DSA - Seminar 1 – ADT Bag

ADT Bag (also called MultiSet)

- A Bag is similar to a set, but the elements do not have to be unique.
- It is similar to a shopping bag/cart: I can buy multiple pieces of the same product and the order in which I buy the elements is not important.
- The order of the elements is not important
- There are no positions in a Bag:
 - o There are no operations that take a position as parameter or that return a position.
 - The added elements are not neccessarily stored in the order in which they were added (they can be stored in this way, but there is no guarantee, and we should not make any assumptions regarding the order of the elements).
 - o For example:
 - We add to an initially empty Bag the following elements: 1, 3, 2, 6, 2, 5, 2
 - If we print the content of the Bag, the elements can be printed in any order:
 - 1, 2, 2, 2, 3, 6, 5
 - 1, 3, 2, 6, 2, 5, 2
 - 1, 5, 6, 2, 3, 2, 2
 - Etc.

```
Domain: \mathcal{B} = \{b \mid b \text{ is a Bag with elements of the type TElem}\}
```

Interface (set of operations):

pre: $b \in \mathcal{B}$, $e \in TElem$

```
\frac{\text{init(b)}}{\text{pre: true}} \\ \text{post: b} \in \mathcal{B}, \text{ b is an empty Bag}
\frac{\text{add(b, e)}}{\text{pre: b} \in \mathcal{B}, \text{ e} \in \text{TElem}} \\ \text{post: b'} \in \mathcal{B}, \text{ b'} = \text{b} \cup \{\text{e}\} \text{ (Telem } e \text{ is added to the Bag)}
\frac{\text{remove(b, e)}}{\text{pre: b} \in \mathcal{B}, \text{ e} \in \text{TElem}} \\ \text{post: b'} \in \mathcal{B}, \text{ b'} = \text{b} \setminus \{\text{e}\} \text{ (one ocurrence of e was removed from the Bag).}} \\ \text{remove} \leftarrow \begin{cases} \text{true, if an element was removed (size(b') < size(b))} \\ \text{false, if e was not present in b (size(b') = size(b))} \end{cases}
```

```
\mathsf{post} \colon search \leftarrow \begin{cases} \textit{true}, \textit{if } e \in \mathbf{B} \\ \textit{false}, \textit{otherwise} \end{cases}
size(b)
           pre: b \in \mathcal{B}
          post: size \leftarrow the number of elements from b
nrOccurrences(b, e)
          pre: b \in \mathcal{B}, e \in Telem
           post: nrOccurrences \leftarrow the number of occurrences of e in b
destroy(b)
          pre: b \in \mathcal{B}
          post: b was destroyed
iterator(b, i)
          pre: b \in \mathcal{B}
          post: i \in I, i is an iterator over b
ADT Iterator
          - Has access to the interior structure of the Bag and it has a current element from the Bag.
Domain: I = \{i \mid i \text{ is an iterator over b } \in \mathcal{B} \}
Interface:
init(i, b)
           pre: b \in \mathcal{B}
          post: i \in I, i is an iterator over b. i refers to the first element of b, or it is invalid if b is empty
valid(i)
          pre: i \in I
          post: valid \leftarrow \begin{cases} true, if \ the \ current \ element \ from \ i \ is \ a \ valid \ one \\ false, otherwise \end{cases}
first(i)
          pre: i \in I
          post: i' \in I, the current element from i' refers to the first element from the bag or i is invalid if
the bag is empty
next(i)
           pre: i \in I, valid(i)
           post: i' \in I, the current element from i' refers to the next element from the bag b.
          throws: exception if i is not valid
getCurrent(i, e)
```

pre: $i \in I$, valid(i)

post: $e \in TElem$, e is the current element from i throws: exception if i is not valid

Reprezentation:

1.

- A dynamic array of elements, where every element can appear multiple times.
- The iterator will contain a current position from the dynamic array

1	3	2	6	2	5	2

2.

