

function FORWARD-BACKWARD(\mathbf{ev} , $prior$) **returns** a vector of probability distributions

inputs: \mathbf{ev} , a vector of evidence values for steps $1, \dots, t$

$prior$, the prior distribution on the initial state, $\mathbf{P}(\mathbf{X}_0)$

local variables: \mathbf{fv} , a vector of forward messages for steps $0, \dots, t$

\mathbf{b} , a representation of the backward message, initially all 1s

\mathbf{sv} , a vector of smoothed estimates for steps $1, \dots, t$

$\mathbf{fv}[0] \leftarrow prior$

for $i = 1$ **to** t **do**

$\mathbf{fv}[i] \leftarrow \text{FORWARD}(\mathbf{fv}[i - 1], \mathbf{ev}[i])$

for $i = t$ **down to** 1 **do**

$\mathbf{sv}[i] \leftarrow \text{NORMALIZE}(\mathbf{fv}[i] \times \mathbf{b})$

$\mathbf{b} \leftarrow \text{BACKWARD}(\mathbf{b}, \mathbf{ev}[i])$

return \mathbf{sv}