Compiler Construction

Lexical Analysis

Chapter -3

Regular Expressions

1. **All Strings that start with "tab" or end with "bat"**
   tab{A,…,Z,a,..,z}*|{A,…,Z,a,….,z}*bat

2. **All Strings in Which Digits 1,2,3 exist in ascending numerical order:**
   {A,…,Z}*1 {A,…,Z}*2 {A,…,Z}*3 {A,…,Z}*

3. **All strings of lowercase letters in which the letters are in ascending lexicographic order.**

   a*b*c*……z*

Regular Expression

All strings of lowercase letters that contain the five vowels in order.

want -> other* a (other|a)* e (other|e)* i (other|i)* o (other|o)* u (other|u)*

other -> [bcdfghjklmnpqrstvwxyz]

All strings of a's and b's that do not contain the substring abb.

$b^*(a^+b?)^*$

All strings of a's and b's that do not contain the subsequence abb.

$b^* \mid b^*a^+ \mid b^*a^+ba^*$

Regular Expressions

1. **All strings of lowercase letters that contain the five vowels in order**

   C → b|c|d|f……..|z
   C*a(C|a)*e(C|e)* i (C|i)* o (C|o)* u(C|u)*

2. **All strings of a's and b's with an odd number of a's**

   b* (ab*ab*)*ab*

3. **All stirings of 0's and 1's in which any two 0's in α are separated by three 1's**

   $1^*(0111)^*01^* + 1^*$

Find Regular Languages

1. a(a|b)*a
2. ((ε|a)b*)*
3. (a|b)*a(a|b)(a|b)
4. a*ba*ba*ba*
5. (aa|bb)* ((ab|ba)(aa|bb)*(ab|ba)(aa|bb)*)*

Regular Definitions

Regular Definitions: Associate names with Regular Expressions

For Example : PASCAL IDs

letter → A | B | C | ... | Z | a | b | ... | z
digit → 0 | 1 | 2 | ... | 9
id → letter (letter | digit)*

Shorthand Notation:

"+" : one or more $r^* = r^+ \mid \in$ (Kleene) & $r^+ = r\, r^*$ (Positive)
"?" : zero or one r?=r | ∈
[range] : set range of characters (replaces "|")
[A-Z] = A | B | C | ... | Z

Example Using Shorthand : PASCAL IDs

id → [A-Za-z][A-Za-z0-9]*

Regular Definitions

Unsigned Number **1240, 39.45, 6.33E15, or 1.578E-41**

digit → 0 | 1 | 2 | ... | 9
digits → digit digit*
optional_fraction → . digits | ∈
optional_exponent → (E (+ | -| ∈) digits) | ∈
num → digits optional_fraction optional_exponent

Shorthand

digit → 0 | 1 | 2 | ... | 9
digits → digit+
optional_fraction → (. digits) ?
optional_exponent → (E (+ | -) ? digits) ?
num → digits optional_fraction optional_exponent

Regular Definitions

How can we use concepts developed so far to assist in recognizing tokens of a source language ?

Assume Following Tokens:

if, then, else, relop, id, num

What language construct are they used for ?

Given Tokens, What are Patterns ?

if → if
then → then
else → else
relop → < | <= | > | >= | = | <>
id → letter (letter | digit)*
num → digit + (. digit +) ? (E(+ | -) ? digit +) ?

What does this represent ?

Grammar:
stmt → |if *expr* then *stmt*
|if *expr* then *stmt* else *stmt*
|∈
expr → *term* relop *term* | *term*
term → id | num

Other tasks done by Lexical Analyzer

Scan away *blanks*, new lines, tabs
Can we Define Tokens For These?

blank → **blank**
tab → **tab**
newline → **newline**
delim → **blank | tab | newline**
ws → **delim** $^{+}$

Ans: No token is returned to parser

Pattern, Token, Attribute-Value

Regular Expression	Token	Attribute-Value
ws	-	-
if	if	-
then	then	-
else	else	-
id	id	pointer to table entry
num	num	Exact value
<	relop	LT
<=	relop	LE
=	relop	EQ
<>	relop	NE
>	relop	GT
>=	relop	GE

