quad a = \frac{1}{2}$$

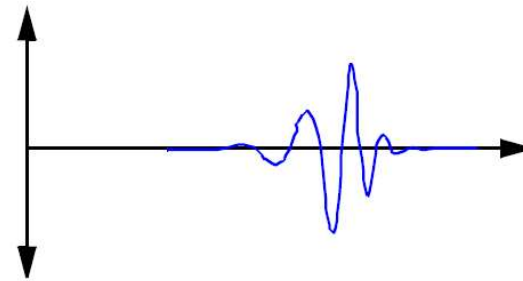
$$f(t) = \psi(4t) \quad ; \quad a = \frac{1}{4}$$

## 4. Discrete Wavelet Transform

- Shifting a wavelet simply means delaying (or hastening) its onset.



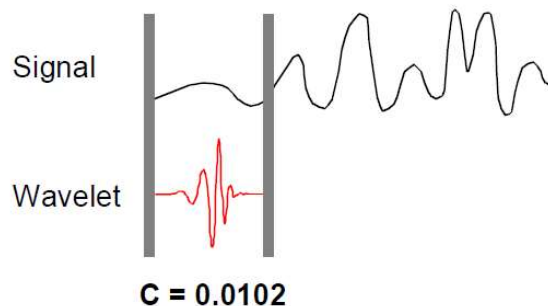
Wavelet function  
 $\psi(t)$



Shifted wavelet function  
 $\psi(t-k)$

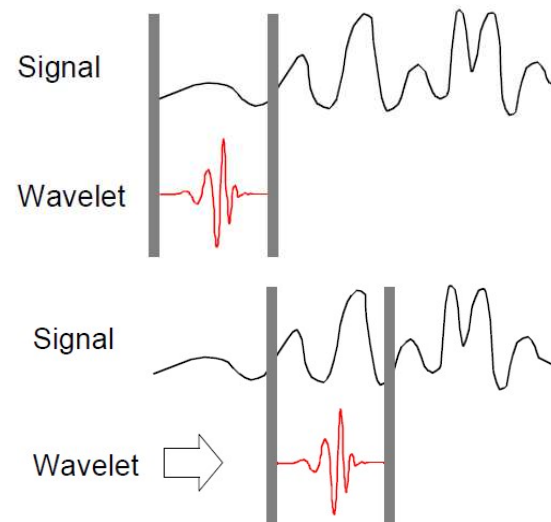
## 4. Discrete Wavelet Transform

- The CWT is the sum over all time of the signal multiplied by scaled, shifted versions of the wavelet.
- Computing the CWT:
  1. Take a wavelet and **compare** it to a section at the start of the original signal.
  2. Calculate a number,  $C$ , that represents **how closely correlated** the wavelet is with this section of the signal.



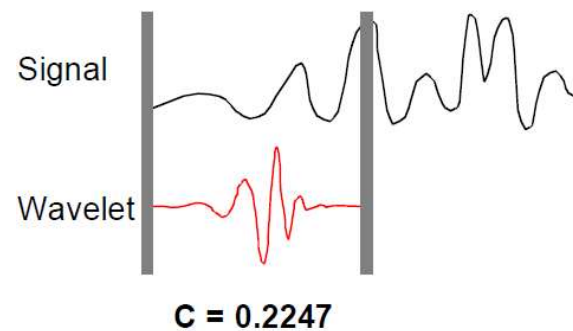
## 4. Discrete Wavelet Transform

- Computing the CWT:
  1. Compute the inner product of the signal and the wavelet.
  2. Scale the result by the wavelet's energy.
  3. Shift the wavelet to the right and repeat steps 1 and 2 until you've covered the whole signal.



## 4. Discrete Wavelet Transform

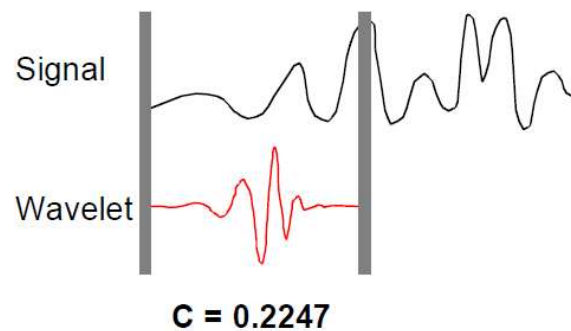
- Computing the CWT:
  4. Scale (stretch) the wavelet and repeat steps 1 through 3.



5. Repeat steps 1 through 4 for all scales.

## 4. Discrete Wavelet Transform

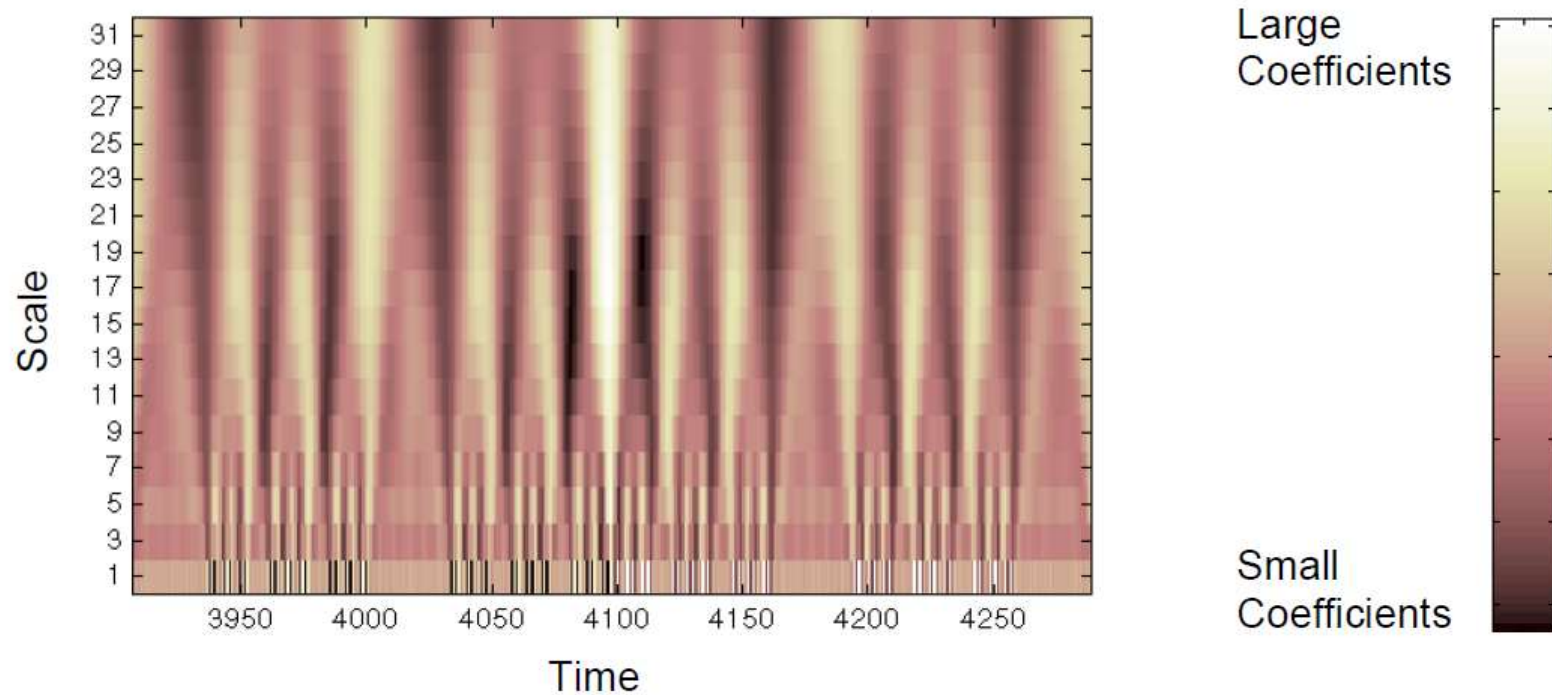
- Computing the CWT:
  4. Scale (stretch) the wavelet and repeat steps 1 through 3.



5. Repeat steps 1 through 4 for all scales.
- When you're done, you'll have the coefficients produced at different scales by different sections of the signal.

## 4. Discrete Wavelet Transform

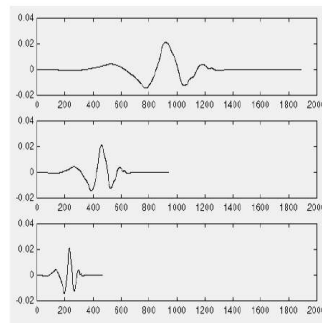
- How to make sense of all these coefficients?



## 4. Discrete Wavelet Transform

- There is a correspondence between wavelet scales and frequency:

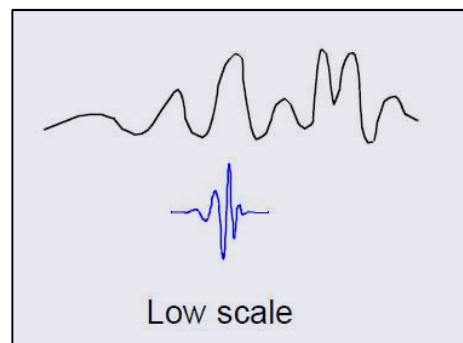
➤ Low scale → Compressed wavelet → Rapidly changing details → High frequency



$$f(t) = \psi(t) \quad ; \quad a = 1$$

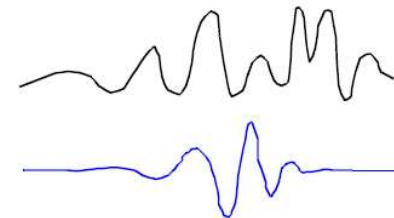
$$f(t) = \psi(2t) \quad ; \quad a = \frac{1}{2}$$

$$f(t) = \psi(4t) \quad ; \quad a = \frac{1}{4} \quad \leftarrow$$



Signal

Wavelet



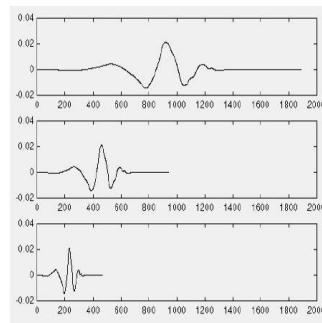
High scale



## 4. Discrete Wavelet Transform

- There is a correspondence between wavelet scales and frequency:

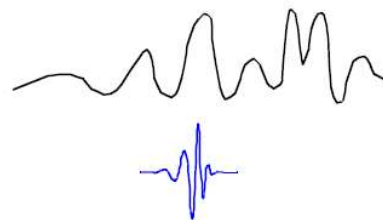
- High scale  $a \rightarrow$  Stretched wavelet  $\rightarrow$  Slowly changing, coarse features  $\rightarrow$  Low frequency



$$f(t) = \psi(t) \quad ; \quad a = 1 \quad \leftarrow$$

$$f(t) = \psi(2t) \quad ; \quad a = \frac{1}{2}$$

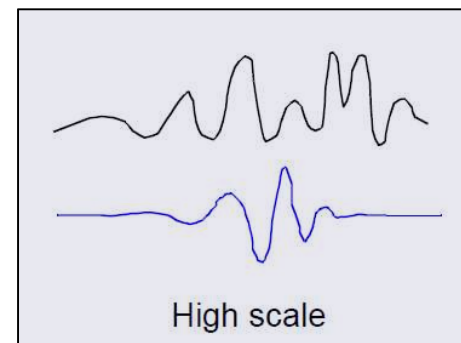
$$f(t) = \psi(4t) \quad ; \quad a = \frac{1}{4}$$



