

# CS480

# Translators

LALR(1) Parsing/Ambiguous  
Grammars

Finish Chap. 4

shift-reduce - carry sets are disjoint  
 reduce, reduce LR(1) Parse...

$S' \rightarrow S$

1.  $S \rightarrow T \text{ else } F;$

2.  $T \rightarrow E$

3.  $T \rightarrow i;$

4.  $F \rightarrow E$

5.  $E \rightarrow E + i$

6.  $E \rightarrow i$

**Configuring set**

I0:  $S' \rightarrow \bullet S, \$$

$S \rightarrow \bullet T \text{ else } F;, \$$

$T \rightarrow \bullet E, \text{ else}$

$T \rightarrow \bullet i;, \text{ else}$

$E \rightarrow \bullet E + i, \text{ else}/+$

$E \rightarrow \bullet i, \text{ else}/+$

I1:  $S' \rightarrow S \bullet, \$$

I2:  $S \rightarrow T \bullet \text{ else } F;, \$$

I3:  $T \rightarrow E \bullet, \text{ else}$

$E \rightarrow E \bullet + i, \text{ else}/+$

I4:  $T \rightarrow i \bullet;, \text{ else}$

$E \rightarrow i \bullet, \text{ else}/+$

I5:  $S \rightarrow T \text{ else } \bullet F;, \$$

$F \rightarrow \bullet E, ;$

$E \rightarrow \bullet E + i, ;/+$

$E \rightarrow \bullet id, ;/+$

**Successor**

I1

I2

I3

I4

I3

I4

Accept

I5

Reduce 2

I6

I7

Reduce 6

I8

I9

I9

I10

**Configuring set**

I6:  $E \rightarrow E + \bullet i, \text{ else}/+$

I7:  $T \rightarrow i; \bullet, \text{ else}$

I8:  $S \rightarrow T \text{ else } F \bullet;, \$$

I9:  $F \rightarrow E \bullet, ;$

$E \rightarrow E \bullet + i, ;/+$

I10:  $E \rightarrow i \bullet, ;/+$

