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# Lab07 - optimalization exercises,

## Pawel Drapiewski 17.04.2018 r.

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## 1st excercise from Optimalization\_problem-s.pdf

```
%  
%  
%  
% x |  
%  /\ /\ /\ /\ /\ /\ /\ /\  
%  /\ /\ River /\ /\ /\  
%  
% Fence length = 2400  
  
% solving the problem using gp option  
clear all;  
close all;  
  
cvx_begin gp  
variables x y  
maximize x * y  
subject to  
    2 * x + y <= 2400  
cvx_end  
  
fprintf('x = %4.2f, y = %4.2f \n', x, y)  
fprintf('GP solution %4.2f \n', x * y)  
  
% this problem using logaritms  
clear all;  
close all;  
  
cvx_begin
```

```

variables  a b
maximize  a + b
subject to
    log(2 * exp(a) + exp(b)) <= log(2400)

cvx_end

x = exp(a);
y = exp(b);

fprintf('x = %4.2f, y = %4.2f \n', x, y)
fprintf('Logarithm solution %4.2f \n', x * y)

% Result
% In both cases the results are good

```

Successive approximation method to be employed.  
 SDPT3 will be called several times to refine the solution.  
 Original size: 10 variables, 3 equality constraints  
 2 exponentials add 16 variables, 10 equality constraints

Cones		Errors				
Mov	Act	Centering	Exp cone	Poly cone	Status	
2/	2	6.133e-01	2.918e-02	0.000e+00	Solved	
2/	2	7.273e-02	3.967e-04	0.000e+00	Solved	
2/	2	6.470e-03	3.127e-06	0.000e+00	Solved	
2/	2	5.528e-04	2.267e-08	0.000e+00	Solved	
0/	2	4.705e-05	1.171e-12	0.000e+00	Solved	

Status: Solved  
 Optimal value (cvx\_optval): +720000

x = 600.00, y = 1200.00  
 GP solution 720000.00  
 CVX Warning:

Models involving "log" or other functions in the log, exp, and entropy family are solved using an experimental successive approximation method.  
 This method is slower and less reliable than the method CVX employs for other models. Please see the section of the user's guide entitled [The successive approximation method](file:///C:/Users/drape/OneDrive/Documents/MATLAB/Teoria_optymalizacji/cvx/doc/advanced.html#the-successive-approximation-method) for more details about the approach, and for instructions on how to suppress this warning message in the future.

Successive approximation method to be employed.  
 SDPT3 will be called several times to refine the solution.  
 Original size: 9 variables, 3 equality constraints  
 2 exponentials add 16 variables, 10 equality constraints

```
-----
Cones  /
Mov/Act / Centering  Errors
                        Exp cone   Poly cone / Status
-----+-----+-----
  2/  2 / 6.133e-01  2.918e-02  0.000e+00 / Solved
  2/  2 / 7.273e-02  3.967e-04  0.000e+00 / Solved
  2/  2 / 6.470e-03  3.127e-06  0.000e+00 / Solved
  2/  2 / 5.527e-04  2.254e-08  0.000e+00 / Solved
  0/  0 / 4.464e-05  0.000e+00  0.000e+00 / Solved
-----
```

Status: Solved

Optimal value (cvx\_optval): +13.487

x = 600.00, y = 1200.00

Logarithm solution 720000.00

## 2nd excercise from Optimization\_problem-s.pdf

```
% #####
% ##### - building
% |
% | y
% ----- - fence
%      x
%
% Fence is 500 feet long
% Problem: Find the largest area

% Solution using gp
clear, close all

cvx_begin gp
variables x y
maximize x * y
subject to
    2 * y + x <= 500
cvx_end

fprintf('x = %4.2f, y = %4.2f \n', x, y)
fprintf('GP solution %4.2f \n', x * y)

% Solution using Logarithms
clear, close all

cvx_begin
variables log_x log_y
maximize log_x + log_y
subject to
    log(exp(log_x) + 2*exp(log_y)) <= log(500)
cvx_end
```

```
x = exp(log_x);
y = exp(log_y);

fprintf('x = %4.2f, y = %4.2f \n', x, y)
fprintf('Logarithm solution %4.2f \n', x * y)

% Results
% In both cases the result is the good optimal result
```

Successive approximation method to be employed.

