

**Statistical Modeling of the Red Sea Chlorophyll  
Concentration and Application to the ERSEM  
Ecological Model**

Thesis by  
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# Chapter 1

## Motivation

### 1.1 Importance of phytoplankton

Phytoplankton are unicellular, free-floating, photosynthetic algae that live in the upper layers of bodies of water (ocean, lakes, rivers or ponds). There exists a wide diversity of phytoplankton species. To this date, about 5000 of them have been identified [1]. Phytoplankton are also highly variable in sizes, ranging from 0.2m for cyanobacteria to 200m for the largest species of diatom [2]. In the oceans, phytoplankton live in the surface layer where there is enough sunlight for photosynthesis.

Phytoplankton plays a fundamental role for the ocean ecology. It is the basis of the marine food web and traps most of the energy used by pelagic ecosystems [2]. Zooplankton graze phytoplankton which are then consumed by higher trophic levels. It has been estimated that nearly 98% of the ocean primary productivity comes from phytoplankton [2]. Phytoplankton are also responsible for maintaining the dissolved oxygen level necessary for other species to survive. However, high phytoplankton concentration also impact their environment by creating dead zone when they die and are decomposed by bacteria, consuming all the available oxygen [2]. Due to the rapid growth of phytoplankton, it responds very well to changes in its environment,

making it a key parameter to monitor the water quality [3].

Due to phytoplankton place at the bottom of the marine food chain, it is a key factor for fisheries. Productive fishing zones like the regions in the Arabian seas, Californian coast, north-west African coast and Chilean coast are explained by the upwelling of cold nutrient rich water favourable to phytoplankton, which in turn feeds higher trophic levels. On the other hand, during the El-Nino phenomenon creates less favourable conditions for phytoplankton in the Eastern Pacific, resulting in a dramatic reduction of fish catches of fisheries in the western coast of South America [4]. Remotely-sensed chlorophyll data have been routinely used since the past decades to help fisheries predict the timing phytoplankton blooms [4]

Phytoplankton also plays the role of a biological CO<sub>2</sub> pump and strongly impact the Earth climate. During photosynthesis, phytoplankton captures carbon and releases oxygen. A part of this organic material stays in the food web, either transmitted to higher trophic level, or degraded by bacteria. Another part, however, sinks to the bottom of the ocean and sediments. It is estimated that phytoplankton account for 48% of Earth carbon fixation [2].

## 1.2 Measuring Chlorophyll Concentration

Chlorophyll is a molecule present in algae, phytoplankton and plants that is critical for photosynthesis. Phytoplankton is a poor absorber of green light, and is responsible for the coloration of plants. When phytoplankton are present in high concentrations the water also takes a detectable green coloration (it can also take a red or blue coloration depending on the type of phytoplankton dominating) [4]. This offers a way to estimate the chlorophyll concentration of the water, which is act as a proxy for phytoplankton concentration.

In-situ measurements of chlorophyll are however expensive and have limited temporal and spatial coverage [4]. In-situ measurement of chlorophyll concentration can be gathered through scientific cruises, buoy stations or gliders (unmanned submarines). These methods are expensive to deploy and therefore the coverage is limited. Political issues, like in the Red Sea, can also be a practical barrier to in-situ measurements.

Satellite measurements of chlorophyll provide excellent proxies for phytoplankton concentrations with a good temporal and spatial coverage [4]. The SeaWiFS, MODIS and MERIS missions have provided an uninterrupted coverage of the world since 1997. High-resolution maps of daily chlorophyll concentration are freely accessible to the scientific community. Despite some limitations, in particular of missing data due to cloud coverage and sunglint, or problematic values in coastal areas, remotely-sensed chlorophyll concentration are used intensively by the scientific community. In regions, like in the Red Sea, where little in-situ measurements are available [5], it is often the most important data source.

### **1.3 Chlorophyll Concentration in the Red Sea**

Typical tropical seas (TTS), like the Red Sea, are characterized by a highly stratified structure, where warm nutrient-depleted surface water is separated by cold nutrient-rich by a steep gradient of temperature zone called pycnocline. The pycnocline acts as barrier that prevents nutrients to reach the surface water. As a result, TTS are oligotrophic and have low chlorophyll concentrations. Until recently, marine biologists have thought that TTS had therefore a very low productivity. However, recent investigations have contested this idea, that different upwelling mechanisms exist that bring new nutrients to the surface water.