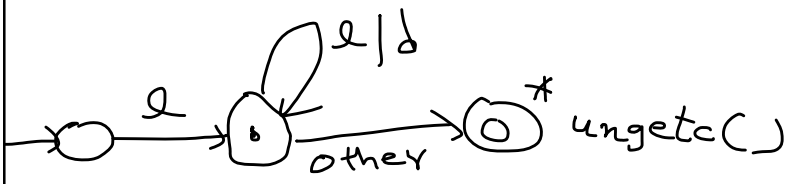
Note: Each token has a unique token identifier to define category of lexemes

(DFA)

Transition Diagrams

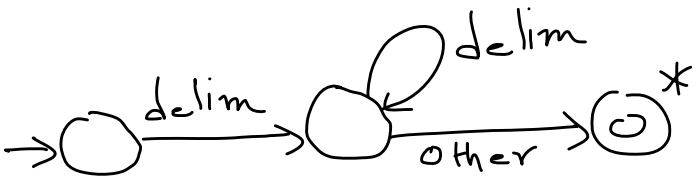
For Example : PASCAL IDs

letter → A | B | C | ... | Z | a | b | ... | z
digit → 0 | 1 | 2 | ... | 9
id → letter (letter | digit)*



Transition Diagrams

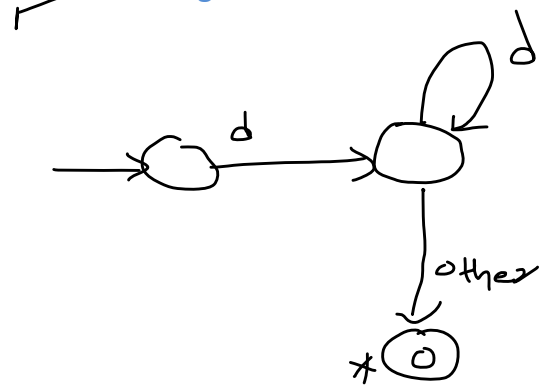
blank → blank
tab → tab
newline → newline
delim → blank | tab | newline
ws → delim +



