Software Systems Verification and Validation



Vescan Andreea, PHD, Assoc. Prof.



Faculty of Mathematics and Computer Science Babeş-Bolyai University

2023-2024





Software Systems Verification and Validation

"Tell me and I forget, teach me and I may remember, involve me and I learn."

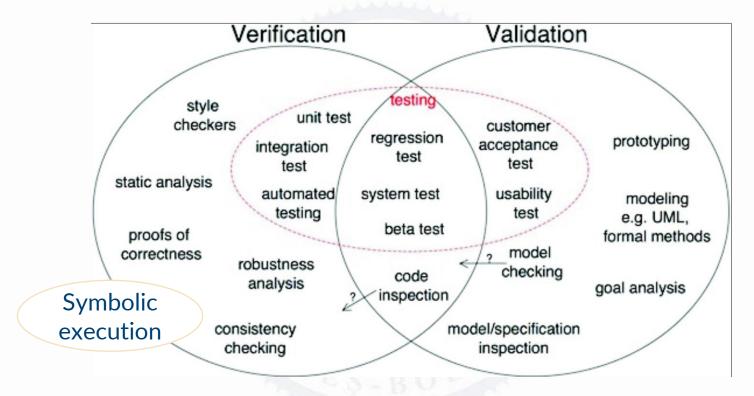
(Benjamin Franklin)

(Next)/Today Lecture

Correctness



What we will learn!



• http://www.easterbrook.ca/steve/2010/11/the-difference-between-verification-and-validation/

Outline

- Correctness
- Floyd's Method -Inductive assertions, Partial correctness, Termination
- Hoare Logic, Semantics of Hoare triples, Partial correctness, Total correctness
- Dijkstra's Language, Guarded commands, Nondeterminacy, Formal Derivation of Programs
- Developing correct programs from specification, Refinement, Rules of Refinement, Examples
- Static analysis, JML- Java Modeling Language, ESC/Java2- Extended Static Checker for Java
- Questions

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Program verification methods - Correctness

- Lecture 1 Verification and Validation
 - Verification/Validation
 - reviews products to ensure their quality → correctness
 - · static and dynamic analysis techniques
 - A correct program is one that does exactly what it is intended to do, no more and no less.
 - A formally correct program is one whose correctness can be proved mathematically.
 - This requires a language for specifying precisely what the program is intended to do.
 - · Specification languages are based in mathematical logic.
 - Until recently, correctness has been an academic exercise. Now it is a key element of critical software systems.
- Program verification correctness
 - 1. proof-based, computer-assisted, program-verification approach, mainly used for programs which we expect to terminate and produce a result
 - 2. model-based, automatic, property-verification approach, mainly used for concurrent, reactive systems (originally used in a post-development stage) model checking (Lecture 9)
 - 3. Developing correct algorithms from specification (Carroll Morgan, "Programming from Specification)

Correctness-by-Construction.

Originally intended as a mere means of programming algorithms that are correct by construction - -Dijkstra (1968), Hoare (1971),

the approach found its way into commercial development processes of complex systems - Hall (2002), Hall and Chapman (2002)

2012, The Correctness-by-Construction Approach to Programming, Authors: Kourie, Derrick G., Watson, Bruce W.

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2016, Correctness-by-Construction and Post-hoc Verification: Friends or Foes?, Maurice H. ter Beek1(B), Reiner H"ahnle2, and Ina Schaefer3

2023, Automated Software Engineering Conference, The 5th International Workshop on Automated and verifiable Software system DEvelopment (ASYDE)

Topic: Correct-by-construction software development

(https://conf.researchr.org/track/ase-2023/ase-2023--workshop--asyde#the-5th-international-workshop-on-automated-and-verifiable-software-system-development-aside)

- Correctness Tools
 - Theorem provers (PVS), Modeling languages (UML and OCL), Specification languages (JML), Programming language support (Eiffel, Java, Spark/Ada), Specification Methodology (Design by contract)
- · Methods for prooving program correctness
 - Floyd's Method Inductive assertions
 - · Hoare Semantics of Hoare triples

4/17/2024 Suit A Lawrence Counted to

Aplicability

- Partial correctness of the program
- Termination of the program
- Total correctness = Partial correctness + Termination of the program

Uses

- The condition satisfied by the initial values of the program.
- The condition to be satisfied by the output of the program.
- Source code of the program.