SDPT3 will be called several times to refine the solution.

Original size: 10 variables, 3 equality constraints

2 exponentials add 16 variables, 10 equality constraints

```
-----
Cones  |           Errors           |
Mov/Act | Centering  Exp cone  Poly cone | Status
-----+-----+-----+-----
2/  2 | 6.133e-01  2.918e-02  0.000e+00 | Solved
2/  2 | 7.273e-02  3.967e-04  0.000e+00 | Solved
2/  2 | 6.470e-03  3.127e-06  0.000e+00 | Solved
2/  2 | 5.528e-04  2.267e-08  0.000e+00 | Solved
0/  2 | 4.705e-05  1.171e-12  0.000e+00 | Solved
-----
```

Status: Solved

Optimal value (cvx\_optval): +31250

x = 250.00, y = 125.00

GP solution 31250.00

Successive approximation method to be employed.

SDPT3 will be called several times to refine the solution.

Original size: 9 variables, 3 equality constraints

2 exponentials add 16 variables, 10 equality constraints

```
-----
Cones  |           Errors           |
Mov/Act | Centering  Exp cone  Poly cone | Status
-----+-----+-----+-----
2/  2 | 6.133e-01  2.918e-02  0.000e+00 | Solved
2/  2 | 7.273e-02  3.967e-04  0.000e+00 | Solved
2/  2 | 6.470e-03  3.127e-06  0.000e+00 | Solved
2/  2 | 5.527e-04  2.254e-08  0.000e+00 | Solved
0/  0 | 4.464e-05  0.000e+00  0.000e+00 | Solved
-----
```

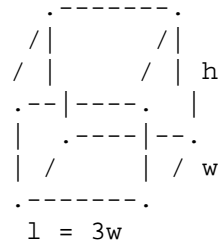
Status: Solved

Optimal value (cvx\_optval): +10.3498

x = 250.00, y = 125.00

Logarithm solution 31250.00

## 3rd exercise from Optimization\_problem-s.pdf



top and bottom material cost = \$10 per ft<sup>2</sup> sides material cost = \$6 per ft<sup>2</sup>

```
% GP solution
clear, close all

cvx_begin gp
variables w
minimize 60 * w * w + 800 / w
subject to
    w <= 1 % because lhw <= 50 we can write as 50w^4 < 50, so w <= 1
cvx_end

h = 50 / 3 * w * w;
l = 3 * w;

fprintf('w = %4.2f, h = %4.2f, l = %4.2f \n', w, h, l)
fprintf('GP solution %4.2f \n', 60 * w^2 + 48 * w * h)
fprintf('Box volume %4.2f \n', l * h * w)

% Logarithm solution
clear, close all

cvx_begin
variables log_w
minimize 60 * exp(log_w) * exp(log_w) + 800 / exp(log_w)
subject to
    exp(log_w) <= log(1)
cvx_end

w = exp(log_w);
h = 50 / ( 3 * w * w);
l = 3 * w;

fprintf('w = %4.2f, h = %4.2f, l = %4.2f \n', w, h, l)
fprintf('Logarithm solution %4.2f \n', 60 * w^2 + 48 * w * h)
fprintf('Box volume %4.2f \n', l * h * w)

% Results
% The Logarithm optimization found good value and GP not, not even
close
```

% enough

Successive approximation method to be employed.

SDPT3 will be called several times to refine the solution.

Original size: 10 variables, 4 equality constraints

2 exponentials add 16 variables, 10 equality constraints

```
-----
Cones  |           Errors           |
Mov/Act | Centering  Exp cone   Poly cone | Status
-----+-----+-----+-----
2/  2 | 2.753e+00  5.599e-01  0.000e+00 | Solved
2/  2 | 8.717e-02  5.065e-04  0.000e+00 | Solved
2/  2 | 2.987e-03  5.867e-07  0.000e+00 | Solved
0/  1 | 1.532e-04  9.313e-10  0.000e+00 | Solved
-----
```

Status: Solved

Optimal value (cvx\_optval): +860

w = 1.00, h = 16.67, l = 3.00

GP solution 860.00

Box volume 50.00

Successive approximation method to be employed.