Transition Diagrams

digit → 0 | 1 | 2 | … | 9
digits → digit digit*

Num → digits

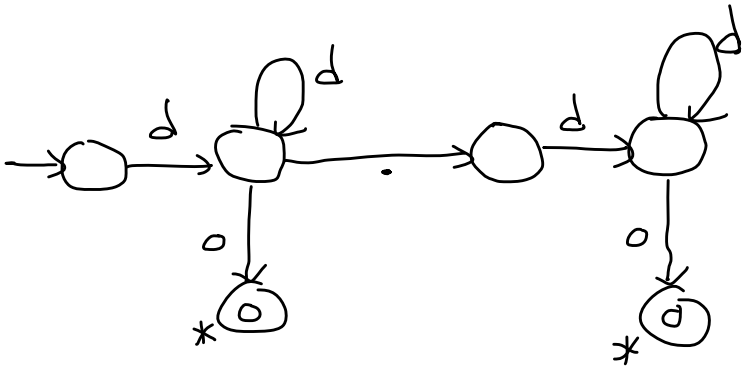


Transition Diagrams

digit → 0 | 1 | 2 | … | 9
digits → digit digit*
optional_fraction → . digits | ∈

12.45

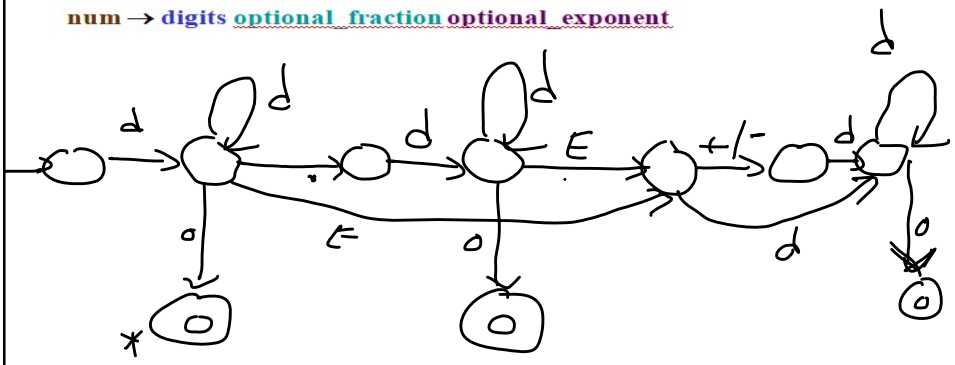
Num → digits optional_fraction



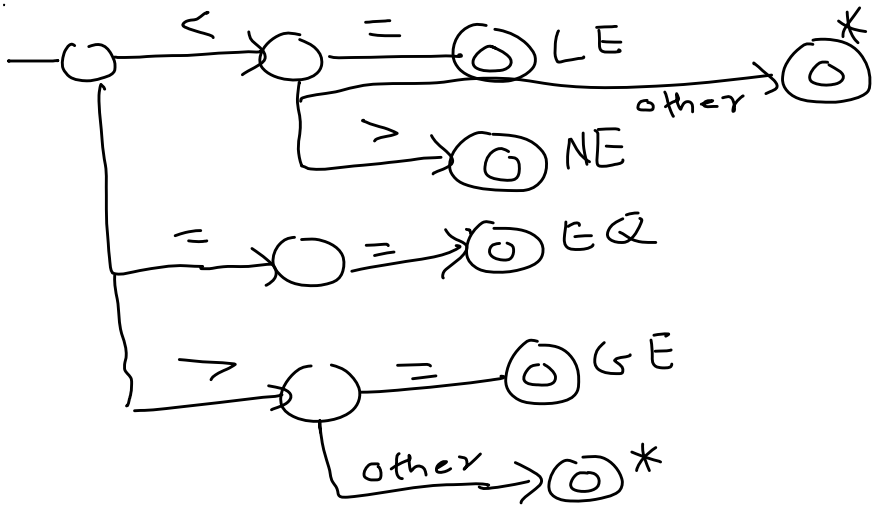
Transition Diagrams

Unsigned Number 1240, 39.45, 6.33E15, or 1.578E-41

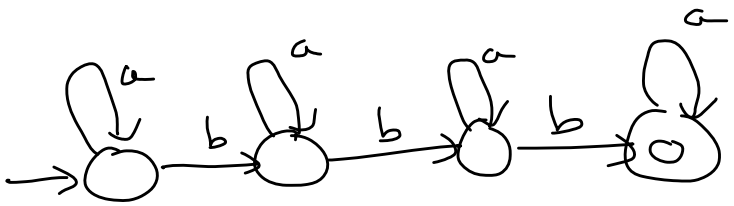
digit → 0 | 1 | 2 | ... | 9
digits → digit digit*
optional_fraction → . digits | ∈
optional_exponent → (E (+ | - | ∈) digits) | ∈
num → digits optional_fraction optional_exponent



Transition Diagrams (Relational Operators)



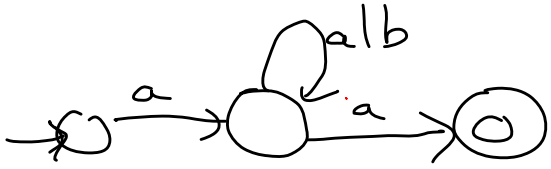
Transition Diagram
a*ba*ba*ba*



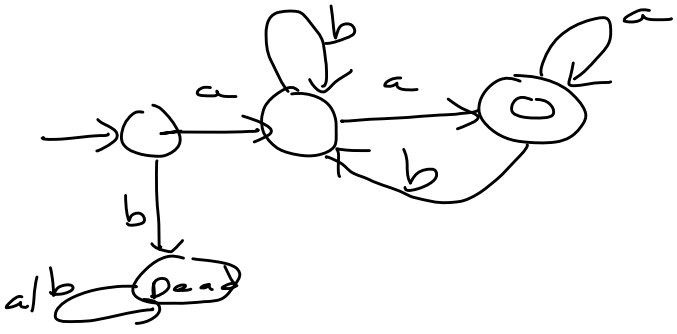
DFA

Transistion Diagram
a(a|b)*a

NFA:



DFA



Transition Diagram (DFA)

(a|b)*a(a|b)(a|b)

Try Yourself

Transition Diagram (DFA)

(aa|bb)* ((ab|ba)(aa|bb)*(ab|ba)(aa|bb)*)*

Try Yourself