Method:

- Cut the loops
- Find an appropriate set of inductive assertions.
- Construct the verification/termination conditions.
- **Theorem**: If all verification conditions are true, then the program is partially correct, i.e., whenever it terminates the result is correct.
- Remark. The method is useful when it is combined with termination.



Robert W Floyd (June 8, 1936 -September 25, 2001)

Partial correctness - steps

- Cutting points are chosen inside the algorithm
 - 1 point at the beginning of the algorithm, 1 point at the end;
 - 2 At least 1 point for each loop statement
- For each cutting point an assertion (invariant predicate) is chosen.
 - 1 Entry point $\varphi(X)$;
 - 2 Ending point $\psi(X, Z)$.
- Construction of the verification conditions
 - Path from *i* to $j \alpha$;
 - P_i and P_i are assertions in i and j;
 - $R_{\alpha}(X,Y)$ predicate that gives the condition for path α ;
 - $r_{\alpha}(X,Y)$ function that gives the transformations of the variables Y from path α ;
- Theorem: If all the verification conditions are true then *P* is partial correct.



Robert W Floyd (June 8, 1936 -September 25, 2001)

Partial correctness - example

```
• Algorithm for z=x^y z:=1;\ u:=x;\ v:=y; A: \varphi(X)::=(v>0 \land (y\geq 0)) While (v>0) execute B: \eta(X,Y)::=z*u^v=x^y If (v \text{ is even}) then u:=u*u;\ v:=v/2; else v:=v-1;\ z:=z*u; endIf endWhile endAlg; C: \psi(X,Z)::=z=x^y
```



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Termination- steps

- Cut the loops and find "good" inductive assertions.
- Choose a well-formed set M (i.e., an ordered set without infinite strictly decreasing sequences)
- To demonstrate that some termination conditions hold: passing from one cutting point to another the values of some functions in the well-ordered set decrease.
- In point i a function is chosen $u_i: D_X \times D_Y \to M$ and the termination condition on α is: $\forall X \forall Y (\varphi(X) \land R_{\alpha}(X,Y) \to (u_i(X,Y) > u_i(X,r_{\alpha}(X,Y))))$.
- **Remark**. If partial correctness was demonstrated then the termination condition can be: $\forall X \forall Y (P_i(X) \land R_{\alpha}(X,Y) \rightarrow (u_i(X,Y) > u_i(X,r_{\alpha}(X,Y))))$.
- Theorem: If all the termination conditions hold then the program *P* terminates.



