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Digital System Design

Clip Lecture series

Spring_2020



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Jiangxi University of Science and Technology

Analysis of Sequential circuits

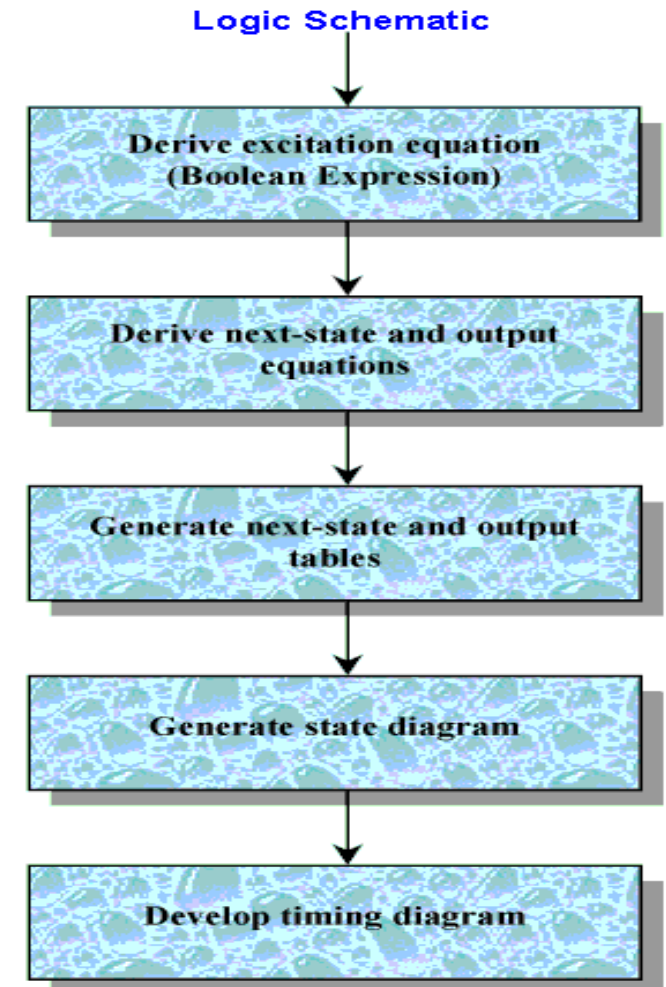
5 important example

Design of Sequential Circuits



The behavior of a sequential circuit is determined from the inputs, the outputs and the states of its flip-flops. Both the output and the next state are a function of the inputs and the present state. The suggested analysis procedure of a sequential circuit is set out in Figure below.

- We start with the logic schematic from which we can derive excitation equations for each flip-flop input.
- Then, to obtain next-state equations, we insert the excitation equations into the characteristic equations.
- The output equations can be derived from the schematic, and once we have our output and next-state equations, we can generate the next-state and output tables as well as state diagrams.
- When we reach this stage, we use either the table or the state diagram to develop a timing diagram which can be verified through simulation.



Design of Sequential Circuits

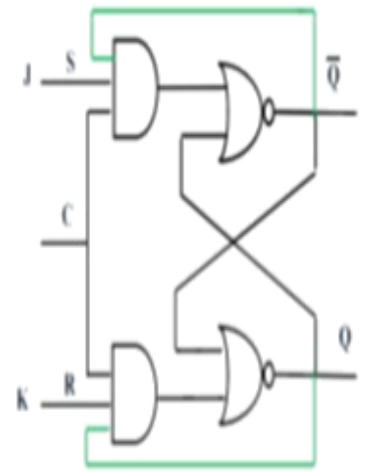


- The main step to design the sequential circuits
 - Analyses and understand the question
 - Extract the state table based on given data
 - Assign a number of required FF
 - Select the type of FF
 - Finding the excitation table base on state table
 - Simplification of input function of FF
 - Design the circuit

Review.....

Table 5.1
Flip-Flop Characteristic Tables

J/K Flip-Flop			
J	K	Q(t + 1)	
0	0	Q(t)	No change
0	1	0	Reset
1	0	1	Set
1	1	Q'(t)	Complement

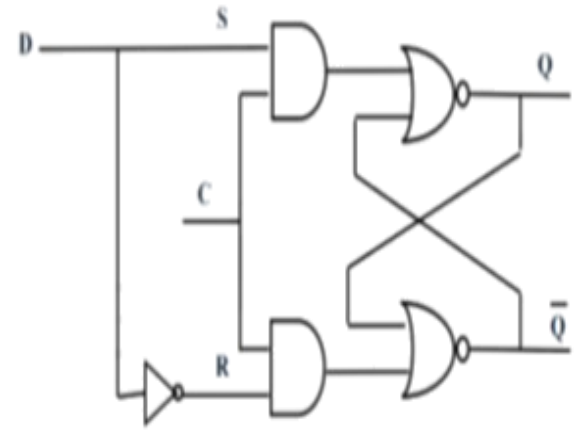


$$Q^* = J\bar{Q} + KQ$$

D Flip-Flop

D	Q(t + 1)	
0	0	Reset
1	1	Set

$$Q^* = D$$

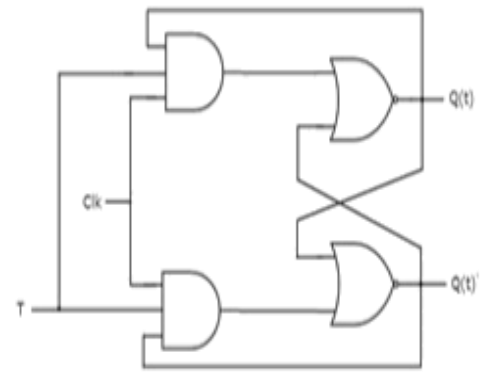


(b) Graphic Symbol

DR AJM

T Flip-Flop

T	Q(t + 1)	
0	Q(t)	No change
1	Q'(t)	Complement



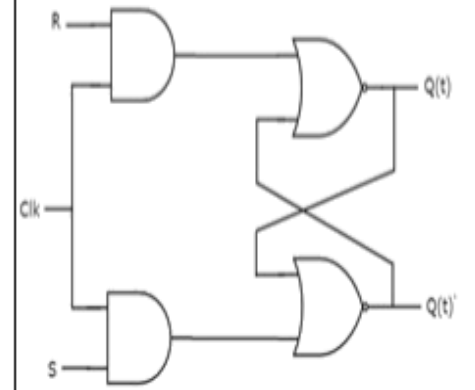
$$Q(t+1) = T \oplus Q(t)$$

SR FF

S	R	Q*
0	0	Q
0	1	0
1	0	1
1	1	X

$$Q^* = S + \bar{R}.Q$$

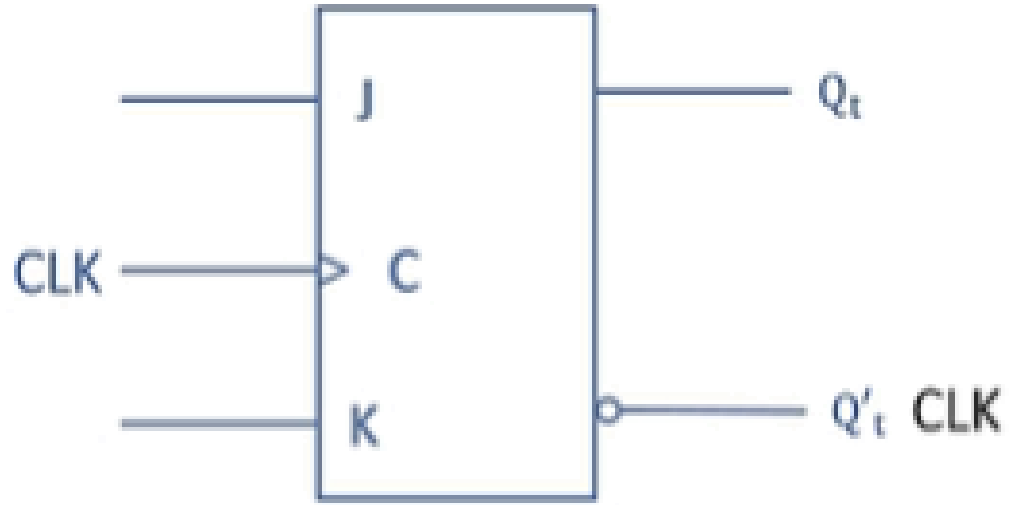
$$S.R = 0$$



All FF type

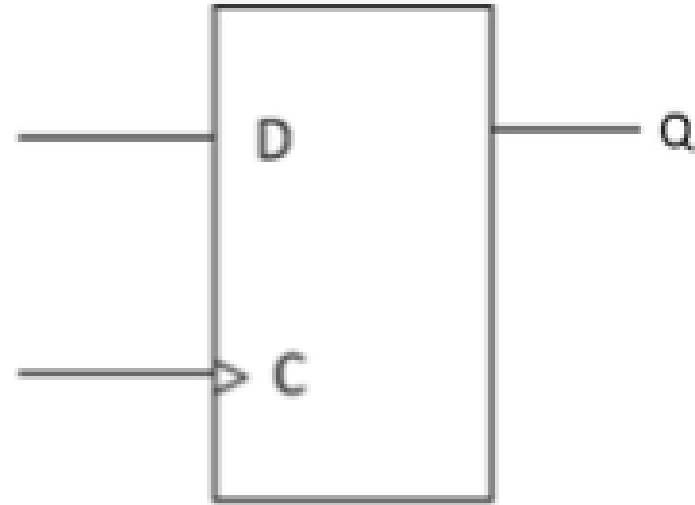


JK-FF



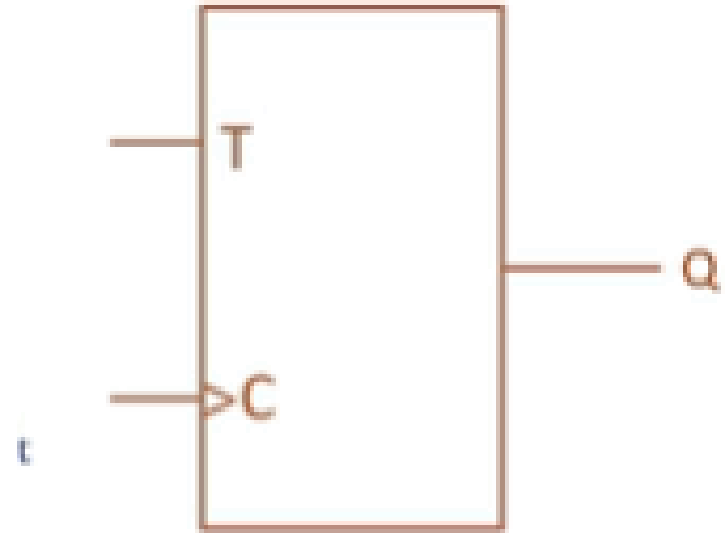
J	K	Q_{t+1}
0	0	Q_t
0	1	0
1	0	1
1	1	Q'_t