Despite being an oligotrophic and challenging environments for marine life, the Red Sea presents a surprisingly rich and diverse ecosystem. Most of it lives in the very developed coral reef system. The source of nutrient for sustaining such a developed ecosystem is not well understood yet, but the interaction with the open sea through the mesoscale eddies is believed to play an important role.

Remotely-sensed chlorophyll data show an important seasonality of the Red Sea primary productivity, that has been linked to winter deep mixing, and the inversion of the wind direction in the southern Red Sea, enhancing intrusion of nutrient rich Gulf of Aden water. Despite this strong seasonality, there is a large interannual variability caused by the unpredictable occurrence of large phytoplanktonic blooms. Diverse causes have been hypothesized for these blooms such as wind-induced mixing, eddies or dust storms carrying nutrients.

Although the Red Sea environment is relatively preserved, it is under increasing pressure due to human activities. An abrupt increase of temperature has occurred in the last decade that threatens the fragile coral reef system. Moreover, the increasing urbanization and fishing activity contribute to the fragilization of this unique ecosystem.

## 1.4 Chlorophyll Concentration Prediction

Models can be useful to identify causes behind the chlorophyll patterns we observe in the Red Sea. Many hypotheses have been made about the drivers of chlorophyll concentration in this regions, but some of them have not been yet investigated through models. The role played by the exchange of water with the Gulf of Aden and winter overturning in the northern Red Sea have been successfully modeled with circulation and ecological models. However, the interaction between the open sea and coral reefs

and the role of sand storms has not been investigated yet. Models, can also be helpful in discovering new dynamics affecting the chlorophyll concentration. In particular, the interaction between the productivity level of the different regions of the Red Sea has not been studied yet.

Model predictions for chlorophyll concentration can also have practical applications. Phytoplankton blooms can be harmful to humans and marine life and are closely monitored in many regions of the world. In the Red Sea, where tourism and aquaculture are developing it is likely to become a concern too. Phytoplankton is also directly, and indirectly through zooplankton, the cause of microfouling that affects desalination plants. Anticipating a phytoplanktonic bloom might therefore be helpful in taking preventive actions. Finally, due to their short life-cycle, phytoplankton concentration reacts quickly to changes the environment, making it a key variable in water quality monitoring.

## 1.5 Modeling Chlorophyll Concentration

Ecological ordinary differential equation (ODE) deterministic models are a popular way to model marine ecology. Such models can be as simple as the nutrient-phytoplankton-zooplankton (NPZ) model that only has three variables representing two trophic level, or as complex as the European regional seas ecosystem model (ERSEM) that has dozens of variables and represent many ecological, biological and chemical interactions. Such a model has been couple to the MITgcm circulation model used to simulate the Red Sea ecology. However the complexity of these models makes them difficult to deploy and interpret their results.

On the other hand, data-driven statistical models are relatively easier to apply. They are relevant when the phenomenon producing the data is very complex or poorly

known. They have been applied to predict chlorophyll concentration, mostly in small regions that have complex dynamics. Some statistical models, such as linear regression, GAM or tree regression have the advantage of being easy to interpret, and can be used to understand the dynamics driving the chlorophyll concentration.

Phenomena such as propagation and diffusion play a key role in the chlorophyll spatial concentration, but are difficult to represent without spatial modeling. There is also a difference in the chlorophyll patterns of different regions of the Red Sea, in particular between the nutrient rich southern Red Sea and the oligotrophic northern Red Sea, and between the open ocean and the coastal waters. There is however no clear cut division between regions with different pattern, making it difficult to divide the Red Sea into regions. Finally the different regions of the Red Sea are believed to interact. A model is therefore needed to account for the spatial and temporal interaction of the chlorophyll.