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Termination- example

```
• Algorithm for z=x^y z:=1;\ u:=x;\ v:=y; A: \varphi(X)::=(v>0 \land (y\geq 0)) While (v>0) execute B: \eta(X,Y)::=z*u^v=x^y If (v \text{ is even}) then u:=u*u;\ v:=v/2; else v:=v-1;\ z:=z*u; endIf endWhile endAlg; C: \psi(X,Z)::=z=x^y
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Questions

- The meaning of a statement is described by a triple
 - $\{\varphi\}$ P $\{\psi\}$, where φ is called the precondition and ψ is called the postcondition.

{P} S {Q}

"when started in a state satisfying P, any terminating execution of S ends in a state satisfying Q"

• If P does not terminate, we make no guarantees.

- Partial correctness
 - $\models_{par} \{\varphi\}P\{\psi\}$
 - only if P actually terminates.
- Total correctness
 - $\models_{tot} \{\varphi\}P\{\psi\}$
 - the program P is guaranteed to terminate.



The Grand Verification Challenge Hoare 2003

Develop a compiler which verifies that the program is correct

https://vimeo.com/39256698

Charles Antony Richard Hoare (11 January 1934, Colombo, Sri Lanka)



An Advanced Study Institute of the NATO Security Through Science Committee and the Institut få 1/2 Informatik

the Institut fA¹/₄r Informatik, Technische UniversitĤt MÄ¹/₄nchen, Germany,

Software System Reliability and Security

August 1 to August 13 2006

M. Broy (director)
O. Kupferman (director)
C.A.R. Hoare (co-director)
A. Pnueli (co-director)

Katharina Spies (secretary

The Summer School is also substantially supported by the DAAD under the program "Deutsche Sommerakademie 2006", and the town and the county of Marktoberdorf





Partial correctness



- The Grand Verification Challenge Hoare 2003
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(11 January 1934, Color

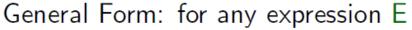
Rules

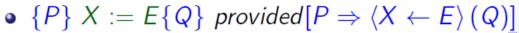
- Assignment
- Sequencing
- Conditional
- Loop

Charles Antony Richard Hoare (11 January 1934, Colombo, Sri Lanka)

Partial correctness

Assignment





- Consider the triple $\{P\}X := Y + 2\{Q\}$
 - Given predicate Q, for what predicate P does this hold?
 - for any P such that $[P \Rightarrow \langle X \leftarrow Y + 2 \rangle (Q)]$
- Examples
 - $\{P_0\} X := Y + 2 \{X \le Y + 2\}$ $P_0 \equiv true$
 - $\{P_1\} X := Y + 2 \{X < 0\}$ $P_1 \equiv (Y + 2 < 0)$
 - $\{P_2\} X := Y + 2 \{Y < 0\}$ $P_2 \equiv (Y < 0)$
 - $\{P_3\} \ X := X + 2 \ \{X \text{ is even}\}\$ $P_3 \equiv (X \text{ is even})$



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Partial correctness

Sequencing

We can conclude

 $\{P\}$ S; $T\{Q\}$ if we can find a predicate R such that $\{P\}$ S $\{R\}$ and $\{R\}$ $T\{Q\}$

Examples

- $\{P_0\} X := 2 * X; X := X + 1\{X > 0\}$ $P_0 \equiv (2 * X + 1 > 0)]$
- $\{P_1\} X := Y; Y := 3 \{X + Y < 5\}$ $\{P_1 \equiv (Y + 3 < 5)]$



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Partial correctness

Conditional

• We can conclude $\{P\}$ IF (C) THEN S ELSE T END $\{Q\}$ provided we can show $\{P \land C\}$ S $\{Q\}$ and $\{P \land \neg C\}$ T $\{Q\}$



```
• \{?\} \{((x > y) \Rightarrow Q_0) \land ((x \le y) \Rightarrow Q_1)\}

IF (x > y) THEN Q_0: \{(m|x - y) \land (m|y)\}

x := x - y

ELSE Q_1: \{(m|x) \land (m|y - x)\}

y := y - x

END

Q: \{(m|x) \land (m|y)\}

• So our final proof obligations are
```

 $[(x > y) \Rightarrow (m|x - y) \land (m|y) \text{ and}$ $[(x < y) \Rightarrow (m|x) \land (m|y - x)]$



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4/17/2024

4 m b 4 A b

Partial correctness

Loop

- How can we conclude
 {P} WHILE (G) DO S END {Q}
 At the end of the loop (assuming it terminates), we know ¬G
 But in general we dont know how often S is executed...
- Suppose we have a predicate J that is preserved by S $\{J\}S\{J\}$ such a J is called a loop invariant Then, at the end of the loop, we can conclude $J \land \neg G$ To establish the postcondition, we need J such that $[J \land \neg G \Rightarrow Q]$
- We can conclude
 {P} WHILE (G) DO S END {Q}
 provided we can find a loop invariant J such that

$$[P \Rightarrow J]$$

$$[J \land \neg G \Rightarrow Q]$$

$$\{G \land J\}S\{J\}$$

J holds at loop entry
J establishes Q at loop exit
J is preserved by each iteration



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Develop a compiler which verifies that the program is correct

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Exponentiation using multiplication

•
$$\{(A > 0) \land (B \ge 0)\}\ S\ \{R = A^B\}$$