SDPT3 will be called several times to refine the solution.

Original size: 10 variables, 4 equality constraints

2 exponentials add 16 variables, 10 equality constraints

```
-----
Cones  |           Errors           |
Mov/Act | Centering  Exp cone   Poly cone | Status
-----+-----+-----+-----
2/  2 | 1.048e+00  8.094e-02  0.000e+00 | Solved
2/  2 | 5.885e-02  2.501e-04  0.000e+00 | Solved
2/  2 | 3.838e-03  1.033e-06  0.000e+00 | Solved
0/  2 | 2.576e-04  4.745e-09  0.000e+00 | Solved
-----
```

Status: Solved

Optimal value (cvx\_optval): +637.595

w = 1.88, h = 4.71, l = 5.65

Logarithm solution 637.60

Box volume 50.00

## 4th exercise from Optimalization\_problem-s.pdf

```

      .----- .
      / |      / |
      / |      / | h
      .--|-----|
      | .-----|--.
      | /      | / w

```

.-----.  
l = w

We have only 10 m<sup>2</sup> of material

```
% Solution
clear, close all

cvx_begin gp
variables w h
maximize w * w * h % what is V = lwh
subject to
    2 * w * w + 4 * w * h <= 10
cvx_end

h = (5 - w * w) / (2 * w);
l = w;

fprintf('w = %4.2f, h = %4.2f, l = %4.2f \n', w, h, l)
fprintf('Box volume %4.2f \n', l * h * w)
```

Successive approximation method to be employed.

SDPT3 will be called several times to refine the solution.

Original size: 13 variables, 3 equality constraints

2 exponentials add 16 variables, 10 equality constraints

Cones		Errors				
Mov/Act	Centering	Exp cone	Poly cone	Status		
2/ 2	1.030e+00	8.095e-02	0.000e+00	Solved		
2/ 2	6.350e-02	2.917e-04	0.000e+00	Solved		
2/ 2	5.248e-03	2.044e-06	0.000e+00	Solved		
0/ 2	3.890e-04	9.348e-09	0.000e+00	Solved		

Status: Solved

Optimal value (cvx\_optval): +2.15166

w = 1.29, h = 1.29, l = 1.29

Box volume 2.15

## 5th exercise from Optimization\_problems.pdf

Make cylinder that hold 1.5 liters of liquid. Minimize the dimensions

```
% Solution
clear, close all

cvx_begin gp
variables h r
minimize 2 * pi * r * r + 2 * pi * r * h
```

```

subject to
    pi * r * r * h == 1500
cvx_end

fprintf('h = %4.2f, r = %4.2f \n', h, r)
fprintf('Needed material [m^2]: %4.2f \n', 2 * pi * r * r + 2 * pi * r
    * h)
fprintf('Valume of the cylider needed: %4.2f \n', pi * r * r * h)

```

*Successive approximation method to be employed.*

*SDPT3 will be called several times to refine the solution.*

*Original size: 12 variables, 3 equality constraints*

*2 exponentials add 16 variables, 10 equality constraints*

---

Cones		Errors				
Mov/Act		Centering	Exp cone	Poly cone		Status
<hr/>						
2/	2	1.048e+00	8.095e-02	0.000e+00		Solved
2/	2	5.885e-02	2.501e-04	0.000e+00		Solved
2/	2	3.840e-03	1.032e-06	0.000e+00		Solved
0/	2	2.577e-04	4.672e-09	0.000e+00		Solved

---

Status: Solved

Optimal value (cvx\_optval): +725.396

$h = 12.41, r = 6.20$

Needed material [m<sup>2</sup>]: 725.40

Valume of the cylider needed: 1500.00

## 6th excercise from Optimalization\_problem-s.pdf

```
clear, close all;
```

```

cvx_begin gp
variables x y h
maximize x * y * h
subject to
    x + 2 * h <= 14
    y + 2 * h <= 10
cvx_end