Classical geostatistics is the most widely used spatial statistical models. It models spatial data as the realization of a two dimensional Gaussian process, of which one can estimate the parameters. Geostatistics can be easily extended to spatio-temporal datasets. Many flexible ways of constructing space-time covariance functions for these models have been proposed recently. Space-time geostatistics has been applied to many environment studies, but not to chlorophyll data yet.

# Chapter 2

## Plan

### 2.1 Task 1: Dataset building and Exploration

*Duration: 2 months (by December 2014)*

*Submission: Journal of Marine Systems*

*Collaborator: Dionysios Raitsos*

#### 2.1.1 Motivation

A preliminary task to data modeling, is the gathering, cleaning and exploration of the data. Given the complexity and the size (40 GB) of the data, this is not an easy task. This first data analysis, will reveal if enough data has been gathered to make meaningful forecast, and what accuracy we can expect from the models. This step will also provide information that will help in designing statistical models: most significant variables, differences between regions, relevant data transformation, etc. Finally, this step will identify patterns in the data that will be useful to qualitatively evaluate predictive models.

### 2.1.2 Open Questions

- Can we efficiently identify outliers in the chlorophyll values?
- Is there a way to efficiently fill the missing values in the chlorophyll dataset?
- Can the data help understanding the mechanisms behind extreme blooms in the Red Sea?
- Can the hypothesizes about the dynamics behind the chlorophyll seasonal cycle be confirmed by the data?
- Are there more blooms in the past years?

### 2.1.3 Method and Work Done

1. Identify data sources and load the data60
2. Clean the data and fill missing values (DINEOF).....50
3. Align and format the data in order to have a unique dataset...0
4. Explore the dataset..20
  - Study the correlation between chlorophyll and other variables (Linear Regression, GAM, data transformations)
  - Select variables (Lasso, single variable regression, multistep regression)
  - Study the regional aggregation (ACF)
  - Explore spatiotemporal correlations (hovmoller plots, PCA, variograms)
  - Estimate the Bayes factor/



### 2.1.4 Expected Outcomes

- A cleaned dataset that can be used in the following tasks
- A comprehensive exploration of the available data for chlorophyll study in the Red Sea
- A preliminary variable selection
- A clear picture of the major spatio-temporal patterns in the data
- A critical evaluation of the current hypothesis about the chlorophyll dynamics in the Red Sea

## 2.2 Task 2: Forecasting Chlorophyll Concentration in Regional Aggregates

*Duration: 2 months (by February 2015)*

*Submission: Progress in Oceanography*

*Collaborator: Dionysios Raitsos*

### 2.2.1 Motivation

Chlorophyll data is very complex. It is therefore useful to first simplify it by aggregating it spatially. The space-time dynamics of the chlorophyll data reflects the highly nonlinear dynamics of the underlying physical, chemical and biological phenomena. As shown by the north-south gradient and the seasonal behavior, the resulting space-time process is nonstationary in time and in space. The high-dimensionality in space can be reduced by considering a regional aggregation of the results. This would allow us to focus on the global scale phenomena: such as the interactions between neighboring regions, the time-scale of large events and the difference in the physical variables affecting the chlorophyll concentration in each region. In the following tasks, these simple predictive models will also be a reference for evaluating more complex ones.

### 2.2.2 Open Questions

- Is the biological aggregation of the Red Sea proposed by (Raitsos 2013) statistically meaningful?
- Can clustering methods be used to identify marine ecological zones based on chlorophyll data?

- Can a simple forecasting model allow us to understand the causes of chlorophyll blooms?
- Can the current hypotheses about the seasonal chlorophyll dynamics be validated?

### 2.2.3 Method

1. Define datasets (training and test datasets, cross-validation).....	0
2. Variable selection (Lasso, L1 regression, single-variable linear regression).....	0
3. Define regional aggregations (unsupervised learning, Hierarchical clustering, K-means).....	50
4. Forecasts chlorophyll concentration (linear regression, GAM models, diagnostic, k-nearest neighbors).....	0
5. Predicting future extreme blooms (nearest-neighbours, logistic regression, decision trees).....	0

### 2.2.4 Expected Outcomes

- A regional division of the Red Sea that has been quantitatively evaluated.
- A critic of current hypothesis about the chlorophyll dynamics in the Red Sea.
- A lower bound on the performance of a more sophisticated model.
- An assessment of the limitation of aggregate methods for Chlorophyll data.
- An understanding on how the treatment of spatial correlations can improve the results.

