

# Neural Networks

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**CNPq**

MINISTRY OF  
EDUCATION

MINISTRY OF  
SCIENCE, TECHNOLOGY  
AND INNOVATIONS



# Outline

- 1 Introduction
- 2 GlassNet
- 3 ViscNet
- 4 Acknowledgments

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# Famous models based on Neural Networks



**ChatGPT**



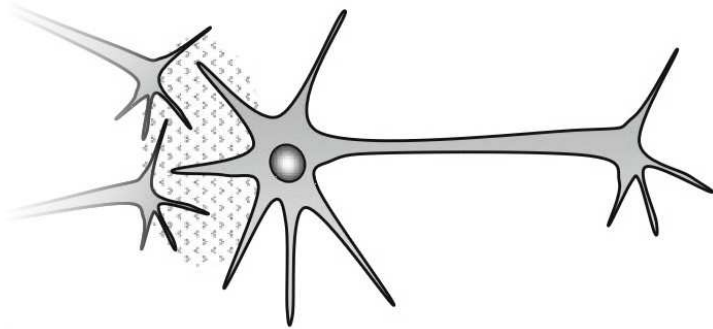
**Midjourney**



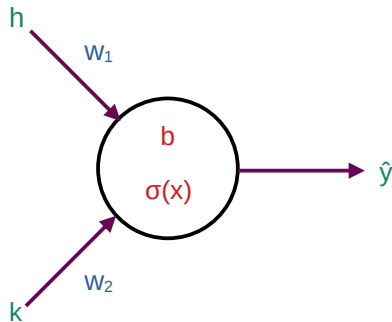
# Study material

See <https://github.com/drcassar/bam2024>

# Neurons and synapses

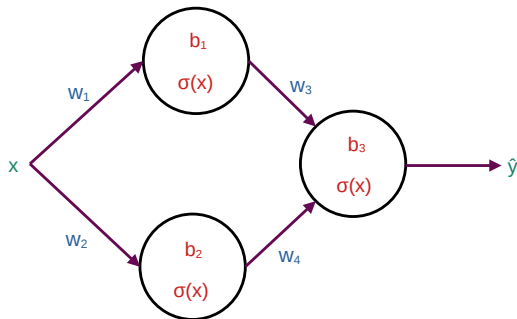


# Artificial neurons and artificial synapses (Perceptron)



$$\hat{y} = \sigma(hw_1 + kw_2 + b)$$

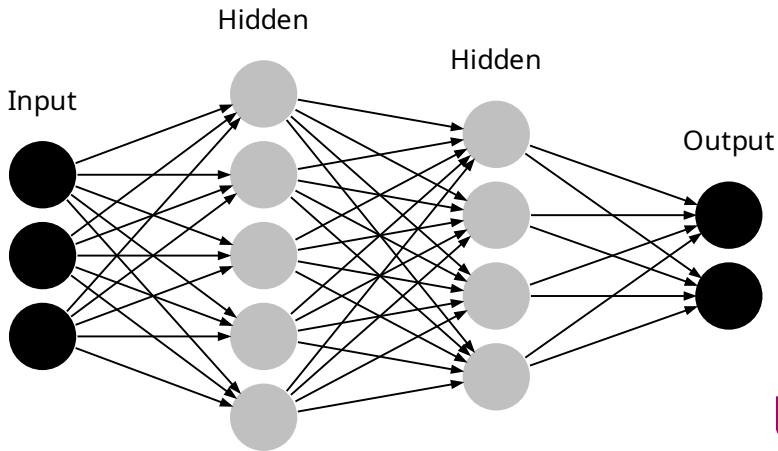
# Artificial neurons in series and in parallel



$$\hat{y} = \sigma\left(\sigma(xw_1 + b_1) \cdot w_3 + \sigma(xw_2 + b_2) \cdot w_4 + b_3\right)$$



# Multilayer Perceptron Neural Networks



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# GlassNet — multitask deep learning model