Low scale

Signal

Wavelet

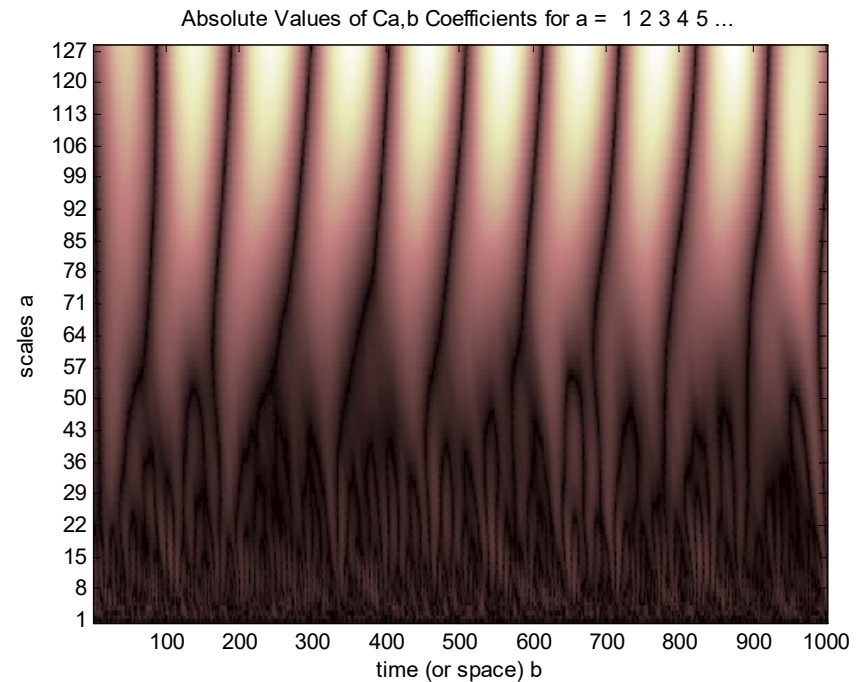
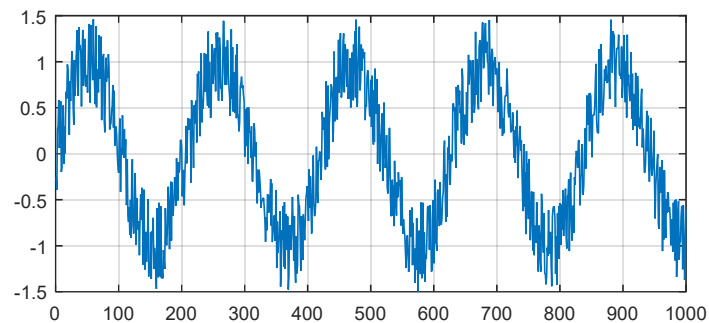


High scale

## 4. Discrete Wavelet Transform

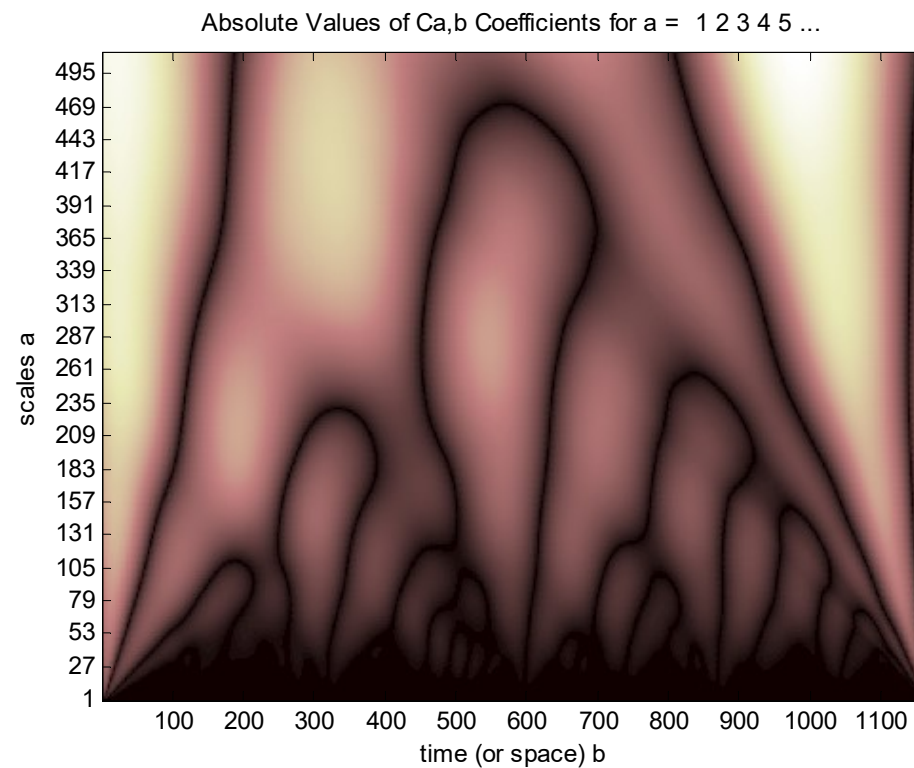
- There is a correspondence between wavelet scales and frequency:

```
load noissin;  
c = cwt(noissin,1:128,'db4','plot');
```



## 4. Discrete Wavelet Transform

- MATLAB: s32Lunar.m



## 4. Discrete Wavelet Transform

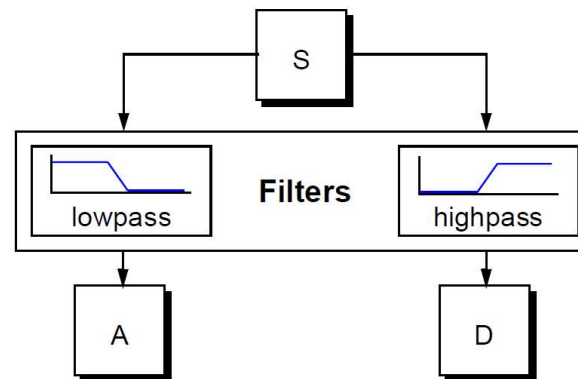
- What is “**continuous**” about the Continuous Wavelet Transform (CWT) are the **scales** at which it operates.
- CWT can operate at **every scale**, from that of the original signal up to some maximum scale which you determine.
- The CWT is also **continuous** in terms of **shifting**.
- What if we choose only a **subset** of **scales** and **positions** at which to make our calculations?
  - It turns out, that if we choose scales and **positions based on powers of two** then our analysis will just as **accurate**.
- We obtain such an analysis from the **Discrete Wavelet Transform** (DWT).

## 4. Discrete Wavelet Transform

- An efficient way to implement this scheme **using filters** was developed in 1988 by **Mallat**.
- For many signals, the **low-frequency** content is the most important part. It is what gives the signal its **identity**.
- The **high-frequency** content, on the other hand, imparts **nuance**.
- It is for this reason that, in wavelet analysis, we often speak of **approximations** and **details**.

## 4. Discrete Wavelet Transform

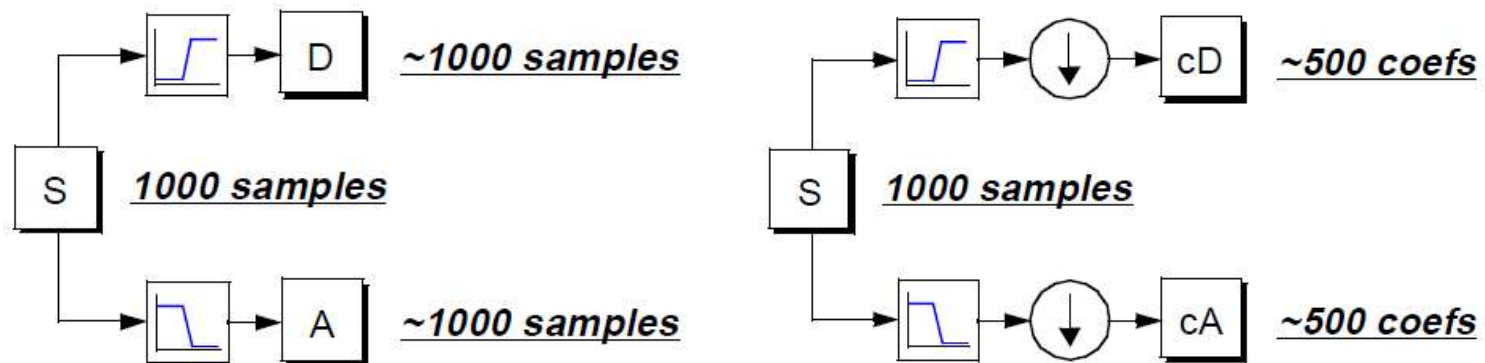
- The **approximations** are the high-scale, low-frequency components of the signal.
- The **details** are the low-scale, high-frequency components.
- The filtering process, at its most basic level, looks like this:



- If we actually perform this operation on a real digital signal, we wind up with **twice as much data** as we started with.

## 4. Discrete Wavelet Transform

- To correct this problem, we introduce the notion of **downsampling**.
- This simply means **throwing away** every second data point.

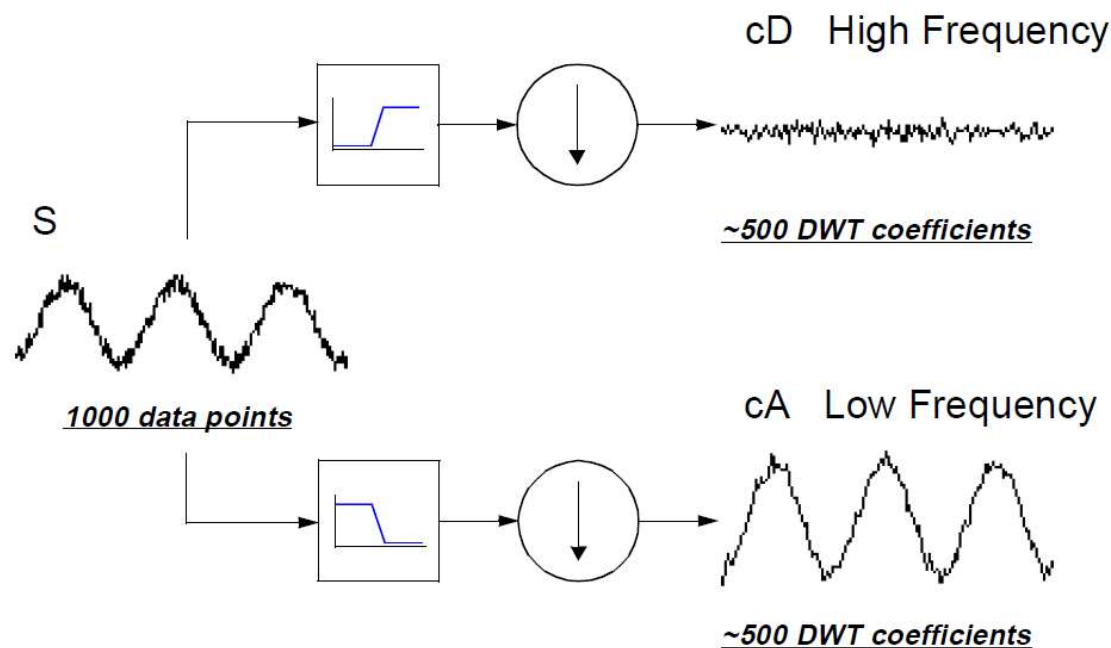


- The process on the right, which includes downsampling, produces **DWT coefficients**.