I11:  $E \rightarrow E + i \bullet, \text{ else}/+$

I12:  $S \rightarrow T \text{ else } F; \bullet, \$$

I13:  $E \rightarrow E + \bullet i, ;/+$

I14:  $E \rightarrow E + i \bullet, ;/+$

**Successor**

I11

Reduce 3

I12

Reduce 4

I13

Reduce 6

Reduce 5

Reduce 1

I14

Reduce 5

# LR(1) Parse Table...

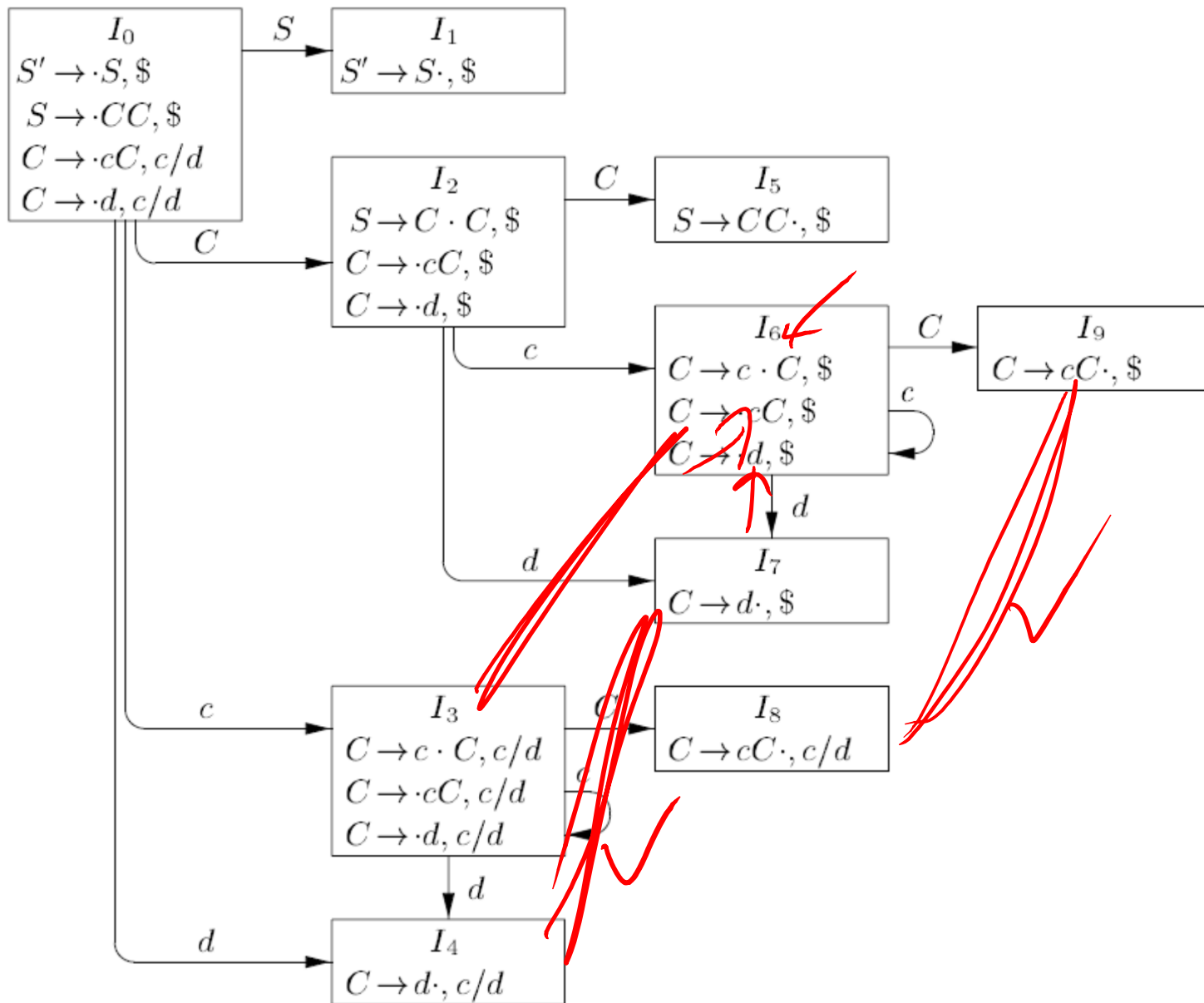
Stack	i	;	else	+	\$	S	T	F	E
0	s4					1	2		3
1					A				
2			s5						
3			R2	s6					
4		s7	r6	r6					
5	s10							8	9
6	s11								
7			r3						
8		s12							
9		r4		s6					
10		r6		r6					
11		r5	r5	r5					
12					r1				
13	s14								
14		r5		r5					

# LR(1) Conditions

1. For any item in the set  $[A \rightarrow \underline{u} \bullet x \underline{v}, a]$  with  $x$  as a terminal, there is no item in the set of the form  $[B \rightarrow \underline{v} \bullet, x]$ . In the action table, this translates no shift-reduce conflict for any state. The successor function for  $x$  either shifts to a new state or reduces, but not both.
2. The lookaheads for all complete items within the set must be disjoint, e.g. set cannot have both  $[A \rightarrow \underline{u} \bullet, a]$  and  $[B \rightarrow \underline{v} \bullet, a]$ . This translates to no reduce-reduce conflict on any state. If more than one non-terminal could be reduced from this set, it must be possible to uniquely determine which is appropriate from the next input token.