Composition (input):  $2\text{SiO}_2 \cdot \text{CaO} \cdot \text{MgO}$

$T_0 = 1702\text{ K}$	$\log_{10}(\eta(1673\text{ K})) = 0.15$	$\log_{10}(\rho(273\text{ K})) = 10.4$	$\log_{10}(\alpha_L(433\text{ K})) = -5.10$
$T_1 = 1567\text{ K}$	$\log_{10}(\eta(1773\text{ K})) = 0.03$	$\log_{10}(\rho(373\text{ K})) = 10.3$	$\log_{10}(\alpha_L(483\text{ K})) = -5.13$
$T_2 = 1438\text{ K}$	$\log_{10}(\eta(1873\text{ K})) = -0.23$	$\log_{10}(\rho(423\text{ K})) = 7.65$	$\log_{10}(\alpha_L(623\text{ K})) = -5.09$
$T_3 = 1362\text{ K}$	$\log_{10}(\eta(2073\text{ K})) = -0.85$	$\log_{10}(\rho(573\text{ K})) = 7.99$	$C_p(293\text{ K}) = 813\text{ J/(kg.K)}$
$T_4 = 1298\text{ K}$	$\log_{10}(\eta(2273\text{ K})) = -1.01$	$\log_{10}(\rho(1073\text{ K})) = 0.91$	$C_p(473\text{ K}) = 953\text{ J/(kg.K)}$
$T_5 = 1238\text{ K}$	$\log_{10}(\eta(2473\text{ K})) = -1.11$	$\log_{10}(\rho(1273\text{ K})) = -0.93$	$C_p(673\text{ K}) = 942\text{ J/(kg.K)}$
$T_6 = 1181\text{ K}$	$T_g = 1008\text{ K}$	$\log_{10}(\rho(1473\text{ K})) = -2.01$	$C_p(1073\text{ K}) = 1438\text{ J/(kg.K)}$
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$T_8 = 1107\text{ K}$	$T_{\text{liq}} = 1666\text{ K}$	$E = 97\text{ GPa } G = 38\text{ GPa}$	$C_p(1473\text{ K}) = 1534\text{ J/(kg.K)}$
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$T_{11} = 1022\text{ K}$	$T_{\text{strain}} = 984\text{ K}$	$D(1073\text{ K}) = 2.60\text{ g/cm}^3$	$\log_{10}(U_{\text{max}}) = -4.31$
$T_{12} = 1001\text{ K}$	$T_{\text{soft}} = 1054\text{ K}$	$D(1273\text{ K}) = 2.87\text{ g/cm}^3$	$T_c = 1176\text{ K } T_x = 1151\text{ K}$
$\log_{10}(\eta(773\text{ K})) = 12.4$	$T_{\text{dil}} = 1037\text{ K } V_D = 58$	$D(1473\text{ K}) = 2.83\text{ g/cm}^3$	$\gamma(T > T_g) = 0.46\text{ J/m}^2$
$\log_{10}(\eta(873\text{ K})) = 12.0$	$n_D = 1.61\text{ } n(\text{low}) = 2.16$	$D(1673\text{ K}) = 2.59\text{ g/cm}^3$	$\gamma(1173\text{ K}) = 0.34\text{ J/m}^2$
$\log_{10}(\eta(973\text{ K})) = 11.8$	$n(\text{high}) = 2.34$	$\kappa = 1.23\text{ W/(m.K)}$	$\gamma(1473\text{ K}) = 0.37\text{ J/m}^2$
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$\log_{10}(\eta(1473\text{ K})) = 1.55$			
$\log_{10}(\eta(1573\text{ K})) = 0.63$			

# Building GlassNet: data pipeline

## Query:

- SciGlass database
- 85 properties
- Minor chemical filtering (H to Bi)

## Before deduplication:

- $\sim 280\,000$  entries

## After deduplication:

- $\sim 220\,000$  entries (10% reserved for testing!)

