Course Overview

- -> Bayesian Inference
- -> Markor Chain Monte Carlo
 - Tempering
 - Adaptive MCMC
 - HMC
 - · Unbiased MCMC

Bayesian Statistics

data a viewed as a realization of X

model: $\left\{ f_{G} : \Theta \in \Theta \right\}$

Assume: X~ fo

Q: Is there some true fixed parameters a that generated

the model ?

Bayesian: View initially 0 mm then

update $\pi(d\theta|x) \ll f_{\theta}(x)\pi(d\theta)$

A dvantages

- · full dist for infurence
- · incorporated prim info

Disaduantage

- · Prior missperification
- · Computationally difficult

Memc

- best tool to sample from # (delx)
- Ravi Kannan et al (1991)

Showed much better than any deterministic method.

Rnk: Pseudo-Bagesian Informer

Fo (x) => \((delx) = Fo (x) = (de)

To (2) dessn't necessarlily near
to be a cleasity

 $\underline{\mathsf{E}_{\mathsf{X}:}} \ (\mathsf{X}_{\mathsf{I}},\ldots,\mathsf{X}_{\mathsf{n}}) = \mathsf{X} \sim \mathsf{N} \left(\mathsf{o},\;\mathsf{o}^{-1}\right)$

 $\forall (6|x) < exp \left\{ -\frac{1}{2} + f(x_6) - \frac{1}{2} \right\}$ $= \frac{1}{2} \log dt + 6$

Approximate lihelihood by

$$\tilde{\pi}(6|x) \propto \tilde{\pi} f_{\theta_i}(x_i|x_{(-i)}) \pi(\theta)$$

Markov Chain Monte Carlo

Let It be a measure ou X(RP)

we want to produce samples from tr.

MCMC: design MC s.t.

$$P(x_n \in A) \longrightarrow \pi(A)$$

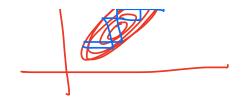
YA ∈ Jx measurable sets.

Many ways to build those

- Cirbbs Sampler ((coordinate desc.)

(onld be bad . - high correlation





- Metropolis-Hastings (Gradient descent)

Take Q(xy) another Kernel

Set $\alpha(x,y) = \min \left\{ 1, \frac{\pi(y) \, \alpha(y,x)}{\pi(x) \, \alpha(x,y)} \right\}$

 $P(x,dy) = \alpha(x,y) Q(x,y) dy + (1-\alpha(x,y)) S(dy)$

 $\alpha(x) = \int_{\mathcal{X}} \alpha(x,y) Q(x,y) dy$

a: Hour do me choose Q?