Graph Sampling-based Meta-Learning for Molecular Property Prediction

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Abstract

Molecular property is usually observed with a limited number of samples, and researchers have considered property prediction as a few-shot problem. One important fact that has been ignored by prior works is that each molecule can be recorded with several different properties simultaneously. To effectively utilize many-to-many correlations of molecules and properties, we propose a Graph Sampling-based Meta-learning (GS-Meta) framework for few-shot molecular property prediction. First, we construct a Molecule-Property relation Graph (MPG): molecule and properties are nodes, while property labels decide edges. Then, to utilize the topological information of MPG, we reformulate an episode in meta-learning as a subgraph of the MPG, containing a target property node, molecule nodes, and auxiliary property nodes. Third, as episodes in the form of subgraphs are no longer independent of each other, we propose to schedule the subgraph sampling process with a contrastive loss function, which considers the consistency and discrimination of subgraphs. Extensive experiments on 5 commonly-used benchmarks show GS-Meta consistently outperforms state-of-the-art methods by 5.71%-6.93% in ROC-AUC and verify the effectiveness of each proposed module. Our code is available at https://github.com/HICAI-ZJU/GS-Meta.
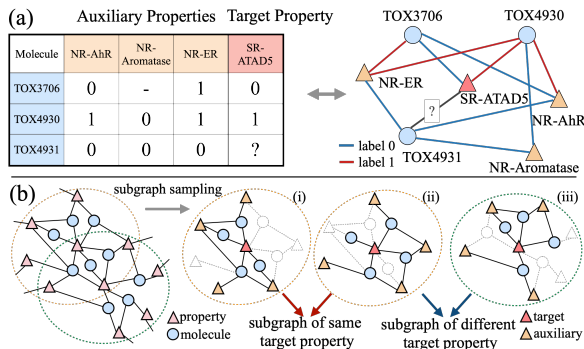
Figure 1: (a) An example of the Molecule-Property relation Graph (MPG) built based on the Tox21 dataset [Wu *et al.*, 2018]. To predict the SR-ATAD5 property of the TOX4931 molecule, we can utilize some auxiliary properties to form an MPG where molecules and properties are nodes and edges represent property labels (0 or 1). (b) An example of subgraph sampling. Given the MPG, we can sample a pair of subgraphs with the same target property (*e.g.*, (i) and (ii)) as positive samples and another pair with different target properties (*e.g.*, (ii) and (iii)) as negative samples.

1 Introduction

Drug discovery is of great significance to public health and the development of new drugs is a long and costly process. In the early lead optimization phase, researchers need to select a large number of molecules as candidates and conduct virtual screening to avoid wasting resources on molecules that are unlikely to possess the desired properties [Riniker and Landrum, 2013; Sliwoski *et al.*, 2014]. Recently, deep learning plays an important role in this process, and several deep

models have been investigated to predict molecular property [Song *et al.*, 2020; Fang *et al.*, 2022; Fang *et al.*, 2023]. In the practical settings, only a few molecules can be made and tested in the wet-lab experiments [Altae-Tran *et al.*, 2017; Guo *et al.*, 2021]. The limited amount of annotated data often hinders the generalization ability of deep learning models in practical applications [Bertinetto *et al.*, 2016].

Deficient annotated data is often termed a few-shot learning (FSL) problem [Wang *et al.*, 2020]. Typically, meta-learning [Hospedales *et al.*, 2021], which aims to learn how to learn, is used to solve the few-shot problem and several prior works have incorporated meta-learning into molecular property prediction. For example, Meta-GNN [Guo *et al.*, 2021] employed a classic meta-learning method, MAML [Finn *et al.*, 2017], with self-supervised tasks including bond reconstruction and atom type prediction. Wang *et al.* constructed a relation graph of molecules and designed a meta-learning strategy to selectively update model parameters.

However, these works have neglected an important fact that, unlike common FSL settings including image classification, a molecule can be observed with multiple properties

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simultaneously, such as a number of possible side effects. There is also a correlation between different properties, for example, endocrine disorders and cardiac diseases caused by drug side effects may occur together because they share disease pathway [Fuchs and Whelton, 2020]. In predicting the property of a molecule, we can leverage other available labeled properties of the same molecule. When we know some properties of one molecule and are faced with new properties that have fewer labels, we postulate that utilizing these known property labels can alleviate the label insufficiency problem.

To effectively utilize such correlations, we propose a Graph Sampling-based Meta-learning framework, GS-Meta. First, to accurately describe the many-to-many relations among molecules and properties, we build a Molecule-Property relation Graph (MPG), where nodes are molecules and properties, and edges between molecules and properties indicate the label of the molecules in the properties (Figure 1(a)). Second, to employ the inherent graph topology of MPG, we propose to reformulate an episode as a subgraph of MPG, which is composed of a target property node, molecule nodes as well as auxiliary property nodes (Figure 1(b)). Third, in conventional meta-learning [Vinyals *et al.*, 2016], episodes are considered to be independently distributed and sampled from a uniform distribution. However, subgraphs are connected in our MPG due to intersecting molecules and edges, they are no longer independent of each other. We propose a learnable sampling scheduler and specify the subgraph dependency in two aspects: (1) subgraphs centered on the same target property node can be seen as different views describing the same task and thus they should be consistent with each other; and (2) subgraphs centered on different target property nodes are episodes of different tasks, and their semantic discrepancy should be enlarged. Hence, we solve this dependency via a contrastive loss function. In short, our contributions are summarized as follows:

- We propose to use auxiliary properties when facing new target property in the few-shot regime and construct a Molecule-Property relation Graph to model the relations among molecules and properties so that the information of the relevant properties can be used through the topology of the constructed graph.

- We propose a Graph Sampling-based Meta-learning framework, which reformulates episodes in meta-learning as sampled subgraphs from the constructed MPG, and schedules the subgraph sampling process with a contrastive loss function.

- Experiments on five benchmarks show that our method consistently outperforms state-of-the-art FSL molecular property prediction methods by 5.71%-6.93% in terms of ROC-AUC.

2 Related Work

Few-shot Learning for Molecules   The few-shot learning (FSL) problem [Vinyals *et al.*, 2016; Chen *et al.*, 2019] occurs when there are limited labeled training data per object of interest. Often, meta-learning is used to solve the few-shot learning problem. For example, MAML [Finn *et al.*, 2017]

learns a good parameter initialization and updates through gradient descents. However, the existing methods are usually investigated for image classification but not tailored to the different settings of molecular property prediction [Wang *et al.*, 2021]. Recent efforts have been paid to fill this gap. Guo *et al.* propose to use molecule-specific tasks including masked atoms and bonds prediction to guide the model focus on the intrinsic characteristics of molecules. Wang *et al.* connect molecules in a homogeneous graph to propagate limited information between similar instances. However, all the prior works have ignored the relationships between molecular properties, *i.e.*, some auxiliary available properties can be used in predicting new molecular properties, and they fail to investigate the relationship.

Episode Scheduler in Meta-learning   Most meta-learning approaches leverage a uniform episode sampling strategy in the training process. To exploit relations between episodes, prior methods have investigated how to schedule episodes to enhance the generalization of meta-knowledge. Liu *et al.* design a greedy class-pair based strategy rather than uniform sampling. Fei *et al.* consider the relationship of episodes to overcome the poor sampling problem. Yao *et al.* propose a neural scheduler to decide which tasks to select from a candidate set. In this work, we schedule episodes with the lens of subgraph sampling and encourage the consistency between subgraphs of the same target property and discrimination between different target properties via a contrastive loss function.