```
\{(A > 0) \land (B \ge 0)\}

R := ?; b := 0 R := 1

WHILE (b \ne B) DO J : R = A^b

R := ?; R := R * A;

b := b + 1

END

\{R = A^B\}
```

- The meaning of a statement is described by a triple
 - $\{\varphi\}$ P $\{\psi\}$, where φ is called the precondition and ψ is called the postcondition.



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{P} S {Q}

"when started in a state satisfying P, any terminating execution of S ends in a state satisfying Q"

- If P does not terminate, we make no guarantees.
 - Partial correctness
 - $\models_{par} \{\varphi\}P\{\psi\}$
 - only if P actually terminates.
 - Total correctness
 - $\models_{tot} \{\varphi\}P\{\psi\}$
 - the program P is guaranteed to terminate.
- The "total correctness" interpretation also requires termination
 - "when started in a state satisfying P, any execution of S must terminate in a state satisfying Q "

Termination

Rules

- Assignment
- Sequencing
- Conditional
- Loop
 - Assignment $\{P\} \ X := E \ \{Q\} \ provided \ [P \Rightarrow \langle X \leftarrow E \rangle(Q)]$
 - Sequencing $\{P\}$ S; $T\{Q\}$ provided $\{P\}$ S $\{R\}$ and $\{R\}$ T $\{Q\}$ for some R
 - Conditional $\{P\} \ IF \ (G) \ THEN \ S \ ELSE \ T \ END \ \{Q\} \ provided \\ \{P \land G\} \ S \ \{Q\} \ and \ \{P \land \neg G\} \ T\{Q\}$
 - Note: Same as the rules for partial correctness!



The Grand Verification Challenge Hoare 2003

Develop a compiler which verifies that the program is correct

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- Total correctness rule for loops
- Consider{P} WHILE (G) DO S END {Q}
- How do we show that the loop terminates?
- One method find an integer expression V such that the value of V is nonnegative (that is $V \ge 0$), and the value of V (strictly) decreases in every iteration that is, $\{V = K\}$ S $\{V < K\}$

• Such an expression is called a "loop variant"



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Exponentiation using multiplication