## 2.3 Task 3: Global geostatistical model for forecasting

*Duration: 1 month (by March 2015)*

*Submission: Spatial Statistics*

### 2.3.1 Motivation

Geostatistical methods can be used to construct dynamical models for forecasting the chlorophyll concentrations that we can compare to deterministic models. Geostatistics is a robust method to model spatio-temporal data. Recently there has been a lot of research on expanding it to model spatio-temporal data. With Kriging, these models are powerful ways to do spatio-temporal prediction. As a particular case of Kriging, by predicting the spatial future field given the observation of the present field, we can derive a linear dynamical model. This linear model can be employed in a filtering setting like the Kalman filter. This is a desirable setup, as it is similar to the way deterministic models are employed to do forecasts given past observations.

### 2.3.2 Open Questions

- Can a global geostatistical model fit chlorophyll data?
- How non stationary is the data in time and space?
- What spatiotemporal covariance functions best fit the chlorophyll data?
- Can geostatistical methods be employed in a filtering setup?

### 2.3.3 Method

This task has already been started and had been the object of a submission for publication. The remaining work includes: Use the new dataset and the new covariates Compare the results to the ones of with the regional aggregates Expected Outcomes A methodology to employ a geostatistical model in a filtering problem. A characterization of the space-time non stationarity of the data, and the interaction of the temporal and spatial dimensions. An understanding of how spatial aggregation and geostatistical models can be used in the same model.

## 2.4 Task 4: Local geostatistical model for forecasting

*Duration: 3 months (by June 2015)*

*Submission: Journal of the American Statistical Association (Case Study)*

*Collaborator: Raphael Huser*

### 2.4.1 Motivation

This part will bring together the results of the two preceding tasks to develop a predictive model that takes into account the large-scale dynamics and the regional spatio-temporal dynamics. In task 2, a predictive model is built, that represents the large scales behaviour of the Red Sea, but the spatial dimension inside each region is not addressed. We expect local features to play a role, such as the proximity to the coast, the bathymetry, proximity to other regions or major cities, etc. In task 3, we developed a methodology to use a geostatistical model in a dynamic fashion to do pixel-scale forecast. In this task, each regions will be modeled separately by a local geostatistical model that can do local prediction. These models will have access to aggregate covariates from neighboring regions in represent the global scale behaviours.

### 2.4.2 Open Questions

- What are the most adapted space-time covariance models for chlorophyll data?
- How to use global covariates in a geostatistical model?
- What are the differences in the fine-scale dynamics of chlorophyll in each region?

- Can the fine scale behaviour of phytoplankton be predicted accurately?
- What are the spatial features that are important for the chlorophyll dynamics?

### **2.4.3 Method**

- Extract local dataset from previous tasks
- Design the training and test datasets, and the cross-validation method
- Design and evaluate the mean function given the past covariates
- Fit the local geostatistical model to the residuals.
- Evaluate the model predictions and compare the results with task 2 and 3.

### **2.4.4 Expected Outcomes**

- A methodology to aggregate local geostatistical models
- An improvements in the prediction skills over the models of task 2 and 3.
- An understanding of the differences between each regions.
- A critical evaluation of the space-time covariance models for fitting chlorophyll data.
- A better characterization of the regional chlorophyll dynamics.

## 2.5 Task 5: Assimilation of 1D ecological models and comparison to statistical models

*Duration: 3 months (by September 2015)*

*Submission: Journal of Geophysical Research*

*Collaborator: George Triantafyllou / Boujeema*

### 2.5.1 Motivation

The three previous tasks focus on constructing increasingly sophisticated predictive models for the chlorophyll concentration in the Red Sea. In this part these models will be compared to a 1D ecological model (ERSEM). This model is well detailed and very complex. The goal of this part will be to identify the merits of each modeling approach, and propose ways in which they can complement each other. To allow for comparison, the model will be run in each of the regions found in task 2. Available data will also be assimilated to the model through a smoothing assimilation scheme that will use an expectation-maximization algorithm for parameters estimation.

