

Homework 5.1

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Exercise 6.2 (a) $E[X_1] = \mu$

$$E\left[\frac{X_2+X_3}{2}\right] = \frac{2\mu}{2} = \mu$$

$$E[\hat{\mu}_3] = .1 * \mu + .2 * \mu + .3 * \mu + .4 * \mu = \mu$$

$$E[\bar{X}] = \frac{4 * \mu}{4} = \mu$$

(b) $Var[\hat{\mu}_1] = \sigma^2$

$$Var[\hat{\mu}_2] = .5\sigma^2$$

$$Var[\hat{\mu}_3] = (.1^2 + .2^2 + .3^2 + .4^2) * \sigma^2$$

$$Var[\hat{\mu}_3] = .3\sigma^2 \quad Var[\hat{\mu}_4] = \frac{4}{16} * \sigma^2 = \frac{\sigma^2}{4} \quad \text{This one has the smallest variance.}$$

Exercise 6.5 (a) $E[\hat{p}_1] = p$ unbiased.

$$E[\hat{p}_2] = .5 \text{ unbiased}$$

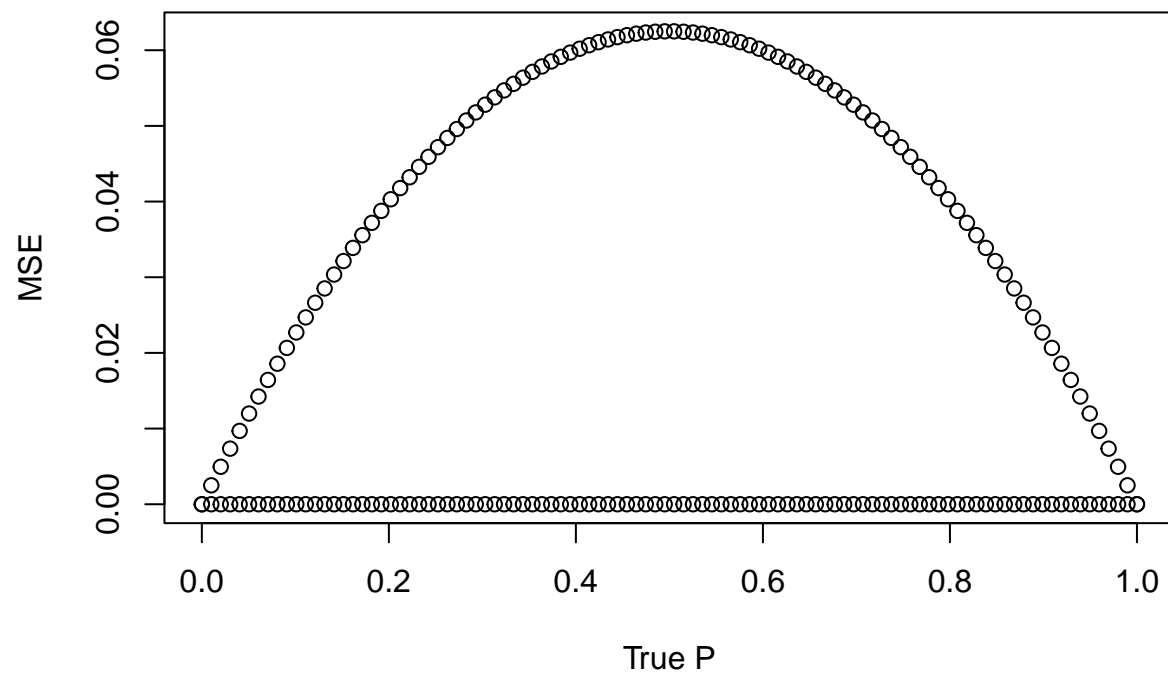
(b) $Var[\hat{p}_1] = \frac{p(1-p)}{n}$

$$Var[\hat{p}_2] = 0 \text{ this one has the lower variance}$$

(c) $MSE[\hat{p}_1] = 0^2 + \frac{p(1-p)}{n}$

$$MSE[\hat{p}_2] = 0^2 + 0$$

```
p=seq(from = 0,to = 1,length.out=100)
mse1=p*(1-p)/4
mse2=matrix(0,1,100)
plot(p,mse1,xlab="True P",ylab="MSE")
points(p,mse2)
```



Exercise 6.8

```
p=.43  
n=611  
error = sqrt(p*(1-p)/n)  
error
```

```
## [1] 0.02002862
```