## 4. Discrete Wavelet Transform

- To correct this problem, we introduce the notion of **downsampling**.

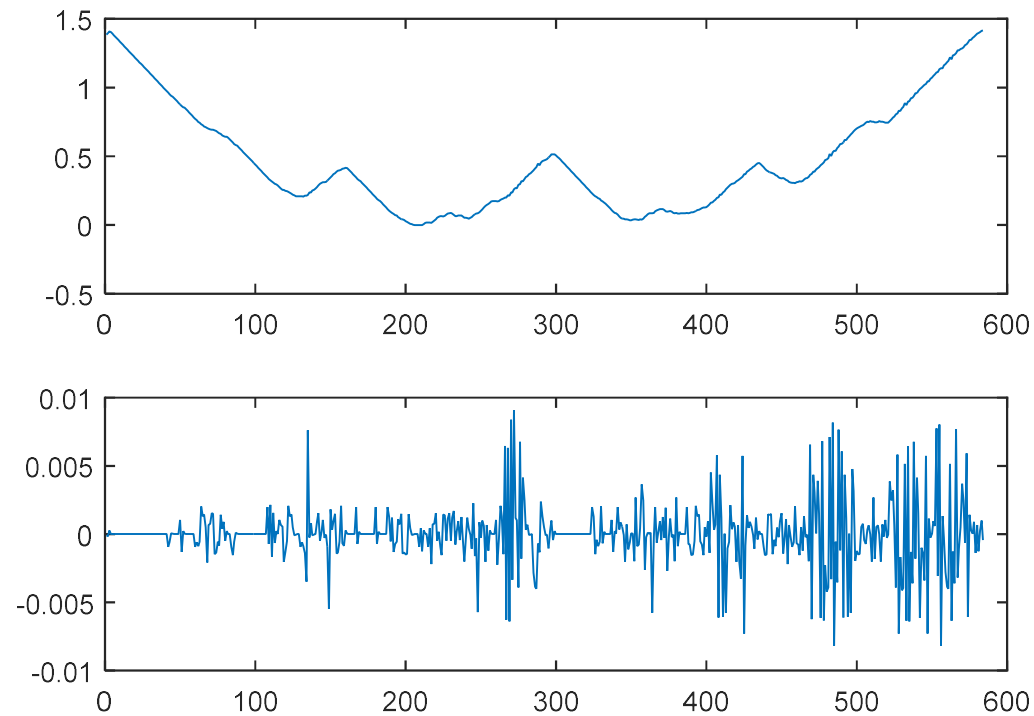
```
s = sin(20.*linspace(0,pi,1000)) + 0.5.*rand(1,1000);  
[cA,cD] = dwt(s,'db2');
```





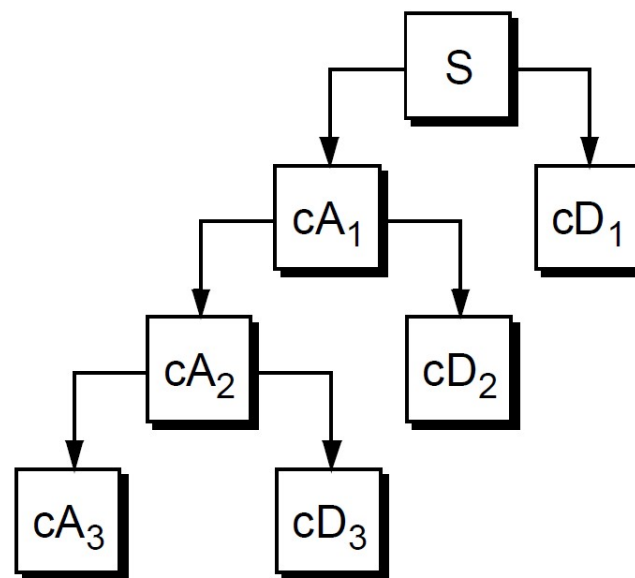
## 4. Discrete Wavelet Transform

- MATLAB: s39ApproxDet.m



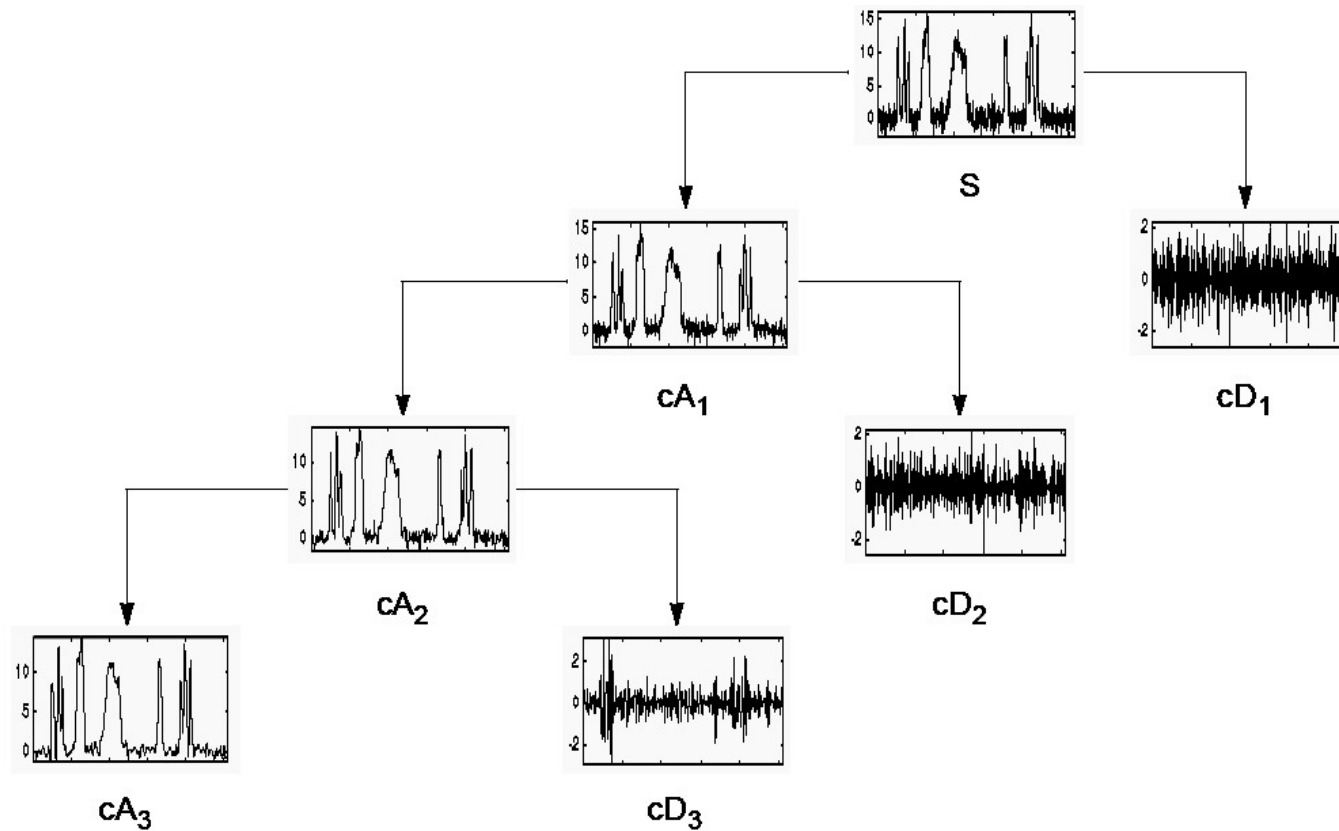
## 4. Discrete Wavelet Transform

- The decomposition process can be iterated, with successive approximations being decomposed in turn, so that one signal is broken down into many lower-resolution components.
- This is called the wavelet decomposition tree.



## 4. Discrete Wavelet Transform

- The decomposition process can be iterated.

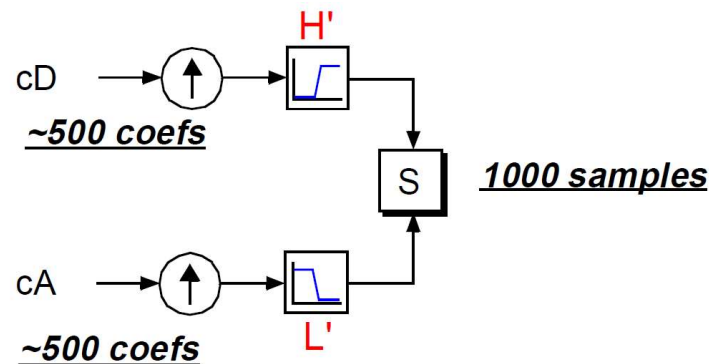
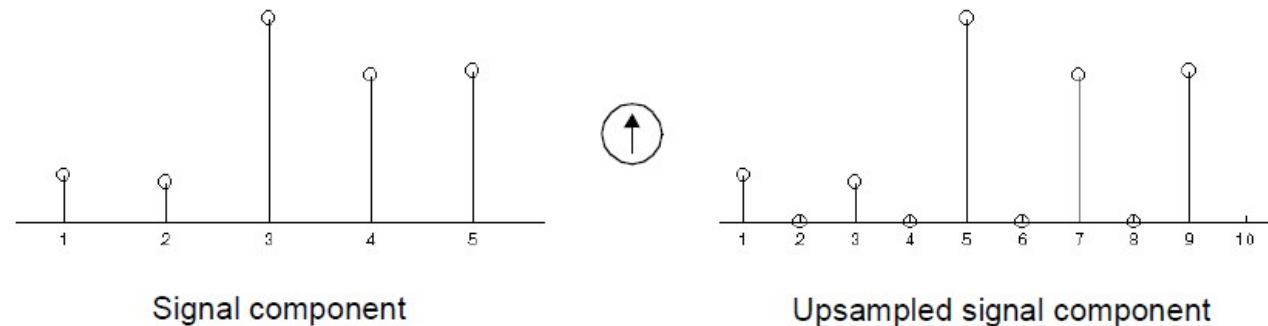


## 4. Discrete Wavelet Transform

- We've learned how the discrete wavelet transform can be used to analyze, or decompose, signals and images.
- The other half of the story is how those components can be assembled back into the original signal with no loss of information.
- This process is called reconstruction, or synthesis.
- The mathematical manipulation that effects synthesis is called the inverse discrete wavelet transform (IDWT).