```

```
fprintf('x=%2.4f, y=%2.4f, h=%2.4f \n', x, y, h)
```

```
fprintf('Result: %2.4f \n', x * y * h)
```

*Successive approximation method to be employed.*

*SDPT3 will be called several times to refine the solution.*

*Original size: 19 variables, 7 equality constraints*

*4 exponentials add 32 variables, 20 equality constraints*

---

Cones		Errors				

---



```

Mov/Act | Centering  Exp cone  Poly cone | Status
-----+-----+-----+-----
 4/  4 | 1.230e+00  1.146e-01  0.000e+00 | Solved
 4/  4 | 6.665e-02  3.307e-04  0.000e+00 | Solved
 4/  4 | 5.780e-03  2.481e-06  0.000e+00 | Solved
 0/  4 | 4.386e-04  1.402e-08  0.000e+00 | Solved
-----
Status: Solved
Optimal value (cvx_optval): +120.164

x=10.1633, y=6.1633, h=1.9184
Result: 120.1644

```

## 7th excercise from Optimization\_problem-s.pdf

Print sheet: .-----, | 2 inch | - outter rectangle is template | ----- | - inner rectangle is print area 1 1  
| \_\_\_\_ | |1.5 inch | .-----.

Maximize the printed area Whole template have 200 in<sup>2</sup> area.

```

% Solution
clear, close all;

cvx_begin
variables log_with_w log_with_h
maximize log_with_w + log_with_h % original: (w - 2) * (h - 3.5)
subject to
    log((exp(log_with_w) + 2) * (exp(log_with_h) + 3.5)) <= log(200);
cvx_end

w = exp(log_with_w) + 2;
h = exp(log_with_h) + 3.5;

fprintf('w=%2.4f, h=%2.4f \n', w, h)
fprintf('Maximized printed area: %2.4f \n', (w - 2) * (h - 3.5))
fprintf('Template area %2.4f \n', w * h);

```

Successive approximation method to be employed.

SDPT3 will be called several times to refine the solution.

Original size: 17 variables, 7 equality constraints

4 exponentials add 32 variables, 20 equality constraints

```

-----
Cones   |
Mov/Act | Centering  Exp cone  Poly cone | Status
-----+-----+-----+-----
 4/  4 | 1.654e+00  2.048e-01  0.000e+00 | Solved
 4/  4 | 5.087e-02  1.898e-04  0.000e+00 | Solved
 4/  4 | 3.978e-03  1.157e-06  0.000e+00 | Solved
 0/  2 | 3.012e-04  6.567e-09  0.000e+00 | Solved
-----
Status: Solved

```

Optimal value (cvx\_optval): +4.88407

w=10.6904, h=18.7083

Maximized printed area: 132.1669

Template area 200.0000

## 8th exercise from Optimization\_problem-s.pdf

```
clear, close all;

cvx_begin
variables r h
maximize 12 * r - (2 + pi/2) * r^2
subject to
    2*h + 2*r + pi*r == 12;
cvx_end

fprintf('r=%2.4f, h=%2.4f \n', r, h)
fprintf('Window surface: %2.4f \n', 12 * r - (2 + pi/2) * r^2)
```

