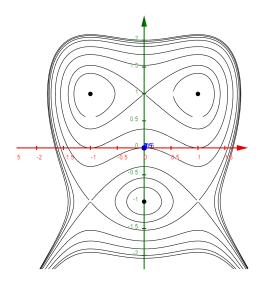
MATH 118

Local and global extrema

1. (a) The contour plot for x = f(x, y) is shown below. Suppose $f_x(1.5, 1) > 0$, $f_x(-1.5, 1) < 0$, and $f_y(0, -1.5) > 0$, and that $\{(-1, 1), (0, 1), (1, 1), (-1, -1), (0, -1), (1, -1)\}$ is the set of all the critical points of f(x, y). Guess the classification of the critical points of f(x, y).



(b) The function in part (a) is $f(x,y) = x^4 - 2x^2 + y^3 - 3y$. Confirm your answer in part (a) by calculating and classifying the critical points of f(x,y).

2. Find the global maximum and minimum values of $f(x,y) = x^2 + y^2 - 4xy + 2$ if $0 \le x \le 3$ and $0 \le y \le 2$.

3. It's estimated that a company's profit in selling x units of good A and y units of good B is

$$\pi(x,y) = 1500 + 80x - 10x^2 + 40xy + 40y - 60y^2.$$

It costs the company \$200 to produce each unit of good A, and \$100 to produce each unit of good B, and they cannot spend more than \$1000 on production costs.

(a) Write down the "physical" domain of the profit function.

(b) How many units of each good should the company produce in order to maximize their profit?

(c)