3 Graph Sampling-based Meta-Learning

This section presents the proposed Graph Sampling-based Meta-learning framework, as shown in Figure 2. We first define the few-shot molecular property prediction problem (Section 3.1). To establish and exploit the many-to-many relation between molecules and properties, we construct a Molecule-Property relation Graph (MPG) and then reformulate an episode in meta-learning as a subgraph from the MPG (Section 3.2). With this reformulation, we investigate to consider consistency and discrimination between subgraphs and schedule the subgraph sampling to facilitate meta-learning (Section 3.3). Finally, the training and testing strategies are described (Section 3.4).

3.1 Problem Definition

Following [Altae-Tran *et al.*, 2017; Guo *et al.*, 2021], the few-shot molecular property prediction is conducted on a set of tasks $\{\mathcal{T}\}$, where each task $\mathcal{T}$ is to predict a property p of molecules. The training set $\mathcal{D}_{train}$ consists of several tasks $\{\mathcal{T}_{train}\}$, denoted as $\mathcal{D}_{train} = \{(x_i, y_{i,t})|t \in \mathcal{T}_{train}\}$, where x_i is a molecule and $y_{i,t}$ is the label of x_i on the t-th task. And the testing set $\mathcal{D}_{test} = \{(x_j, y_{j,t})|t \in \mathcal{T}_{test}\}$ is composed of a set of tasks $\{\mathcal{T}_{test}\}$. $\{p_{train}\}$ and $\{p_{test}\}$ are denoted as properties corresponding to tasks $\{\mathcal{T}_{train}\}$ and $\{\mathcal{T}_{test}\}$, and training properties and testing properties are disjoint, *i.e.*, $\{p_{train}\} \cap \{p_{test}\} = \emptyset$. The objective is to learn a predictor on $\mathcal{D}_{train}$ and to predict novel properties with a few labeled molecules in $\mathcal{D}_{test}$.
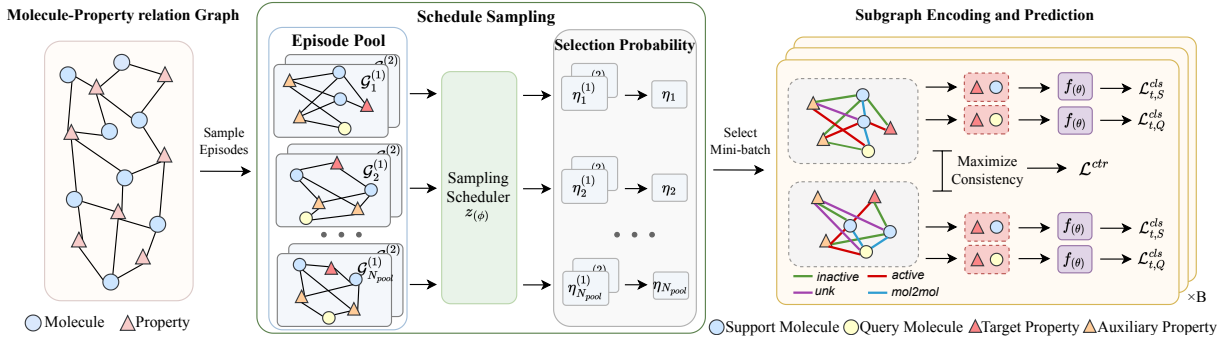
Figure 2: A 2-way 1-shot overview of GS-Meta. Firstly a Molecule-Property relation Graph (MPG) is constructed. Then, an episode candidate pool is randomly sampled, and the subgraph sampling scheduler $z_{(\phi)}$ is used to compute the selection probability η and select a mini-batch containing B episode pairs from the candidate pool. Finally, the relation learning module $f_{(\theta)}$ encodes each subgraph and outputs a classification loss $\mathcal{L}^{cls}$ within an episode and a contrastive loss $\mathcal{L}^{ctr}$ across episodes.

To deal with the few-shot problem, the episodic training paradigm has shown great promise in meta-learning [Finn *et al.*, 2017]. Without loading all training tasks $\{\mathcal{T}_{train}\}$ into memory, batches of episodes $\{E_t\}_{t=1}^B$ are sampled iteratively in practical training process. To construct an episode E_t, a target task $\mathcal{T}_t$ is firstly sampled from $\{\mathcal{T}_{train}\}$, then a labeled support set S_t and a query set Q_t are sampled. Usually, there are two classes (*i.e.*, *active* (y=1) or *inactive* (y=0)) in each molecular property prediction task, and a 2-way K-shot episode means that the support set $\mathcal{S}_t$ consists of 2 classes with K molecules per class, *i.e.*, $\mathcal{S}_t = \{(x_i^s, y_{i,t}^s)\}_{i=1}^{2K}$, and query set $\mathcal{Q}_t = \{(x_i^q, y_{i,t}^q)\}_{i=1}^{M}$ contains M molecules. In this case, we can define the episode as $E_t = (\mathcal{S}_t, \mathcal{Q}_t)$.

3.2 Molecule-Property Relation Graph

Graph Construction and Initialization To leverage the rich information behind the relations among properties and molecules, we construct a Molecule-Property relation Graph (MPG) that explicitly describes such relations. The graph is denoted as $\mathcal{G} = (\mathcal{V}, \mathcal{E})$, where $\mathcal{V}$ denotes the node set and $\mathcal{E}$ denotes the set of edges $e \in \mathcal{E}$. And there are two types of nodes in the graph, *i.e.*, $\mathcal{V} = \mathcal{V}_M \cup \mathcal{V}_T$, where $\mathcal{V}_M = \{x_m\}$ is the molecule node set and $\mathcal{V}_T = \{p_t\}$ is the property node set. Edges $\mathcal{E} \subseteq \mathcal{V}_M \times \mathcal{V}_T$ are connected between these two types of nodes and the edge type of $e_{i,j}$ is initialized according to the label $y_{i,j}$, *i.e.*, *active* (for y=1) or *inactive* (for y=0).

For a molecule x_i, a graph-based encoder [Xu *et al.*, 2019] is used following [Guo *et al.*, 2021] to obtain its embedding:

$$\boldsymbol{x}_i = f_{mol}(x_i), \tag{1}$$

where $\boldsymbol{x}_i \in \mathbb{R}^d$. For a property node p_t, its embedding is randomly initialized for simplicity with the same length as molecules, *i.e.*, $\boldsymbol{p}_t \in \mathbb{R}^d$. Hence the node features $\boldsymbol{h}_i^0$ are initialized with molecule and property embeddings respectively:

$$\boldsymbol{h}_i^0 = \begin{cases} \boldsymbol{p}_i & \text{for } i \in \mathcal{V}_T \\ \boldsymbol{x}_i & \text{for } i \in \mathcal{V}_M \end{cases}. \tag{2}$$

Moreover, due to the deficiency of data, some molecules may not have labels on some auxiliary properties, leading to a missing edge connection between these molecules and properties. To make the graph topology compact, a special edge type *unk* is used to complement the missing label.

Reformulating Episode as Subgraph The constructed MPG can be very large, *e.g.* in the PCBA dataset [Wang *et al.*, 2012], there are more than 430,000 molecules and 128 properties, and the corresponding MPG can contain more than 10 million edges. It is therefore computationally infeasible to directly work on the whole graph to predict molecular properties. Instead, we resort to subgraphs sampled from the MPG and connect them to episodes in meta-learning.