```
• \{(A > 0) \land (B \ge 0)\}\ S \{R = A^B\}
```

• Recall loop invariant $J: R = A^b \land (B \ge b);$ $\{(A > 0) \land (B \ge 0)\}$ R := 1; b := 0WHILE $(b \ne B)$ DO $J: R = A^b \land (B \ge b);$ R := R * A; b := b + 1END $\{R = A^B\}$

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Questions

Guarded command

- "guarded command" a statement list prefixed by a boolean expression: only when this boolean expression is initially true, is the statement list eligible for execution
- ullet < guarded command >::=< guard >o< guarded list >
- < guard >::=< boolean expression >
- \bullet < guarded list >::=< statement > $\{$; < statement > $\}$
- < guarded command set >::= < guarded command > $\{\Box < guarded \ command > \}$
- \bullet < alternative construct >::= **if** < guarded command set > **fi**
- ullet < repetitive construct >::= do < guarded command set > do
- < statement >::=< alternative construct > |
 < repetitive construct > | "other statements"



Edsger Wybe Dijkstra (May 11, 1930 - August 6, 2002)

Nondeterminacy

- Example 1 if $x \ge y \to m := x$ $\Box y \ge x \to m := y$ fi
- Example 2 compute k s.t. for fixed value n and fixed function f(i) (defined for $0 \le i < n$), k will eventually satisfy $0 \le k < n$ and $(\forall i : 0 \le i < n : f(k) \ge f(i))$.

$$k := 0; j := 1;$$

do $j \neq n \rightarrow \mathbf{if} \ f(j) \leq f(k) \rightarrow j := j + 1$
 $\Box f(j) \geq f(k) \rightarrow k := j; \ j := j + 1$
fi

od



Edsger Wybe Dijkstra (May 11, 1930 - August 6, 2002)

Weakest pre-conditions

- Hoare introduced sufficient pre-conditions such that the mechanism will not produce the wrong result but may fail to terminate.
- Dijkstra introduced necessary and sufficient preconditions such that the mechanism are guaranteed to produce the right result.
 - = weakest pre-conditions
- wp(S, R), where S denotes a statement list, R some condition on the state of the system.
- wp called a "predicate transformer" because it associates a pre-condition to any post-condition R.



Edsger Wybe Dijkstra (May 11, 1930 - August 6, 2002)

Properties of wp

- 1 Law of the Excluded Miracle For any S, for all states: wp(S, F) = F
- ② For any S and any two post-conditions, such that for all states $P \Rightarrow Q$, for all states:
 - $wp(S, P) \Rightarrow wp(S, Q)$
- To any S and any two post-conditions P and Q, for all states: wp(S, P) and wp(S, Q) = wp(S, P) and wp(S, Q)
- For any deterministic S and any post-conditions P and Q, for all states:

$$(wp(S, P) \text{ or } wp(S, Q)) \Rightarrow wp(S, P \text{ or } Q)$$



Edsger Wybe Dijkstra (May 11, 1930 - August 6, 2002)

Assignment and concatenation operator

Assignment

The semantics of x := E are given by: $wp("x := E", R) = R_E^x$, R_E^x -denotes a copy of the predicate defining R in which each occurrence of the variable x is replaced by E.

• Concatenation operator; The semantics of the; operator are given by: wp("S1; S2", R) = wp(S1, wp(S2, R)).



Edsger Wybe Dijkstra (May 11, 1930 - August 6, 2002)

The Alternative Construct

- Let IF denote: **if** $B_1 o SL_1 \square ... \square B_n o SL_n$ **fi** Let BB denote: $(\exists i : 1 \le i \le n : B_i)$, then, by definition $wp(IF, R) = (BB \text{ and } (\forall i : 1 \le i \le n : B_i \Rightarrow wp(SL_i, R)))$.
- Theorem 1 From $(\forall i: 1 \leq i \leq n: (Q \text{ and } B_i) \Rightarrow wp(SL_i, R)$ for all states we can conclude that $(Q \text{ and } BB) \Rightarrow wp(IF, R)$ holds for all states.)
- Let t denote some integer function, and wdec(S, t)
- Theorem 2 From $(\forall i : 1 \le i \le n : (Q \text{ and } B_i) \Rightarrow wdec(SL_i, t))$ for all states we can conclude that $(Q \text{ and } BB) \Rightarrow wdec(IF, t)$ hold for all states.
- By definition, $wdec(S, t) = (tmin(X) \le t(X) 1) = (tmin(X) < t(X)).$