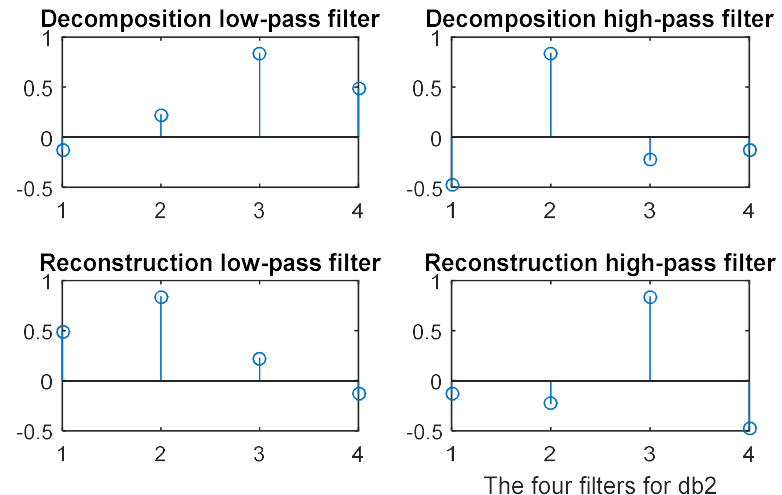
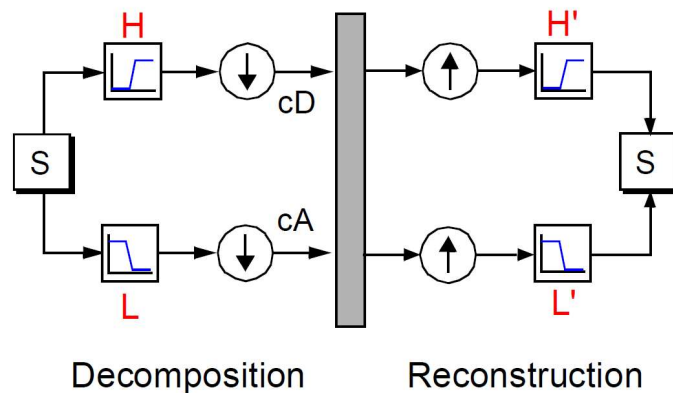
## 4. Discrete Wavelet Transform

- Wavelet analysis involves filtering and downsampling.
- The wavelet reconstruction process consists of upsampling and filtering.



## 4. Discrete Wavelet Transform

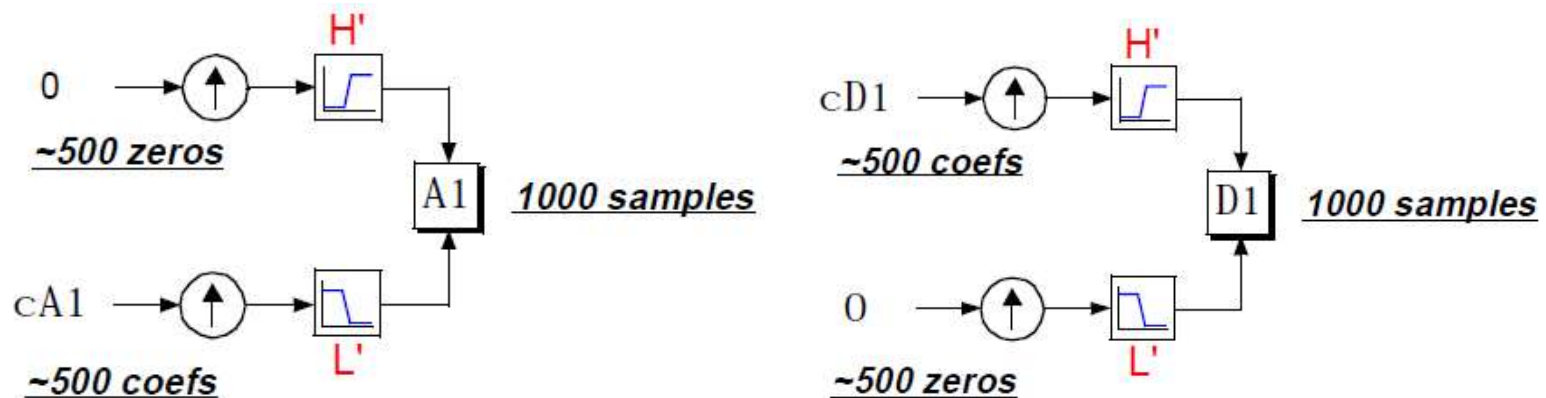
- Wavelet analysis involves filtering and downsampling.
- By carefully choosing the decomposition and reconstruction filters we can “cancel out” the effects of aliasing caused by the subsampling.
- **Quadrature mirror filters:**



- MATLAB: `s44Filters.m`

## 4. Discrete Wavelet Transform

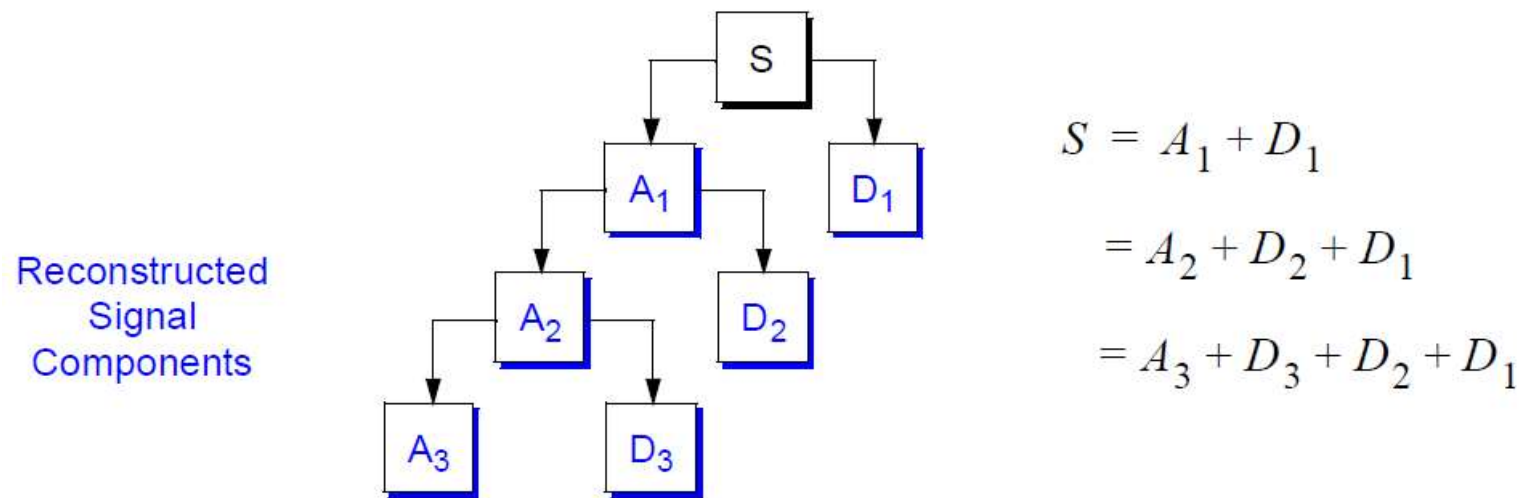
- It is also possible to reconstruct the approximation A and detail D themselves **from their coefficient vectors**  $c_A$  and  $c_D$ .



- And  $S = A_1 + D_1$ .

## 4. Discrete Wavelet Transform

- Extending this technique to a multi-level analysis.





## 4. Discrete Wavelet Transform

- The choice of filters not only determines whether perfect reconstruction is possible, it also determines the shape of the wavelet we use to perform the analysis.
- To construct a wavelet of some practical utility, you seldom start by drawing a waveform.
- Instead, it usually makes more sense to design the appropriate filters and then use them to create the waveform.

## 4. Discrete Wavelet Transform

- Example:

- Starting from the reconstruction low-pass filter  $L'$

```
[L, H, Lprime, Hprime] = wfilters('db2')
```

```
Lprime = [0.4830    0.8365    0.2241   -0.1294]
```

- If we reverse the order  $L_{mult}$  and then multiply every second sample by  $-1$ , we obtain the highpass filter  $H'$ :

```
Hprime = [-0.1294   -0.2242   -0.8365    0.4830]
```

- Next, upsample  $H_{prime}$  by two, inserting zeros in alternate positions:

```
HU = [-0.1294  0 -0.2241  0  0.8365  0 -0.4830  0]
```

## 4. Discrete Wavelet Transform

- Example:

- Convolve the upsampled vector with the original lowpass filter:

```
H2 = conv(HU, Lprime);
```

- If we iterate this process several more times, repeatedly upsampling and convolving the resultant vector with the four-element filter vector Lprime, a pattern begins to emerge.
  - Scale the final result by  $(\sqrt{2})^i$ , where  $i$  is the number of iterations.
- This result shows that the wavelet's shape is determined entirely by the coefficients of the reconstruction filters.

## 4. Discrete Wavelet Transform

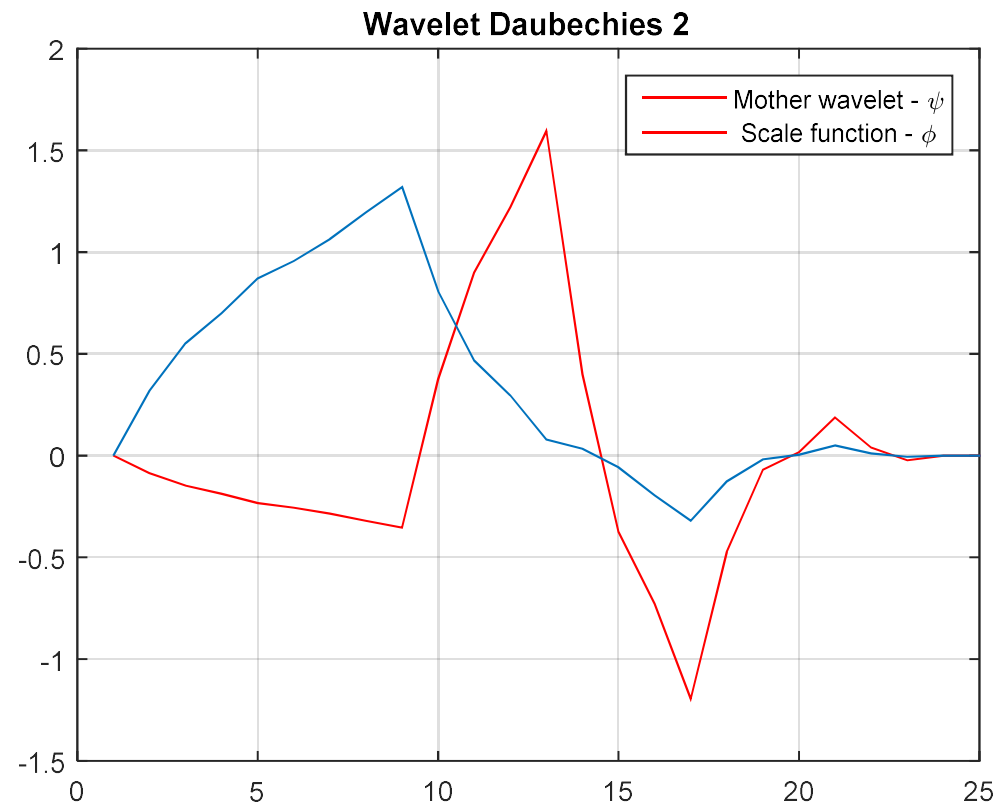
- This relationship has profound implications.
- It means that you cannot choose just any shape, call it a wavelet, and perform an analysis.
- At least, you can't choose an arbitrary wavelet waveform if you want to be able to reconstruct the original signal accurately.
- You are compelled to choose a shape determined by
- quadrature mirror decomposition filters.