The episodic meta-learning, which is trained iteratively by sampling batches of episodes, has proven to be an effective training strategy [Finn *et al.*, 2017]. Therefore, to adopt episodic meta-learning on MPG, we propose to reformulate the episode as a subgraph. Specifically, an episode of task $\mathcal{T}_t$ is equivalent to a subgraph containing a property node p_t in $\mathcal{V}_T$, and molecules connected to p_t. Hence, the support set $\mathcal{S}_t$ can be reformulated as a subgraph of MPG:

$$\mathcal{S}_t \sim \mathcal{G}_t^S = \{(x_i, e_{i,t}, p_t), y_{i,t} | x_i \in \mathcal{N}(p_t)\}_{i=1}^{2K}, \tag{3}$$

where p_t is a property node, and $\mathcal{N}(p_t)$ is the neighbors of p_t. A query molecule is sampled as the query set, denoted as:

$$\mathcal{Q}_t \sim \mathcal{G}_t^Q = \{(x_j, p_t), y_{j,t} | x_j \in \mathcal{N}(p_t)\}. \tag{4}$$

By merging two subgraphs, the episode E_t is reformulated as:

$$E_t \sim \mathcal{G}_t = \mathcal{G}_t^S \cup \mathcal{G}_t^Q. \tag{5}$$

The node and edge set of $\mathcal{G}_t$ are denoted as $\mathcal{V}^t$ and $\mathcal{E}^t$ respectively.

Since molecules have multiple properties, other available properties can be used when predicting a novel property of the same molecule. To leverage these auxiliary properties, we add some other property nodes connected to molecule nodes into the subgraph:

$$\mathcal{G}_t^A = \{(x_i, e_{i,a}, p_a), y_{i,a} | p_a \in \mathcal{N}(x_i) \backslash p_t\}_{a=1}^{N_a}, \tag{6}$$

where N_a is the number of auxiliary property, p_a is the auxiliary property node, $x_i \in \mathcal{V}_M^t$ is a molecule node in $\mathcal{G}_t$, and $\mathcal{G}_t^A$ is an auxiliary subgraph. With $\mathcal{G}_t^A$, we extend $\mathcal{G}_t$ as:

$$\mathcal{G}_t = \mathcal{G}_t \cup \mathcal{G}_t^A. \tag{7}$$

and there are totally $2K + N_a + 2$ nodes, $2K$ support molecules, one query molecule, one target property, and N_a auxiliary properties. **From here on out, an episode of meta-learning and a subgraph of the MPG are semantically equivalent in this paper.**

Subgraph Encoding and Prediction   We adopt a massage passing schema [Hamilton *et al.*, 2017] to iteratively update each sampled subgraph $\mathcal{G}_t$. In contrast to the previous work which only takes labels as edges [Cao *et al.*, 2021], we also consider relations between molecules, and design an edge predictor to estimate connections between molecules at each iteration:

$$\alpha_{i,j}^l = \sigma \left(\text{MLP} \left(\exp \left(-|h_i^{l-1} - h_j^{l-1}| \right) \right) \right), \quad (8)$$

where σ is Sigmoid function, h_i^{l-1} and h_j^{l-1} are embeddings of molecules x_i and x_j at (l-1)-th iteration respectively, and $\alpha_{i,j}^l$ is the estimated connection weight between x_i and x_j. To avoid connecting dissimilar molecules, only top-k (k is hyperparameter) edges with the largest estimated weights are kept and the edge type is *mol2mol*. Overall, there are four types of edges in $\mathcal{G}_t$, which are *active*, *inactive* and *unk* between a molecule and a property, and *mol2mol* between molecules.

After constructing the complete subgraph, node embeddings are updated as follows:

$$h_i^l = \text{GNN}^{l-1} \left(h_i^{l-1}, h_j^{l-1}, h_{i,j}^{l-1}, w_{i,j}^l | j \in \mathcal{N}(i) \right), \quad (9)$$

where h_i^l is the embedding of node i at the *l*-th iteration, $h_{i,j}^l$ is edge embedding initialized according to edge type, $\mathcal{N}(i)$ is neighbors of node i, and $w_{i,j}^l$ is the edge weight defined as:

$$w_{i,j}^l = \begin{cases} \alpha_{i,j}^l & e_{i,j} \in \mathcal{E}_{M,M} \\ 1 & \text{otherwise} \end{cases}, \quad (10)$$

where $\mathcal{E}_{M,M}$ is the set of edges between molecules. After L iterations, the final embedding of molecule h_i^L and the property h_t^L are we concatenated to predict the label:

$$\hat{y}_{i,t} = \sigma \left(f_{cls} \left([h_i^L \oplus h_t^L] \right) \right), \quad (11)$$

where $\hat{y}_{i,t} \in \mathbb{R}^1$ is the prediction, and $\oplus$ is a concatenation operation. **For simplicity, we denote $f_{(\theta)}$ as the relation learning module with parameter θ, which includes molecular encoder f_{mol}, property initial embeddings, GNN layers, edge predictors, and classifier f_{cls}.** More details are illustrated in Appendix A.3.

In each subgraph $\mathcal{G}_t$, the task classification loss on the support set $\mathcal{S}_t$ is calculated:

$$\mathcal{L}_{t,\mathcal{S}}^{cls} \left(f_{(\theta)} \right) = -\sum_{\mathcal{S}_t} \left(y \log \hat{y} + (1-y) \log (1-\hat{y}) \right), \quad (12)$$

where y and $\hat{y}$ are short for $y_{i,t}$ and $\hat{y}_{i,t}$ for clarity. Similarly, we can calculate the classification loss on the query set $\mathcal{L}_{t,\mathcal{Q}}^{cls}$.

3.3   Subgraph Sampling Scheduler

Previous few-shot molecular property prediction methods [Guo *et al.*, 2021; Wang *et al.*, 2021] randomly sample episodes with a uniform probability, under the assumption

that they are independent and of equal importance. However, subgraphs centered on different target properties are potentially connected to each other in the built MPG, due to the existence of intersecting nodes or edges. Hence, considering the subgraph dependency, we are motivated to develop a subgraph sampling scheduler that determines which episodes to use in the current batch during meta-training.

Consistency and Discrimination between Subgraphs   We specify the subgraph dependency in two aspects. (1) Each subgraph only has a small number of molecules (K per class), and cannot contain all the information about the target property. For the same target property, subgraphs with different molecules (subgraph (i) and (ii) in Figure 1(b)) can be seen as different views describing the same task and they should be consistent with each other. (2) Meanwhile, subgraphs centered on different target property nodes (subgraph (ii) and (iii) in Figure 1(b)) are episodes of different tasks, and their semantic discrepancy should be enlarged.

Towards this end, the subgraph sampling scheduler, denoted as $z_{(\phi)}$ with parameters ϕ, adopts a pairwise sampling strategy. That is, two subgraphs $\mathcal{G}_t^{(1)}$ and $\mathcal{G}_t^{(2)}$ of the same target property p_t are sampled simultaneously. Specifically, at the beginning of each mini-batch, we randomly sample a pool of subgraph candidates, $P = \{(\mathcal{G}_t^{(1)}, \mathcal{G}_t^{(2)})\}_{t=1}^{N_{pool}}$, which are pairs of subgraphs for the same target property. For a subgraph $\mathcal{G}_t$, the scheduler $z_{(\phi)}$ outputs its selection probability η_t via two steps. The first step calculates the subgraph embedding g_t:

$$g_t = h_t^L + \sigma \left(\sum_{i \in \mathcal{V}^t \setminus p_t} h_i^L \right), \quad (13)$$

which is the pooling of the final embedding of each node, and h_t^L is final embedding of target property p_t. Then, we take g_t as input to the scheduler $z_{(\phi)}$ to get the selection probability η_t:

$$\eta_t = z_1 \left(g_t + z_2 \left(\sum_{t' \in P \setminus \mathcal{G}_t} g_{t'} \right) \right), \quad (14)$$

where z_1 and z_2 are MLP and together constitute $z_{(\phi)}$. Then, η_t is normalized by softmax to get a reasonable probability value. Thus, for each episode pair $(\mathcal{G}_t^{(1)}, \mathcal{G}_t^{(2)})$ in the candidate pool, the selection probability can be computed as $(\eta_t^{(1)} + \eta_t^{(2)})/2$, and we sample B from N_{pool} in the candidate pool to form a mini-batch according to selection probability.