D-FF



D	Q_{t+1}
0	0
1	1

T-FF

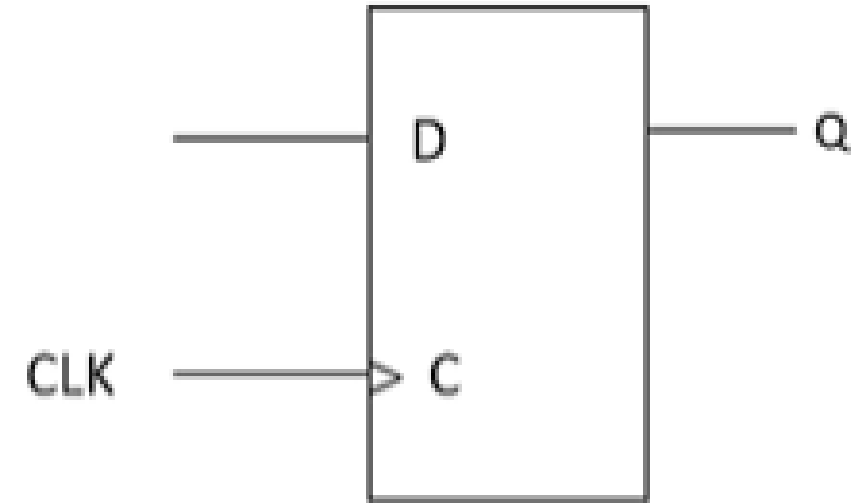


T	Q_{t+1}
0	Q_t
1	Q'_t

All FF type

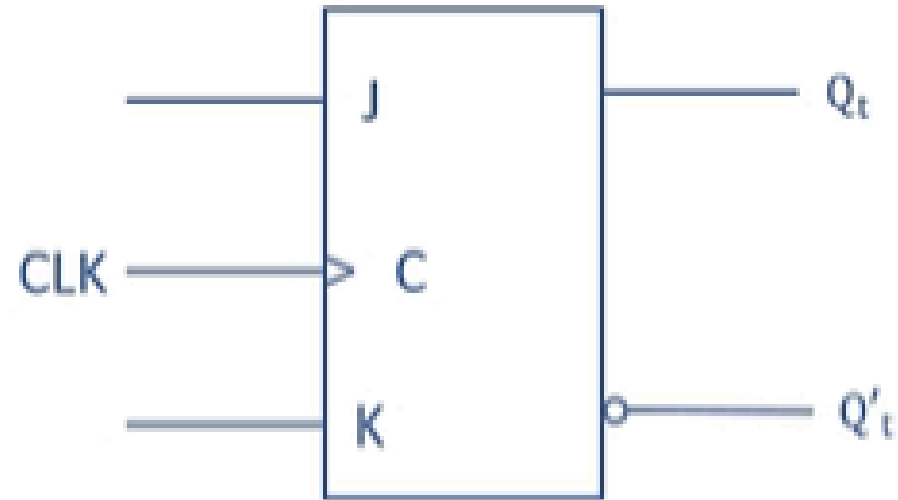


D-FF



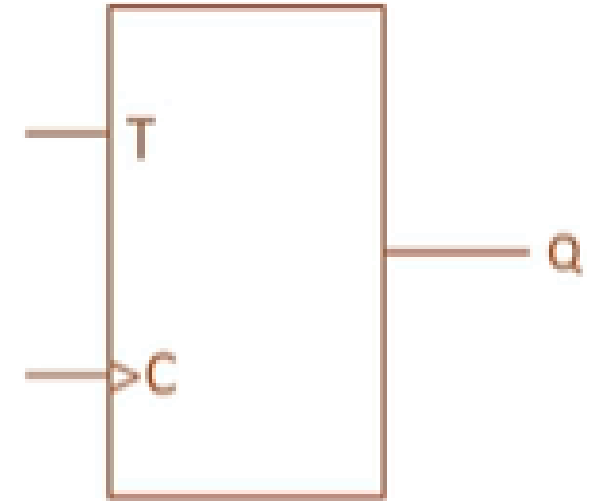
D	Q_{t+1}
0	0
1	1

JK-FF



J	K	Q_{t+1}
0	0	Q_t
0	1	0
1	0	1
1	1	Q'_t

T-FF



T	Q_{t+1}
0	Q_t
1	Q'_t

JK-FF



CHARACTERISTIC TABLE

J	K	Q_{t+1}
0	0	$Q_t = 0$
0	1	0
1	0	1
1	1	$Q'_t = 1$

CHARACTERISTIC EQUATION

$$Q(\text{next}) = JQ' + K'Q$$

EXCITATION TABLE

Q_t	Q_{t+1}	J	K
0	0	0	X
0	1	1	X
1	0	X	1
1	1	X	0

Example 1

Design a sequential circuit which work based on below table with JK FF

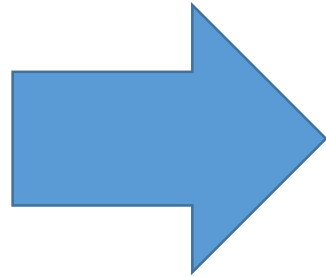
Current state		Input	Next state	
A	B	X	A	B
0	0	0	0	0
0	0	1	0	1
0	1	0	1	0
0	1	1	0	1
1	0	0	1	0
1	0	1	1	1
1	1	1	1	1
1	1	0	0	0



Example 1



Q_t	Q_{t+1}	J	K
0	0	0	X
0	1	1	X
1	0	X	1
1	1	X	0

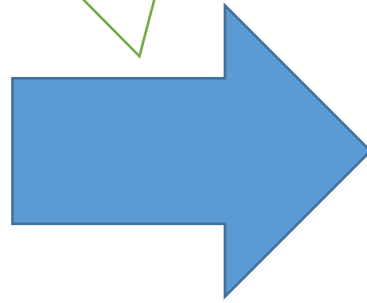


Current state			Input		Next state		FF A Input	
A	B	X	A	B	J_A	K_A		
0	0	0	0	0	0	X		
0	0	1	0	1				
0	1	0	1	0				
0	1	1	0	1				
1	0	0	1	0				
1	0	1	1	1				
1	1	1	1	1				
1	1	0	0	0				

Example 1

Now You
TRY To Solve

Q_t	Q_{t+1}	J	K
0	0	0	X
0	1	1	X
1	0	X	1
1	1	X	0



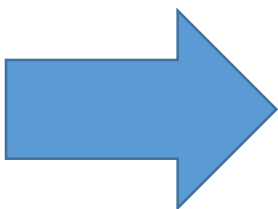
Current state		Input	Next state		FF A Input	
A	B	X	A	B	J_A	K_A
0	0	0	0	0	0	X
0	0	1	0	1		
0	1	0	1	0		
0	1	1	0	1		
1	0	0	1	0		
1	0	1	1	1		
1	1	1	1	1		
1	1	0	0	0		



Example 1



Q_t	Q_{t+1}	J	K
0	0	0	X
0	1	1	X
1	0	X	1
1	1	X	0

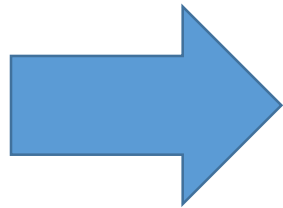


Current state		Input	Next state		FF A Input		FF B Input	
A	B	X	A	B	J_A	K_A	J_B	K_B
0	0	0	0	0				
0	0	1	0	1				
0	1	0	1	0				
0	1	1	0	1				
1	0	0	1	0				
1	0	1	1	1				
1	1	1	1	1				
1	1	0	0	0				

Example 1



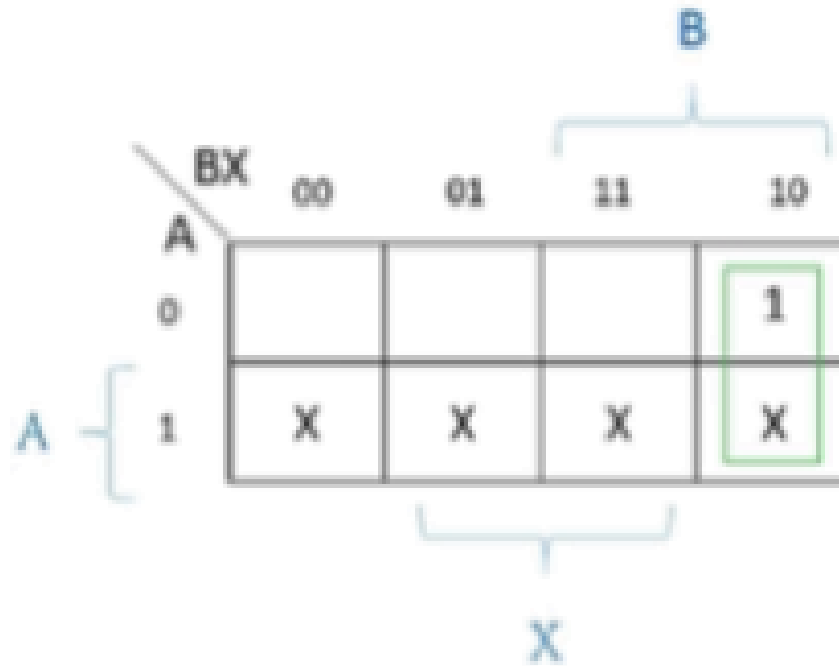
Q_i	Q_{i+1}	J	K
0	0	0	X
0	1	1	X
1	0	X	1
1	1	X	0



Current state		Input	Next state		FF A Input		FF B Input	
A	B	X	A	B	J_A	K_A	J_B	K_B
0	0	0	0	0	0	X	0	X
0	0	1	0	1	0	X	1	X
0	1	0	1	0	1	X	X	1
0	1	1	0	1	0	X	X	0
1	0	0	1	0	X	0	0	X
1	0	1	1	1	X	0	1	X
1	1	1	1	1	X	0	X	0
1	1	0	0	0	X	1	X	1