# LR(1) vs. LALR(1)

- LR(1) more powerful
- LALR(1) has less states



# LALR(1) Parse Table/Brute Force

STATE	ACTION			GOTO	
	<i>c</i>	<i>d</i>	\$	<i>S</i>	<i>C</i>
0	s <u>36</u>	s <u>47</u>		1	2
1			acc		
2	s36	s47			5
<u>36</u>	s36	s47			<u>89</u>
<u>47</u>	r3	r3	r3		
5			r1		
<u>89</u>	r2	r2	r2		

Figure 4.43: LALR parsing table for the grammar of Example 4.54

# LALR Parse...

$S' \rightarrow S$

1.  $S \rightarrow T \text{ else } F;$
2.  $T \rightarrow E$
3.  $T \rightarrow i;$
4.  $F \rightarrow E$
5.  $E \rightarrow E+i$
6.  $E \rightarrow i$

<i>Configuring set</i>	<i>Successor</i>	<i>Configuring set</i>	<i>Successor</i>
I0: $S' \rightarrow \bullet S, \$$	I1	I6: $E \rightarrow E+\bullet i, \text{ else}/+$	I11
$S \rightarrow \bullet T \text{ else } F;, \$$	I2	I7: $T \rightarrow i;\bullet, \text{ else}$	Reduce 3
$T \rightarrow \bullet E, \text{ else}$	I3	I8: $S \rightarrow T \text{ else } F\bullet;, \$$	I12
$T \rightarrow \bullet i;, \text{ else}$	I4	I9: $F \rightarrow E\bullet, ;$	Reduce 4
$E \rightarrow \bullet E+i, \text{ else}/+$	I3	$E \rightarrow E\bullet+i, ;/+$	I13
$E \rightarrow \bullet i, \text{ else}/+$	I4	I10: $E \rightarrow i\bullet, ;/+$	Reduce 6
I1: $S' \rightarrow S\bullet, \$$	Accept	I11: $E \rightarrow E+i\bullet, \text{ else}/+$	Reduce 5
I2: $S \rightarrow T\bullet \text{ else } F;, \$$	I5	I12: $S \rightarrow T \text{ else } F;\bullet, \$$	Reduce 1
I3: $T \rightarrow E\bullet, \text{ else}$	Reduce 2	I13: $E \rightarrow E+\bullet i, ;/+$	I14
$E \rightarrow E\bullet+i, \text{ else}/+$	I6	I14: $E \rightarrow E+i\bullet, ;/+$	Reduce 5
I4: $T \rightarrow i\bullet;, \text{ else}$	I7		
$E \rightarrow i\bullet, \text{ else}/+$	Reduce 6		
I5: $S \rightarrow T \text{ else } \bullet F;, \$$	I8		
$F \rightarrow \bullet E, ;$	I9		
$E \rightarrow \bullet E+i, ;/+$	I9		
$E \rightarrow \bullet id, ;/+$	I10		



# LALR Parse Table...

Stack	i	;	else	+	\$	S	T	F	E
0	s4					1	2		3
1					A				
2			s5						
3			r2	s613					
4		s7	r6	r6					
5	s10							8	9
613	s1114								
7			r3						
8		s12							
9		r4		s613					
10		r6		r6					
1114		r5	r5	r5					
12					r1				

