



江西理工大学
Jiangxi University of Science and Technology
信息工程学院
School of information engineering



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Clip Lecture series

Digital System Design

Spring_2020



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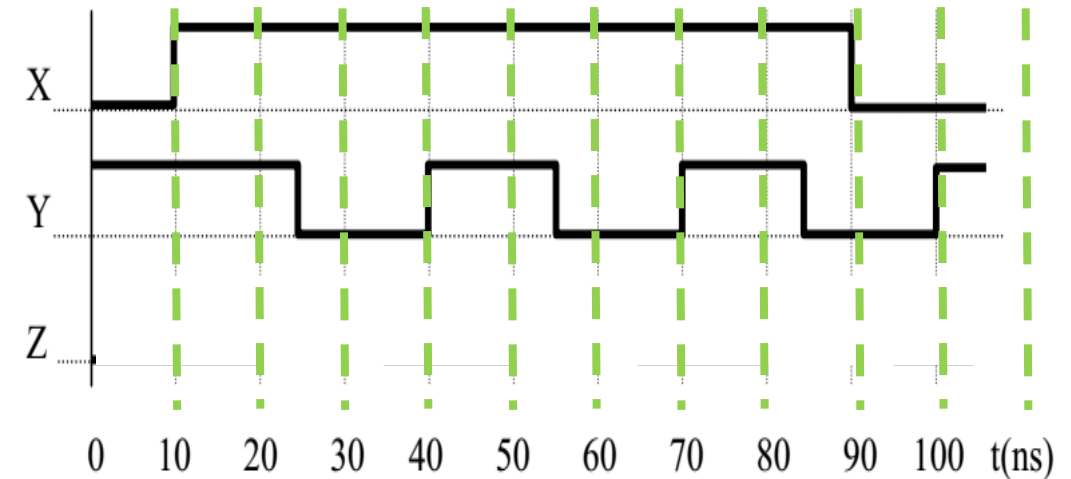
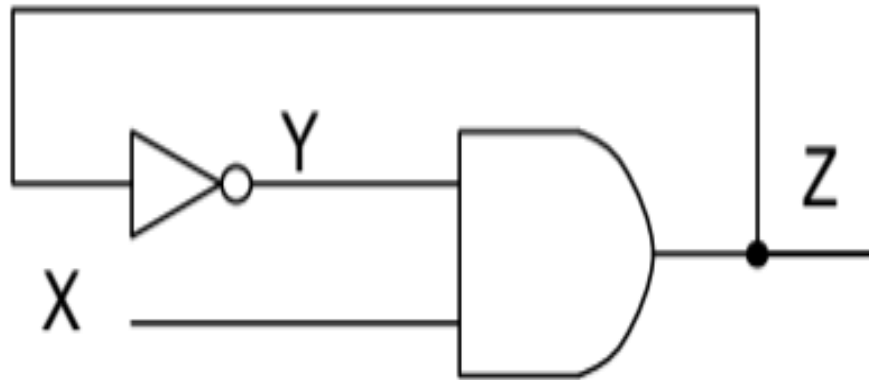
Sequential Circuits