State table

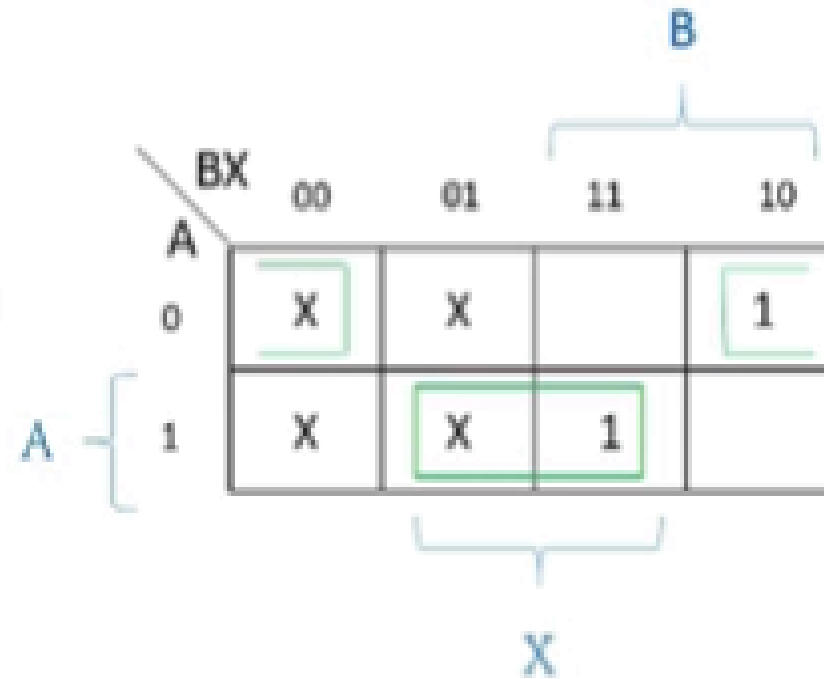
FF A Input		FF B Input	
J_A	K_A	J_B	K_B
0	X	0	X
0	X	1	X
1	X	X	1
0	X	X	0
X	0	0	X
X	0	1	X
X	0	X	0
X	1	X	1



$$J_A = B X'$$

A	B	X	
0	1	0	1
1	0	0	X
1	0	1	X
1	1	1	X
1	1	0	X

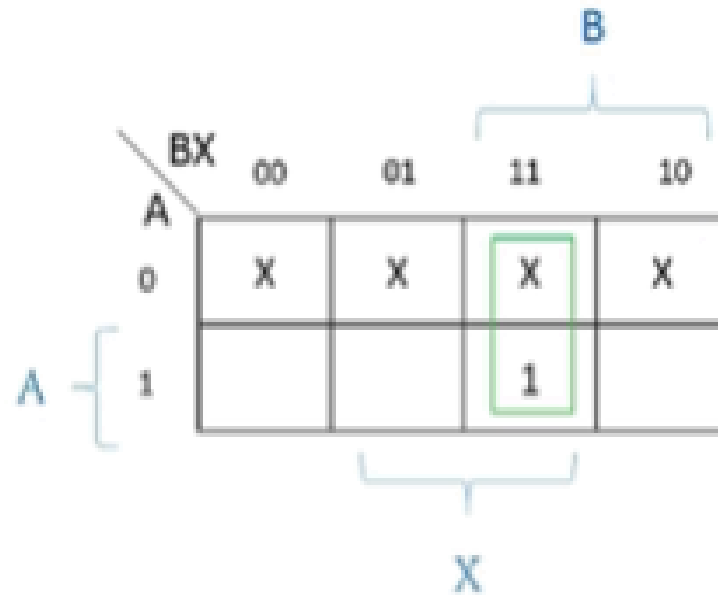
FF A Input		FF B Input	
I_A	K_A	I_B	K_B
0	X	0	X
0	X	1	X
1	X	X	1
0	X	X	0
X	0	0	X
X	0	1	X
X	0	X	0
X	1	X	1



A	B	X	
0	0	0	X
0	0	1	X
0	1	0	1
1	0	0	1
1	0	1	X
1	1	1	1

$$K_B = AX + A'X'$$

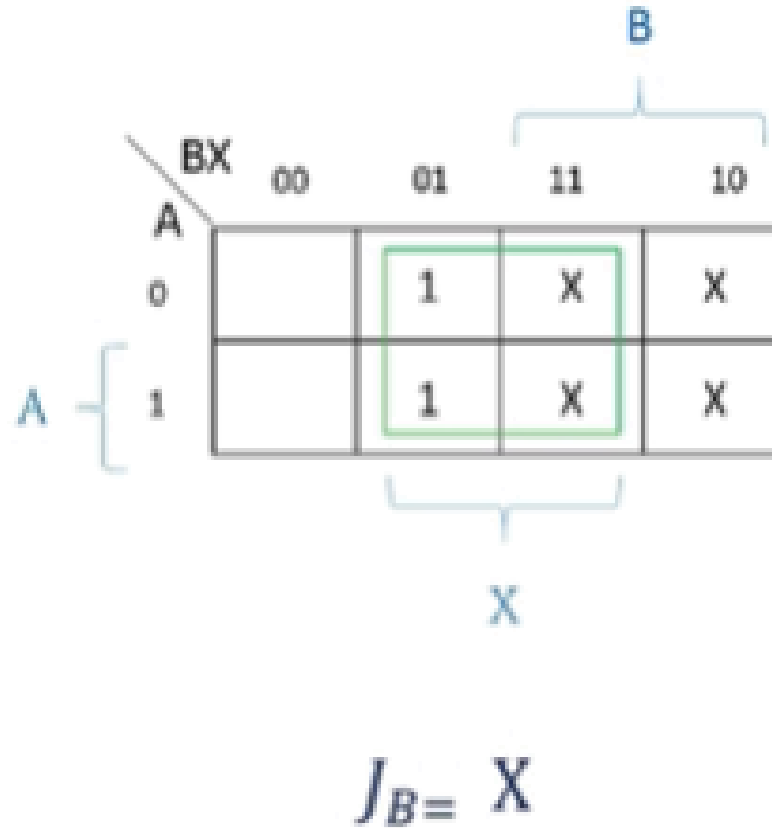
FF A Input		FF B Input	
J_A	K_A	J_B	K_B
0	X	0	X
0	X	1	X
1	X	X	1
0	X	X	0
X	0	0	X
X	0	1	X
X	0	X	0
X	1	X	1



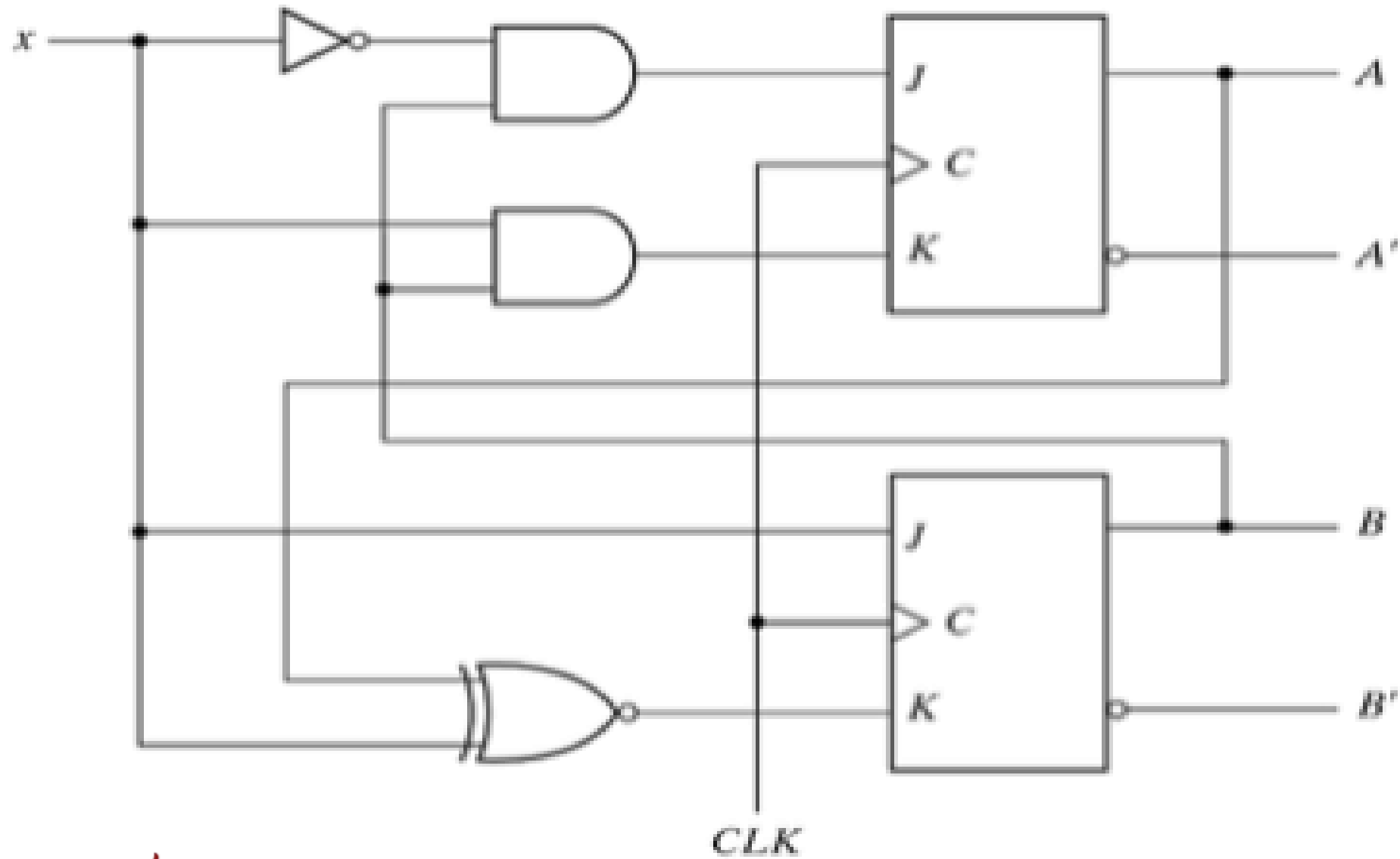
$$K_A = BX$$

A	B	X	
0	0	0	X
0	0	1	X
0	1	1	X
0	1	0	X
1	1	1	1

FF A Input		FF B Input	
J_A	K_A	J_B	K_B
0	X	0	X
0	X	1	X
1	X	X	1
0	X	X	0
X	0	0	X
X	0	1	X
X	0	X	0
X	1	X	1

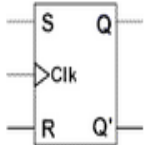
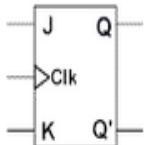
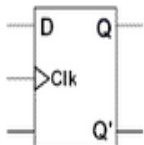
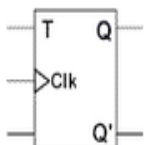