Calling SDPT3 4.0: 3 variables, 1 equality constraints

```
-----
num. of constraints = 1
dim. of sdp var = 2, num. of sdp blk = 1
*****
SDPT3: Infeasible path-following algorithms
*****
version predcorr gam expon scale_data
HKM      1      0.000 1      0
it pstep dstep pinfeas dinfeas gap      prim-obj      dual-obj
cputime
-----
0/0.000/0.000/4.5e+00/1.5e+00/2.0e+02/ 3.570796e+01 0.000000e+00/
0:0:00/ chol 1 1
1/0.868/1.000/5.9e-01/1.4e-02/9.4e+00/-1.720249e+01 -1.169740e+01/
0:0:00/ chol 1 1
2/0.992/1.000/4.8e-03/1.4e-03/6.6e-01/-1.012252e+01 -1.064597e+01/
0:0:00/ chol 1 1
3/0.982/0.988/8.6e-05/1.8e-04/9.5e-03/-1.008255e+01 -1.008518e+01/
0:0:00/ chol 1 1
4/0.960/0.982/3.5e-06/1.8e-05/2.2e-04/-1.008182e+01 -1.008148e+01/
0:0:00/ chol 1 1
5/0.941/0.974/2.1e-07/4.9e-07/9.3e-06/-1.008179e+01 -1.008178e+01/
0:0:00/ chol 1 1
6/0.989/0.988/2.3e-09/7.4e-09/4.8e-07/-1.008178e+01 -1.008178e+01/
0:0:00/ chol 1 1
7/1.000/1.000/0.0e+00/1.8e-10/5.5e-08/-1.008178e+01 -1.008178e+01/
0:0:00/
stop: max(relative gap, infeasibilities) < 1.49e-08
```

```
-----
number of iterations      = 7
primal objective value = -1.00817847e+01
dual  objective value = -1.00817848e+01
gap := trace(XZ)         = 5.53e-08
relative gap             = 2.61e-09
actual relative gap      = 2.37e-09
rel. primal infeas (scaled problem) = 0.00e+00
rel. dual      "      "      "      = 1.82e-10
rel. primal infeas (unscaled problem) = 0.00e+00
rel. dual      "      "      "      = 0.00e+00
norm(X), norm(Y), norm(Z) = 3.8e+00, 1.0e+01, 1.4e+01
norm(A), norm(b), norm(C) = 2.0e+00, 2.0e+00, 1.0e+01
Total CPU time (secs) = 0.39
CPU time per iteration = 0.06
termination code      = 0
DIMACS: 0.0e+00  0.0e+00  2.7e-10  0.0e+00  2.4e-09  2.6e-09
-----
```

```
-----
Status: Solved
Optimal value (cvx_optval): +10.0818
```

```
r=1.6803, h=1.6802
Window surface: 10.0818
```

## 9th exercise from Optimization\_problem-s.pdf

```
% The biggest possible rectangle drawn into circle of radius 4
% x, y - sides of the rectangle

% Solution
clear, close all;

cvx_begin
variables v
maximize 256 * v - 16 * v * v
subject to
    - v <= 0
cvx_end

u = 16 - v;
x = sqrt(u);
y = sqrt(v);

fprintf('x=%2.4f, y=%2.4f \n', x, y)
fprintf('Rectnalg area: %2.4f \n', 2 * x + 2 * y)
```

```
Calling SDPT3 4.0: 4 variables, 2 equality constraints
For improved efficiency, SDPT3 is solving the dual problem.
```

```

-----
num. of constraints = 2
dim. of sdp var = 2, num. of sdp blk = 1
dim. of linear var = 1
*****
SDPT3: Infeasible path-following algorithms
*****
version predcorr gam expon scale_data
HKM 1 0.000 1 0
it pstep dstep pinfeas dinfeas gap prim-obj dual-obj
cputime
-----
0/0.000/0.000/1.7e+00/8.4e+00/5.5e+03/ 2.129058e+02 0.000000e+00/
0:0:00/ chol 1 1
1/0.804/0.819/3.3e-01/1.6e+00/5.0e+02/ 2.619005e+02 1.224143e+03/
0:0:00/ chol 1 1
2/0.622/0.630/1.2e-01/5.9e-01/2.0e+02/ 5.178792e+02 1.252930e+03/
0:0:00/ chol 1 1
3/0.669/0.631/4.1e-02/2.2e-01/9.1e+01/ 7.923507e+02 1.180887e+03/
0:0:00/ chol 1 1
4/0.818/0.688/7.5e-03/6.9e-02/2.9e+01/ 9.806937e+02 1.092807e+03/
0:0:00/ chol 1 1
5/1.000/0.998/4.6e-08/7.1e-04/4.8e+00/ 1.027793e+03 1.023820e+03/
0:0:00/ chol 1 1
6/0.970/1.000/3.4e-09/7.0e-05/1.1e-01/ 1.024091e+03 1.024060e+03/
0:0:00/ chol 1 1
7/0.939/1.000/1.1e-09/6.8e-10/1.0e-02/ 1.024006e+03 1.023996e+03/
0:0:00/ chol 1 1
8/0.980/0.982/1.8e-10/2.3e-10/2.4e-04/ 1.024000e+03 1.024000e+03/
0:0:00/ chol 1 1
9/0.988/0.989/3.6e-12/3.8e-11/2.8e-06/ 1.024000e+03 1.024000e+03/
0:0:00/
stop: max(relative gap, infeasibilities) < 1.49e-08
-----
number of iterations = 9
primal objective value = 1.02400000e+03
dual objective value = 1.02400000e+03
gap := trace(XZ) = 2.83e-06
relative gap = 1.38e-09
actual relative gap = 1.39e-09
rel. primal infeas (scaled problem) = 3.63e-12
rel. dual " " " = 3.81e-11
rel. primal infeas (unscaled problem) = 0.00e+00
rel. dual " " " = 0.00e+00
norm(X), norm(Y), norm(Z) = 1.0e+03, 6.4e+01, 6.5e+01
norm(A), norm(b), norm(C) = 3.0e+00, 2.6e+02, 2.0e+00
Total CPU time (secs) = 0.29
CPU time per iteration = 0.03
termination code = 0
DIMACS: 3.6e-12 0.0e+00 3.8e-11 0.0e+00 1.4e-09 1.4e-09
-----