### 2.5.2 Open Questions

- Are statistical methods competitive for forecasting chlorophyll concentrations?
- How can statistical and deterministic models complements each other?
- Can statistical method forecast interesting dynamical features?
- Are there significant regional differences in the relative performances of both approaches?
- How to estimate the parameters of ecological models?



### **2.5.3 Method**

1. Define the metrics for comparison
2. Calibrate the ERSEM model on each of the regions
3. Define an assimilation scheme and the data for the ERSEM model
4. Implement the assimilation scheme
5. Run the simulation and aggregate the results
6. Do the comparisons with the statistical models

### **2.5.4 Expected Outcomes**

- A complete set of measures of the prediction skills of each approach.
- A method to estimate assimilation and model parameters in an assimilated ecological model.
- A set of case studies of the behaviours of each method for forecasting interesting events.
- An understanding of the limitations of geostatistical models to predict nonlinear dynamics.
- Propositions on how the two approaches can complement each other.

## 2.6 Task 6: Improving an Ecological Model Data Assimilation Scheme through Statistical Predictive Models

*Duration: 3 months (by September 2015)*

*Submission: Journal of Geophysical Research*

*Collaborator: George Triantafyllou / Boujeema*

### 2.6.1 Motivation

In the previous task, we compared the forecasts of the ecological ERSEM model to that of the statistical models we developed from tasks 2 to 4. In this task we will study how these two approaches can be complementary. Specifically, we will study the use of statistical forecasts model to improve the forecasts of the ERSEM ecological model. The forecasts of the statistical models will be treated as observations, that can be assimilated by the filtering scheme used with the ERSEM model, and will give an improved forecast. When real observations will be available, they will be assimilated sequentially. This, method will allow the different ERSEM models on each cluster to communicate indirectly their states to one another.

### 2.6.2 Open Questions

- Can statistical predictive models be used to communicate information between deterministic model?
- Would the access to information about other regions improve the model forecasts?

- What are the global patterns of ecological dynamics in the Red Sea?

### **2.6.3 Method**

1. Define new assimilation scheme
2. Define metrics to measure model improvement
3. Prepare training and test datasets
4. Train statistical model
5. Run simulation with assimilation of statistical observation
6. Compare with results of task 5

### **2.6.4 Expected Outcomes**

- An improvement in the prediction skills of the deterministic approach
- A methodology to couple deterministic ecological models through statistical models
- Insights on the global ecological dynamics of the Red Sea

# Chapter 3

## Literature Review

### 3.1 Red Sea large-scale phytoplankton dynamics

Because of the lack of in-situ data, the large-scale phytoplankton dynamics of the Red Sea remain largely unknown [5, 6]. However, in recent studies, remotely-sensed data and computer simulation have been used to improve our knowledge of the biology of this region. The Red Sea is deficient in the major nutrients [7], and the only significant input of fresh water comes from the Gulf of Aden. This explains a general increase of chlorophyll concentration from north to south with the NCRS having the lowest concentration [5]. The Red Sea also displays a distinct seasonality, with the highest chlorophyll concentration in winter. A minor summer peak is also observed around July, everywhere except in the NRS [5]. Despite this regularity, a strong interannual variability is observed, with blooms that can reach mesotrophic concentration levels [5]. According to [6], the variations in the Red Sea ecology are mainly driven by circulation. In the rest of this section, we explore some of the mechanisms that have been linked to the major features chlorophyll concentration.

The exchange of water with the nutrient-rich Gulf of Aden is a major driving mechanism for the whole Red Sea [6]. It is the most important source of nutrients.

The maximum chlorophyll concentration observed in the SRS during the winter is due to the wind-driven water intrusion [5]. In Summer, this exchange of water is believed to be the only significant source of nutrients for the whole Red Sea. The influence of the water intrusion weakens in as the latitude increases, explaining the lowest concentration in the northern half of the Red Sea [5].

Stratification and deep convection also play an important role in allowing nutrient-rich deep waters to mix with waters of the euphotic zone. The vertical mixing is the most vigorous in the NRS during the winter, explaining why its chlorophyll concentration is higher than in the NCRS, where there is a lack of mixing [5]. The NRS mixing is believed to be driven by wind [5].