9 Example and review:
Flip-flop/Basic Flip-Flop



Example_1

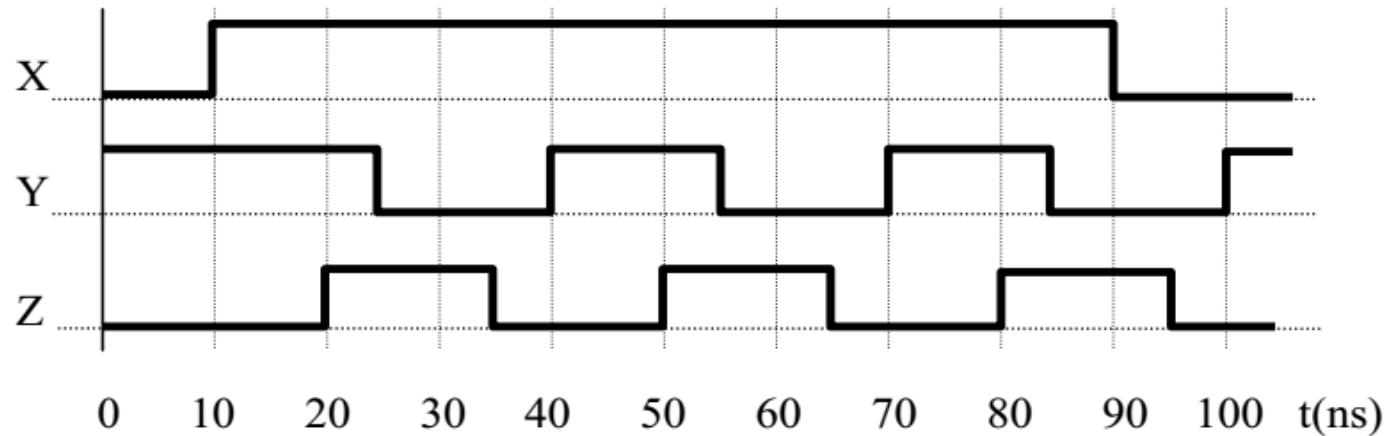
Assume that the inverter in the network below has a propagation delay of 5 ns and the AND gate has a propagation delay of 10 ns. Draw a timing diagram for the network showing X, Y, and Z. Assume that X is initially 0, Y is initially 1, X becomes 1 for 80 ns, and then X is 0 again.

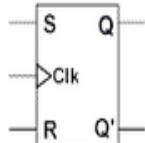
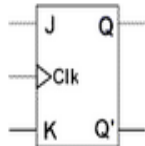
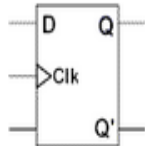
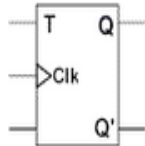


Example_1(solution)

Solution 1. You must remember to take into account delays. Steps for the solution:

1. Draw an empty timing diagram
2. Write related characteristic equation: $Z = XY = XZ'$
3. Plot initial states for X and Y
4. Plot remaining diagram by considering appropriate delays