## 4. Discrete Wavelet Transform

- The **mother wavelet** function  $\psi$  is determined by the highpass filter, which also produces the **details** of the wavelet decomposition.
- There is an additional function associated with some but not all wavelets. This is the so-called **scaling** function,  $\phi$ .
- It is determined by the lowpass quadrature mirror filters, and thus is associated with the **approximations** of the wavelet decomposition.
- Iteratively upsampling and convolving the lowpass filter produces a shape approximating the **scaling function**.

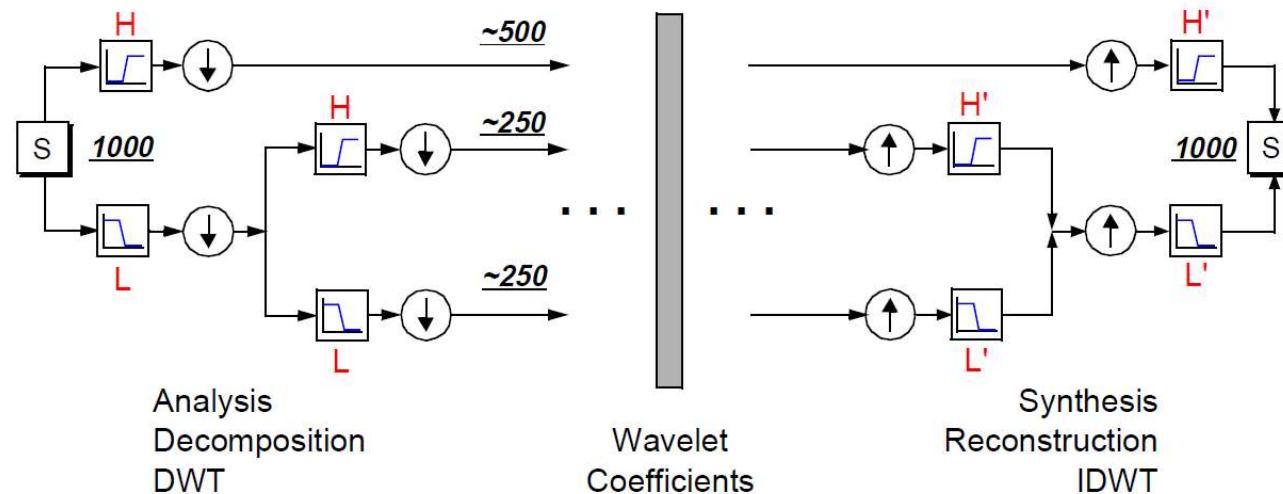
## 4. Discrete Wavelet Transform

- MATLAB: s53WaveFilters.m



## 4. Discrete Wavelet Transform

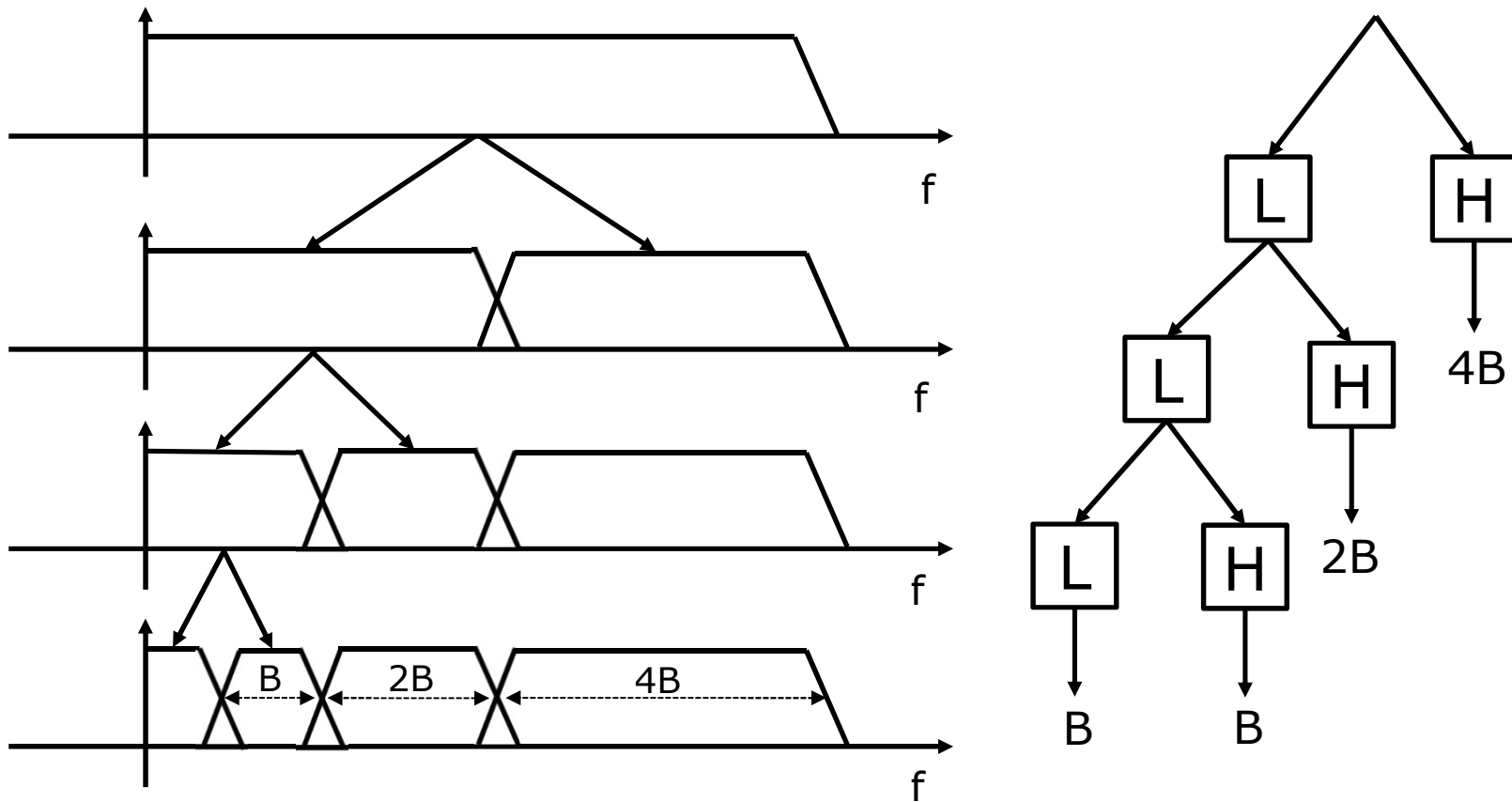
- Multistep analysis-synthesis:



- Of course, there is no point breaking up a signal merely to have the satisfaction of immediately reconstructing it.
- We perform wavelet analysis because the coefficients thus obtained have many known uses, de-noising and compression being foremost among them.

## 4. Discrete Wavelet Transform

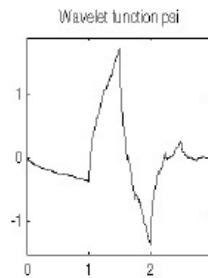
- Multistep analysis-synthesis:



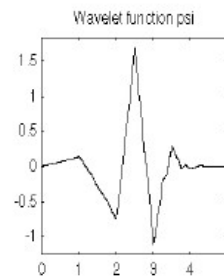


## 4. Discrete Wavelet Transform

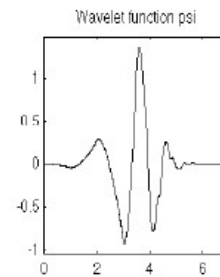
- Examples of wavelets: nine members of the Daubechies family.