To encourage consistency between subgraphs of the same target property and discrimination between different target properties, we adopt the NT-Xent loss [Hjelm *et al.*, 2019] which is widely used in contrastive learning. Subgraphs of the same target property are positive pairs and those of different target properties are negatives, and the contrastive loss in a mini-batch is as follows:

$$\mathcal{L}^{ctr} = \frac{1}{B} \sum_{t=1}^{B} -\log \frac{e^{\text{sim}\left(g_t^{(1)}, g_t^{(2)}\right)/\tau}}{\sum_{t'=1, t' \neq t}^{B} e^{\text{sim}\left(g_t^{(1)}, g_{t'}^{(2)}\right)/\tau}}, \quad (15)$$

where B is mini-batch size, $\text{sim}(\cdot, \cdot)$ is cosine similarity and τ is the temperature parameter.

Algorithm 1 Training and optimization algorithm.

Input: Molecule-Property relation Graph (MPG)
Output: Relation learning module $f_{(\theta)}$, subgraph sampling scheduler $z_{(\phi)}$.

1: **while** not done **do**
2:    Sample N_{pool} episode pairs $\{(\mathcal{G}_t^{(1)}, \mathcal{G}_t^{(2)})\}_{t=1}^{N_{pool}}$ as candidates
3:    Calculate selection probability η_t by Eqn. (14) for each candidate episode
4:    Select B episode pairs $\{(\mathcal{G}_t^{(1)}, \mathcal{G}_t^{(2)})\}_{t=1}^{B}$ from candidates according to η_t to form a mini-batch
5:    **for** $t = 1, \ldots, B$ **do**
6:       Calculate classification loss on support set $\mathcal{L}_{t,\mathcal{S}}^{cls}$ by Eqn. (12) on both $\mathcal{G}_t^{(1)}$ and $\mathcal{G}_t^{(2)}$
7:       Do inner-loop update $\theta' \leftarrow \theta - \beta_{inner} \nabla_\theta \mathcal{L}_{t,\mathcal{S}}^{cls} (f_{(\theta)})$ on both $\mathcal{G}_t^{(1)}$ and $\mathcal{G}_t^{(2)}$
8:       Calculate classification loss on query set $\mathcal{L}_{t,\mathcal{Q}}^{cls}$ by Eqn. (12) on both $\mathcal{G}_t^{(1)}$ and $\mathcal{G}_t^{(2)}$
9:    **end for**
10:   Calculate contrastive loss $\mathcal{L}^{ctr}$ by Eqn. (15)
11:   Do outer-loop optimization by Eqn. (17)
12:   Update scheduler z by Eqn. (19)
13: **end while**

3.4 Training and Testing

In this subsection, we introduce the optimization strategy of relation learning module $f_{(\theta)}$ and subgraph sampling scheduler $z_{(\phi)}$ in training and testing.

Optimization of Relation Learning Module Following [Finn *et al.*, 2017], a gradient descent strategy is adopted to obtain a good initialization. Firstly, at the beginning of a mini-batch, subgraph sampling scheduler z is used to sample B episode pairs $\{(\mathcal{G}_t^{(1)}, \mathcal{G}_t^{(2)})\}_{t=1}^{B}$ from candidates.

For each episode, in the inner-loop optimization, the loss on the support set defined in Eqn.(12) is computed to update the parameters θ by gradient descent:

$$\theta' \leftarrow \theta - \beta_{inner} \nabla_\theta \mathcal{L}_{t,\mathcal{S}}^{cls} (f_{(\theta)}), \quad (16)$$

where β_{inner} is the learning rate. After updating the parameter, the loss of query set is computed, denoted as $\mathcal{L}_{t,\mathcal{Q}}^{cls}$. Finally, we do an outer loop to optimize both the classification and contrastive loss with learning rate β_{outer} across the mini-batch:

$$\theta \leftarrow \theta - \beta_{outer} \nabla_\theta \mathcal{L} (f_{(\theta')}), \quad (17)$$

where the meta-training loss $\mathcal{L}(f_{(\theta')})$ is computed across the mini-batch:

$$\mathcal{L}(f_{(\theta')}) = \frac{1}{2B} \sum_{t=1}^{B} \left(\mathcal{L}_{t,\mathcal{Q}}^{cls\,(1)} + \mathcal{L}_{t,\mathcal{Q}}^{cls\,(2)} \right) + \lambda \mathcal{L}^{ctr}, \quad (18)$$

where λ is hyperparameter and $\mathcal{L}^{ctr}$ is defined by Eqn.(15), and $\mathcal{L}_{t,\mathcal{Q}}^{cls\,(1)}$, $\mathcal{L}_{t,\mathcal{Q}}^{cls\,(2)}$ are query loss of $\mathcal{G}_t^{(1)}$ and $\mathcal{G}_t^{(2)}$ respectively. The complete procedure is described in Algorithm 1.

In testing, for a new property p_t in $\{p_{test}\}$, auxiliary properties are selected from $\{p_{train}\}$ and $f_{(\theta)}$ is finetuned by Eqn.(16).

Optimization of Subgraph Sampling Scheduler Since sampling cannot be directly differentiated, similar to [Yao *et al.*, 2021], we use policy gradient [Williams, 1992] to optimize the scheduler $z_{(\phi)}$. To encourage mining negative samples that are indistinguishable from positives, it is intuitive to take the value of contrastive loss $\mathcal{L}^{ctr}$ as reward R:

$$\phi \leftarrow \phi + \gamma \nabla_\phi \log P(\boldsymbol{\eta})(R - b), \quad (19)$$

where $\boldsymbol{\eta} = \{\eta_t\}_{t=1}^{B}$ is selection probability of sampled episode in a mini-batch, γ is learning rate and b is moving average of reward.

4 Experiments

The following research questions guide the remainder of the paper. (**RQ1**) Can our proposed GS-Meta outperform SOTA baselines? (**RQ2**) How do auxiliary properties affect the performance? (**RQ3**) Can the episode reformulation and sampling scheduler improve performance? (**RQ4**) How to interpret the scheduler that models the episode relationship?

4.1 Experimental Setup

We use five common few-shot molecular property prediction datasets from the MoleculeNet [Wu *et al.*, 2018]. Details are in Appendix B.

For a comprehensive comparison, we adopt two types of baselines: (1) *methods with molecular encoder learned from scratch*, including Siamese [Koch *et al.*, 2015], ProtoNet [Snell *et al.*, 2017], MAML [Finn *et al.*, 2017], TPN [Liu *et al.*, 2019], EGNN [Kim *et al.*, 2019], Iter-RefLSTM [Altae-Tran *et al.*, 2017], and PAR [Wang *et al.*, 2021]; and (2) *methods which leverage pre-trained molecular encoder*, including Pre-GNN [Hu *et al.*, 2020], Meta-MGNN [Guo *et al.*, 2021], Pre-PAR [Wang *et al.*, 2021] and we denote Pre-GS-Meta as our method equipped with Pre-GNN. More details about these baselines are in Appendix C.1. We run experiments 10 times with different random seeds and report the mean and standard deviations.

4.2 Main Results (RQ1)

The overall performance is shown in Table 1. The experimental results show that our GS-Meta and Pre-GS-Meta outperform all baselines consistently with 6.93% and 5.71% average relative improvement respectively. Moreover, those relation-graph-based methods (*i.e.,* TPN, EGNN, PAR and GS-Meta) mostly perform better than traditional methods. This indicates that it is effective to exploit relations between molecules in a graph and it is more effective to exploit both molecules and properties together as our method performs best. Further, the improvement varies across different datasets. For example, GS-Meta gains 13.68% improvement on SIDER but 0.93% improvement on MUV. We argue this is due to the fact that there are more auxiliary properties available on SIDER, and also that there are no missing labels in SIDER compared to 84.2% missing labels on MUV. Fewer auxiliary properties and the presence of missing labels prevent utilizing information from auxiliary properties. This phenomenon is further investigated in Section 4.3.