The Red Sea circulation is strongly influenced by mesoscale eddies [8] that could impact primary production. In particular, the anti-cyclonic eddy in the CRS is believed to control the June concentration peak and summer productivity in this region, by transporting nutrients and/or phytoplankton from the adjacent coral reefs [5]. The cold core eddy in the NRS also plays a role in enhancing the vertical mixing in that region.

Aerial depositions could also be an important input of nutrient for the Red Sea, but it has been largely left unexplored [6]. [5] noticed for example that the Sand storms in the Red Sea most frequently happen in June and July, coinciding with the summer chlorophyll peak.

## 3.2 Challenges with remotely-sensed chlorophyll data

Chlorophyll remotely-sensed data in the Red Sea suffer from many problems that need to be taken into account before using them. Until recently, the data coverage in the southern Red Sea was almost 0% during the summer due to sunglint, clouds and aerosols [9]. However the OC-CCI data product that merges different chlorophyll data sources considerably increases the Red Sea coverage. However, this new dataset has not been used to revisit the assumption made in the large-scale Red Sea phytoplankton productivity. If for case I open water, the data in the Red Sea has been shown to be of quality comparable with that the rest of the world [10], case II waters remain a challenge, especially in the SRS where the water is particularly shallow and the coral reef extended [6, 5]. These problems generally lead to an overestimation of the chlorophyll level, but not necessarily to erroneous values [5].

One of the most popular algorithm for the data filling of remotely-sensed data is DINEOF. It is an EOF based data filling approach introduced by [11]. It has been used for multivariate reconstruction of SST fields using chlorophyll data in [12]. In [13], it has been employed to fill chlorophyll data with 70% of missing values. [Taylors 2013] has compared DINEOF with other EOF-based reconstruction algorithms and shown that the former is the best method for data filling. DINEOF has been employed in several other chlorophyll studies [14, 15].

## 3.3 Data Assimilation for marine ecology models

Data assimilation schemes are used to improve the simulations of ecological dynamics models by correcting their predictions with observations. The most common use of

data assimilation is to improve the forecast of an ecological model, by providing it with an estimated initial state. Such prediction capabilities are deployed in operational expert systems, for example to study the impact of human activities on the ecosystem of the Gulf of Pagasitikos [16]. The deployment of such a forecasting system in the Red Sea is currently under study [6]. Hindcasting, the estimation of unobserved variables, is another application of assimilation scheme. [17] showed that they could improve the seasonal and annual hindcast of non assimilated biogeochemical properties in a shelf area (Western English Channel). Finally, data assimilation can be used for reanalysis, to provide estimates of past years biogeochemical variables [18].

In the marine ecology modeling community, two assimilation schemes have been widely used: the Ensemble Kalman filters (EnKF) and the Singular Evolutive Extended Kalman filter (SEIK). The Stochastic EnKF, a Monte-Carlo approximation of the Kalman Filter, has been used in [17, 19]. However, it suffers from sampling errors when the ensemble size is smaller than the number of observations, as is usually the case when assimilating remotely-sensed data. The Singular Evolutive Interpolated Kalman filter (SEIK) is a deterministic version of the EnKF that do not suffer from sampling problems, as it projects the propagated error in a low-dimensional subspace. SEIK has been used by [20, 16]. SEEK is a reduced order version of the Extended Kalman filter (EK), that is intractable in high-dimensions. Like SEIK, it projects the error covariance in a low dimensional space. SEEK has a long history in data assimilation for marine ecology models and is still used in recent studies [18, 16, 21]. [16] shows that SEIK and SEEK are both comparably robust methods for highly non linear systems.

Current assimilation schemes are however affected by problems that have been addressed in the past years. First, biogeochemical variables are usually positive concentration, whereas Kalman filters expect Gaussian variables, and log-transformation

can fail at solving this issue [17]. However, [18] has successfully introduced Gaussian anamorphosis transformations to solve this issue. Second, ecological blooms are intermittent and highly nonlinear, conditions that are challenging for assimilation schemes [20, 16]. Third, SEIK and SEEK both project the error covariance in a subspace, resulting in an underestimation of the estimation error. [21] studied different ways to propagate the error covariance in order to alleviate this issue. Finally, the model error statistics are required by Kalman-derived filters, but are difficult to estimate. [20] proposes to use the  $H_\infty$  method with SEIK in order to remove this requirement.