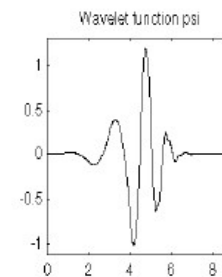
db2



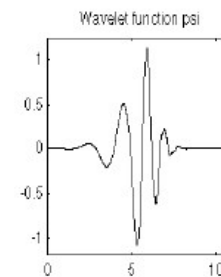
db3



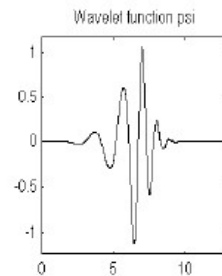
db4



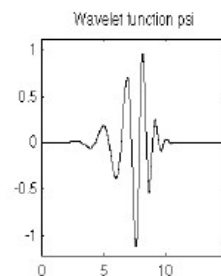
db5



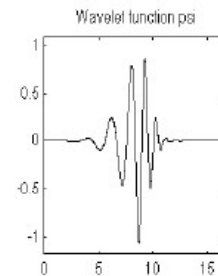
db6



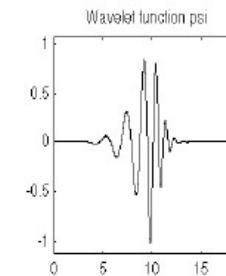
db7



db8



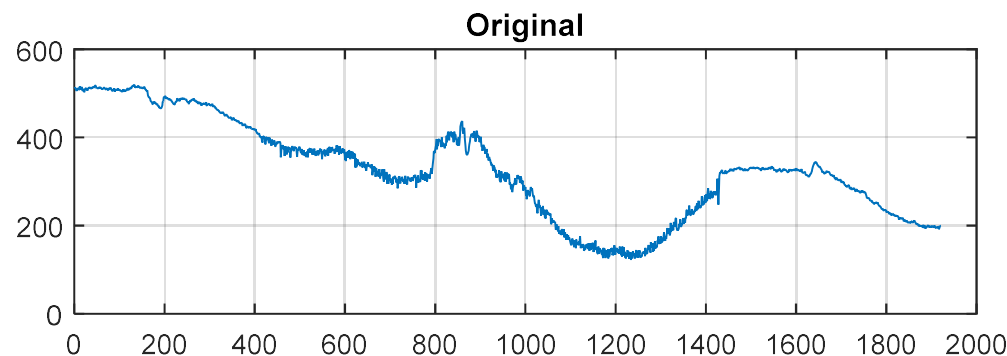
db9



db10

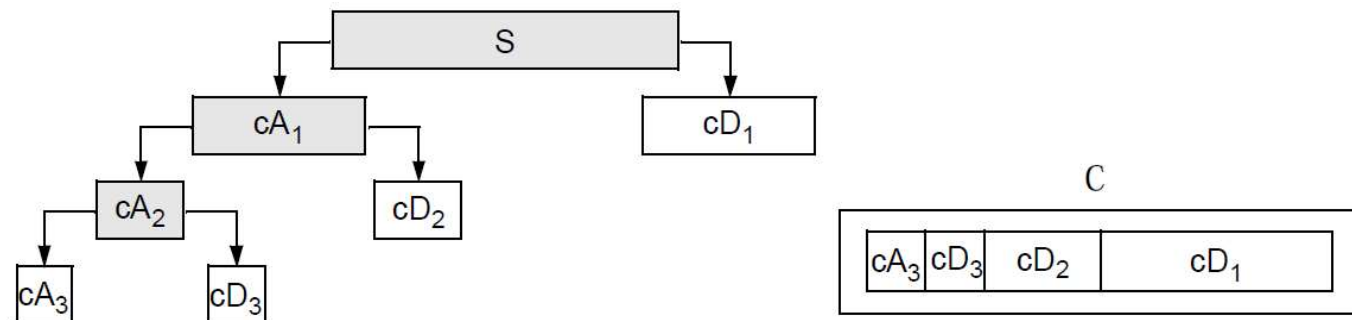
## 4. Discrete Wavelet Transform

- Example of One-Dimensional Analysis:
  - This example involves a real-world signal — electrical consumption measured over the course of three days.
  - This signal is particularly interesting because of noise introduced when a defect developed in the monitoring equipment as the measurements were being made.
  - Wavelet analysis effectively removes the noise.



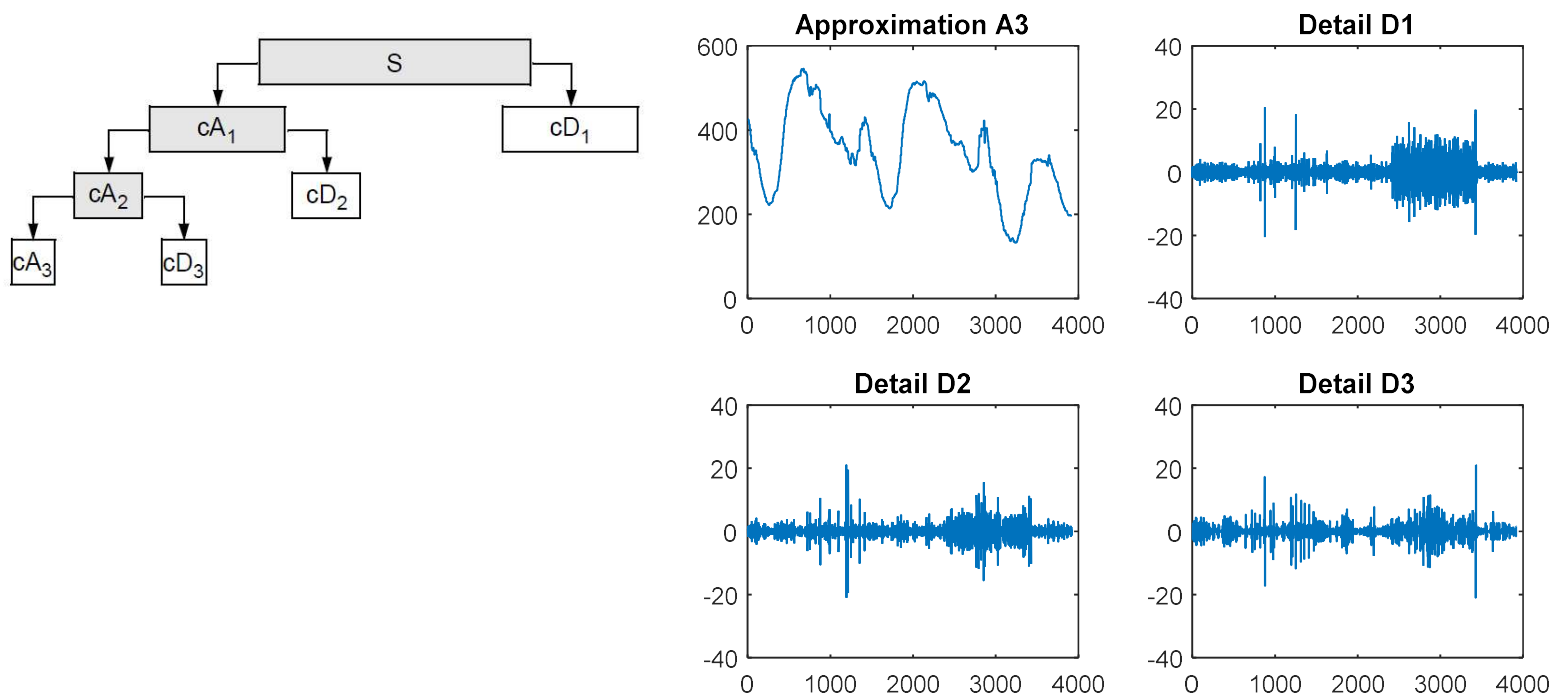
## 4. Discrete Wavelet Transform

- Example of One-Dimensional Analysis:
  - Level 3 decomposition of the signal (again using the 'db3' wavelet).



## 4. Discrete Wavelet Transform

- Example of One-Dimensional Analysis:
  - Level 3 decomposition of the signal (again using the 'db3' wavelet).



## 4. Discrete Wavelet Transform

- Example of One-Dimensional Analysis:
  - Setting a threshold

Detail Level 1



Detail Level 2



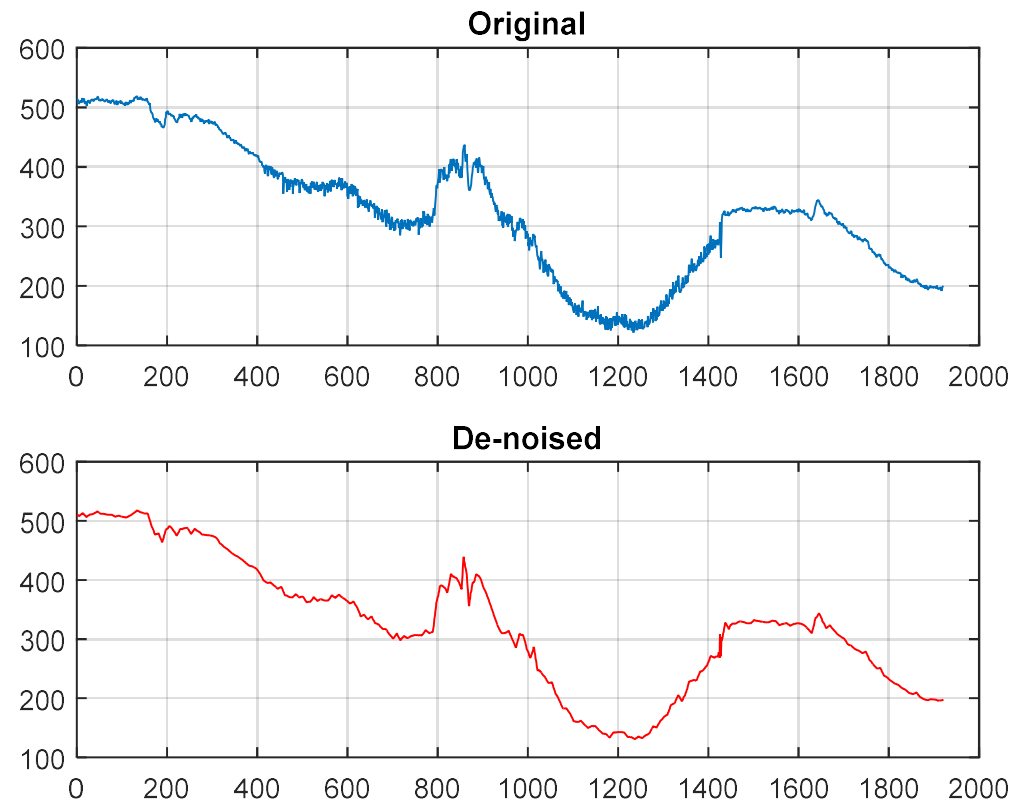
Detail Level 3



## 4. Discrete Wavelet Transform

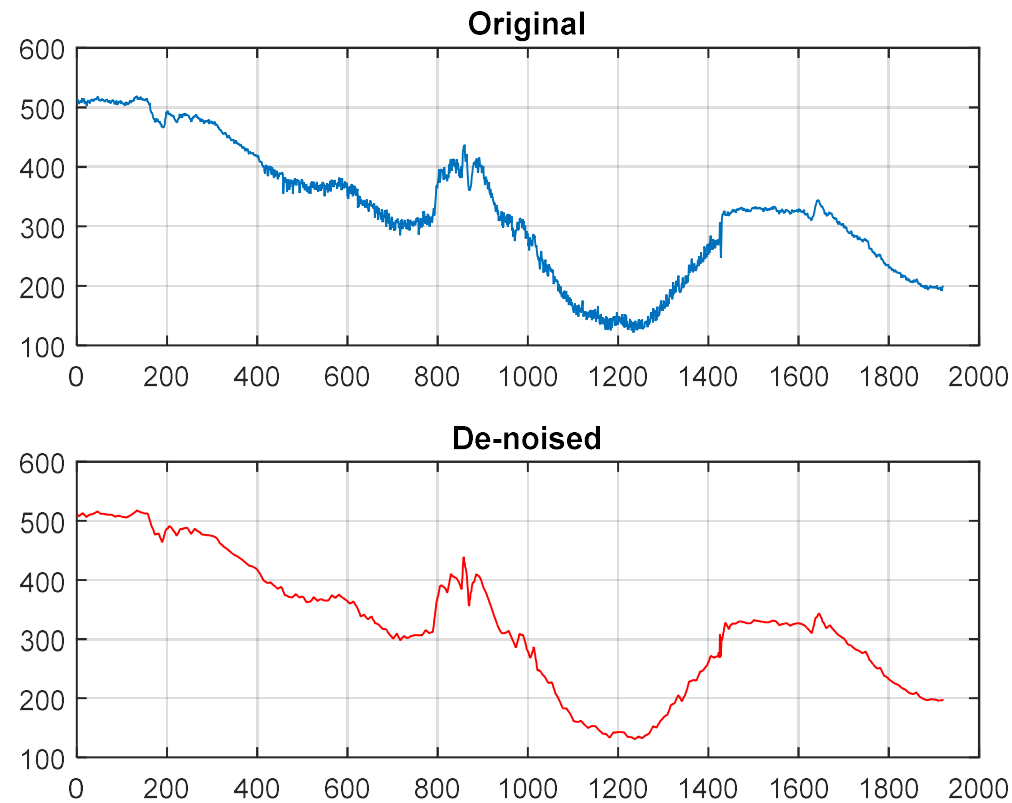
- Example of One-Dimensional Analysis:

- Reconstruction



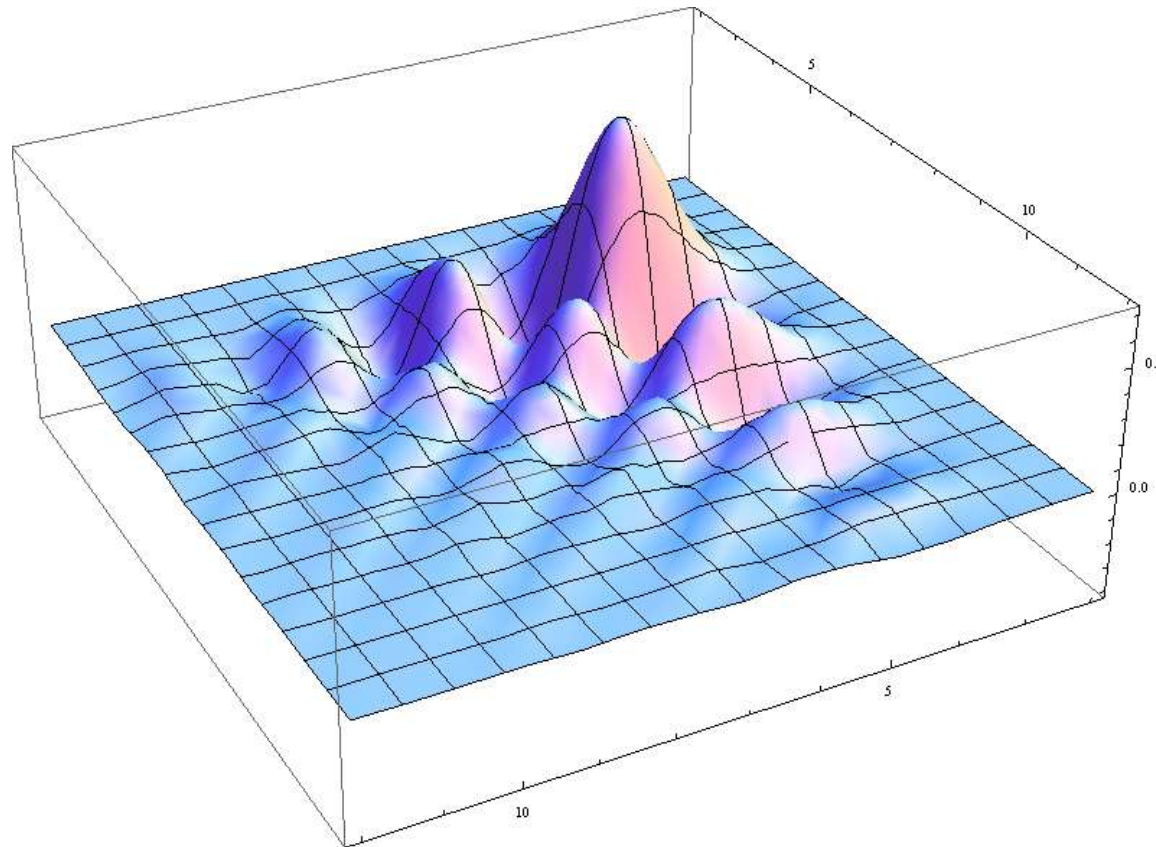
## 4. Discrete Wavelet Transform

- MATLAB: s61Denoise1D.m



## 4. Discrete Wavelet Transform

- Two-Dimensional Analysis



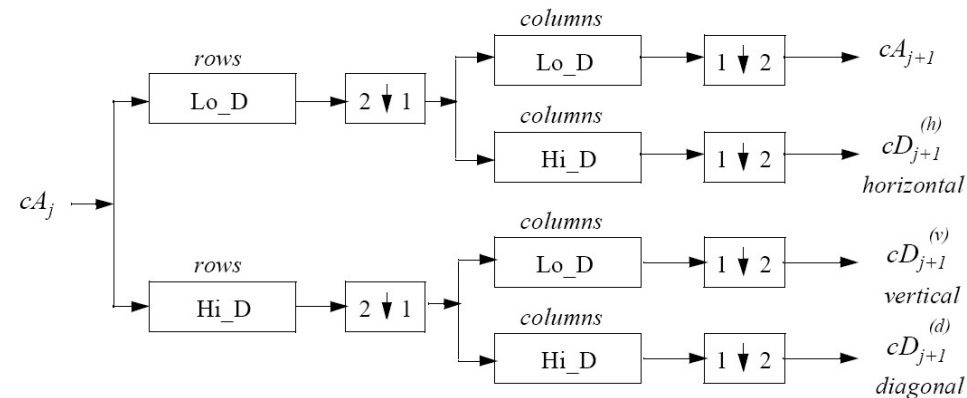


## 4. Discrete Wavelet Transform

- Two-Dimensional Analysis

### Two-Dimensional DWT

#### Decomposition step



Where:

- $\begin{bmatrix} 2 \\ \downarrow \\ 1 \end{bmatrix}$  Downsample columns: keep the even indexed columns.
- $\begin{bmatrix} 1 \\ \downarrow \\ 2 \end{bmatrix}$  Downsample rows: keep the even indexed rows.
- $\begin{matrix} \text{rows} \\ \boxed{X} \end{matrix}$  Convolve with filter X the rows of the entry.
- $\begin{matrix} \text{columns} \\ \boxed{X} \end{matrix}$  Convolve with filter X the columns of the entry.

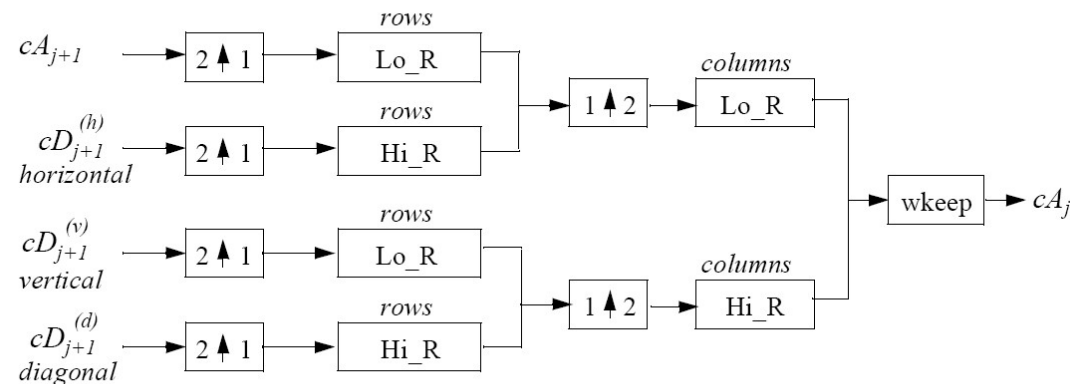
**Initialization**  $cA_0 = s$  for the decomposition initialization.

## 4. Discrete Wavelet Transform

- Two-Dimensional Analysis

### Two-Dimensional IDWT

#### Reconstruction step

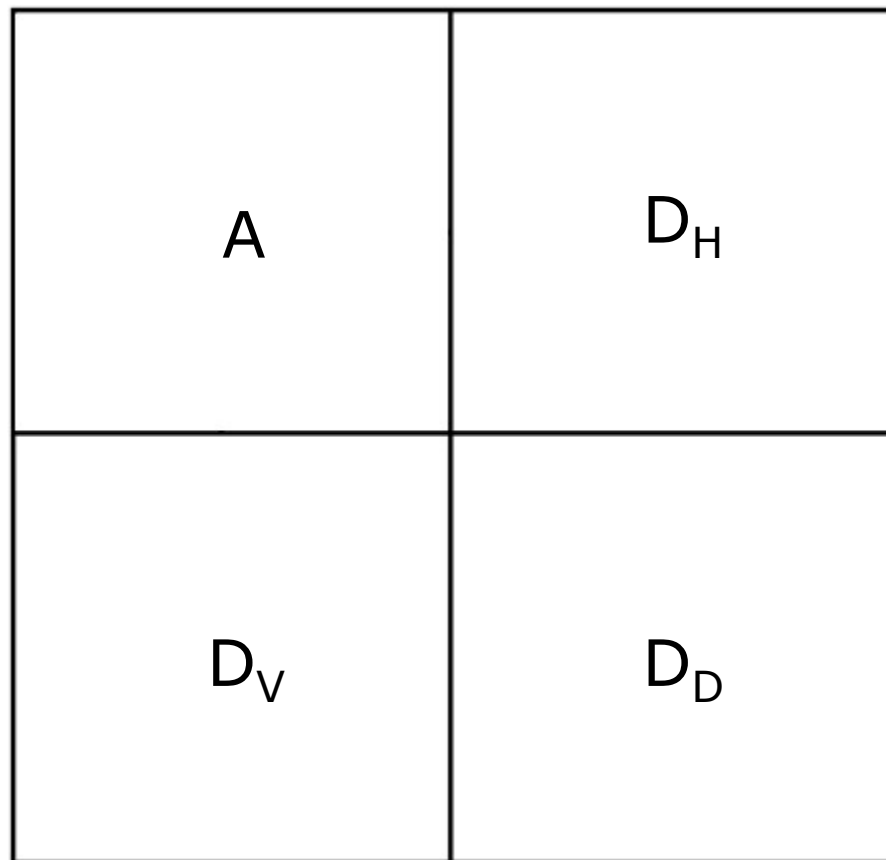


Where:

$2 \uparrow 1$	Upsample columns: insert zeros at odd-indexed columns.
$1 \uparrow 2$	Upsample rows: insert zeros at odd-indexed rows.
$\begin{matrix} \text{rows} \\ \boxed{X} \end{matrix}$	Convolve with filter X the rows of the entry.
$\begin{matrix} \text{columns} \\ \boxed{X} \end{matrix}$	Convolve with filter X the columns of the entry.

