

CS480

Translators

LALR(1) Parsing/Ambiguous
Grammars

Finish Chap. 4

Odds and Ends

- Test Friday, 3/7
- Milestone 4???
- Dr. Stevenson speaks 3/3, Monday

~~white strings ops~~

Sunday night
-if, stdout

int → float for
float arith.

Extra credit +5

anything
but ints &
floats

type checking, e.g.

[+ string float]

Try this – Quiz 8...

- Determine if the Grammar is SLR(1) or LR(1)

① $S \rightarrow T \text{ else } F;$ $I_0: S' \rightarrow \cdot S, \$ \quad I_1$
 ② $T \rightarrow E$ $S \rightarrow \cdot T \text{ else } F; , \$ \quad I_2$
 ③ $T \rightarrow i;$ $T \rightarrow \cdot E, \text{ else } \quad I_3$
 ④ $F \rightarrow E$ $T \rightarrow \cdot i, \text{ else } \quad I_4$
 ⑤ $E \rightarrow E + i$ $E \rightarrow \cdot E + i, \text{ else } \quad I_3$ $E \rightarrow \cdot E + i, + \quad I_3$
 ⑥ $E \rightarrow i$ $E \rightarrow \cdot i, \text{ else } \quad I_4$ $E \rightarrow \cdot i, + \quad I_4$

- Construct a parse table for the grammar
- Add 2 questions for Dr. Stevenson on languages, compilers, or AI

LR(1) Parse...

$S' \rightarrow S$

1. $S \rightarrow T \text{ else } F;$
2. $T \rightarrow E$
3. $T \rightarrow i;$
4. $F \rightarrow E$
5. $E \rightarrow E + i$
6. $E \rightarrow i$

<i>Configuring set</i>	<i>Successor</i>	<i>Configuring set</i>	<i>Successor</i>
I0: $S' \rightarrow \bullet S, \$$	I1	I6: $E \rightarrow E + \bullet i, \text{ else } /+$	I11
$S \rightarrow \bullet T \text{ else } F;, \$$	I2	I7: $T \rightarrow i; \bullet, \text{ else}$	Reduce 3
$T \rightarrow \bullet E, \text{ else}$	I3	I8: $S \rightarrow T \text{ else } F \bullet;, \$$	I12
$T \rightarrow \bullet i;, \text{ else}$	I4	I9: $F \rightarrow E \bullet, ;$	Reduce 4
$E \rightarrow \bullet E + i, \text{ else } /+$	I3	$E \rightarrow E \bullet + i, ; /+$	I13
$E \rightarrow \bullet i, \text{ else } /+$	I4	I10: $E \rightarrow i \bullet, ; /+$	Reduce 6
I1: $S' \rightarrow S \bullet, \$$	Accept	I11: $E \rightarrow E + i \bullet, \text{ else } /+$	Reduce 5
I2: $S \rightarrow T \bullet \text{ else } F;, \$$	I5	I12: $S \rightarrow T \text{ else } F; \bullet, \$$	Reduce 1
I3: $T \rightarrow E \bullet, \text{ else}$	Reduce 2	I13: $E \rightarrow E + \bullet i, ; /+$	I14
$E \rightarrow E \bullet + i, \text{ else } /+$	I6	I14: $E \rightarrow E + i \bullet, ; /+$	Reduce 5
I4: $T \rightarrow i \bullet;, \text{ else}$	I7		
$E \rightarrow i \bullet, \text{ else } /+$	Reduce 6		
I5: $S \rightarrow T \text{ else } \bullet F;, \$$	I8		
$F \rightarrow \bullet E, ;$	I9		
$E \rightarrow \bullet E + i, ; /+$	I9		
$E \rightarrow \bullet id, ; /+$	I10		

LR(1) Parse Table...