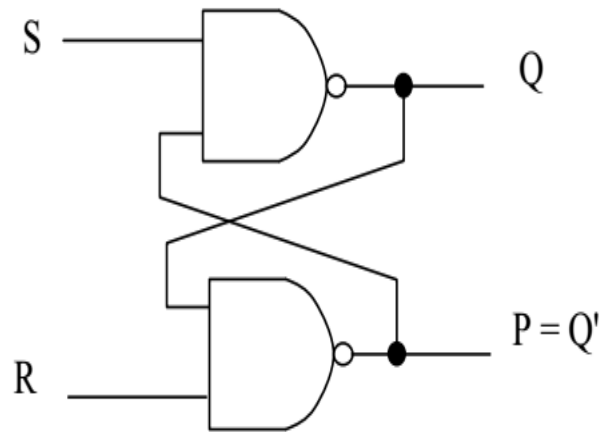


FLIP-FLOP NAME	FLIP-FLOP SYMBOL	CHARACTERISTIC TABLE	CHARACTERISTIC EQUATION	EXCITATION TABLE																																			
SR		<table><tr><th>S</th><th>R</th><th>Q_(next)</th></tr><tr><td>0</td><td>0</td><td>Q</td></tr><tr><td>0</td><td>1</td><td>0</td></tr><tr><td>1</td><td>0</td><td>1</td></tr><tr><td>1</td><td>1</td><td>?</td></tr></table>	S	R	Q _(next)	0	0	Q	0	1	0	1	0	1	1	1	?	$Q_{(next)} = S + R'Q$ $SR = 0$	<table><tr><th>Q</th><th>Q_(next)</th><th>S</th><th>R</th></tr><tr><td>0</td><td>0</td><td>0</td><td>X</td></tr><tr><td>0</td><td>1</td><td>1</td><td>0</td></tr><tr><td>1</td><td>0</td><td>0</td><td>1</td></tr><tr><td>1</td><td>1</td><td>X</td><td>0</td></tr></table>	Q	Q _(next)	S	R	0	0	0	X	0	1	1	0	1	0	0	1	1	1	X	0
S	R	Q _(next)																																					
0	0	Q																																					
0	1	0																																					
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0	0	0	X																																				
0	1	1	0																																				
1	0	0	1																																				
1	1	X	0																																				
JK		<table><tr><th>J</th><th>K</th><th>Q_(next)</th></tr><tr><td>0</td><td>0</td><td>Q</td></tr><tr><td>0</td><td>1</td><td>0</td></tr><tr><td>1</td><td>0</td><td>1</td></tr><tr><td>1</td><td>1</td><td>Q'</td></tr></table>	J	K	Q _(next)	0	0	Q	0	1	0	1	0	1	1	1	Q'	$Q_{(next)} = JQ' + K'Q$	<table><tr><th>Q</th><th>Q_(next)</th><th>J</th><th>K</th></tr><tr><td>0</td><td>0</td><td>0</td><td>X</td></tr><tr><td>0</td><td>1</td><td>1</td><td>X</td></tr><tr><td>1</td><td>0</td><td>X</td><td>1</td></tr><tr><td>1</td><td>1</td><td>X</td><td>0</td></tr></table>	Q	Q _(next)	J	K	0	0	0	X	0	1	1	X	1	0	X	1	1	1	X	0
J	K	Q _(next)																																					
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D		<table><tr><th>D</th><th>Q_(next)</th></tr><tr><td>0</td><td>0</td></tr><tr><td>1</td><td>1</td></tr></table>	D	Q _(next)	0	0	1	1	$Q_{(next)} = D$	<table><tr><th>Q</th><th>Q_(next)</th><th>D</th></tr><tr><td>0</td><td>0</td><td>0</td></tr><tr><td>0</td><td>1</td><td>1</td></tr><tr><td>1</td><td>0</td><td>0</td></tr><tr><td>1</td><td>1</td><td>1</td></tr></table>	Q	Q _(next)	D	0	0	0	0	1	1	1	0	0	1	1	1														
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Q	Q _(next)	D																																					
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T		<table><tr><th>T</th><th>Q_(next)</th></tr><tr><td>0</td><td>Q</td></tr><tr><td>1</td><td>Q'</td></tr></table>	T	Q _(next)	0	Q	1	Q'	$Q_{(next)} = TQ' + T'Q$	<table><tr><th>Q</th><th>Q_(next)</th><th>T</th></tr><tr><td>0</td><td>0</td><td>0</td></tr><tr><td>0</td><td>1</td><td>1</td></tr><tr><td>1</td><td>0</td><td>1</td></tr><tr><td>1</td><td>1</td><td>0</td></tr></table>	Q	Q _(next)	T	0	0	0	0	1	1	1	0	1	1	1	0														
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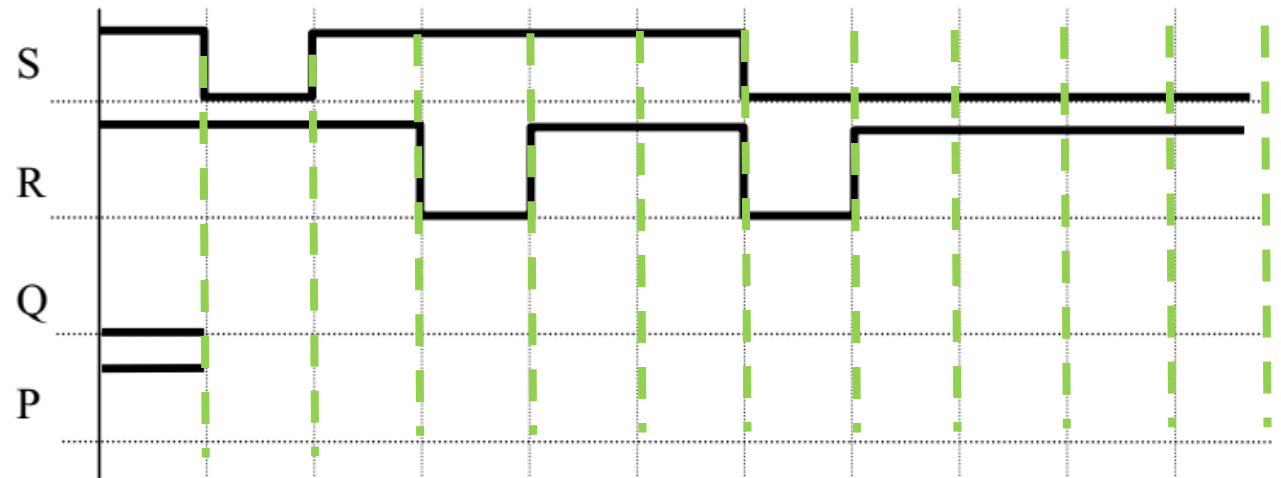
Example_2



A flip-flop can be constructed from two NAND gates connected as follows:



(c) Complete the following timing diagram for the flip-flop.