Method	Tox21		SIDER		MUV		ToxCast		PCBA	
	10-shot	1-shot	10-shot	1-shot	10-shot	1-shot	10-shot	1-shot	10-shot	1-shot
Siamese	$80.40_{(0.35)}$	$65.00_{(1.58)}$	$71.10_{(4.32)}$	$51.43_{(3.31)}$	$59.96_{(5.13)}$	$50.00_{(0.17)}$	-	-	-	-
ProtoNet	$74.98_{(0.32)}$	$65.58_{(1.72)}$	$64.54_{(4.32)}$	$57.50_{(2.34)}$	$65.88_{(4.11)}$	$58.31_{(3.18)}$	$68.87_{(0.43)}$	$58.55_{(0.52)}$	$64.93_{(1.94)}$	$55.79_{(1.45)}$
MAML	$80.21_{(0.24)}$	$75.74_{(0.48)}$	$70.43_{(0.76)}$	$67.81_{(1.12)}$	$63.90_{(2.28)}$	$60.51_{(3.12)}$	$68.30_{(0.59)}$	$61.12_{(0.94)}$	$66.22_{(1.31)}$	$62.04_{(1.73)}$
TPN	$76.05_{(0.24)}$	$60.16_{(1.18)}$	$67.84_{(0.95)}$	$62.90_{(1.38)}$	$65.22_{(5.82)}$	$50.00_{(0.51)}$	-	-	-	-
EGNN	$81.21_{(0.16)}$	$79.44_{(0.22)}$	$72.87_{(0.73)}$	$70.79_{(0.95)}$	$65.20_{(2.08)}$	$62.18_{(1.76)}$	$74.02_{(1.11)}$	$64.17_{(0.89)}$	$69.92_{(1.85)}$	$62.14_{(1.58)}$
IterRefLSTM	$81.10_{(0.17)}$	$\underline{80.97}_{(0.10)}$	$69.63_{(0.31)}$	$71.73_{(0.14)}$	$49.56_{(5.12)}$	$48.54_{(3.12)}$	-	-	-	-
PAR	$\underline{82.06}_{(0.12)}$	$80.46_{(0.13)}$	$\underline{74.68}_{(0.31)}$	$\underline{71.87}_{(0.48)}$	$\underline{66.48}_{(2.12)}$	$\underline{64.12}_{(1.18)}$	$\underline{74.78}_{(1.53)}$	$\underline{69.45}_{(1.24)}$	$\underline{70.05}_{(0.94)}$	$\underline{67.77}_{(1.04)}$
GS-Meta	$\mathbf{85.85}_{(0.26)}$	$\mathbf{84.32}_{(0.89)}$	$\mathbf{83.72}_{(0.54)}$	$\mathbf{82.84}_{(0.67)}$	$\mathbf{67.11}_{(1.95)}$	$\mathbf{64.70}_{(2.88)}$	$\mathbf{81.55}_{(0.19)}$	$\mathbf{80.03}_{(0.26)}$	$\mathbf{72.16}_{(0.71)}$	$\mathbf{70.03}_{(1.56)}$
Pre-GNN	$82.14_{(0.08)}$	$81.68_{(0.09)}$	$73.96_{(0.08)}$	$73.24_{(0.12)}$	$67.14_{(1.58)}$	$64.51_{(1.45)}$	-	-	-	-
Meta-MGNN	$82.97_{(0.10)}$	$82.13_{(0.13)}$	$75.43_{(0.21)}$	$73.36_{(0.32)}$	$68.99_{(1.84)}$	$65.54_{(2.13)}$	-	-	-	-
Pre-PAR	$\underline{84.93}_{(0.11)}$	$\underline{83.01}_{(0.09)}$	$\underline{78.08}_{(0.16)}$	$\underline{74.46}_{(0.29)}$	$\underline{69.96}_{(1.37)}$	$\underline{66.94}_{(1.12)}$	$\underline{79.41}_{(0.08)}$	$\underline{76.58}_{(0.15)}$	$\underline{73.71}_{(0.61)}$	$\underline{72.49}_{(0.61)}$
Pre-GS-Meta	$\mathbf{86.91}_{(0.41)}$	$\mathbf{86.46}_{(0.55)}$	$\mathbf{85.08}_{(0.54)}$	$\mathbf{84.45}_{(0.26)}$	$\mathbf{70.18}_{(1.25)}$	$\mathbf{67.15}_{(2.04)}$	$\mathbf{83.81}_{(0.16)}$	$\mathbf{81.57}_{(0.18)}$	$\mathbf{79.40}_{(0.43)}$	$\mathbf{78.16}_{(0.47)}$

Table 1: ROC-AUC scores on benchmark datasets, compared with methods learned from scratch (first group) and methods that leverage pre-trained molecular encoder (second group). The best is marked with **boldface** and the second best is with underline.
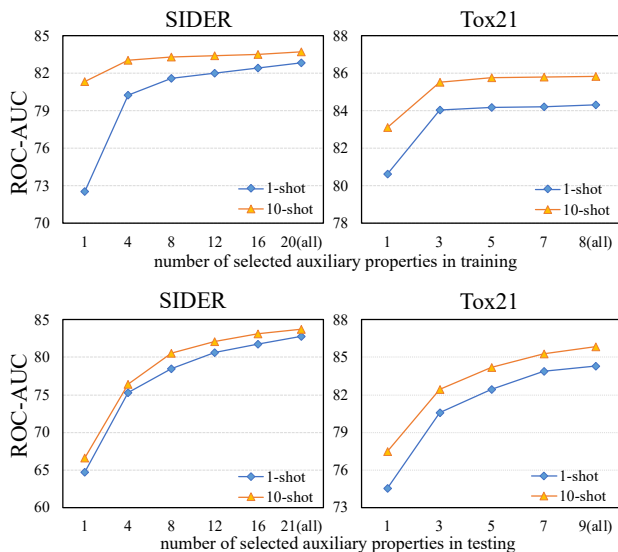

Figure 3: Performance of different numbers of selected auxiliary properties in training (top) and testing (bottom).

Figure 4: Performance with different missing label ratios in SIDER, Tox21 and ToxCast-CEETOX under the 10-shot scenario.

4.3 Analysis of Auxiliary Property (RQ2)

Effect of the Number of Auxiliary Properties We explore the effect of auxiliary properties by varying the number of sampled auxiliary properties. Since auxiliary property sampling occurs during both training and testing, here we consider two scenarios: 1) **effect of the number of sampled auxiliary properties during training**: keep the number of sampled auxiliary properties during testing constant and change the number during training; 2) **effect of the number of sampled auxiliary properties during testing**: keep the number of sampled auxiliary properties during training constant and change the number during testing.

As shown in Figure 3, the performance improves as the number of auxiliary properties increases in both training and testing, confirming our motivation that known properties of molecules help predict new properties. This is because more auxiliary properties contain more information at each training and inference step. In addition, reducing the number of auxiliary properties in training has less impact on performance 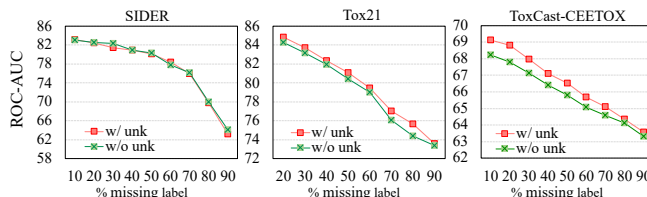than in testing, which suggests that when faced with a large number of auxiliary properties, sampling some of them during training can be an effective way to train the model and does not lead to significant performance degradation.