# When LALR(1) fails...

$S' \rightarrow S$

$S \rightarrow aBc \mid bCc \mid aCd \mid bBd$

$B \rightarrow e$

$C \rightarrow e$

I0:  $S' \rightarrow \bullet S, \$$

$S \rightarrow \bullet aBc, \$$

$S \rightarrow \bullet bCc, \$$

$S \rightarrow \bullet aCd, \$$

$S \rightarrow \bullet bBd, \$$

I1:  $S' \rightarrow S\bullet, \$$

I2:  $S \rightarrow a\bullet Bc, \$$

$S \rightarrow a\bullet Cd, \$$

$B \rightarrow \bullet e, c$

$C \rightarrow \bullet e, d$

I3:  $S \rightarrow b\bullet Cc, \$$

$S \rightarrow b\bullet Bd, \$$

$C \rightarrow \bullet e, c$

$B \rightarrow \bullet e, d$

I4:  $S \rightarrow aB\bullet c, \$$

I5:  $S \rightarrow aC\bullet d, \$$

**I6:  $B \rightarrow e\bullet, c$**

**$C \rightarrow e\bullet, d$**

I7:  $S \rightarrow bC\bullet c, \$$

I8:  $S \rightarrow bB\bullet d, \$$

**I9:  $B \rightarrow e\bullet, d$**

**$C \rightarrow e\bullet, c$**

I10:  $S \rightarrow aBc\bullet, \$$

I11:  $S \rightarrow aCd\bullet, \$$

I12:  $S \rightarrow bCc\bullet, \$$

I13:  $S \rightarrow bBd\bullet, \$$

# LALR Table Construction

- Merge at the end vs. as you go

$S' \rightarrow S$

$S \rightarrow V = E$

$E \rightarrow F \mid E + F$

$F \rightarrow V \mid \text{int} \mid (E)$

$V \rightarrow \text{id}$

I0:  $S' \rightarrow \bullet S, \$$

$S \rightarrow \bullet V = E, \$$

$V \rightarrow \bullet \text{id}, =$

I1:  $S' \rightarrow S \bullet, \$$

I2:  $S' \rightarrow V \bullet = E, \$$

I3:  $V \rightarrow \text{id} \bullet, =$

I4:  $S \rightarrow V = \bullet E, \$$

$E \rightarrow \bullet F, \$/+$

$E \rightarrow \bullet E + F, \$/+$

$F \rightarrow \bullet V, \$/+$

$F \rightarrow \bullet \text{int}, \$/+$

$F \rightarrow \bullet (E), \$/+$

$V \rightarrow \bullet \text{id}, \$/+$

I5:  $S \rightarrow V = E \bullet, \$$

$E \rightarrow E \bullet + F, \$/+$

I6:  $E \rightarrow F \bullet, \$/+$

I7:  $F \rightarrow V \bullet, \$/+$

I8:  $F \rightarrow \text{int} \bullet, \$/+$

I9:  $F \rightarrow (\bullet E), \$/+$

$E \rightarrow \bullet F, )/+$

$E \rightarrow \bullet E + F, )/+$

$F \rightarrow \bullet V, )/+$

$F \rightarrow \bullet \text{int}, )/+$

$F \rightarrow \bullet (E), )/+$

$V \rightarrow \bullet \text{id}, )/+$

I10:  $F \rightarrow (E \bullet), \$/+$


$E \rightarrow E \bullet + F, )/+$

???? I11:  $E \rightarrow F \bullet, )/+$

???? I12:  $F \rightarrow V \bullet, )/+$


# Quiz #9

- Convince yourself (and me) that the ambiguous grammar for expressions is not LR(1).





$E \rightarrow E + E$   
 $\quad | E * E$   
 $\quad | (E)$   
 $\quad | \text{id}$

- Is the following grammar LR(1)? Is it LALR(1)?



$S \rightarrow Aa \mid bAc \mid Bc \mid bBa$   
 $A \rightarrow d$   
 $B \rightarrow d$

# Test 2 Review

- Difference between Top-Down and Bottom-Up Parsing
  - Derivation vs. Reduction
- What is a handle?
- Transforming Grammars
  - Left Recursion 
  - Left Factor 
- Determine if grammar is LL(1)
  - Calculate First and Follow
  - Build LL(1) Parse Table
- Determine if grammar is LR(0)
  - Build LR(0) Parse Table
- Determine if grammar is SLR(1)
  - Build SLR(1) Parse Table
- Determine if grammar is LR(1)
  - Build LR(1) Parse Table
  - Can it be LALR(1)???

no lookahead  
put reduce on all symbols  
can't have a shift or another reduce  
whole follow set  
① two reduce w/o disjoint follow  
② shift symbol can't be in follow