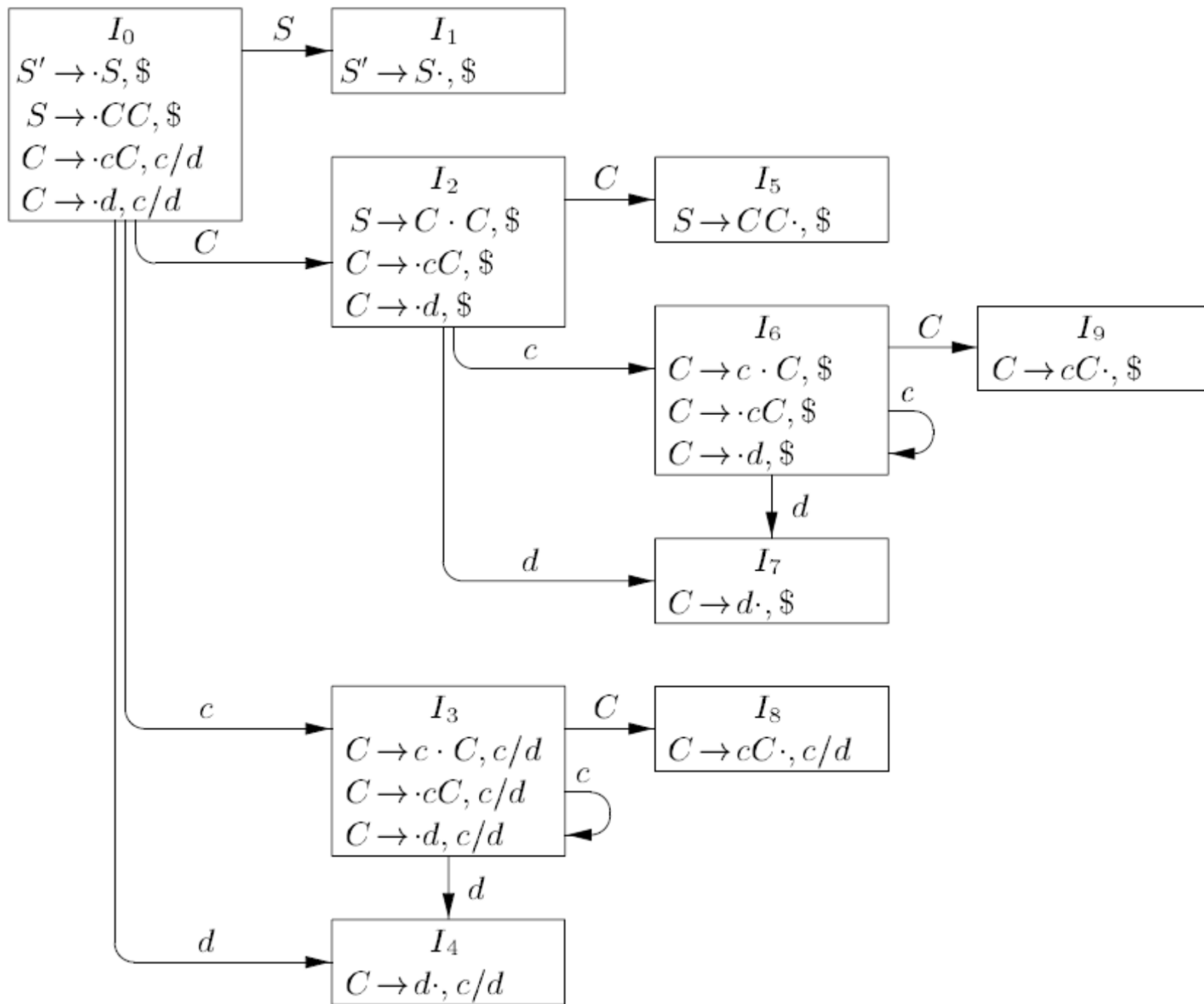
Stack	i	;	else	+	\$	S	T	F	E
0	s4					1	2		3
1					A				
2			s5						
3			R2	s6					
4		s7	r6	r6					
5	s10							8	9
6	s11								
7			r3						
8		s12							
9		r4		s6					
10		r6		r6					
11		r5	r5	r5					
12					r1				
13	s14								
14		r5		r5					

LR(1) Conditions

1. For any item in the set $[A \rightarrow \underline{u} \bullet x \underline{v}, a]$ with x as a terminal, there is no item in the set of the form $[B \rightarrow \underline{v} \bullet, x]$. In the action table, this translates no shift-reduce conflict for any state. The successor function for x either shifts to a new state or reduces, but not both.
2. The lookaheads for all complete items within the set must be disjoint, e.g. set cannot have both $[A \rightarrow \underline{u} \bullet, a]$ and $[B \rightarrow \underline{v} \bullet, a]$. This translates to no reduce-reduce conflict on any state. If more than one non-terminal could be reduced from this set, it must be possible to uniquely determine which is appropriate from the next input token.

LR(1) vs. LALR(1)

- LR(1) more powerful
- LALR(1) has less states



LALR(1) Parse Table/Brute Force

STATE	ACTION			GOTO	
	<i>c</i>	<i>d</i>	\$	<i>S</i>	<i>C</i>
0	s36	s47		1	2
1			acc		
2	s36	s47			5
36	s36	s47			89
47	r3	r3	r3		
5			r1		
89	r2	r2	r2		

Figure 4.43: LALR parsing table for the grammar of Example 4.54

LALR Parse...

$S' \rightarrow S$

1. $S \rightarrow T \text{ else } F;$
2. $T \rightarrow E$
3. $T \rightarrow i;$
4. $F \rightarrow E$
5. $E \rightarrow E+i$
6. $E \rightarrow i$