Effect of the Ratio of Missing Labels We further investigate the effect of missing labels on auxiliary properties by randomly masking labels in the training set, which means the model has less training data and fewer auxiliary properties possible for testing. Two different approaches are compared: 1) **w/ *unk***: completing missing label with a special edge *unk*; 2) **w/o *unk***: no process of the missing label.

Figure 4 shows the results under the 10-shot scenario. Since the proportion of missing labels in the training set on Tox21 itself is higher than 10%, we start masking from 20%. The performance gradually decreases as the percentage of missing labels increases. In addition, *unk* edges have no noticeable effect on SIDER, but improve performance on Tox21 and ToxCast-CEETOX by 0.81% and 0.96% respectively. This can be due to imbalanced labeling: SIDER is more balanced than Tox21 and ToxCast-CEETOX. Moreover, the results show that when masking 70%, 40% and 40% training labels on SIDER, Tox21 and ToxCast-CEETOX respectively, our method still achieves a comparable performance against SOTA. It proves that our method has robust and promising performance despite the missing training data. Results under the 1-shot scenario is in Figure 6 in Appendix.

4.4 Analysis of Episode Reformulation and Sampling Scheduler (RQ3)

Ablation Study We conduct ablations to study the effectiveness of episode reformulation and sampling scheduler. For episode reformulation, the following variants are analyzed: 1)**w/o m2m**: remove *mol2mol* edges in MPG; 2)**w/o E**:

Method	1-shot	10-shot
GS-Meta	**84.32**	**85.85**
w/o m2m	83.91($\downarrow$0.41)	84.80($\downarrow$1.05)
w/o E	72.54($\downarrow$11.78)	75.93($\downarrow$9.92)
w/o S	83.14($\downarrow$1.18)	84.51($\downarrow$1.34)
w/o CL	83.30($\downarrow$1.02)	84.66($\downarrow$1.19)
w/o S, w/o CL	82.64($\downarrow$1.68)	84.32($\downarrow$1.53)

Table 2: Ablation study on Tox21

Method	1-shot	10-shot
PAR	70.41(0.83s)	74.65(1.13s)
PAR (w/ ATS)	69.94(2.42s)	75.10(2.90s)
GS-Meta	**85.94**(3.11s)	**87.67**(3.59s)
GS-Meta (w/ ATS)	84.73(6.80s)	86.88(7.11s)
GS-Meta (w/o S)	84.72(2.20s)	86.81(2.60s)

Table 3: Performance and time cost on ToxCast-BSK

remove edge type in MPG, *i.e.*, do message passing in Eqn.(9) without $h_{i,j}$. For the sampling scheduler, the following variants are analyzed: 1)**w/o S**: randomly select episode without a sampling scheduler; 2)**w/o CL**: optimize model parameters in Eqn. (17) without contrastive loss $\mathcal{L}^{ctr}$; 3)**w/o S, w/o CL**: do not use scheduler and contrastive loss.

As in Table 2, GS-Meta outperforms all the variants, indicating that our proposed subgraph reformulation and scheduling strategy are effective. Results on SIDER are in Table 10 in Appendix. Removing the type of edges causes a significant performance drop, which validates that the information of labels can be fused into the graph by using them as edge types. And removing both contrastive loss and the scheduler degrades the model performance, indicating that our design of contrastive loss and the scheduler is reasonably effective.

Comparing with Other Scheduler To further explore the effects of the designed sampling scheduler, we compare PAR and our GS-Meta with other scheduler. Here we adopt ATS [Yao *et al.*, 2021], which is a SOTA task scheduler for meta-learning proposed recently. ATS takes gradient and loss as input to characterize the difficulty of candidate tasks. For a comprehensive evaluation, we compare both the performance and time cost of a mini-batch during training.

The results on ToxCast-BSK are in Table 3, where (w/ ATS) indicates using ATS as the sampling scheduler and (w/o S) indicates randomly selecting without the scheduler. Note that the original PAR itself does not have a scheduler. We reach two conclusions. First, ATS does not improve performance significantly (*PAR(w/ ATS)* vs *PAR*, *GS-Meta(w/ ATS)* vs *GS-Meta(w/o S)*). This suggests that ATS is not applicable in our scenario of few-shot molecular property prediction and the SOTA methods. And our scheduler is able to improve the model performance (*GS-Meta* vs *GS-Meta(w/o S)*). Secondly, ATS is more time-consuming. ATS is around three times slower compared with random sampling (*PAR(w/ ATS)* vs *PAR*, *GS-Meta(w/ ATS)* vs *GS-Meta(w/o S)*), but our scheduler is faster (*GS-Meta* vs *GS-Meta(w/o S)*). This is because ATS needs to compute the loss and gradient backpropagation for each candidate and sample a validation set to get the reward for optimization. While our approach is to reformulate an episode as a subgraph and get the representation of episode by directly encoding it. And we use a contrastive loss to uni-
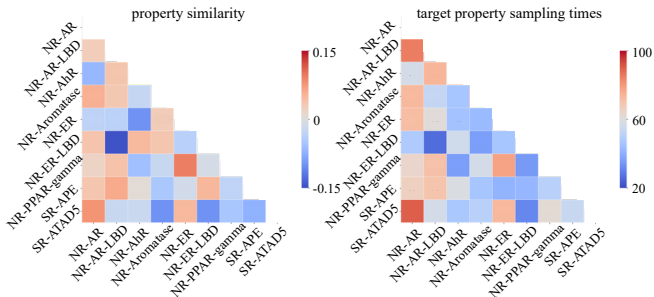

Figure 5: Heatmap of property similarity and statistics of target property sampling times on Tox21.

formly model the relationship between episodes and as an optimization reward for the scheduler. Results on ToxCast-APR are in Table 11 in Appendix.

4.5 Interpretation of the Scheduler (RQ4)
To understand the sampling scheduler, we visualize the sampling result of 9 properties in the training set on Tox21 in Figure 5. The cosine similarity of property embeddings on Tox21 is also visualized. In the sampling result heatmap, the value in row i column j indicates the number of times that property i and property j are sampled in the same mini-batch at the same time. And we run the scheduler 200 times to statistically count the results.

We observe that more similar properties are sampled into the same mini-batch more frequently, *e.g.*, property SR-ATAD5 with property NR-AR and property NR-ER with property NR-PPAR-gamma. And dissimilar properties are sampled less frequently in one mini-batch, *e.g.*, property NR-ER-LBD with property NR-AR-LBD and property SR-ATAD5 with property NR-ER-LBD. This indicates that our scheduler prefers to put similar properties in one mini-batch, analogous to mining hard negative samples. Nevertheless, the sampling result is not exactly consistent with the property embedding similarity, because the scheduler's input is the final pooled embedding of the subgraph, not only the embedding of the target property.

5 Conclusion
We propose a Graph Sampling-based Meta-learning framework to effectively leverage other available properties to predict new properties with a few labeled samples in molecular property prediction. Specifically, we construct a Molecule-Property relation Graph and reformulate an episode in meta-learning as a subgraph of MPG. Further, we consider subgraph consistency and discrimination and schedule the subgraph sampling via a contrastive loss. Empirical results show GS-Meta outperforms previous methods consistently.

This work only considers 2-way classification tasks and does not involve regression tasks. This is because the commonly-used benchmarks for few-shot molecular property prediction are 2-way tasks and few are eligible regression datasets. Our method can generalize to multi-class and regression cases, by assigning different edge attribute values. We put this in future works.

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Appendix

A Details of GS-Meta

A.1 Notations

For ease of understanding, we summarize notations and descriptions in Table 5.