# Feature engineering — physicochemical elemental properties

Atomic number  
Atomic radius\*  
Atomic volume  
Atomic weight  
BCC lattice parameter+  
Bandgap energy+  
Boiling point  
Covalent radius  
C<sub>6</sub> coefficient  
Density  
Dipole polarizability  
Effective nuclear charge  
Electron affinity  
Electronegativity\*  
Energy per atom+

Energy to remove the first electron  
FCC lattice parameter+  
Fusion enthalpy  
Glawe's number  
Heat of formation  
Magnetic moment+  
Mass number of the most abundant isotope  
Maximum ionization energy  
Melting point  
Mendeleev's number  
Number of electrons  
Number of filled d valence orbitals  
Number of filled f valence orbitals  
Number of filled p valence orbitals

Number of filled s valence orbitals  
Number of neutrons  
Number of oxidation states  
Number of protons  
Number of unfilled d valence orbitals  
Number of unfilled f valence orbitals  
Number of unfilled p valence orbitals  
Number of unfilled s valence orbitals  
Number of unfilled valence orbitals  
Number of valence electrons  
Pettifor's number  
Single-bond covalent radius  
Van der Waals radius\*  
Volume per atom+

# Feature engineering

Composition:  $\text{SiO}_2$

Property: atomic number

Element order: [H O Na Si]

$$\mathbf{C} = [0 \quad 0.67 \quad 0 \quad 0.33]$$

$$\mathbf{S} = [1 \quad 8 \quad 11 \quad 14]$$

# Feature engineering

Composition:  $\text{SiO}_2$

Property: atomic number

Element order:  $[\text{H} \quad \text{O} \quad \text{Na} \quad \text{Si}]$

$$\mathbf{C} = [0 \quad 0.67 \quad 0 \quad 0.33]$$

$$\mathbf{S} = [1 \quad 8 \quad 11 \quad 14]$$

---

$$\mathbf{C} \circ \mathbf{S} = [0 \quad 5.36 \quad 0 \quad 4.62]$$

# Feature engineering

Composition:  $\text{SiO}_2$

Property: atomic number

Element order:  $[\text{H} \quad \text{O} \quad \text{Na} \quad \text{Si}]$

$$\mathbf{C} = \begin{bmatrix} 0 & 0.67 & 0 & 0.33 \end{bmatrix}$$

$$\mathbf{S} = \begin{bmatrix} 1 & 8 & 11 & 14 \end{bmatrix}$$

---

$$\mathbf{C} \circ \mathbf{S} = \begin{bmatrix} 0 & 5.36 & 0 & 4.62 \end{bmatrix}$$

$$\text{mean}(\mathbf{C} \circ \mathbf{S}) = 4.99$$

$$\text{max}(\mathbf{C} \circ \mathbf{S}) = 5.36$$

$$\text{min}(\mathbf{C} \circ \mathbf{S}) = 4.62$$

$$\text{sum}(\mathbf{C} \circ \mathbf{S}) = 9.98$$

$$\text{std}(\mathbf{C} \circ \mathbf{S}) = 0.37$$

$\circ$ : Hadamard product

Calculations disregard the zero-valued elements of  $(\mathbf{C} \circ \mathbf{S})$



# Feature engineering

Composition:  $\text{Na}_2\text{O} \cdot \text{SiO}_2$

Property: atomic number

Element order:  $[\text{H} \quad \text{O} \quad \text{Na} \quad \text{Si}]$

$$\mathbf{C} = \begin{bmatrix} 0 & 0.5 & 0.33 & 0.17 \end{bmatrix}$$

$$\mathbf{S} = \begin{bmatrix} 1 & 8 & 11 & 14 \end{bmatrix}$$

---

$$\mathbf{C} \circ \mathbf{S} = \begin{bmatrix} 0 & 4 & 3.63 & 2.38 \end{bmatrix}$$