- A dynamic array of unique elements, and for each element its frequency (either two dynamic arrays, or one single dynamic array of pairs).
- The iterator will have a current position and a current frequency for the element.

```
(1,1) (3,1) (2,3) (5,1) (6,1)
```

Python implementation

- Note: lists from Python are actually Dynamic Arrays

Version 1:

```
class Bag:
    def init (self):
       self. elems = []
    def add(self, e):
        self. elems.append(e)
    def remove(self, e):
        if e in self.__elems:
            self. elems.remove(e)
            return True
        return False
    def search(self, e):
       return e in self. elems
    def size(self):
       return len(self. elems)
    def nrOccurrences(self, e):
        count = 0
        for elem in self. elems:
            if elem == e:
               count = count + 1
        return count
```

```
def iterator(self):
        return BagIterator(self)
class BagIterator:
    def __init__(self, bag):
       self. bag = bag
       self._current = 0
    def first(self):
       self.__current = 0
    def valid(self):
        return self. current < self. bag.size()</pre>
    def next(self):
        if self. current == self. bag.size():
           raise ValueError() #in Python e raise, nu throw. ValueError e
eroare built-in in Python, puteti folosi orice
       self.__current += 1
    def getCurrent(self):
        if self.__current == self.__bag.size():
           raise ValueError()
        return self. bag. Bag elems[self. current]
```

Main program:

```
from Bag import Bag, BagIterator
def createIntBag():
    intBag = Bag()
    intBag.add(6)
    intBag.add(11)
    intBag.add(77)
    intBag.add(7)
    intBag.add(4)
    intBag.add(6)
    intBag.add(77)
    intBag.add(6)
    return intBag
def createStringBag():
    stringBag = Bag()
    stringBag.add("data")
    stringBag.add("structure")
    stringBag.add("and")
    stringBag.add("algorithms")
    stringBag.add("data")
    stringBag.add("data")
    stringBag.add("algorithms")
    return stringBag
def printBag(bag):
    it = bag.iterator()
    while it.valid():
        print(it.getCurrent())
        it.next()
    print("Over. Let's start again")
    it.first()
    while it.valid():
        print(it.getCurrent())
        it.next()
def main():
    b1 = createIntBag()
    printBag(b1)
    print("Number of occurrences for 77: ", b1.nrOccurrences(77))
    b2 = createStringBag()
    printBag(b2)
    print("Number of occurrences for data: ", b2.nrOccurrences("data"))
main()
```

Version 2:

```
class BagF:
    def __init__(self):
        self.\underline{\phantom{a}}elems = []
        self._ freq = []
    def add(self, e):
        found = False
        for i in range(len(self.__elems)):
             if self.__elems[i] == e:
                 self.__freq[i] += 1
                 found = True
        if not found:
             self.__elems.append(e)
             self. freq.append(1)
    def remove(self, e):
        for i in range(len(self. elems)):
             if self. elems[i] == e:
                 self. freq[i] -= 1
                 if self. freq[i] == 0:
                     del self.__elems[i]
del self.__freq[i]
                 return True
        return False
    def search(self, e):
        return e in self. elems
    def size(self):
        contor = 0
        for fr in self.__freq:
             contor += fr
        return contor
    def nrOccurrences(self, e):
        for i in range(len(self. elems)):
             if e == self. elems[i]:
                 return self. freq[i]
        return 0
    def iterator(self):
        return BagFIterator(self)
class BagFIterator:
    def __init__(self, bag):
    self.__bag = bag
        self.\__currentE = 0
        self.__currentFr = 1
    def first(self):
        self. currentE = 0
```

```
def valid(self):
    return self.__currentE < len(self.__bag._BagF__elems)

def next(self):
    if self.__currentE == len(self.__bag._BagF__elems):
        raise ValueError()
    self.__currentFr += 1
    if self.__currentFr > self.__bag._BagF__freq[self.__currentE]:
        self.__currentFr = 1

def getCurrent(self):
    if self.__currentE == len(self.__bag._BagF__elems):
        raise ValueError()
    return self._bag._BagF__elems[self._currentE]
```