Example_2(solution)



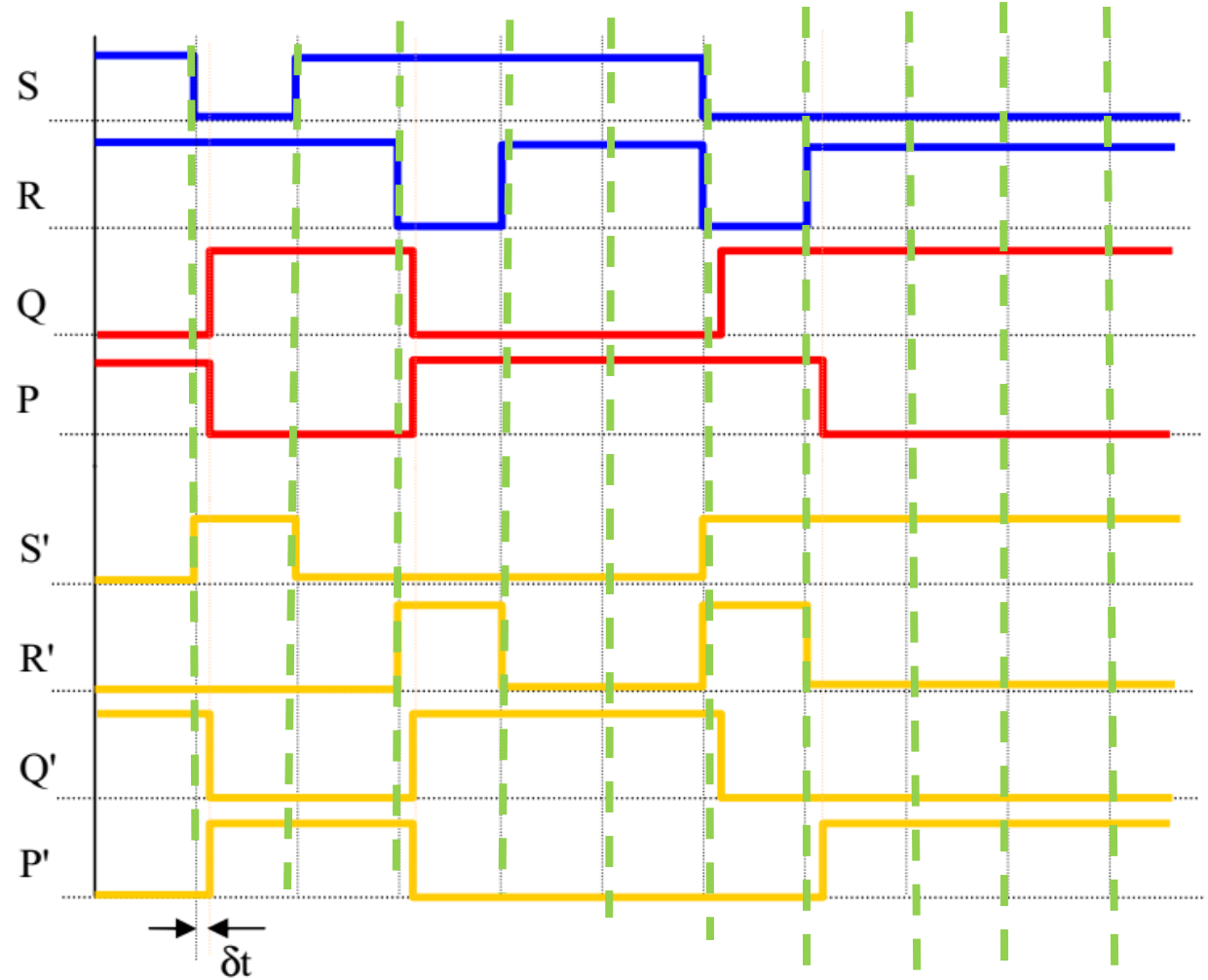
A δt time delay should be considered when constructing timing diagram. Although it is not required, drawing S' , P' , R' , and Q' is helpful.

