

$$f(x_1, x_2, x_3) = \overline{x_1} x_2 \overline{x_3} \vee x_1 \overline{x_2} \overline{x_3} \vee \overline{x_1} x_2 x_3 \vee x_1 \overline{x_2} x_3 =$$

$$= m_2 \vee m_4 \vee m_6 \vee m_3 \vee m_5$$

descending order $\Rightarrow Sf = \left\{ \overset{m_4}{(1, 0, 0)}, \overset{m_2}{(0, 1, 0)}, \overset{m_6}{(1, 1, 0)}, \overset{m_5}{(1, 0, 1)}, \overset{m_3}{(0, 1, 1)} \right\}$

Group

I

$x_1 \quad x_2 \quad x_3$

1 0 0 m_4

0 1 0 m_2

II

1 1 0 m_6

1 0 1 m_5

0 1 1 m_3

I + II

1 - 0 $m_4 \vee m_6 = x_1 \overline{x_3} = max_1$

0 1 - $m_2 \vee m_3 = x_1 x_2 = max_2$

1 0 - $m_4 \vee m_5 = x_1 \overline{x_2} = max_3$

- 1 0 $m_2 \vee m_6 = x_2 \overline{x_3} = max_4$

$$M(f) = \{ \text{max}_1, \text{max}_2, \text{max}_3, \text{max}_4 \} =$$

$$= \{ x_1 \bar{x}_3, \bar{x}_1 x_2, x_1 \bar{x}_2, x_2 \bar{x}_3 \}$$

max terms monoms		max1	max2	max3	max4
min terms					
m_4		*		*	
m_2			*		*
m_6		*			*
m_5				*	
m_3			*		

$$C(f) = \{ \text{max}_2, \text{max}_3 \} = \{ \bar{x}_1 x_2, x_1 \bar{x}_2 \}$$

$$M(f) = \{ \text{max}_1, \text{max}_2, \text{max}_3, \text{max}_4 \} = \{ x_1 \bar{x}_3, \bar{x}_1 x_2, x_1 \bar{x}_2, x_2 \bar{x}_3 \}$$

$M(f) \neq C(f)$ and $C(f) \neq 0 \Rightarrow$ the second case of simplification alg.

$$g(x_1, x_2, x_3) \stackrel{\text{not}}{=} \text{max}_2 \vee \text{max}_3 = \bar{x}_1 x_2 \vee x_1 \bar{x}_2$$

Choose $h(x_1, x_2, x_3)$ as simple as possible \rightarrow

to cover m_6 uncovered by $g(x_1, x_2, x_3)$

Can choose m_{ac_1} or $m_{ac_4} \Rightarrow$ two simplified forms of f are obtained

$$\begin{aligned} f_1^s(x_1, x_2, x_3) &= g(x_1, x_2, x_3) \vee h(x_1, x_2, x_3) = \\ &= m_{ac_2} \vee m_{ac_3} \vee m_{ac_4} = \bar{x}_1 x_2 \vee \bar{x}_1 \bar{x}_2 \bar{x}_3 \end{aligned}$$

$$f_2^s(x_1, x_2, x_3) = - \quad - \quad - = \bar{x}_1 x_2 \vee x_1 \bar{x}_2 \vee x_2 \bar{x}_3$$