A	B	X	
0	0	1	1
0	1	1	X
0	1	0	X
1	1	0	X
1	0	1	X
1	1	1	X



Flip-flop Types



FLIP-FLOP NAME	FLIP-FLOP SYMBOL	CHARACTERISTIC TABLE	CHARACTERISTIC EQUATION	EXCITATION TABLE																																			
SR		<table><tr><th>S</th><th>R</th><th>Q_(next)</th></tr><tr><td>0</td><td>0</td><td>Q</td></tr><tr><td>0</td><td>1</td><td>0</td></tr><tr><td>1</td><td>0</td><td>1</td></tr><tr><td>1</td><td>1</td><td>?</td></tr></table>	S	R	Q _(next)	0	0	Q	0	1	0	1	0	1	1	1	?	$Q_{(next)} = S + R'Q$ $SR = 0$	<table><tr><th>Q</th><th>Q_(next)</th><th>S</th><th>R</th></tr><tr><td>0</td><td>0</td><td>0</td><td>X</td></tr><tr><td>0</td><td>1</td><td>1</td><td>0</td></tr><tr><td>1</td><td>0</td><td>0</td><td>1</td></tr><tr><td>1</td><td>1</td><td>X</td><td>0</td></tr></table>	Q	Q _(next)	S	R	0	0	0	X	0	1	1	0	1	0	0	1	1	1	X	0
S	R	Q _(next)																																					
0	0	Q																																					
0	1	0																																					
1	0	1																																					
1	1	?																																					
Q	Q _(next)	S	R																																				
0	0	0	X																																				
0	1	1	0																																				
1	0	0	1																																				
1	1	X	0																																				
JK		<table><tr><th>J</th><th>K</th><th>Q_(next)</th></tr><tr><td>0</td><td>0</td><td>Q</td></tr><tr><td>0</td><td>1</td><td>0</td></tr><tr><td>1</td><td>0</td><td>1</td></tr><tr><td>1</td><td>1</td><td>Q'</td></tr></table>	J	K	Q _(next)	0	0	Q	0	1	0	1	0	1	1	1	Q'	$Q_{(next)} = JQ' + K'Q$	<table><tr><th>Q</th><th>Q_(next)</th><th>J</th><th>K</th></tr><tr><td>0</td><td>0</td><td>0</td><td>X</td></tr><tr><td>0</td><td>1</td><td>1</td><td>X</td></tr><tr><td>1</td><td>0</td><td>X</td><td>1</td></tr><tr><td>1</td><td>1</td><td>X</td><td>0</td></tr></table>	Q	Q _(next)	J	K	0	0	0	X	0	1	1	X	1	0	X	1	1	1	X	0
J	K	Q _(next)																																					
0	0	Q																																					
0	1	0																																					
1	0	1																																					
1	1	Q'																																					
Q	Q _(next)	J	K																																				
0	0	0	X																																				
0	1	1	X																																				
1	0	X	1																																				
1	1	X	0																																				
D		<table><tr><th>D</th><th>Q_(next)</th></tr><tr><td>0</td><td>0</td></tr><tr><td>1</td><td>1</td></tr></table>	D	Q _(next)	0	0	1	1	$Q_{(next)} = D$	<table><tr><th>Q</th><th>Q_(next)</th><th>D</th></tr><tr><td>0</td><td>0</td><td>0</td></tr><tr><td>0</td><td>1</td><td>1</td></tr><tr><td>1</td><td>0</td><td>0</td></tr><tr><td>1</td><td>1</td><td>1</td></tr></table>	Q	Q _(next)	D	0	0	0	0	1	1	1	0	0	1	1	1														
D	Q _(next)																																						
0	0																																						
1	1																																						
Q	Q _(next)	D																																					
0	0	0																																					
0	1	1																																					
1	0	0																																					
1	1	1																																					
T		<table><tr><th>T</th><th>Q_(next)</th></tr><tr><td>0</td><td>Q</td></tr><tr><td>1</td><td>Q'</td></tr></table>	T	Q _(next)	0	Q	1	Q'	$Q_{(next)} = TQ' + T'Q$	<table><tr><th>Q</th><th>Q_(next)</th><th>T</th></tr><tr><td>0</td><td>0</td><td>0</td></tr><tr><td>0</td><td>1</td><td>1</td></tr><tr><td>1</td><td>0</td><td>1</td></tr><tr><td>1</td><td>1</td><td>0</td></tr></table>	Q	Q _(next)	T	0	0	0	0	1	1	1	0	1	1	1	0														
T	Q _(next)																																						
0	Q																																						
1	Q'																																						
Q	Q _(next)	T																																					
0	0	0																																					
0	1	1																																					
1	0	1																																					
1	1	0																																					

Example2



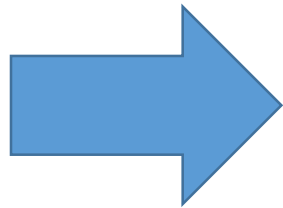
Design a sequential circuit
with the JK FF
which work based on below table

Current state		Input	Next state	
A	B	X	A	B
0	0	0	0	0
0	0	1	0	1
0	1	0	1	0
0	1	1	0	1
1	0	0	1	0
1	0	1	1	1
1	1	0	1	1
1	1	1	0	0

Example2(design)

Based on JK FF the excitation table will be like below

Q_t	Q_{t+1}	J	K
0	0	0	X
0	1	1	X
1	0	X	1
1	1	X	0

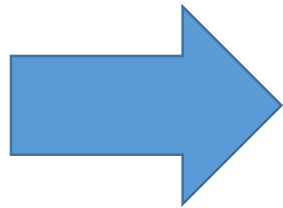


The ckt input			Next state		The ckt o/p			
Current state		Input			FF input			
<i>A</i>	<i>B</i>	<i>x</i>	<i>A</i>	<i>B</i>	<i>JA</i>	<i>KA</i>	<i>JB</i>	<i>KB</i>
0	0	0	0	0				
0	0	1	0	1				
0	1	0	1	0				
0	1	1	0	1				
1	0	0	1	0				
1	0	1	1	1				
1	1	0	1	1				
1	1	1	0	0				

Example2(design)

Based on JK FF the excitation table will be like below

Q_i	Q_{i+1}	J	K
0	0	0	X
0	1	1	X
1	0	X	1
1	1	X	0

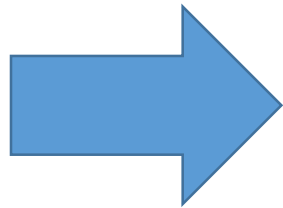


The ckt input			Next state		The ckt o/p			
Current state		Input			FF input			
A	B	x	A	B	JA	KA	JB	KB
0	0	0	0	0	0	X	0	X
0	0	1	0	1				
0	1	0	1	0				
0	1	1	0	1				
1	0	0	1	0				
1	0	1	1	1				
1	1	0	1	1				
1	1	1	0	0				

Example2(design)

Based on JK FF the excitation table will be like below

Q_i	Q_{i+1}	J	K
0	0	0	X
0	1	1	X
1	0	X	1
1	1	X	0



The ckt input			Next state		The ckt o/p			
Current state		Input			FF input			
<i>A</i>	<i>B</i>	<i>x</i>	<i>A</i>	<i>B</i>	<i>JA</i>	<i>KA</i>	<i>JB</i>	<i>KB</i>
0	0	0	0	0	0	X	0	X
0	0	1	0	1	0	X	1	X
0	1	0	1	0	1	X	X	1
0	1	1	0	1	0	X	X	0
1	0	0	1	0	X	0	0	X
1	0	1	1	1	X	0	1	X
1	1	0	1	1	X	0	X	0
1	1	1	0	0	X	1	X	1

K map for FF



		Bx		B	
		00	01	11	10
A	0				1
	1	X	X	X	X

x

$$J_A = Bx'$$

A	B	X	
0	1	0	1
1	0	0	X
1	0	1	X
1	1	1	X
1	1	0	X

		Bx		B	
		00	01	11	10
A	0	X	X	X	X
	1			1	

x

$$K_A = Bx$$

A	B	X	
0	0	0	X
0	0	1	X
0	1	1	X
0	1	0	X
1	1	1	1

K map for FF



		Bx		B	
		00	01	11	10
A	0		1	X	X
	1		1	X	X

$$J_B = x$$

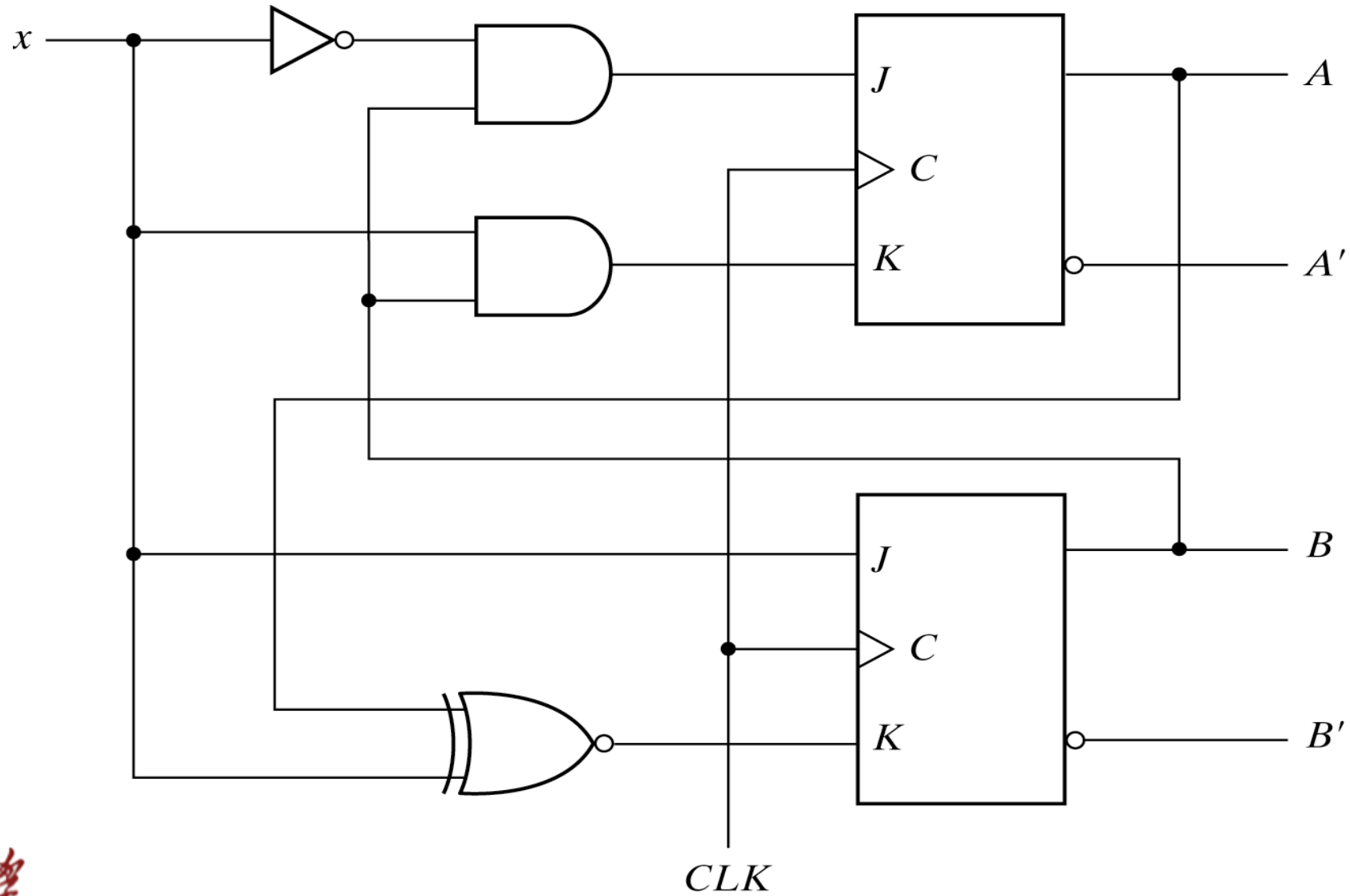
A	B	X	
0	0	1	1
0	1	1	X
0	1	0	X
1	0	1	1
1	1	1	X
1	1	0	X