$$\text{mean}(\mathbf{C} \circ \mathbf{S}) = 3.34$$

$$\text{max}(\mathbf{C} \circ \mathbf{S}) = 4$$

$$\text{min}(\mathbf{C} \circ \mathbf{S}) = 2.38$$

$$\text{sum}(\mathbf{C} \circ \mathbf{S}) = 10.01$$

$$\text{std}(\mathbf{C} \circ \mathbf{S}) = 0.69$$

$\circ$ : Hadamard product

Calculations disregard the zero-valued elements of  $(\mathbf{C} \circ \mathbf{S})$

# Feature engineering — features for clustering

**Composition:**  $\text{Na}_2\text{O} \cdot \text{SiO}_2$

**Property:** atomic number

**Element order:** [H O Na Si]

$$\mathbf{C} = [0 \quad 0.5 \quad 0.33 \quad 0.17]$$

$$[\mathbf{C}] = [0 \quad 1 \quad 1 \quad 1]$$

$$\mathbf{S} = [1 \quad 8 \quad 11 \quad 14]$$

# Feature engineering — features for clustering

**Composition:**  $\text{Na}_2\text{O} \cdot \text{SiO}_2$

**Property:** atomic number

**Element order:** [H O Na Si]

$$\mathbf{C} = [0 \quad 0.5 \quad 0.33 \quad 0.17]$$

$$[\mathbf{C}] = [0 \quad 1 \quad 1 \quad 1]$$

$$\mathbf{S} = [1 \quad 8 \quad 11 \quad 14]$$

---

$$[\mathbf{C}] \circ \mathbf{S} = [0 \quad 8 \quad 11 \quad 14]$$

$$\text{mean}(\mathbf{C} \circ \mathbf{S}) = 11$$

$$\text{max}(\mathbf{C} \circ \mathbf{S}) = 14$$

$$\text{min}(\mathbf{C} \circ \mathbf{S}) = 8$$

$$\text{sum}(\mathbf{C} \circ \mathbf{S}) = 33$$

$$\text{std}(\mathbf{C} \circ \mathbf{S}) = 2.45$$

# Feature engineering — features for clustering

**Composition:**  $\text{Na}_2\text{O} \cdot 2\text{SiO}_2$

**Property:** atomic number

**Element order:** [H O Na Si]

$$\mathbf{C} = [0 \quad 0.56 \quad 0.22 \quad 0.22]$$

$$[\mathbf{C}] = [0 \quad 1 \quad 1 \quad 1]$$

$$\mathbf{S} = [1 \quad 8 \quad 11 \quad 14]$$

---

$$[\mathbf{C}] \circ \mathbf{S} = [0 \quad 8 \quad 11 \quad 14]$$

$$\text{mean}(\mathbf{C} \circ \mathbf{S}) = 11$$

$$\text{max}(\mathbf{C} \circ \mathbf{S}) = 14$$

$$\text{min}(\mathbf{C} \circ \mathbf{S}) = 8$$

$$\text{sum}(\mathbf{C} \circ \mathbf{S}) = 33$$

$$\text{std}(\mathbf{C} \circ \mathbf{S}) = 2.45$$

# Feature engineering — feature selection

Starting point:

elemental fraction (composition)	77
regression physicochemical properties	275
clustering physicochemical properties	275
<hr/>	
TOTAL	627

# Feature engineering — feature selection

Starting point:

elemental fraction (composition)	77
regression physicochemical properties	275
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<hr/>	
TOTAL	627

After Variance Inflation Factor (VIF) selection:

elemental fraction (composition)	64
regression physicochemical properties	12
clustering physicochemical properties	22
<hr/>	
TOTAL	98

# GlassNet: the pipeline

Multitask learning:

- Chemical composition  $\rightarrow$  98 features  $\rightarrow$  Neural network  $\rightarrow$  85 properties

Note:

- Not limited to oxide glasses

# Finding a reasonable neural network architecture (NP-hard)

- Hyperparameter tuning
  - Two runs testing 1000 different architectures
  - Tree-structured Parzen Estimator search
  - With Asynchronous Successive Halving Algorithm (ASHA)
- Cross-validation
  - 10-fold cross-validation
- Training the final model



# GlassNet — new multitask deep learning model

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# Property groups

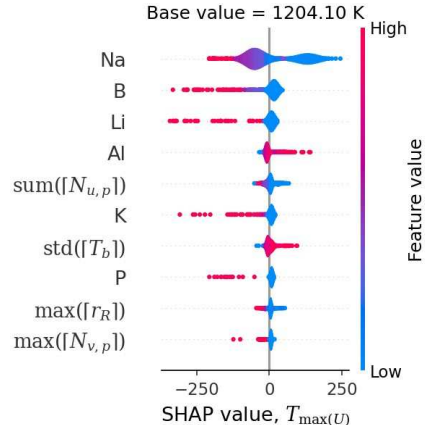
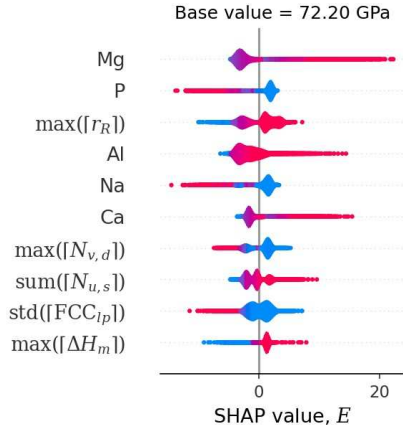
- 1 Viscosity
- 2 Optical properties
- 3 Dielectric properties
- 4 Electrical properties
- 5 Mechanical properties
- 6 Thermal properties
- 8 Density
- 9 Crystallization
- 10 Liquidus temperature
- 11 Surface tension
- 12 Thermal shock resistance

# Was the multitasking approach beneficial?

Yes and no!

- Better results for 24 properties measured in different conditions
- No statistical difference for 29
- Worse results for 24 properties measured in only one condition with more than 10k data points
- Solution: hybrid model (multitask + single-task)

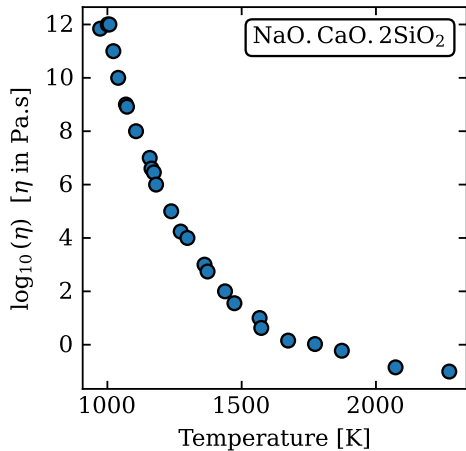
# Opening the black-box with SHAP



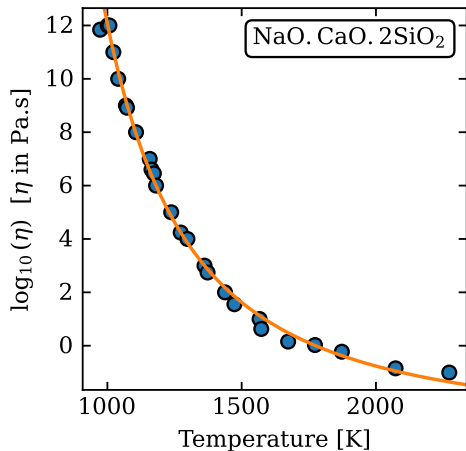
# Most important features for glass design (SHAP analysis)