$$Q = S' + P' \quad P = R' + Q'$$

$$Q_+ = S' + RQ$$

CHARACTERISTIC TABLE		
S	R	$Q_{(next)}$
0	0	Q
0	1	0
1	0	1
1	1	?

$$Q_{(next)} = S + R'Q$$
$$SR = 0$$



Example_3(solution)

Considering the RS_FF

Draw the Output Diagram if the initial value of is zero
($Q=0$ and its sensitive to the rising edge)

CHARACTERISTIC TABLE		
S	R	$Q_{(next)}$
0	0	Q
0	1	0
1	0	1
1	1	?

$$Q_{(next)} = S + R'Q$$

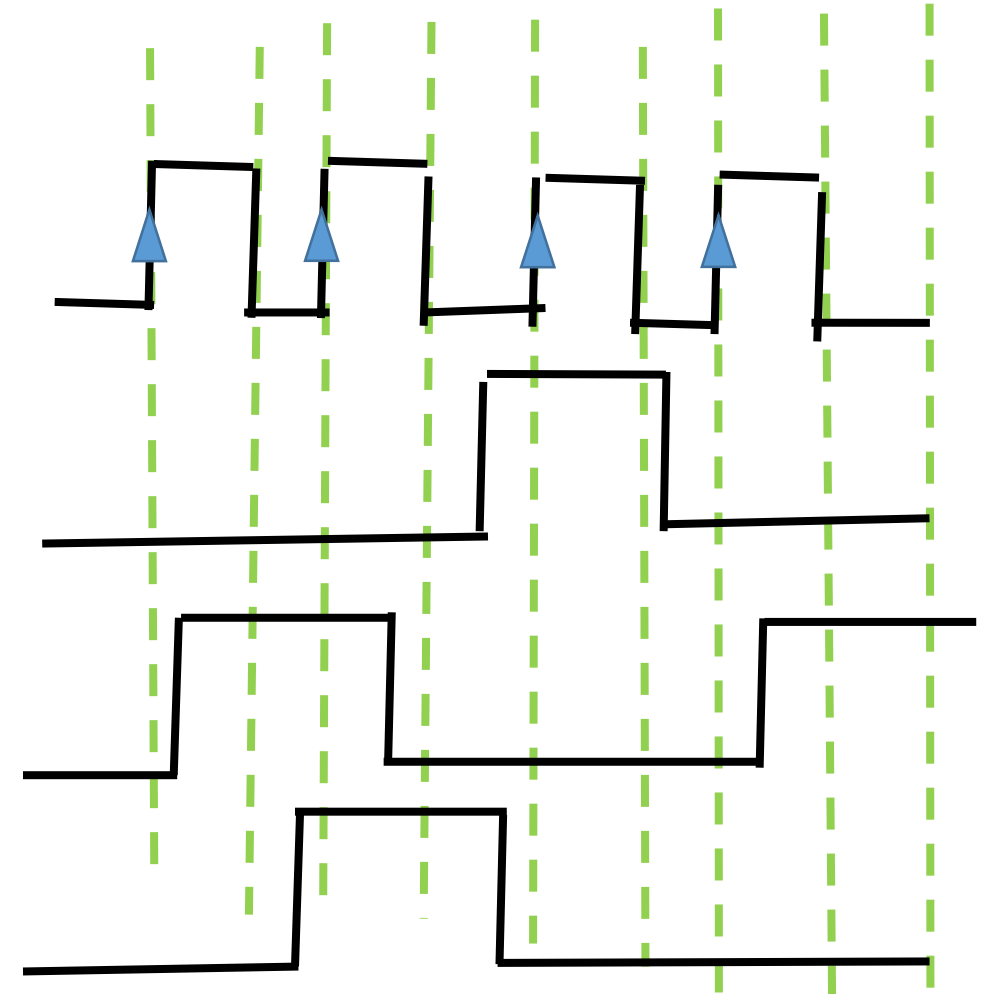
$$SR = 0$$

CLK

R

S

Q





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Make FF from each others

Example_7: Making the Flip flops

- WITH THE HELP OF D ff MAKE THE T TYPE

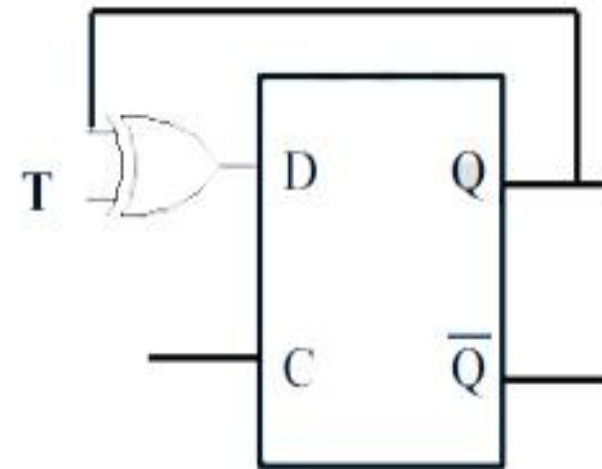
$$Q_{next} = D$$

D-FF equation : $Q^* = D$

