

Stat 346 Homework #7
Due: Wednesday March 22nd in class.

1. You are given the following losses:

800, 1100, 1300, 2150, 2300, 2450, 2650

You fit an inverse exponential to the loss distribution using maximum likelihood.
Determine the resulting estimate of the probability of a loss below 1000. [.219]

2. The following claim experience is observed:

Claim Size	Number of Claims
0 - 1500	15
1500 - 3000	8
3000 - ∞	3

You fit an exponential to the claim size distribution using maximum likelihood.
Show that 1543.431 is the maximum likelihood estimate for mean claims.

3. You are given:

- Fourteen lives are subject to the survival function

$$S(t) = (1 - \frac{t}{k})^{\frac{1}{2}}, \quad 0 \leq t \leq k.$$

- The first two deaths in the sample occurred at time $t = 12$.
- The study ends at time $t = 12$.

Find the maximum likelihood estimate of k . [42]

4. Consider claims following a distribution with the probability density function (PDF) given by:

$$f(x|\theta) = 2\theta x e^{-\theta x^2}, \quad x > 0$$

where θ is an unknown parameter.

Given the following claim amounts:

100, 150, 200, 250, 300, 350, 400

Calculate the Value-at-Risk (VaR) at the 95% confidence level for a new claim based on the most likely value of the unknown parameter.

5. A study on the duration of a particular medical treatment's effect is conducted. The treatment effectiveness duration follows an exponential distribution with mean θ . However, the study faces two constraints:

- (a) Only patients who experience treatment effectiveness for more than 1 month are included in the study (left truncation at 1 month).
- (b) For some patients, the treatment is still effective at the end of the study, marking these data points as right-censored at 6 months.

Given the following observed effectiveness durations (in months) and noting that two observations are right-censored:

2, 3, 4, (6+), (6+)

Determine the MLE for the mean duration θ of the treatment's effectiveness.