		Bx		B	
		00	01	11	10
A	0	X	X		1
	1	X	X	1	

$$K_B = (A \oplus x)'$$

A	B	X	
0	0	0	X
0	0	1	X
0	1	0	1
1	0	0	X
1	0	1	X
1	1	1	1

Design Circuit



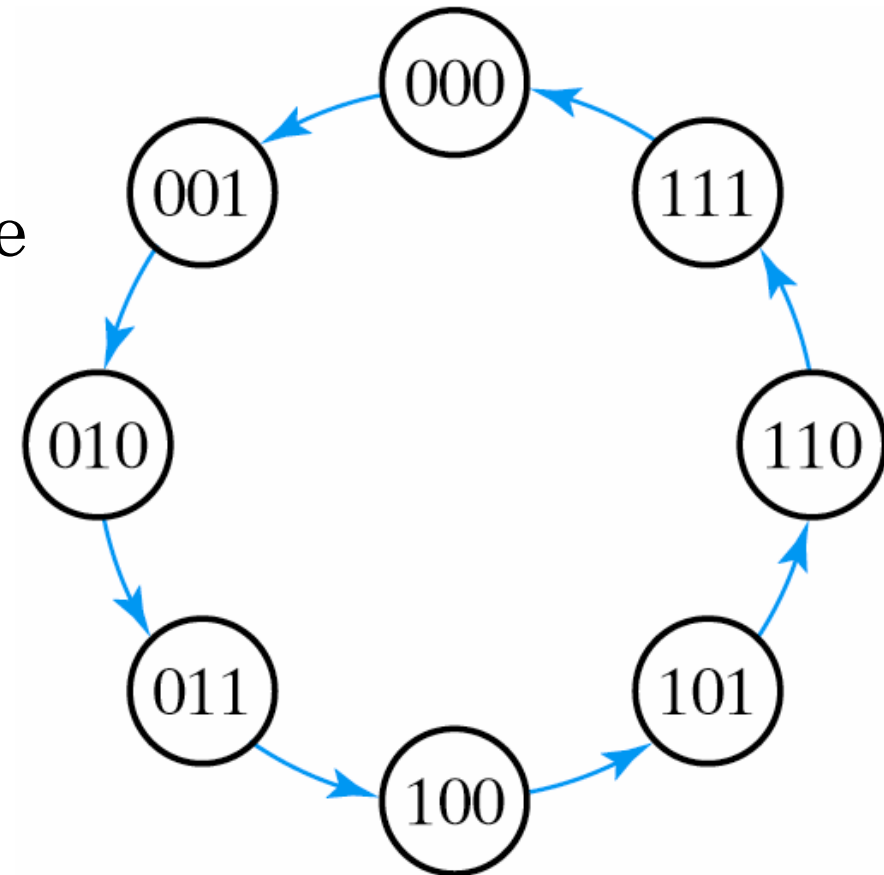
Example 3



- Design a 3 bit counter with the T flip flop, which start from 000 to 111

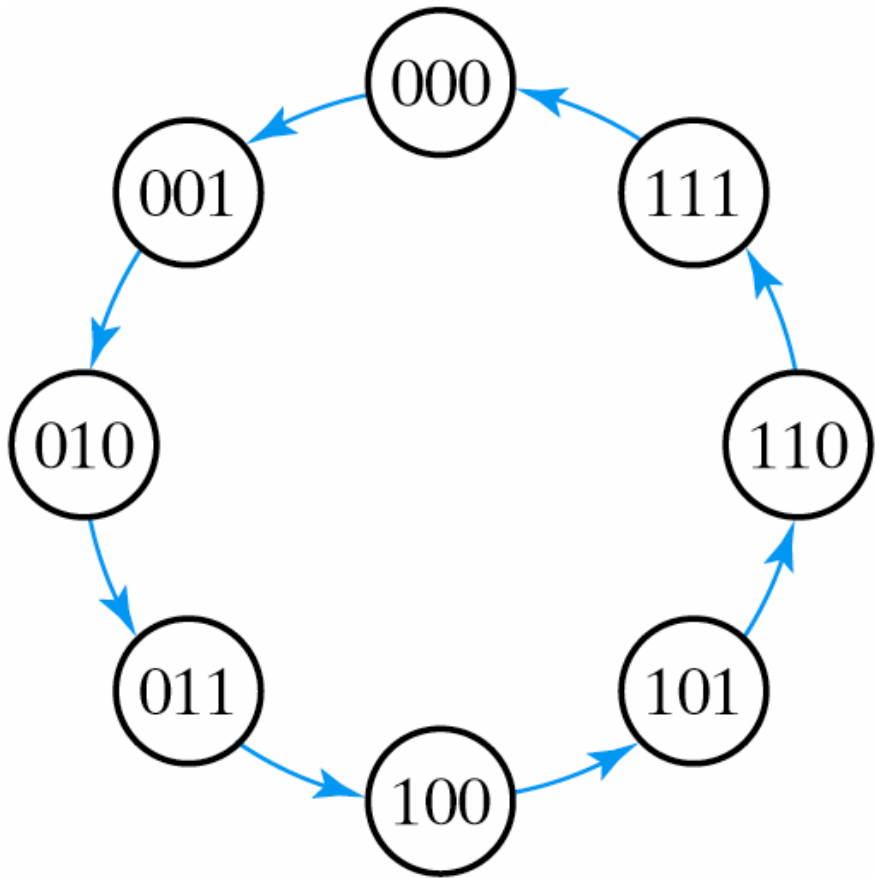
More Example:

Binary Counter – show state diagram and table



Example 3

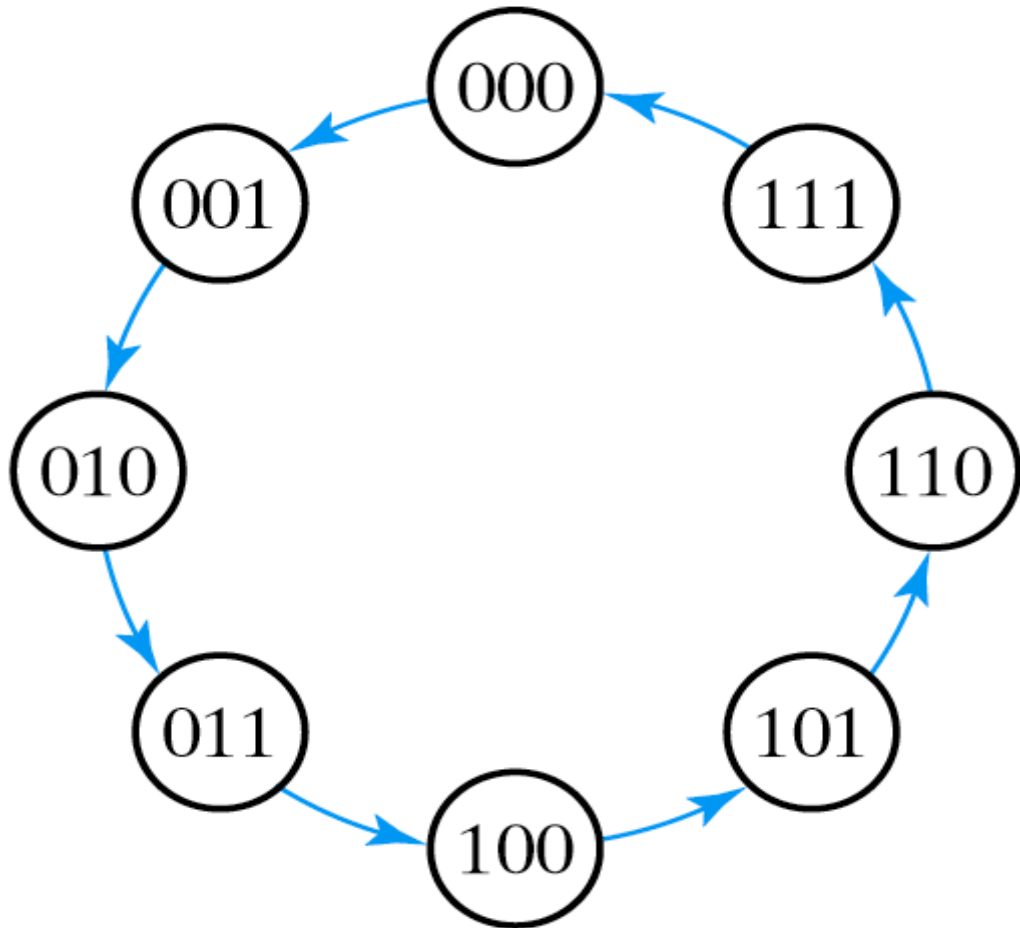
- The excitation circuit



Current state			Next state			FF inputs		
A_2	A_1	A_0	A_2	A_1	A_0	TA_2	TA_1	TA_0
0	0	0	0	0	1	0	0	1
0	0	1	0	1	0			
0	1	0	0	1	1			
0	1	1	1	0	0			
1	0	0	1	0	1			
1	0	1	1	1	0			
1	1	0	1	1	1			
1	1	1	0	0	0			