A.2 Reasons to Sampling Subgraphs as Episodes

The size of the constructed MPG can be very large (*e.g.*, containing more than 400,000 molecules in PCBA dataset), and it is not possible to compute direcly on the whole graph during training. Because the molecular encoder f_{mol} needs to encode each molecule to get the initial embedding of molecular nodes in the graph. Encoding molecules using molecular encoder and encoding MPG using GNN, and then doing gradient back propagation will lead to an Out-of-Memory error.

A.3 GNN Layer

Eqn. (9) follows a message passing paradigm, in which embedding is updated by aggregating the information passed from neighboring nodes and edges. At l-th iteration, firstly the aggregated neighborhood embedding $h^l_{\mathcal{N}_{(i)}}$ is obtained:

$$h^l_{\mathcal{N}_{(i)}} \leftarrow \frac{1}{|\mathcal{N}_{(i)}|} \sum_{j \in \mathcal{N}_{(i)}} \left(\left(h^{l-1}_j + h^{l-1}_{i,j} \right) \times w^l_{i,j} \right) \quad (20)$$

where $\mathcal{N}_{(i)}$ is neighbors of node i, $h^{l-1}_{i,j}$ and $w^l_{i,j}$ is embedding and weight of edge. And then we do combination to process information received from neighborhood and node's previous layer embedding h^{l-1}_i:

$$h^l_i \leftarrow \text{LeakyReLU} \left(\mathbf{W}^{(l)}_{\text{msg}} h^l_{\mathcal{N}_{(i)}} + \mathbf{W}^{(l)}_{\text{root}} h^{l-1}_i \right), \quad (21)$$

where $\mathbf{W}^{(l)}_{\text{msg}}$ and $\mathbf{W}^{(l)}_{\text{root}}$ are trainable parameters included in parameters θ of relation learning module $f_{(\theta)}$.

Dataset	Tox21	SIDER	MUV	ToxCast	PCBA
#Compound	7831	1427	93127	8575	437929
#Property	12	27	17	617	128
#Train Property	9	21	12	451	118
#Test Property	3	6	5	158	10
%Label *active*	6.24	56.76	0.31	12.60	0.84
%Label *inactive*	76.71	43.24	15.76	72.43	59.84
%Missing Label	17.05	0	84.21	14.97	39.32

Table 4: Dataset statistics

B Details of Datasets

B.1 Datasets Description

We conduct experiments on five widely used few-shot molecular property prediction datasets(Table 4) in MoleculeNet benchmark [Wu *et al.*, 2018]:

- Tox21[1] is a public database on compound toxicity, which has been used in the 2014 Tox21 Data Challenge.

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[1] https://tripod.nih.gov/tox21/challenge/

Table 5: Notations and Description

Notation	Description
$\mathcal{D}_{test}$	Training data set
$\mathcal{D}_{test}$	Testing data set
$\{\mathcal{T}_{train}\}$	Training task set
$\{\mathcal{T}_{test}\}$	Testing task set
$\mathcal{S}_t, \mathcal{Q}_t$	Support and query set of task $\mathcal{T}_t$
E_t	One episode of task $\mathcal{T}_t$
$\mathcal{G}$	Sample-Property relation Graph
$\mathcal{V}, \mathcal{E}$	Node and edge set of $\mathcal{G}$
$\mathcal{V}_T$	Property node set
$\mathcal{V}_M$	Molecule node set
p_t	The t-th property node in $\mathcal{G}$
x_i	The i-th molecule node in $\mathcal{G}$
$\{p_{train}\}$	property nodes corresponding to $\{\mathcal{T}_{train}\}$
$\{p_{test}\}$	property nodes corresponding to $\{\mathcal{T}_{test}\}$
$\boldsymbol{p_t}$	Initial embedding of tth property node
$\boldsymbol{x_i}$	Initial embedding of ith molecule node
$e_{i,j}$	Edge between node i and node j
$\mathcal{G}^t_S$	Subgraph in $\mathcal{G}$ analogous to $\mathcal{S}_t$
$\mathcal{G}^t_Q$	Subgraph in $\mathcal{G}$ analogous to $\mathcal{Q}_t$
$\mathcal{G}^t_A$	Auxiliary subgraph in $\mathcal{G}$
$\mathcal{G}_t$	Subgraph in $\mathcal{G}$ analogous to E_t
h^l_i	Embedding of node i at l-th layer
$h^l_{i,j}$	Embedding of edge (i,j) at l-th layer
$\alpha^l_{i,j}$	Estimated weight of molecule edge (i,j) at l-th layer
$w^l_{i,j}$	Edge weight of (i,j) at l-th layer
$\hat{y}_{i,t}$	Predicted label of molecule i on property t
$f_{(\theta)}$	relation learning module with parameter θ
$z_{(\phi)}$	the sampling scheduler with parameter ϕ
g_t	subgraph embedding of $\mathcal{G}_t$
η_t	selection propability
$\mathcal{L}^{ctr}$	Contrastive loss in a minibatch
$\mathcal{L}^{cls}_{t,\mathcal{Q}}$	Classification loss of query set on episode $\mathcal{G}_t$
$\mathcal{L}^{cls}_{t,\mathcal{S}}$	Classification loss of support set on episode $\mathcal{G}_t$

- SIDER [Kuhn *et al.*, 2016] contains marketed drugs and adverse drug reactions(ADR), which are grouped into 27 system organ classes.

- MUV [Rohrer and Baumann, 2009] is selected by applying a redefined nearest neighbor analysis for validation of virtual screening techniques.

- ToxCast [Richard *et al.*, 2016] provides toxicology data for a large quantities of compounds based on in vitro high-throughput screening.

- PCBA [Wang *et al.*, 2012] consists of small molecule bioactivities generated by high-throughput screening.

B.2 Datasets Splitting

We adopt public splits provided by [Altae-Tran *et al.*, 2017] on Tox21, SIDER and MUV. For PCBA, we choose the first 5 and last 5 properties as meta-testing and the rest of properties as meta-training. For ToxCast, since the dataset is sparse overall, but the properties can be grouped according to assay providers, and the grouping gives denser results. We first group the dataset by assay providers to obtain a number of sub-datasets, and after discarding sub-datasets with few properties, each sub-dataset is divided into meta-training and

Assay Provider	#Compound	#Property	#Train Property	#Test Property	%Label *active*	%Label *inactive*	%Missing Label
APR	1039	43	33	10	10.30	61.61	28.09
ATG	3423	146	106	40	5.92	93.92	0.16
BSK	1445	115	84	31	17.71	82.29	0
CEETOX	508	14	10	4	22.26	76.38	1.36
CLD	305	19	14	5	30.72	68.30	0.98
NVS	2130	139	100	39	3.21	4.52	92.27
OT	1782	15	11	4	9.78	87.78	2.44
TOX21	8241	100	80	20	5.39	86.26	8.35
Tanguay	1039	18	13	5	8.05	90.84	1.11

Table 6: Details of sub-datasets of ToxCast.

hyper-parameter	Description	Range	Selected
d	dimension of molecule and property embedding.	300	300
L	number of GNN layer.	1∼3	2
β_{inner}	learning rate in inner-loop.	0.01∼0.5	0.05
β_{outer}	learning rate in outer-loop.	0.001	0.001
γ	learning rate of subgraph sampling scheduler.	0.0001∼0.001	0.0005
τ	temperature in ~~Eqn. (15)~~ Eqn. (18)	0.05∼0.5	0.08
λ	regularization of contrastive loss in ~~Eqn. (15).~~	0.01∼0.5	0.05

Table 7: The hyper-parameters.

