

- PDF uploaded to peergrade - there is also a rubric online we should follow.

Rmk: From a statistical perspective there are canonical tasks we would like to do.

- Modeling
- Inference

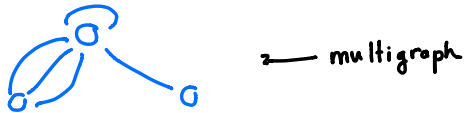
## Review of Graphs

Def: A graph  $G = (V, E)$  elements of  $E$  are (un)ordered pairs of vertices

$V$  vertices  $E$  edges

Def:  $N_v = |V|$  order,  $N_e = |E|$  size

Rule: Graphs may have loops and multiedges



Typically we assume the graph is simple; no loops/multiedges.

Def: A subgraph  $H = (V_H, E_H)$  is another graph s.t.  $V_H \subseteq V, E_H \subseteq E$

An induced subgraph is a subgraph containing the maximal edge set of a specified vertex subset.

Def: Directed graph: edges are ordered pairs.

Weighted graphs: number associated with each edge

- Decorating Graphs: - vertex/edge attributes

Connectivity

- two vertices are adjacent if  $(u,v) \in E$
- vertex is incident to an edge if  $v \in e \in E$ .

• Degree is given by  $\deg(v) = \sum_{u \in V} \mathbb{1}((u,v) \in E)$

• The degree sequence is the sorted list  $d_{(1)} \leq d_{(2)} \leq \dots \leq d_{(n)}$

Prop:  $\sum_{i=1}^n d_{(i)} = 2|E|$  similar notions for in/out degree

Def: - Walk alternating sequence of vertex-edge-vertex from  $v_0 \rightarrow v_1$

- trail is a walk with no repeated edges
- path is a trail with no repeated vertices.
- Circuit is a walk with  $v_0 = v_1$
- Cycle no repeated vertices

Def: A vertex is reachable if there exists a walk from  $u \rightarrow v$

- A graph is connected if every node is reachable
- We call each connected subgraph a component.

Def: In digraphs

- Weakly connected if connected ignoring direction
- Strongly connected if we don't ignore direction.