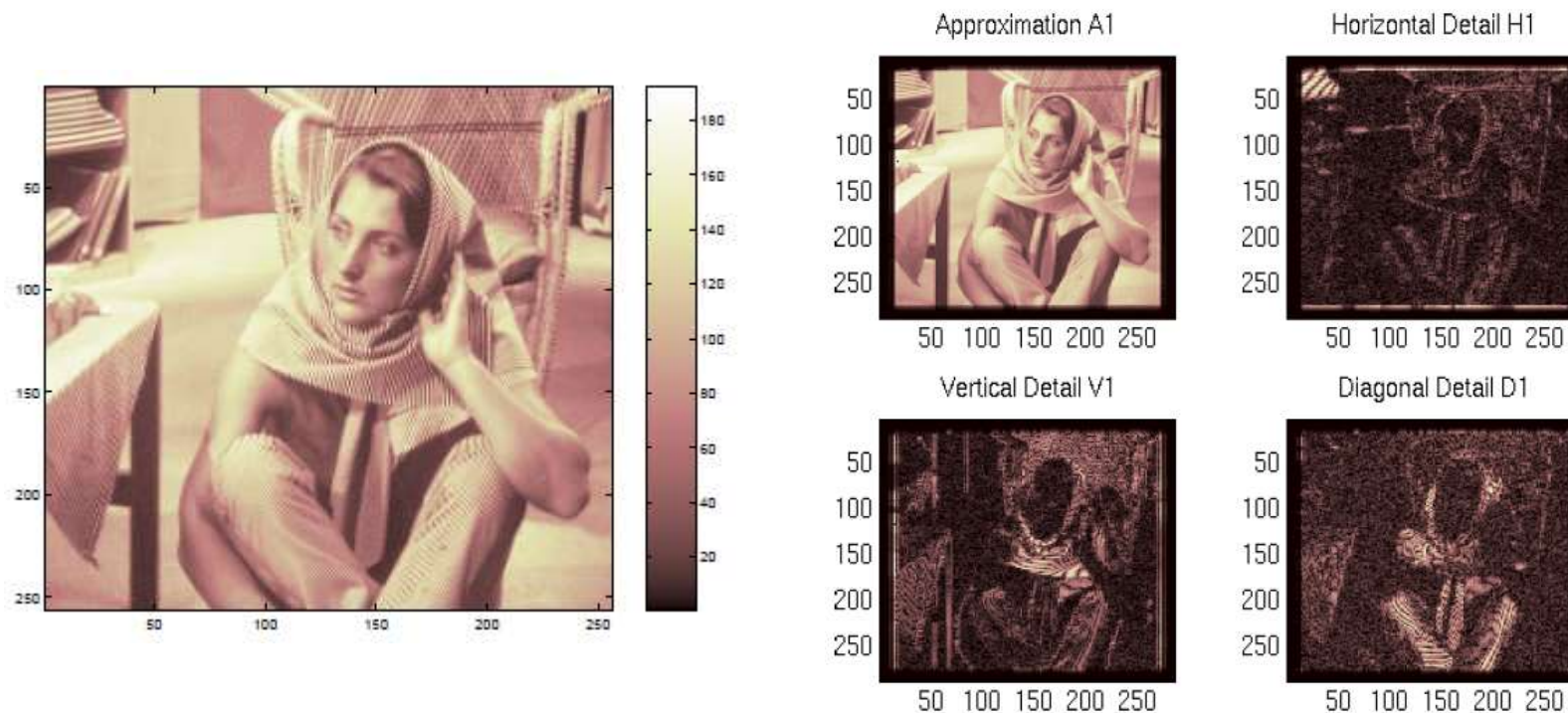
## 4. Discrete Wavelet Transform

- Two-Dimensional Analysis (one-step decomposition)



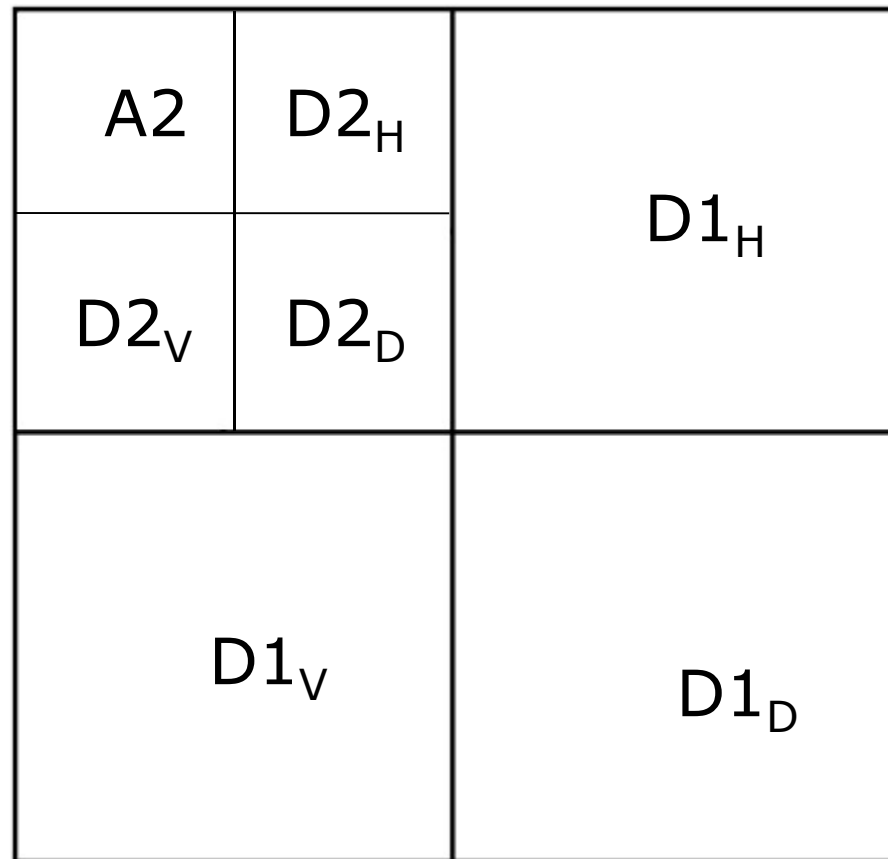
## 4. Discrete Wavelet Transform

- Two-Dimensional Analysis (one-step decomposition)



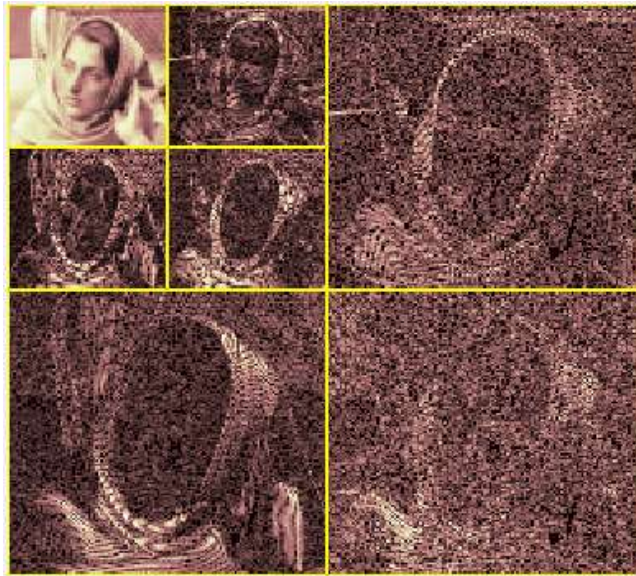
## 4. Discrete Wavelet Transform

- Two-Dimensional Analysis (multiple-level decomposition)



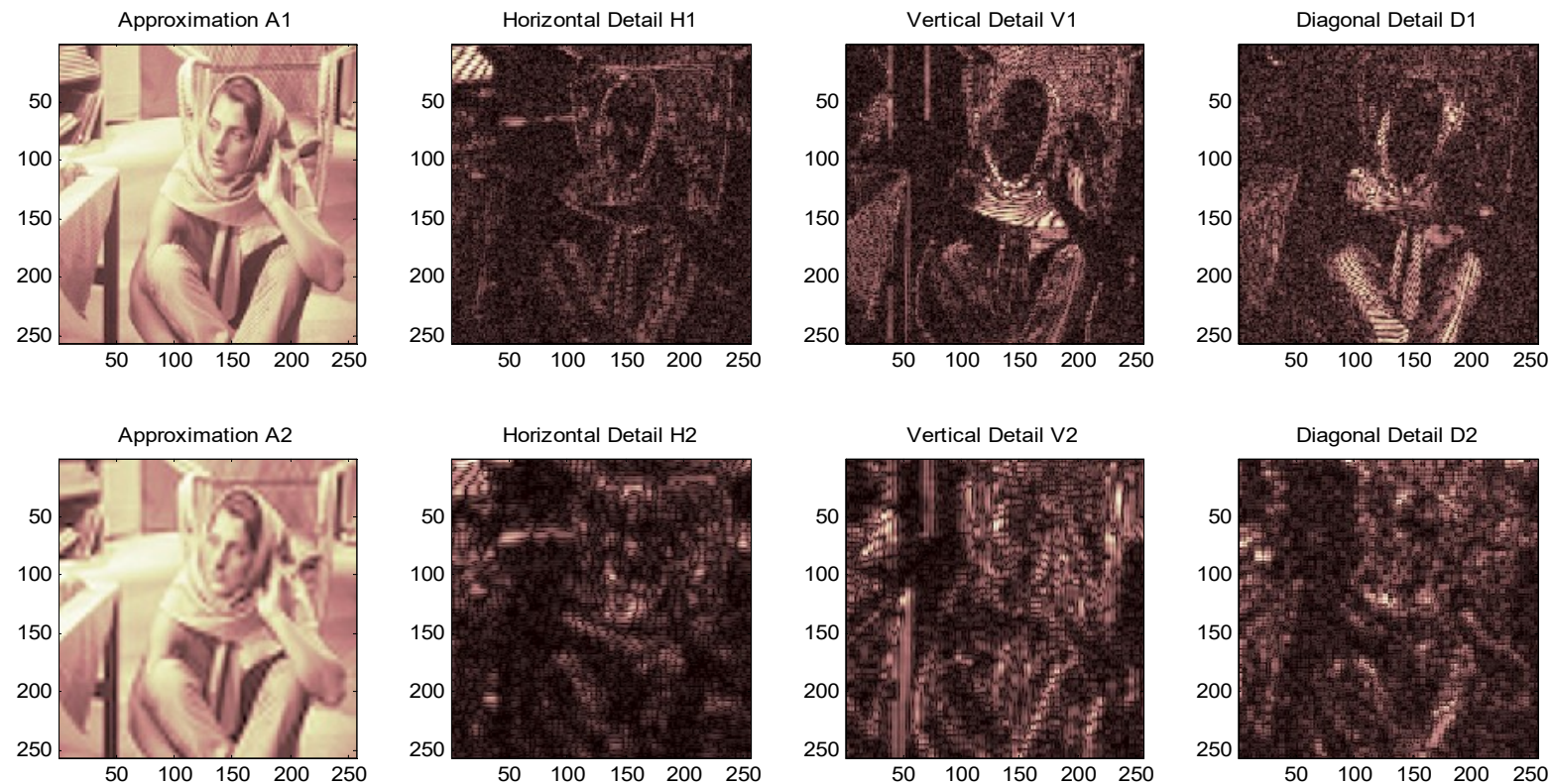
## 4. Discrete Wavelet Transform

- Two-Dimensional Analysis (multiple-level decomposition)



## 4. Discrete Wavelet Transform

- Example of Two-Dimensional Analysis (Extension to Image Denoising, Two-step Decomposition)





## 4. Discrete Wavelet Transform

- Example of Two-Dimensional Analysis (Extension to Image Denoising, Two-step Decomposition): s72Denoise2Da.m





## 4. Discrete Wavelet Transform

- Example of Two-Dimensional Analysis (Extension to Image Denoising, Two-step Decomposition): s73Denoise2Db.m

Noisy Image



Denoised Image



## 4. Discrete Wavelet Transform

- Example of Two-Dimensional Analysis (Extension to Image Denoising, Two-step Decomposition): s74Denoise2Dc.m