T-FF equation : $Q^* = T \oplus Q$

$$D = T \oplus Q$$

$$Q_{next} = TQ' + T'Q$$



Example_8: Making the Flip flops



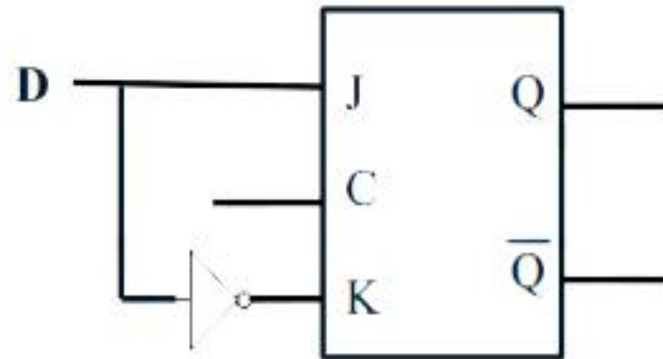
- WITH THE HELP OF JK ff MAKE THE D TYPE

$$Q_{next} = JQ' + K'Q$$

$$D = 0 \rightarrow J = 0, K = 1 \rightarrow Q^* = 0$$

$$D = 1 \rightarrow J = 1, K = 0 \rightarrow Q^* = 1$$

$$Q_{next} = D$$



Example_9: Making the Flip flops



- WITH THE HELP OF T FF make the JK ff

T-FF equation $Q^* = T \oplus Q$

$$T = Q^* \oplus Q$$

JK-FF equation $Q^* = J.\bar{Q} + \bar{K}.Q$

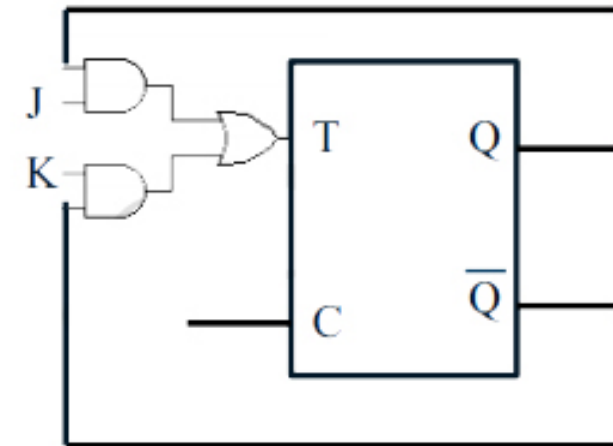
$$Q_{(next)} = JQ' + K'Q$$

$$T = (J.\bar{Q} + \bar{K}.Q) \oplus Q$$

$$T = \overline{(J.\bar{Q} + \bar{K}.Q) . Q + (J.\bar{Q} + \bar{K}.Q) . \bar{Q}}$$