Example 3

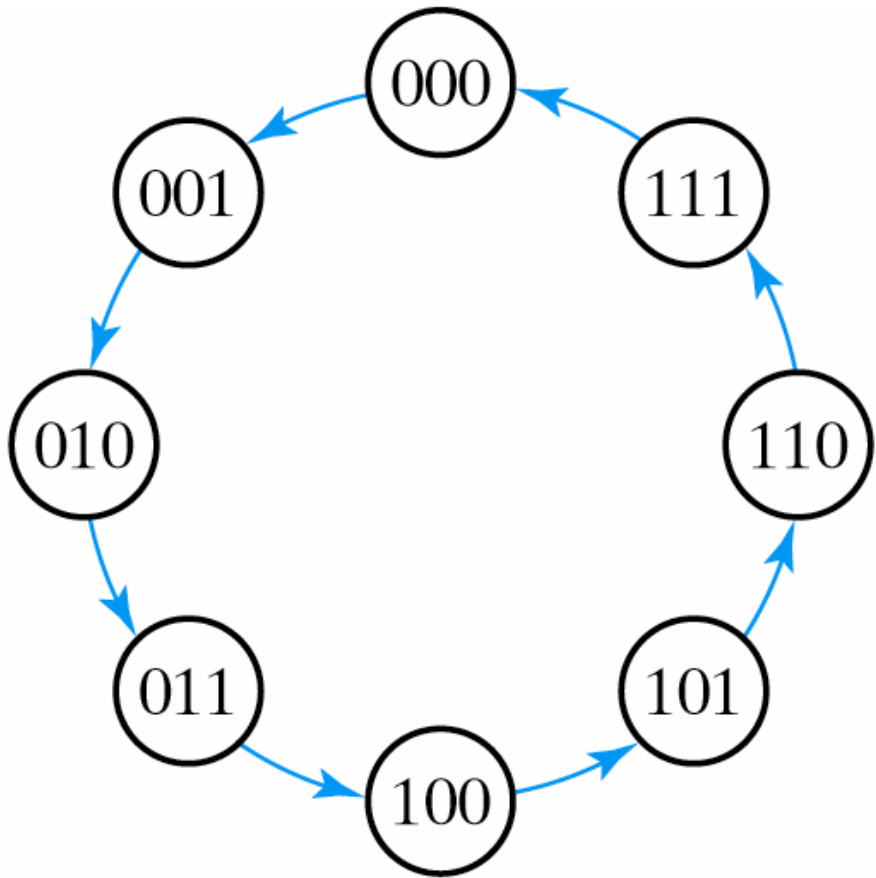
- The excitation circuit



$Q(t)$	$Q(t+1)$	T
0	0	0
0	1	1
1	0	1
1	1	0

Example 3

- The excitation circuit



Current state			Next state			FF inputs		
A_2	A_1	A_0	A_2	A_1	A_0	TA_2	TA_1	TA_0
0	0	0	0	0	1	0	0	1
0	0	1	0	1	0			
0	1	0	0	1	1			
0	1	1	1	0	0			
1	0	0	1	0	1			
1	0	1	1	1	0			
1	1	0	1	1	1			
1	1	1	0	0	0			

Example 3

- K map

		A_1	
A_2			1
			1
		A_0	

$T_{A2} = A_1 A_0$

A2	A1	A3	TA2
0	1	1	1
1	1	1	1

	1	1	
	1	1	

$$T_{A1} = A_0$$

A2	A1	A3	TA1
0	0	1	1
0	1	1	1
1	0	1	1
1	1	1	1

1	1	1	1
1	1	1	1

$$T_{A0} = 1$$

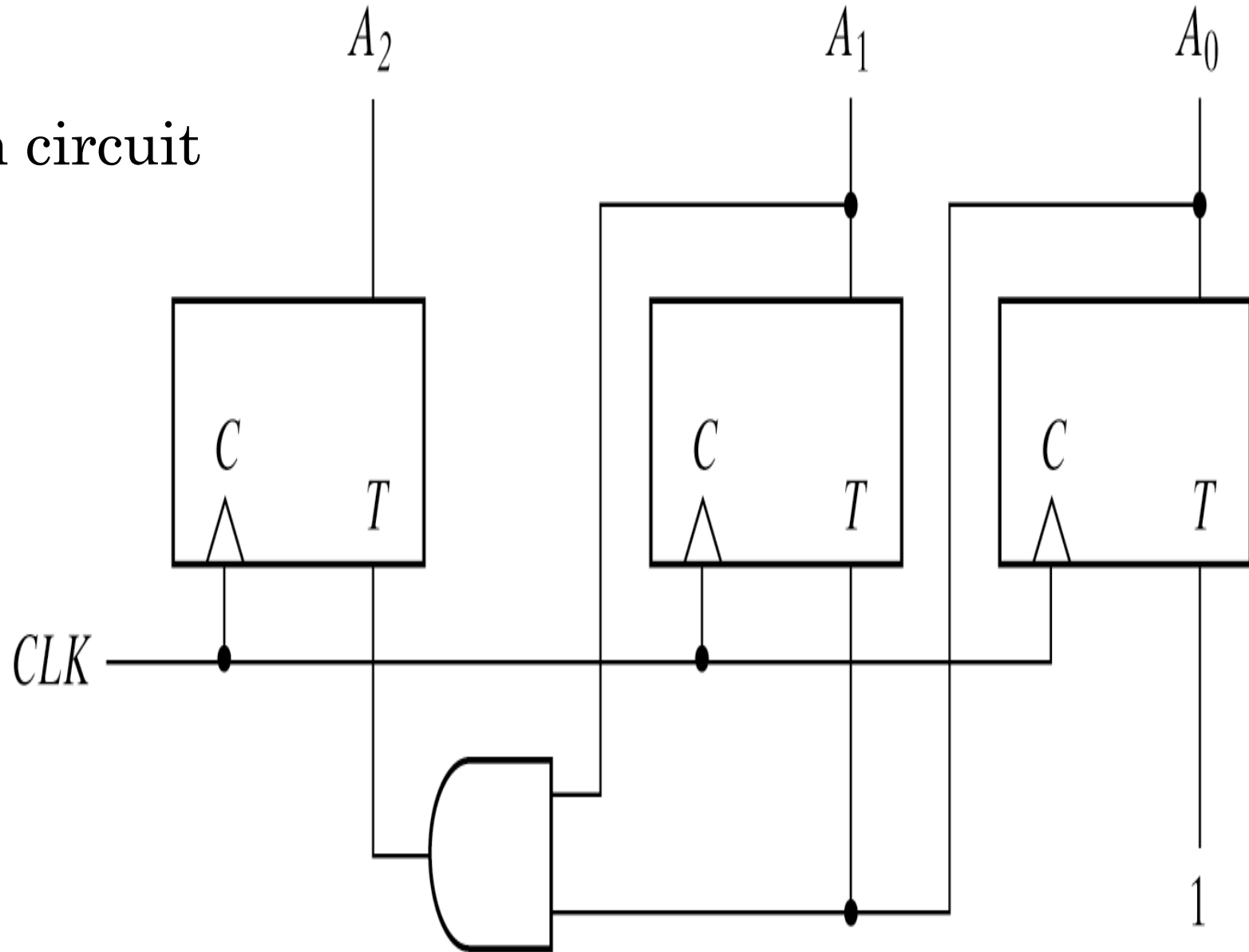
- The design circuit

Current state			Next state			FF inputs		
A_2	A_1	A_0	A_2	A_1	A_0	TA_2	TA_1	TA_0
0	0	0	0	0	1	0	0	1
0	0	1	0	1	0	0	1	1
0	1	0	0	1	1	0	0	1
0	1	1	1	0	0	1	1	1
1	0	0	1	0	1	0	0	1
1	0	1	1	1	0	0	1	1
1	1	0	1	1	1	0	0	1
1	1	1	0	0	0	1	1	1


Example 3

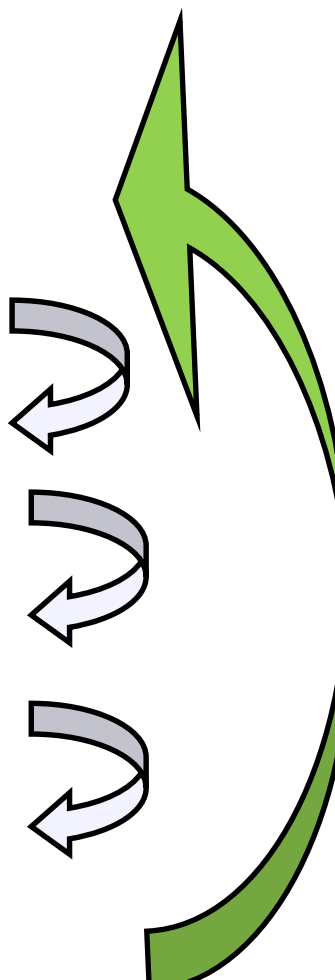


- The design circuit



3 bit counter with JK

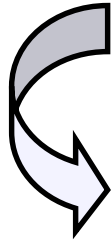
Q2	Q1	Q0	Bit 0
0	0	0	
0	0	1	
0	1	0	
0	1	1	
1	0	0	
1	0	1	
1	1	0	
1	1	1	

Q2	Q1	Q0	Bit 1
0	0	0	
0	0	1	
0	1	0	
0	1	1	
1	0	0	
1	0	1	
1	1	0	
1	1	1	

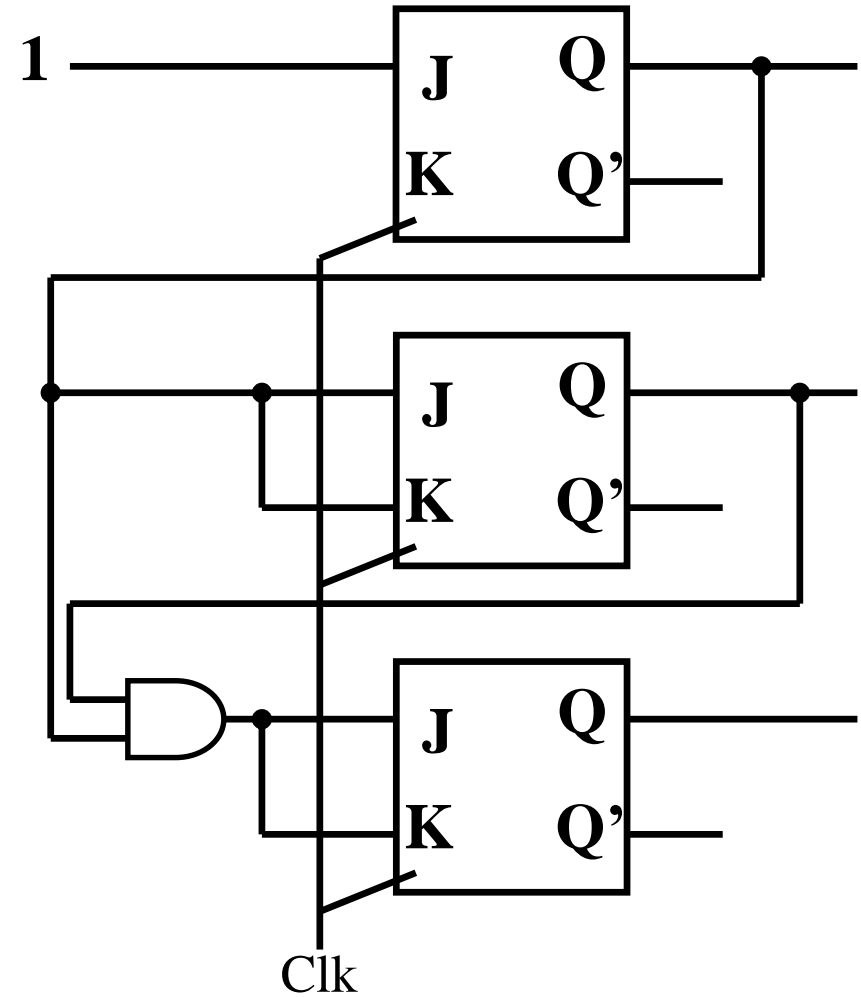
3 bit counter Solve and make the K map and check your design