Viscosity	Optical	Mechanical	Crystallization
B	Pb	$N_{u,s}$	$N_{f,p}$
Na	$N_u$	Na	$N_{u,p}$
Al	Bi	$\Delta H_m$	$\Delta H_m$
K	$N_{f,d}$	$FCC_{lp}$	B
Li	$N_{f,p}$	P	Na
Pb	Ti	Mg	Se
$N_{f,s}$	Nb	Ca	S
Ca	$N_{f,f}$	$r_R$	Te
$\Delta H_m$	La	$N_{f,d}$	$T_b$
P	Ge	Al	V

# Building on top of GlassNet: Viscosity prediction

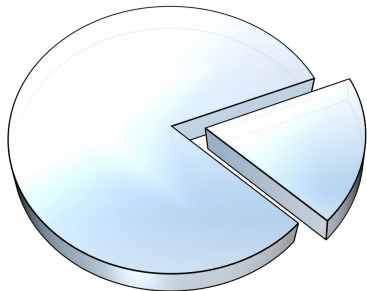


# Building on top of GlassNet: Viscosity prediction



# Open Science

## GlassPy



- Python module
- Free and open source
- Ready-to-use GlassNet
- SciGlass data as a pandas DataFrame

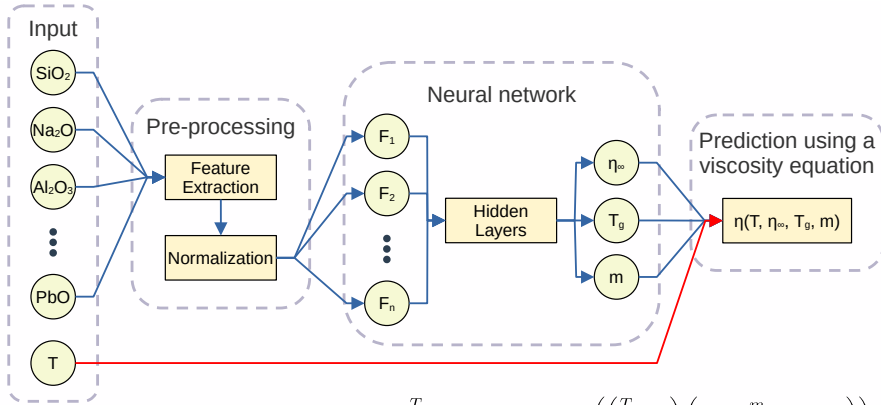
<https://github.com/drcassar/glasspy> (GPLv3 license)  
<https://glasspy.readthedocs.io/> (documentation)



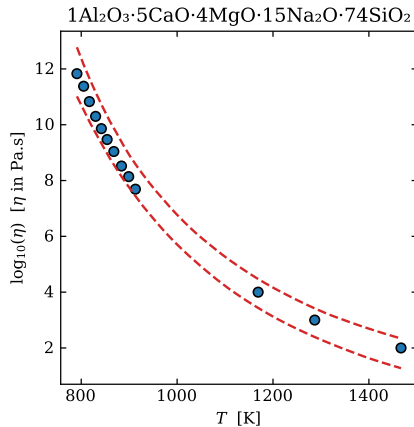
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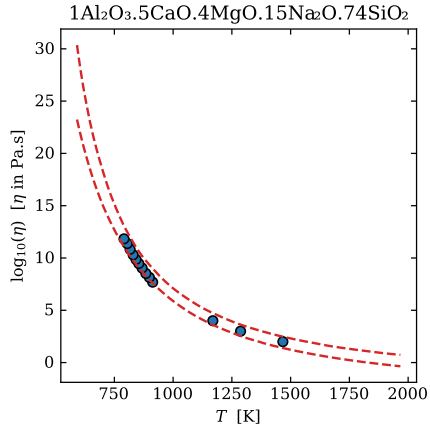
# ViscNet — physics-informed neural network



# ViscNet — prediction and extrapolation



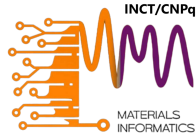
# ViscNet — prediction and extrapolation



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