```

Status: Solved  
Optimal value (cvx\_optval): +1024  
  
x=2.8284, y=2.8284  
Rectnlge area: 11.3137

## 10th exercise from Optimization\_problem-s.pdf

```
% Solution
clear, close all;

cvx_solver sdpt3
cvx_begin
variables y
minimize y * y - 3 * y + 3
subject to
    - y <= 0
cvx_end

x_p2 = y - 1;
x = sqrt(x_p2);
fprintf('x=%2.4f \n', x)
```

Calling SDPT3 4.0: 4 variables, 2 equality constraints  
For improved efficiency, SDPT3 is solving the dual problem.

```
-----
num. of constraints = 2
dim. of sdp var = 2, num. of sdp blk = 1
dim. of linear var = 1
*****
SDPT3: Infeasible path-following algorithms
*****
version predcorr gam expon scale_data
HKM 1 0.000 1 0
it pstep dstep pinfeas dinfeas gap prim-obj dual-obj
cputime
-----
0/0.000/0.000/3.8e+00/8.4e+00/3.0e+02/ 1.000000e+01 0.000000e+00/
0:0:00/ chol 1 1
1/0.962/0.970/1.4e-01/3.4e-01/2.0e+01/ 9.814211e+00 6.526019e-01/
0:0:00/ chol 1 1
2/0.956/0.953/6.4e-03/2.4e-02/2.4e+00/ 4.173971e+00 2.035416e+00/
0:0:00/ chol 1 1
3/1.000/1.000/4.5e-06/2.1e-03/1.7e+00/ 3.402998e+00 1.695028e+00/
0:0:00/ chol 1 1
4/0.987/0.981/6.7e-08/1.3e-04/2.6e-02/ 2.267410e+00 2.242150e+00/
0:0:00/ chol 1 1
5/0.983/0.994/3.9e-10/9.4e-06/3.5e-04/ 2.250230e+00 2.249917e+00/
0:0:00/ chol 1 1
```

```
6/0.940/1.000/4.9e-09/7.8e-11/1.4e-05/ 2.250009e+00 2.249995e+00/
0:0:00/ chol 1 1
7/0.977/1.000/9.2e-10/1.2e-10/4.5e-07/ 2.250000e+00 2.250000e+00/
0:0:00/ chol 2 2
8/1.000/1.000/2.4e-11/1.8e-10/1.1e-08/ 2.250000e+00 2.250000e+00/
0:0:00/
stop: max(relative gap, infeasibilities) < 1.49e-08
```

```
-----
number of iterations = 8
primal objective value = 2.25000001e+00
dual objective value = 2.25000000e+00
gap := trace(XZ) = 1.11e-08
relative gap = 2.01e-09
actual relative gap = 1.84e-09
rel. primal infeas (scaled problem) = 2.41e-11
rel. dual " " " = 1.76e-10
rel. primal infeas (unscaled problem) = 0.00e+00
rel. dual " " " = 0.00e+00
norm(X), norm(Y), norm(Z) = 3.3e+00, 2.7e+00, 3.6e+00
norm(A), norm(b), norm(C) = 3.0e+00, 4.2e+00, 2.0e+00
Total CPU time (secs) = 0.21
CPU time per iteration = 0.03
termination code = 0
DIMACS: 2.5e-11 0.0e+00 1.8e-10 0.0e+00 1.8e-09 2.0e-09
-----
```

```
-----
Status: Solved
Optimal value (cvx_optval): +0.75
```