<i>Configurating set</i>	<i>Successor</i>	<i>Configurating set</i>	<i>Successor</i>
I0: $S' \rightarrow \bullet S, \$$	I1	I6: $E \rightarrow E+\bullet i, \text{ else}/+$	I11
$S \rightarrow \bullet T \text{ else } F;, \$$	I2	I7: $T \rightarrow i;\bullet, \text{ else}$	Reduce 3
$T \rightarrow \bullet E, \text{ else}$	I3	I8: $S \rightarrow T \text{ else } F\bullet;, \$$	I12
$T \rightarrow \bullet i;, \text{ else}$	I4	I9: $F \rightarrow E\bullet, ;$	Reduce 4
$E \rightarrow \bullet E+i, \text{ else}/+$	I3	$E \rightarrow E\bullet+i, ;/+$	I13
$E \rightarrow \bullet i, \text{ else}/+$	I4	I10: $E \rightarrow i\bullet, ;/+$	Reduce 6
I1: $S' \rightarrow S\bullet, \$$	Accept	I11: $E \rightarrow E+i\bullet, \text{ else}/+$	Reduce 5
I2: $S \rightarrow T\bullet \text{ else } F;, \$$	I5	I12: $S \rightarrow T \text{ else } F;\bullet, \$$	Reduce 1
I3: $T \rightarrow E\bullet, \text{ else}$	Reduce 2	I13: $E \rightarrow E+\bullet i, ;/+$	I14
$E \rightarrow E\bullet+i, \text{ else}/+$	I6	I14: $E \rightarrow E+i\bullet, ;/+$	Reduce 5
I4: $T \rightarrow i\bullet;, \text{ else}$	I7		
$E \rightarrow i\bullet, \text{ else}/+$	Reduce 6		
I5: $S \rightarrow T \text{ else } \bullet F;, \$$	I8		
$F \rightarrow \bullet E, ;$	I9		
$E \rightarrow \bullet E+i, ;/+$	I9		
$E \rightarrow \bullet id, ;/+$	I10		

LALR Parse Table...

Stack	i	;	else	+	\$	S	T	F	E
0	s4					1	2		3
1					A				
2			s5						
3			r2	s613					
4		s7	r6	r6					
5	s10							8	9
613	s1114								
7			r3						
8		s12							
9		r4		s613					
10		r6		r6					
1114		r5	r5	r5					
12					r1				

When LALR(1) fails...

$S' \rightarrow S$

$S \rightarrow aBc \mid bCc \mid aCd \mid bBd$

$B \rightarrow e$

$C \rightarrow e$

I0: $S' \rightarrow \bullet S, \$$

$S \rightarrow \bullet aBc, \$$

$S \rightarrow \bullet bCc, \$$

$S \rightarrow \bullet aCd, \$$

$S \rightarrow \bullet bBd, \$$

I1: $S' \rightarrow S\bullet, \$$

I2: $S \rightarrow a\bullet Bc, \$$

$S \rightarrow a\bullet Cd, \$$

$B \rightarrow \bullet e, c$

$C \rightarrow \bullet e, d$

I3: $S \rightarrow b\bullet Cc, \$$

$S \rightarrow b\bullet Bd, \$$

$C \rightarrow \bullet e, c$

$B \rightarrow \bullet e, d$

I4: $S \rightarrow aB\bullet c, \$$

I5: $S \rightarrow aC\bullet d, \$$

I6: $B \rightarrow e\bullet, c$

$C \rightarrow e\bullet, d$

I7: $S \rightarrow bC\bullet c, \$$

I8: $S \rightarrow bB\bullet d, \$$

I9: $B \rightarrow e\bullet, d$

$C \rightarrow e\bullet, c$

I10: $S \rightarrow aBc\bullet, \$$

I11: $S \rightarrow aCd\bullet, \$$

I12: $S \rightarrow bCc\bullet, \$$

I13: $S \rightarrow bBd\bullet, \$$

LALR Table Construction

- Merge at the end vs. as you go

$S' \rightarrow S$

$S \rightarrow V = E$

$E \rightarrow F \mid E + F$

$F \rightarrow V \mid \text{int} \mid (E)$

$V \rightarrow \text{id}$

I0: $S' \rightarrow \bullet S, \$$

$S \rightarrow \bullet V = E, \$$

$V \rightarrow \bullet \text{id}, =$

I1: $S' \rightarrow S \bullet, \$$

I2: $S' \rightarrow V \bullet = E, \$$

I3: $V \rightarrow \text{id} \bullet, =$

I4: $S \rightarrow V = \bullet E, \$$

$E \rightarrow \bullet F, \$/+$

$E \rightarrow \bullet E + F, \$/+$

$F \rightarrow \bullet V, \$/+$

$F \rightarrow \bullet \text{int}, \$/+$

$F \rightarrow \bullet (E), \$/+$

$V \rightarrow \bullet \text{id}, \$/+$

I5: $S \rightarrow V = E \bullet, \$$

$E \rightarrow E \bullet + F, \$/+$

I6: $E \rightarrow F \bullet, \$/+$

I7: $F \rightarrow V \bullet, \$/+$

I8: $F \rightarrow \text{int} \bullet, \$/+$

I9: $F \rightarrow (\bullet E), \$/+$

$E \rightarrow \bullet F,)/+$

$E \rightarrow \bullet E + F,)/+$

$F \rightarrow \bullet V,)/+$

$F \rightarrow \bullet \text{int},)/+$

$F \rightarrow \bullet (E),)/+$

$V \rightarrow \bullet \text{id},)/+$

I10: $F \rightarrow (E \bullet), \$/+$

$E \rightarrow E \bullet + F,)/+$

???? I11: $E \rightarrow F \bullet,)/+$

???? I12: $F \rightarrow V \bullet,)/+$