Bit 2



Q2	Q1	Q0
0	0	0
0	0	1
0	1	0
0	1	1
1	0	0
1	0	1
1	1	0
1	1	1



FF- The excitation table

$Q(t)$	$Q(t+1)$	D	T	R	S	J	K
0	0	0	0	X	0	0	X
0	1	1	1	0	1	1	X
1	0	0	1	1	0	X	1
1	1	1	0	0	X	X	0

Most
Important
Table

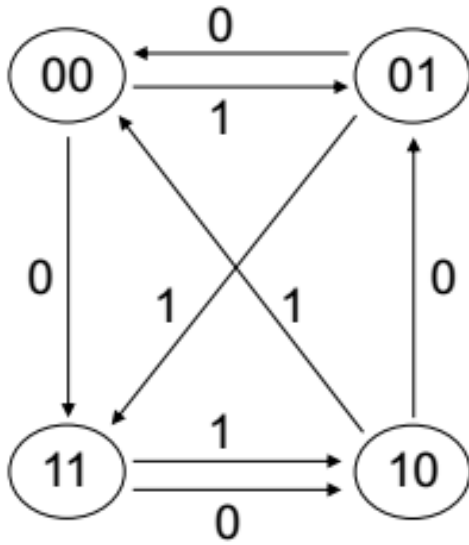
Example 4



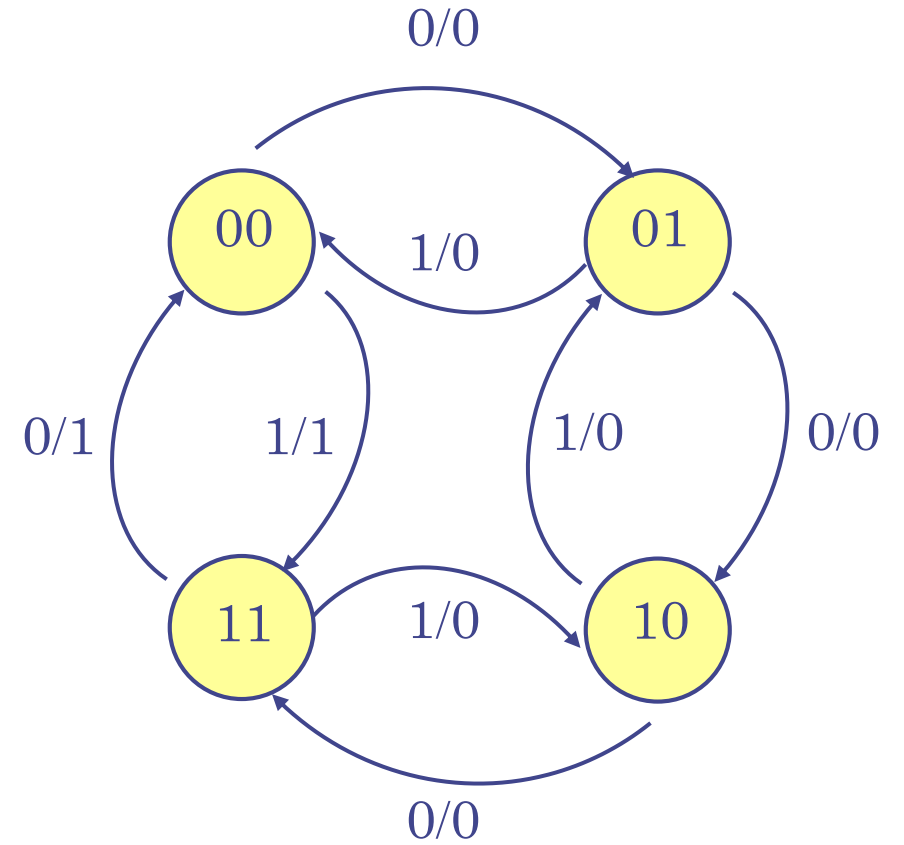
Solve and make the K map and check your design

- Design a 2 bit counter which count with the 0 input up counter and 1 Down counter (Use JK ff)
- With the 0 input : $00 \rightarrow 01 \rightarrow 10 \rightarrow 11 \rightarrow 00 \rightarrow 01 \rightarrow \dots$
- With the 1 input : $00 \rightarrow 11 \rightarrow 10 \rightarrow 01 \rightarrow 00 \rightarrow 11 \rightarrow \dots$

Example 4: State Diagram



present state	next state	
	x=0	x=1
AB	AB	AB
00	11	01
01	00	11
10	01	00
11	10	10



Example 4: The state table

$Q_2(t)$	$Q_1(t)$	x	$Q_2(t+1)$	$Q_1(t+1)$	J_2	K_2	J_1	K_1	Z
0	0	0	0	1	0	X	1	X	0
0	0	1	1	1	1	X	1	X	1
0	1	0	1	0	1	X	X	1	0
0	1	1	0	0	0	X	X	1	0
1	0	0	1	1	X	0	1	X	0
1	0	1	0	1	X	1	1	X	0
1	1	0	0	0	X	1	X	1	1
1	1	1	1	0	X	0	X	1	0