Edsger Wybe Dijkstra (May 11, 1930 - August 6, 2002)

The Alternative Construct - example

- The formal requirements for performing m := max(x, y) is: $R : (m = x \text{ or } m = y) \text{ and } m \ge x \text{ and } m \ge y.$
- Assignment m := x for m = x? $wp("m := x", R) = (x = x \text{ or } x = y) \text{ and } x \ge x \text{ and } x \ge y = x \ge y$
- Theorem 1: $\mathbf{if} x > y \rightarrow m := x \mathbf{fi}$
- But $B \neq T$, so we weakening BB means looking for alternatives which might introduce new guards.
- Alternative: "m := y" that introduces the new guard $wp("m" := y, R) = y \ge x$ if $x \ge y \to m := x$ $\Box y \ge x \to m := y$



Edsger Wybe Dijkstra (May 11, 1930 - August 6, 2002)

The Repetitive Construct

- Let DO denote: $\mathbf{do}B_1 \to SL_1 \square ... \square B_n \to SL_n \mathbf{do}$ Let $H_0 = (R \text{ and non } BB)$ and for k > 0, $H_k(R) = (wp(IF, H_{k-1}(R)))$ or $H_0(R)$ then, by definition: $wp(DO, R) = (\exists k : k \ge 0 : H_k(R))$.
- Theorem 3
 If we have all the states $(P \text{ and } BB) \Rightarrow (wp(IF, P) \text{ and } wdec(IF, t) \text{ and } t \ge 0)$ we can conclude that we have for all states $P \Rightarrow wp(DO, P \text{ and non } BB)$
- T is the condition satisfied by all states, and wp(S, T) is the weakest pre-condition guaranteeing proper termination of S.
- Theorem 4 From $(P \text{ and } BB) \Rightarrow wp(IF, P)$ for all states, we can conclude that we have for all states $(P \text{ and } wp(DO, T) \Rightarrow wp(DO, P \text{ and non } BB))$



Edsger Wybe Dijkstra (May 11, 1930 - August 6, 2002)

The Repetitive Construct - example

- The greatest common divisor: x = gcd(X, Y)
- Choose an invariant relation and variant function.
 establish the relation P to be kept invariant
 do "decrease t as long as possible under variance of P" od
- invariant relation (established by x := X; y := Y): P : gcd(X, Y) = gcd(x, y) and x > 0 and y > 0
- $(P \text{ and } B) \Rightarrow wp("x, y : E1, E2", P))$ = (gcd(X, Y) = gcd(E1, E2) and E1 > 0 and E2 > 0).
 - gcd(X, Y) = gcd(E1, E2) is implied by P
 - invariant for (x, y): wp("x := x y, P) = (gcd(X, Y) = gcd(x y, y)and x y > 0 and y > 0), and guard x > y
 - decrease of the variant function t = x + y $wp("x := x - y", t \le t_0) = (x \le t_0)$ tmin = x, wdec("x := x - y", t) = (x < x + y) = y > 0



Edsger Wybe Dijkstra (May 11, 1930 - August 6, 2002)

- x := X; y := Y**do** $x > y \to x := x - y$ **od**
- But P and BB are not allowed to conclude $x = \gcd(X, Y)$ the alternative y := y x requires a guard y > x
- x:=X; y:=Y **do** $x > y \rightarrow x:=x-y$ $\Box y > x \rightarrow y := y - x$ **od**

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(https://conf.researchr.org/track/ase-2023/ase-2023--workshop--asyde#the-5th-international-workshop-on-automated-and-verifiable-software-system-development-aside)

Static analysis, JML- Java Modeling Language, ESC/Java2- Extended Static Checker for Java

Questions

Developing correct programs from specification[Mor98]

Refinement

• Input data: X $\varphi(X)$ Output data: Z $\psi(X, Z)$

- Abstract program
 - $Z: [\varphi, \psi]$
- Refinement

$$P_1 \prec P_2 \prec ... \prec P_{n-1} \prec P_n$$

- Rules of refinement
 - Assignment rule
 - Sequential composition rule
 - Alternation rule
 - Iteration rule

Carroll Morgan

https://my.c se.unsw.edu. au/staff/staf f_details.php ?ID=carrollm

Developing correct programs from specification[Mor98]

Rules of Refinement

- Assignment rule: $[\varphi(v/e), \psi] \prec v := e$
- Sequential composition rule $(\gamma middlepredicate)$ $[\eta_1, \eta_2] \prec [\eta_1, \gamma]$ $[\gamma, \eta_2]$
- Alternation rule, $G = g_1 \vee g_2 \vee ... \vee g_n$ $[\eta_1, \eta_2] \prec$ if $g_1 \to [\eta_1 \wedge g_1, \eta_2]$ $\Box g_2 \to [\eta_1 \wedge g_2, \eta_2]$ \vdots $\Box g_n \to [\eta_1 \wedge g_n, \eta_2]$