Method	APR	ATG	BSK	CEETOX	CLD	NVS	OT	TOX21	Tanguay
MAML	64.59	55.45	60.36	61.02	66.22	59.84	62.15	59.52	60.92
ProtoNet	57.08	54.92	53.92	60.25	66.25	54.87	63.11	58.27	58.32
EGNN	67.06	57.28	60.82	60.10	71.53	56.56	66.08	63.32	74.80
PAR	_74.24_	_63.48_	_70.41_	_61.44_	_75.76_	_67.56_	_65.72_	_68.94_	_77.54_
GS-Meta	**87.90**	**79.62**	**85.94**	**67.49**	**78.16**	**71.04**	**72.36**	**87.84**	**89.97**
Pre-PAR	_84.69_	_70.38_	_79.89_	_66.57_	_77.83_	_72.51_	_70.41_	_80.33_	_86.64_
Pre-GS-Meta	**89.49**	**81.69**	**87.28**	**68.55**	**78.69**	**74.36**	**73.56**	**89.46**	**91.10**

Table 8: Detailed performance on each sub-dataset of ToxCast in 1-shot scenario.

Method	APR	ATG	BSK	CEETOX	CLD	NVS	OT	TOX21	Tanguay
MAML	72.66	62.09	66.42	64.08	74.57	66.56	64.07	68.04	77.12
ProtoNet	73.58	59.26	70.15	66.12	78.12	65.85	64.90	68.26	73.61
EGNN	80.33	66.17	73.43	66.51	_78.85_	_71.05_	68.21	76.40	_85.23_
PAR	_82.74_	_68.86_	_74.65_	_67.76_	78.33	70.79	_69.12_	_77.34_	83.39
GS-Meta	**88.95**	**80.44**	**87.67**	**69.50**	**79.95**	**74.77**	**73.46**	**88.78**	**90.48**
Pre-PAR	_86.09_	_72.72_	_82.45_	_72.12_	_83.43_	_74.94_	_71.96_	_82.81_	_88.20_
Pre-GS-Meta	**90.15**	**82.54**	**88.21**	**74.19**	**86.34**	**76.29**	**74.47**	**90.63**	**91.47**

Table 9: Detailed performance on each sub-dataset of ToxCast in 10-shot scenario.

meta-testing and the average of the performance of all sub-datasets is finnaly reported. Details of each sub-dataset are shown in Table 6 and detailed results of each sub-dataset are in Table 8 and Table 9.

C   Details of Implementation

All experiments are conducted on a Ubuntu Server with one 32 GB NVIDIA Tesla V100 GPU.

C.1   Baselines

We adopt two types of baselines, and details of each are listed as follows:

Learn from Scratch: FSL methods with a random initialized molecular encoder.

- Siamese [Koch *et al.*, 2015] uses a duel network to determine if inputs are of the same class.

- ProtoNet [Snell *et al.*, 2017] classifies inputs based on distance between class prototypes.

- MAML [Finn *et al.*, 2017] learns a good model parameter initialization and adapts fast on new tasks via optimization.

- TPN [Liu *et al.*, 2019] constructs a relation graph from input samples via similarity of input and makes label propagation.

- EGNN [Kim *et al.*, 2019] constructs a relation graph from input samples via similarity of input and predicts labels by edges in a graph.

- IterRefLSTM [Altae-Tran *et al.*, 2017] adopts a variant of MatchingNet [Vinyals *et al.*, 2016] in molecular property prediction.

- PAR [Wang *et al.*, 2021] leverages class prototypes to update input representations and designs label propagation for similar inputs in relation graph.

Leverage Pre-trained Model: methods which leverage a pretrained molecular encoder [Hu *et al.*, 2020].

- Pre-GNN [Hu *et al.*, 2020] is a pretrained GNN model using self-supervised tasks and is directly finetuned on the support set.

- Meta-MGNN [Guo *et al.*, 2021] uses Pre-GNN and add self-supervised tasks in meta-training.

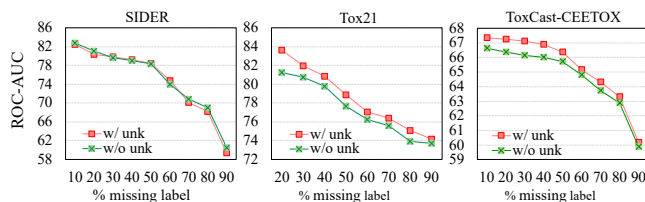- Pre-PAR [Wang *et al.*, 2021] is PAR initialized with Pre-GNN.

Figure 6: Performance with different missing label ratios in SIDER, Tox21 and ToxCast-CEETOX under the 1-shot scenario.

Method	1-shot	10-shot
GS-Meta	**82.84**	**83.72**
w/o m2m	82.12($\downarrow$0.72)	83.09($\downarrow$0.63)
w/o E	57.54($\downarrow$25.30)	61.85($\downarrow$21.87)
w/o S	81.07($\downarrow$1.78)	82.23($\downarrow$1.49)
w/o CL	81.36($\downarrow$1.48)	82.52($\downarrow$1.20)
w/o S, w/o CL	80.69($\downarrow$2.15)	81.94($\downarrow$1.78)

Table 10: Ablation study on SIDER.

Method	1-shot	10-shot
PAR	74.24(0.86s)	82.74(1.07s)
PAR (w/ ATS)	74.51(2.62s)	82.66(3.09s)
GS-Meta	**87.90**(3.04s)	**88.95**(3.47s)
GS-Meta (w/ ATS)	87.02(6.19s)	88.24(7.34s)
GS-Meta (w/o S)	87.10(2.16s)	88.09(2.48s)

Table 11: Performance and time cost on ToxCast-APR.

τ	0.01	0.1	0.5	1
	82.45	82.68	82.57	82.43
λ	0.01	0.1	0.5	1
	82.64	82.77	82.52	81.90

Table 12: Hyper-parameter sensitivity analysis on SIDER under 1-shot setting.

For Tox21, SIDER and MUV, results reported in [Wang *et al.*, 2021] are used. For ToxCast we resplit it and implement baselines using public codes on ToxCast and PCBA.

C.2 GS-Meta

We implement GS-Meta in Pytorch [Paszke *et al.*, 2019] and Pytorch Geometric library [Fey and Lenssen, 2019]. For a fair comparison we adopt a 5-layer GIN [Xu *et al.*, 2019] as molecular encoder for GS-Meta and all baselines. The maximum number of optimization step in meta-training is 2000 and meta-testing is evaluated every 100 steps. MLP in Eqn. (8) and f_{cls} in Eqn. (11) consist two fully connected layers with hidden size 128. Number of candidates N_{pool} and batch size B is 10 and 5 respectively. Hyper-parameter k of connecting molecules is set to 1 in 1-shot and 9 in 10-shot scenario. Table 7 illustrates all the hyper-parameters and the results of hyper-parameter sensitivity analysis are in Table 12. For the number of selected auxiliary properties, on Tox21, SIDER and MUV, we select all possible auxiliary properties in training and testing. On ToxCast and PCBA, the maximum number is 20 in both training and testing.

设定embeddings dimensionality为300，说明了对于每种原子和键的特征（Atom Type、Atom Chirality Tag、Bond Type、Bond Direction），即比如对于Atom Type中的每一种原子类型（如C、O、N等）的特征，在Embedding层都将被映射到/编码为一个300维的嵌入向量，这个维度的大小决定了能够编码多少信息。

这个嵌入维度是一个超参数，更高的维度可以提供更丰富的表示能力，使得模型能够捕捉到更细微的差异和更复杂的模式。但是会增加计算资源以及存在过拟合的风险。这个维度的选择通常基于先前的研究经验，或再根据具体的任务进行调整。（300-500）Embedding层用于将离散的、类别类型的数据转换为连续的、固定长度的向量表示。