### 3.4 Statistical models for chlorophyll concentration

Statistical and machine learning models have been used for estimation and classification problems related to phytoplankton concentrations. One application is the detection of harmful algal bloom from spatio-temporal satellite dataset, that has been addressed in [22], in the Gulf of Mexico, using support vector machines. Another application is the estimation of chlorophyll concentration in case II coastal water using satellite radiance data. This problem has been addressed by [23] on the west coast of South Korea, and by [24] using a global dataset of in situ measurements. The former used the support vector regression algorithm, while the latter used also the random forest algorithm.

Machine learning algorithms, in particular Artificial Neural Networks have been very popular for forecasting regional chlorophyll concentration in regions with very complex dynamics. In such regions, deterministic ecological models are usually too complicated to use and less efficient than data-driven approaches. Neural networks



have been widely used for forecasting chlorophyll concentration in fresh as well as in coastal water systems. In [25], temporal recurrent recursive neural network have been used and found superior to traditional time-series model for daily forecasts of chlorophyll concentration. [26] also used recurrent neural networks for daily chlorophyll forecasting in Lake Taihu, China. [27] combined Neural Network and genetic algorithm for nowcasting and forecasting of the chlorophyll concentration up to 14 days ahead, in the tidal dominated coast of Singapore. Finally, [28] used neural networks for the forecasting of algal bloom with one and two weeks lags in the coastal waters of Hong-Kong.

### **3.5 Space-time geostatistical models for forecasting**

The theory of space-time geostatistics is closely related to that of spatial statistics. In fact, the time dimension is an additional dimension. However, the time and space interactions derive from physical interaction, and must be taken into account in the definition of the covariance function [29]. Some space-time can actually be derived from a physical formulation, such as the frozen fields [29], or SDEs [30, 31].

Despite their theoretical interest, physically-derived space-time covariance function have been little used [29]. More popular, are covariance functions built from simple building blocks. One of the most simple types are separable covariance functions, that are the product of a spatial covariance function and temporal covariance function. They are computationally efficient, but are enable to represent space-time interactions [32, 33], making them of limited use for modeling physical systems. The Cressie, Huang spectral characterization theorem of space-time covariance functions

has opened the door to wider ways of constructing them. For example, [34] presented a simple criterion that allows their construction from a very large class of models.

Space-time geostatistical models have been use in a variety of applications. [35] used it for forecast the outbreaks of an invasive specie. They have been used in meteorology to model temperature fields [36, 31] or wind [32, 34], and in environmental studies for ground-level ozone concentration. [37, 29] present recent more details on the theory of space-time geostatistics and its applications.

# Chapter 4

## Preliminary Results

### 4.1 The Problem is the dataset can be handled

- CHL Outliers can be removed
- Data can be filled with DINEOF
- Data can be aligned and aggregated

### 4.2 The Red Sea can be divided into regions with very different dynamics

- North/South mean
- North/South difference in seasonality
- Blooms are localized

### **4.3 There is enough correlation in the dataset to build predictive models**

- Correlation study between CHL and individual predictors
- Percentage of variance explained in CHL
- Estimating the Bayes Factor (Nearest-neighbor)

### **4.4 Geostatistical methods can be used for forecast**

- Demonstrated in Paper 1

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# APPENDICES

## A Appendix A Title

Detailed experimental procedures, data tables, computer programs, etc. may be placed in appendices. This may be particularly appropriate if the dissertation or thesis includes several published papers.

## **B    Appendix B Title**

Your content goes here.

## C Papers Submitted and Under Preparation

- Author 1 Name, Author 2 Name, and Author 3 Name, “Article Title”, *Submitted to Conference/Journal Name*, further attributes.
- Author 1 Name, Author 2 Name, and Author 3 Name, “Article Title”, *Submitted to Conference/Journal Name*, Mon. Year.