

BME 303: Modern Imaging Diagnostic Systems

Final Formula Sheet

| Material | $\mu@ 30\text{keV}$ | $\mu@ 100\text{keV}$ | Z ($kg/(m^2s)x10^6$) | c (m/s) | $\rho(kg/m^3)$ | T_1 | T_2 | M_0 |
|------------|------------------------------|------------------------|------------------------|---------|----------------|-------|-------|-------|
| Water | $.80 \text{ cm}^{-1}$ | $.1707 \text{ cm}^2/g$ | 1.5 | 1480 | 1000 | 1500 | 1500 | 1.0 |
| Alien Bone | $.9\text{cm}^{-1}$ | $.1855 \text{ cm}^2/g$ | 64 | 4080 | 1500 | 550 | 5 | 0.8 |
| Muscle | $.25\text{cm}^{-1}$ | $.1693\text{cm}^2/g$ | 1.6 | 1070 | 1070 | 600 | 40 | 0.9 |
| Alien Air | $.9.3x10^{-4}\text{cm}^{-1}$ | $.1541\text{cm}^2/g$ | 0.04 | 330 | 1.2 | 500 | 15 | .0004 |

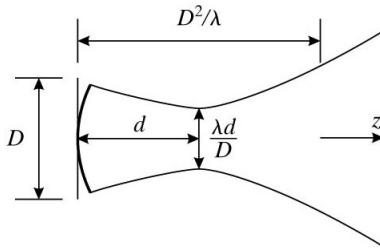
Ultrasound

$$Z = \rho c, \quad p = Zc, \quad f\lambda = c, \quad I = \frac{p^2}{Z}$$

$$A_z = A_0 e^{-\mu_a z}, \quad \alpha = 20 \log_{10}(e) \mu_a$$

$$\text{speed of light } c = 3.0x10^8 \text{ m/s}, \quad f_T = \frac{c_T}{2d_T}$$

$$\frac{\sin(\theta_i)}{\sin(\theta_t)} = \frac{c_1}{c_2}, \quad \frac{p_r}{p_i} = \frac{Z_2 - Z_1}{Z_2 + Z_1}, \quad \frac{p_t}{p_i} = \frac{2Z_2}{Z_2 + Z_1}$$



Magnetic Resonance Imaging

$$M_0 = \frac{B_0 \gamma_{bar}^2 \hbar^2}{4k_{bar} T} P_D, \quad \omega_0 = \gamma B_0, \quad f_0 = \gamma_{bar} B_0, \quad \gamma_{bar} = 42.57 \text{ MHz/T},$$

$$\hbar = 6.626x10^{-34} \text{ Js}, \quad E = \hbar f, \quad 1\text{eV} = 1.602x10^{-19} \text{ J}$$

$$M_z(t) = M_0(1 - e^{-t/T_1}), \quad \text{Spin Echo: } M_{xy} = M_0(1 - e^{-TR/T_1})e^{-TE/T_2}$$

$$\frac{1}{T_2^*} = \frac{1}{T_2} + \frac{1}{T_2'}$$

X-ray Imaging

$$SNR = \sqrt{\mu}, \quad SNR = \frac{\sqrt{\mu}}{\sigma^2}$$

$$m = \frac{d-z}{z}, \quad M = d/z, \quad I_d(x, y) = S(x/m, y/m) * t(x/M, y/M)$$

$$SNR = \frac{I_t - I_d}{\sigma_b}$$

$$C = \frac{f_t - f_g}{f_g}, \quad I = I_0 e^{-\mu x}$$

Radon Transform

$$G(L, \theta) = \int_{-\infty}^{\infty} \int_{-\infty}^{\infty} f(x, y) \delta(x \cos(\theta) + y \sin(\theta) - l) dx dy$$

Nuclear Medicine

$$R_{ext}^2 = R_i^2 + R_c^2, \quad R_C = \frac{d}{l}(l + b + |z|), \quad I_d = \frac{AE}{4\pi r^2}$$

$$X = \frac{1}{Z} \sum_{k=1}^K x_k a_k, \quad Y = \frac{1}{Z} \sum_{k=1}^K y_k a_k, \quad N_t = N_0 e^{-\lambda t}$$

$$SNR = \sqrt{N}$$