Example 4: k_map

		$Q_1(t) x$			
		00	01	11	10
$Q_2(t)$	0	X	X	X	X
	1		1		1

$$K_2 = Q_1(t) \oplus x$$

		$Q_1(t) x$			
		00	01	11	10
$Q_2(t)$	0		1		1
	1	X	X	X	X

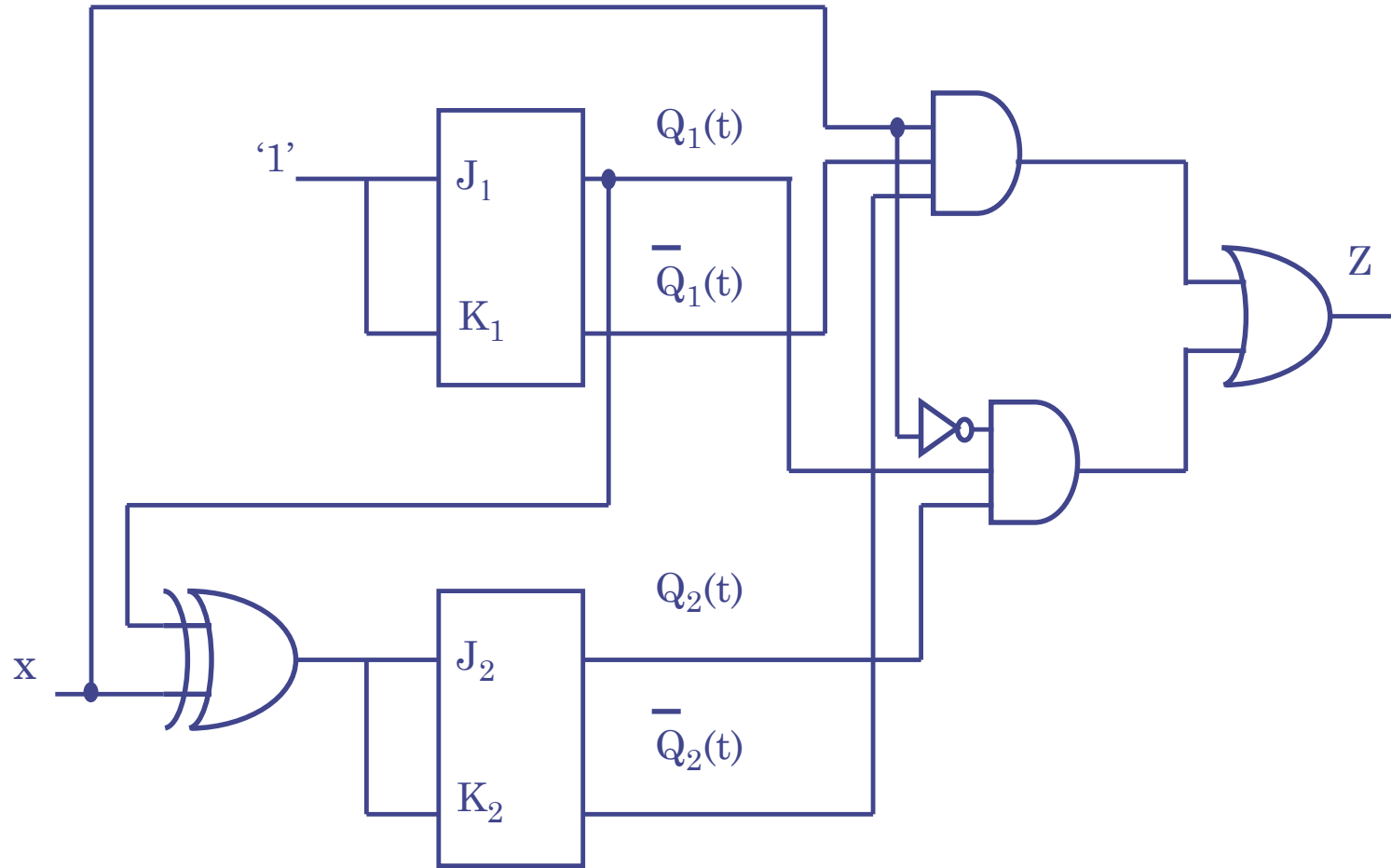
$$J_2 = Q_1(t) \oplus x$$

Q2	Q1	X	K2
0	0	0	X
0	0	1	X
0	1	1	X
0	1	0	X
1	0	1	1
1	1	0	1

Q2	Q1	X	K2
0	0	1	1
0	1	0	1
1	0	0	X
1	0	1	X
1	1	1	X
1	1	0	X



Example 4: Design



Design with D type FF



Solve and make the K map
and check your design

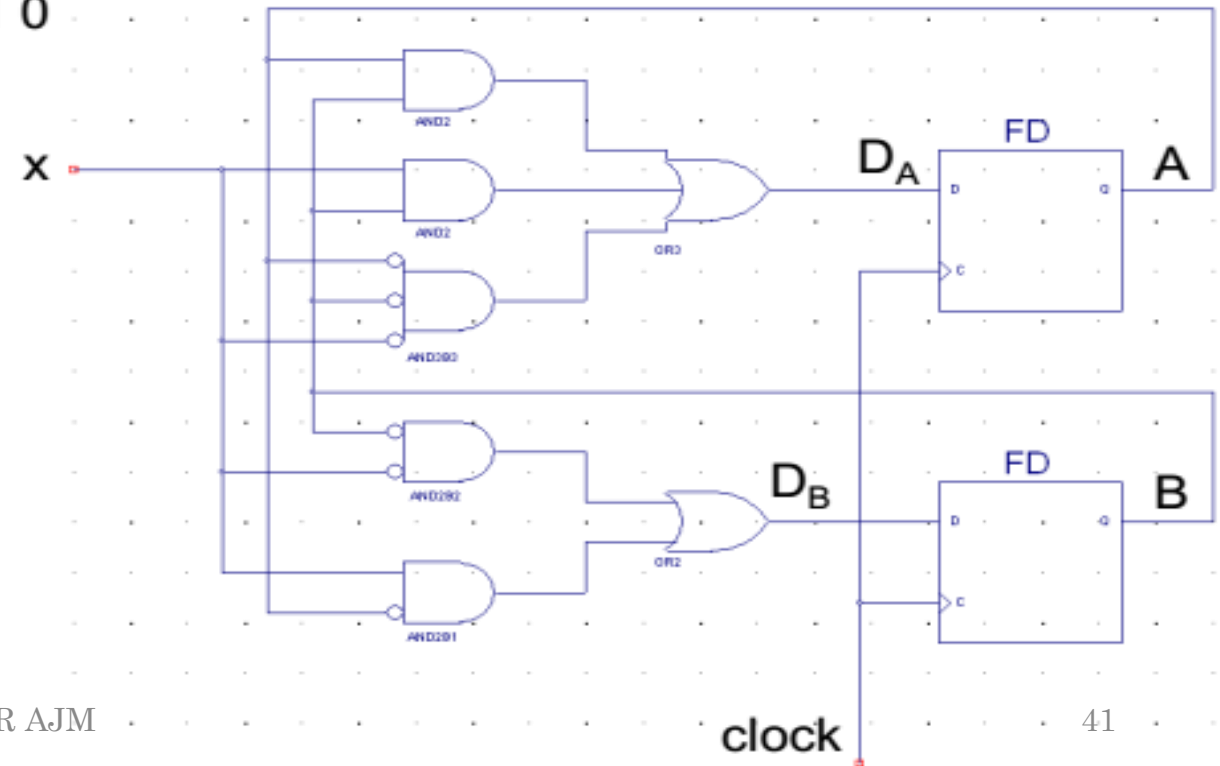
present state	next state	
	x=0	x=1
A B	A B	A B
0 0	1 1	0 1
0 1	0 0	1 1
1 0	0 1	0 0
1 1	1 0	1 0

		D_A			
x	AB	00	01	11	10
0		1	0	1	0
1		0	1	1	0

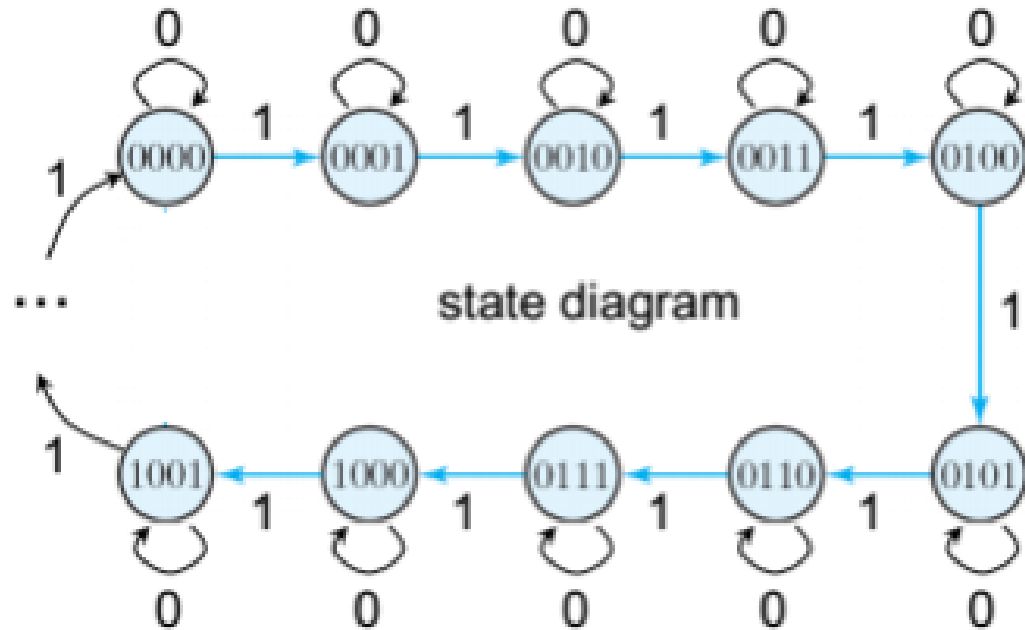
$$D_A = AB + Bx + A'B'x'$$

		D_B			
x	AB	00	01	11	10
0		1	0	0	1
1		1	1	0	0

$$D_B = B'x' + A'x$$



Example 5: Binary Counter



... → 1110 → 1111 → 0000 → 0001 →
0010 → 0011 → 0100 → 0101 → ...

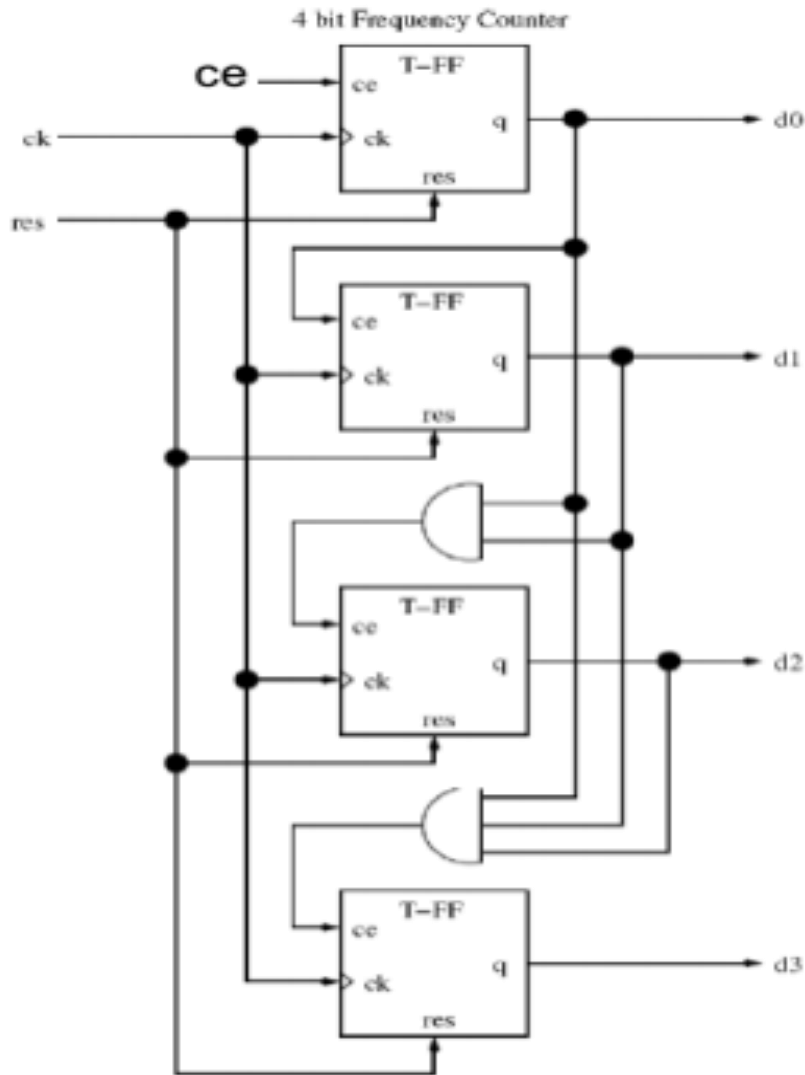


Solve and make the K map and check your design

Example 5: Binary Counter

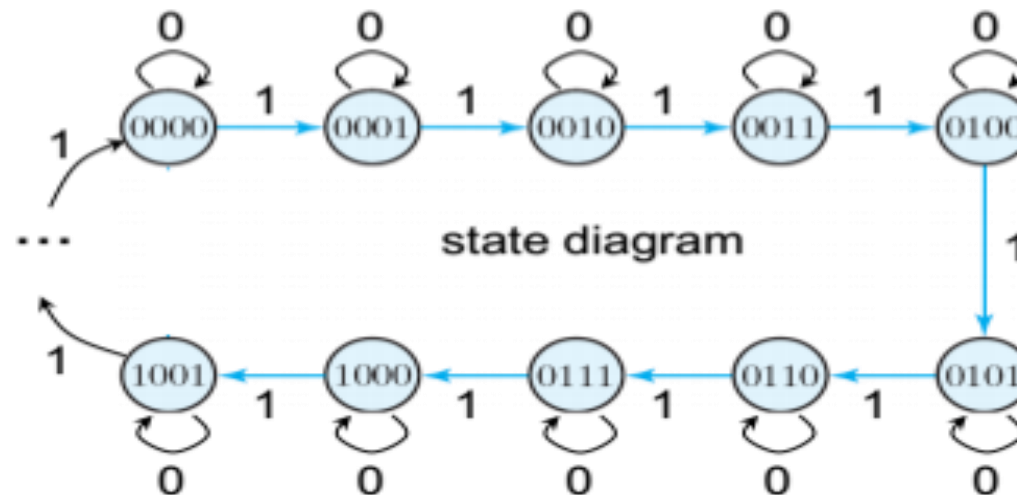


... $\rightarrow 1110 \rightarrow 1111 \rightarrow 0000 \rightarrow 0001 \rightarrow$
 $0010 \rightarrow 0011 \rightarrow 0100 \rightarrow 0101 \rightarrow \dots$



present state	next state	
	ce=0	ce=1
0000	0000	0001
0001	0001	0010
0010	0010	0011
...
1101	1101	1110
1110	1110	1111
1111	1111	0000

\rightarrow state table



Reference

1. Mano book
2. ee.hawaii.edu/~sasaki/EE361/Fall06/Lab/7disp.html
3. https://www.tutorialspoint.com/computer_logical_organization/combinational_circuits.htm
4. http://osp.mans.edu.eg/cs212/Seq_circuits_analysis.htm
5. http://osp.mans.edu.eg/cs212/Seq_circuits_analysis.htm