```
• Iteration rule G = g_1 \vee g_2 \vee ... \vee g_n
[\eta, \eta \wedge \neg G] \prec
\mathbf{do} \ g_1 \to [\eta \wedge g_1, \eta \wedge TC]
\Box g_2 \to [\eta \wedge g_2, \eta \wedge TC]
\vdots
\Box g_n \to [\eta \wedge g_n, \eta \wedge TC]
\mathbf{do}
```

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 - 2015, Experience with correctness-by-construction, B.W. Watson a, D.G. Kourie b, L. Cleophas b,*
 - 2016, Correctness-by-Construction and Post-hoc Verification: Friends or Foes?, Maurice H. ter Beek1(B), Reiner H"ahnle2, and Ina Schaefer3

Correctness Tools

- Theorem provers (PVS), Modeling languages (UML and OCL), Specification languages (JML), Programming language support (Eiffel, Java, Spark/Ada), Specification Methodology (Design by contract)
- · Methods for prooving program correctness
 - Floyd's Method Inductive assertions
 - Hoare Semantics of Hoare triples
 - · Dijkstra's Language- Guarded commands, Nondeterminacy and Formal Derivation of Programs

Program verification methods - Correctness

- Software engineering problem: building/maintaining correct systems.
 - How?
 - Specification
 - Tools
- Formal Methods in Software Engineering
 - Formal languages guarantee
 - Precision (no ambiguity)
 - Certainty (modeling errors)
 - · Automation (automatic verification tools).
- Things to do:
 - 1) make a formal model
 - 2) specify properties for the model
 - 3) **verify/check** the properties

- Formal methods and JML (Java Modeling Language):
 - 1) formal model is Java programming language
 - 2) the properties are specified in JML
 - 3) Properties may be
 - Tested using jmlrac
 - Checked using ESC2Java

What is JML?

- Gary T. Leavens's JML group at the University of Central Florida
- http://www.eecs.ucf.edu/~leavens/JML//index.shtml
- a behavioral interface specification language
- used to specify the behavior of Java modules
- combines
 - design by contract approach
 - the model-based specification approach
 - some elements of the refinement calculus

Tools for using JML

- Runtime assertion checkers (e.g. jmlc/jmlrac)
- Static checkers (ESC2Java)

- Test generation (e.g. jmlunit)
- Formal verification tools (e.g. KeY)
- Design tools (e.g. AutoJML)

Tools for JML

Runtime assertion checking with jmlc/jmlrac

- Special compiler inserts runtime tests for all JML assertions. Any assertion violation results in a special exception.
- · checks specs at run-time
- only tests correctness of specs.
- Find violations at runtime.

JML web page

 http://www.eecs.ucf.edu/~lea vens/JML//index.shtml

Extended static checking with ESC/Java

- Automatically tries to prove simple JML assertions at compile time.
- checks specs at compile-time
- proves correctness of specs.
- Warn about likely runtime exceptions and violations.

ESC/Java2 web page
http://www.kindsoftware.com/products/opensource/ESCJava2/download.html

Design by contract

Contract?

Method contract

Precondition

Specifies "caller's responsibility"

- Constraints on parameter values and target object's state.
- Valid object's states, in which a method can be called. *Intuitively*
- Expression that must hold at the entry to the method.

Postcondition

Specifies "implementation's responsibility"

- Constraints on the method's return value and side effects.
- Relation between initial and final state of the method. *Intuitively*
- Expression that must hold at the exit from the method.

Class contract

Invariant

- Specifies caller's responsibility at the entry to a method and implementation's responsibility at the exit from a method.
- Valid states of class instances (values of fields).

Intuitively

• Expression that must hold at the entry and exit of each method in the class.

Tools for JML

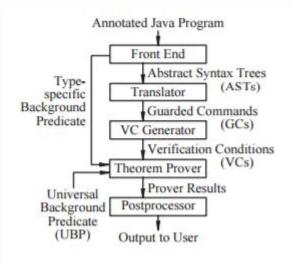
Runtime assertion checking with jmlc/jmlrac

- Special compiler inserts runtime tests for all JML assertions. Any assertion violation results in a special exception.
- checks specs at run-time
- only tests correctness of specs.
- Find violations at runtime.

jmlc and jmlrac - by example

- Compile and Run
- Compile
- jmlc FileName.java
- Run
- jmlrac FileName listOfParam
- Demo 01: Factorial
- Demo02: Integer sqrt

Faculty of Mathematics and Computer Science Babeș-Bolyai University



- Unsound?
- Incomplete?

Tools for JML

Extended static checking with ESC/Java

Automatically tries to prove simple JML assertions at compile time.

- ESC/Java2 by example
- Run
- escj FileName.java
- Demo 01: Fast exponentiation
- Demo 02: MyArray
- Demo 03: MySet

