

$$(\alpha \wedge \beta) \equiv (\beta \wedge \alpha) \text{ commutativity of } \wedge$$

$$(\alpha \vee \beta) \equiv (\beta \vee \alpha) \text{ commutativity of } \vee$$

$$((\alpha \wedge \beta) \wedge \gamma) \equiv (\alpha \wedge (\beta \wedge \gamma)) \text{ associativity of } \wedge$$

$$((\alpha \vee \beta) \vee \gamma) \equiv (\alpha \vee (\beta \vee \gamma)) \text{ associativity of } \vee$$

$$\neg(\neg \alpha) \equiv \alpha \text{ double-negation elimination}$$

$$(\alpha \Rightarrow \beta) \equiv (\neg \beta \Rightarrow \neg \alpha) \text{ contraposition}$$

$$(\alpha \Rightarrow \beta) \equiv (\neg \alpha \vee \beta) \text{ implication elimination}$$

$$(\alpha \Leftrightarrow \beta) \equiv ((\alpha \Rightarrow \beta) \wedge (\beta \Rightarrow \alpha)) \text{ biconditional elimination}$$

$$\neg(\alpha \wedge \beta) \equiv (\neg \alpha \vee \neg \beta) \text{ De Morgan}$$

$$\neg(\alpha \vee \beta) \equiv (\neg \alpha \wedge \neg \beta) \text{ De Morgan}$$

$$(\alpha \wedge (\beta \vee \gamma)) \equiv ((\alpha \wedge \beta) \vee (\alpha \wedge \gamma)) \text{ distributivity of } \wedge \text{ over } \vee$$

$$(\alpha \vee (\beta \wedge \gamma)) \equiv ((\alpha \vee \beta) \wedge (\alpha \vee \gamma)) \text{ distributivity of } \vee \text{ over } \wedge$$