x=0.7071

## 11th exercise from Optimalization\_problem-s.pdf

```
% River - the fastest way to reach point on the opposite bank
```

```
% Solution
```

```
clear, close all;
```

```
cvx_begin
```

```
variables x
```

```
minimize (norm([x 9]) / 6 - x/8)
```

```
subject to
```

```
- x <= 0
```

```
cvx_end
```

```
fprintf('x=%2.4f \n', x)
```

Calling SDPT3 4.0: 4 variables, 2 equality constraints

For improved efficiency, SDPT3 is solving the dual problem.

```

-----
num. of constraints = 2
dim. of socp var = 3,   num. of socp blk = 1
dim. of linear var = 1
*****
SDPT3: Infeasible path-following algorithms
*****
version  predcorr  gam  expon  scale_data
NT      1      0.000  1      0
it pstep dstep pinfeas dinfeas  gap      prim-obj      dual-obj
cputime
-----
0/0.000/0.000/8.5e+00/1.7e+00/1.2e+02/ 0.000000e+00 0.000000e+00/
0:0:00/ chol 1 1
1/0.762/1.000/2.0e+00/1.4e-02/3.7e+01/-2.058565e+00 -4.003185e+00/
0:0:00/ chol 1 1
2/0.988/1.000/2.4e-02/1.4e-03/1.9e+00/-8.144566e-01 -2.341546e+00/
0:0:00/ chol 1 1
3/1.000/0.960/6.3e-09/5.0e-03/7.4e-02/-9.526497e-01 -1.020554e+00/
0:0:00/ chol 1 1
4/0.908/1.000/1.1e-08/1.4e-05/3.9e-03/-9.904720e-01 -9.943559e-01/
0:0:00/ chol 1 1
5/0.920/1.000/3.3e-09/1.4e-06/1.5e-04/-9.920985e-01 -9.922462e-01/
0:0:00/ chol 1 1
6/0.919/0.992/5.1e-09/1.1e-08/6.3e-06/-9.921535e-01 -9.921597e-01/
0:0:00/ chol 1 1
7/0.948/0.987/6.3e-09/1.1e-09/2.2e-07/-9.921567e-01 -9.921568e-01/
0:0:00/ chol 1 2
8/1.000/1.000/1.3e-09/6.0e-10/7.8e-09/-9.921568e-01 -9.921567e-01/
0:0:00/
stop: max(relative gap, infeasibilities) < 1.49e-08
-----
number of iterations = 8
primal objective value = -9.92156759e-01
dual objective value = -9.92156744e-01
gap := trace(XZ) = 7.75e-09
relative gap = 2.60e-09
actual relative gap = -5.23e-09
rel. primal infeas (scaled problem) = 1.31e-09
rel. dual " " " = 5.98e-10
rel. primal infeas (unscaled problem) = 0.00e+00
rel. dual " " " = 0.00e+00
norm(X), norm(Y), norm(Z) = 2.4e-01, 1.7e+01, 2.2e+01
norm(A), norm(b), norm(C) = 2.7e+00, 1.2e+00, 1.0e+01
Total CPU time (secs) = 0.43
CPU time per iteration = 0.05
termination code = 0
DIMACS: 1.4e-09 0.0e+00 6.0e-10 0.0e+00 -5.2e-09 2.6e-09
-----

Status: Solved
Optimal value (cvx_optval): +0.992157

```

$x=10.2049$

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