- checks specs at compile-time
- proves correctness of specs
- Warn about likely runtime exceptions and violations.

Program verification methods - Correctness

- Lecture 1 Verification and Validation
 - Verification/Validation
 - reviews products to ensure their quality → correctness
 - static and dynamic analysis techniques
 - A correct program is one that does exactly what it is intended to do, no more and no less.
 - A formally correct program is one whose correctness can be proved mathematically.
 - This requires a language for specifying precisely what the program is intended to do.
 - Specification languages are based in mathematical logic.
 - Until recently, correctness has been an academic exercise. Now it is a key element of critical software systems.
- Program verification correctness
 - 1. proof-based, computer-assisted, program-verification approach, mainly used for programs which we expect to terminate and produce a result
 - 2. model-based, automatic, property-verification approach, mainly used for concurrent, reactive systems (originally used in a post-development stage) model checking (Lecture 9)
 - 3. Developing correct algorithms from specification (Carroll Morgan, "Programming from Specification)

Correctness-by-Construction.

Originally intended as a mere means of programming algorithms that are correct by construction - -Dijkstra (1968), Hoare (1971),

the approach found its way into commercial development processes of complex systems - Hall (2002), Hall and Chapman (2002)

2012, The Correctness-by-Construction Approach to Programming, Authors: Kourie, Derrick G., Watson, Bruce W.

2015, Experience with correctness-by-construction, B.W. Watson a, D.G. Kourie b, L. Cleophas b,*

2016, Correctness-by-Construction and Post-hoc Verification: Friends or Foes?, Maurice H. ter Beek1(B), Reiner H"ahnle2, and Ina Schaefer3

2023, Automated Software Engineering Conference, The 5th International Workshop on Automated and verifiable Software system DEvelopment (ASYDE)

Topic: Correct-by-construction software development

(https://conf.researchr.org/track/ase-2023/ase-2023--workshop--asyde#the-5th-international-workshop-on-automated-and-verifiable-software-system-development-aside)

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 - Theorem provers (PVS), Modeling languages (UML and OCL), Specification languages (JML), Programming language support (Eiffel, Java, Spark/Ada), Specification Methodology (Design by contract)
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 4/17/2024

 Control of American Countries

 Control of

Correctness by Construction How Can We Build Better

Software, Date: May 31, 2023

Correct-by-construction

SPEAKER Ina Schaefer, Professor of Software Engineering,

Karlsruhe Institute of Technology (KIT), Germany

https://www.youtube.com/watch?v=5Nno9lSggPo



Floyd, Dijkstra, Hoare (25XP)

- Robert Floyd OR Edsger Wybe Dijkstra OR Charles Antony Richard Hoare
- 1 page A4 information (electronic format and printed format)
 - short bio
 - profession
 - Institution
 - known by...
 - awards
 - interesting facts
- Feel free to select a format: plain text, mindmap, other
- Delivery:
 - Today, after 10 minutes
 - 3-4 students per team

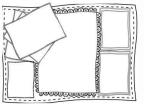
Maindmap



In-class

Doodle map





Next Lecture

Fundmore Invited Lecture

QA&QC DURING THE SOFTWARE DEVELOPMENT LIFE CYCLE

Presenters: Monday

Roxana Soporan 22 April 2024, 8-10 am

Andra Banto Room: 2/I (Main Building)

Outline



- Correctness
- Floyd's Method -Inductive assertions, Partial correctness, Termination
- Hoare Logic, Semantics of Hoare triples, Partial correctness, Total correctness
- Dijkstra's Language, Guarded commands, Nondeterminacy, Formal Derivation of Programs
- Developing correct programs from specification, Refinement, Rules of Refinement, Examples
- Static analysis, JML- Java Modeling Language, ESC/Java2- Extended Static Checker for Java

Questions

References

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- [Hoa69] C. A. R. Hoare, An axiomatic basis for computer programming, *Commun. ACM*, 12(10):576–580, 1969.
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- [Fre10] M. Frentiu, Verificarea si validarea sistemelor soft, Presa Universitara Clujeana, 2010.
- [Mor98] C. Morgan, Programming from Specifications, Prentice Hall International Series in Computing Science, 1998





Software Systems Verification and Validation

"Tell me and I forget, teach me and I may remember, involve me and I learn."

(Benjamin Franklin)