$$T = (\bar{J} + Q).(K + \bar{Q}).Q + J.\bar{Q}$$

$$T = K.Q + J.\bar{Q}$$

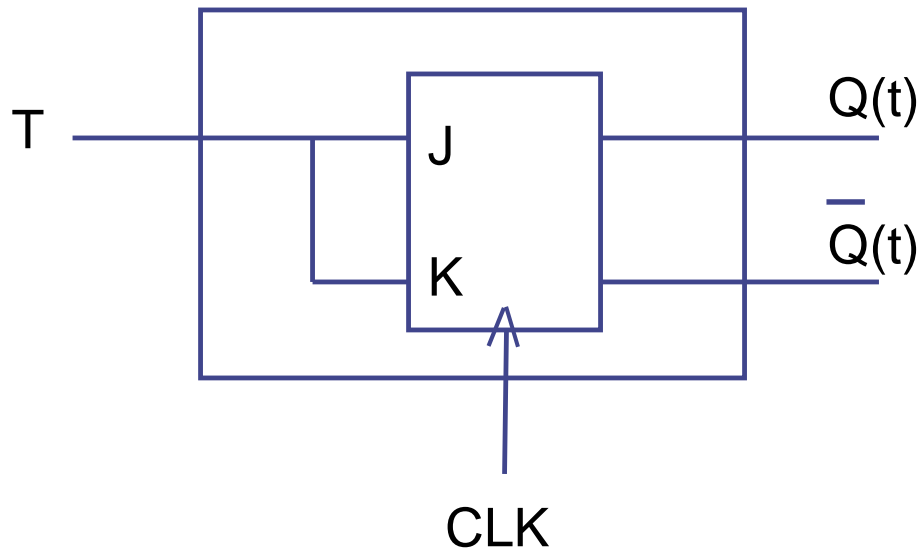


Example_4:

Make the T flip flop from JK FF

$$Q_{next} = JQ' + K'Q$$

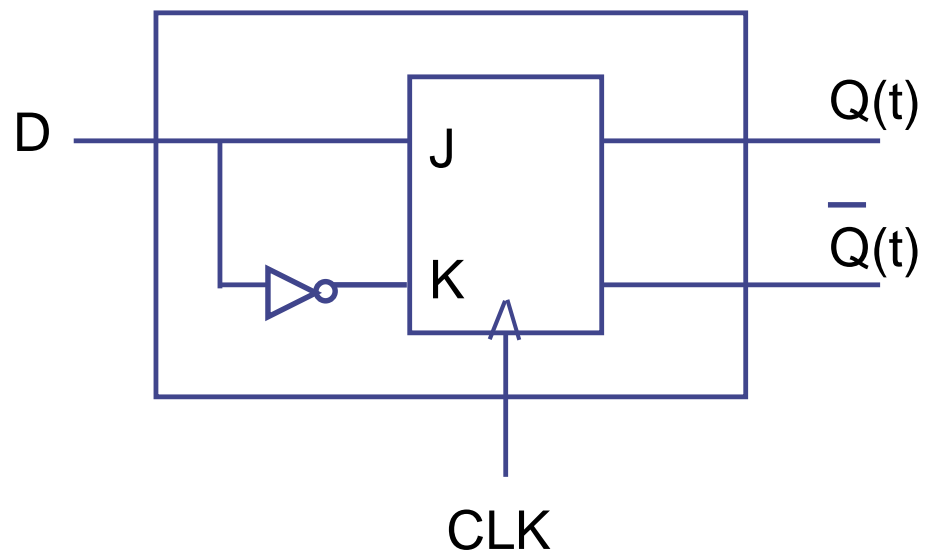
$$Q_{next} = TQ' + T'Q$$



T	J	K	Q(t+1)
0	0	0	Q(t)
1	1	1	$\overline{Q(t)}$

Example_5:

Make the D type flip flop From JK FF



$$Q_{next} = D$$

$$Q_{next} = JQ' + K'Q$$

D	J	K	Q(t+1)
0	0	1	Q(t)
1	1	0	$\overline{Q(t)}$

not



Example_6:



Make the JK FF from T type flip flop

Q(t)	J	K	T	Q(t+1)
0	0	0	0	0
0	0	1	0	0
0	1	0	1	1
0	1	1	1	1
1	0	0	0	1
1	0	1	1	0
1	1	0	0	1
1	1	1	1	0

