

Regression Models: Assignment 2

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Installing libraries used

```
packages = c("dplyr", "MuMIn", "MASS", "leaps", "glmnet", "car")
for (package in packages) {
  install.packages(package)
}
```

Importing libraries

```
library(dplyr)
library(MuMIn)
library(MASS)
library(leaps)
library(glmnet)
library(car)
```

Exercise 1

1 - Model and parameter interpretation

Y = Binary variable representing whether the customer will buy a car or not *income* = annual family income

Therefore we model the response as:

$$Y = \beta_0 + \beta_1 X + \epsilon$$

And our values will be:

$$Y = -1.98079 + 0.04342X + \epsilon$$

The higher the family income, the higher the likeliness that a family will purchase a new car.

```
y = function(x) (-1.98079 + 0.04342 * x)
p = function(y) (exp(y)/(exp(y)+1))
```

2 - 95%-CI for the probability that a family with annual income of 60 thousand dollars will purchase anew car next year.

We calculate the asymptotic $(1 - \alpha)\%$ confidence interval:

$$\hat{\beta}_j \pm z_{\frac{\alpha}{2}} S.E.(\hat{\beta}_j)$$

With our values we get:

```
# CI calculation
l_bound <- 0.04342 - qnorm(0.975) * 0.02011
u_bound <- 0.04342 + qnorm(0.975) * 0.02011
```

$$0.004005124 \leq \hat{\beta}_j \leq 0.08283488$$

```
p(l_bound)
#> [1] 0.5010013
p(u_bound)
#> [1] 0.5206969
```

$$0.5010013 \leq p \leq 0.5206969$$

Therefore for 60 thousand dollar annual income households:

```
L <- -1.98079 + 0.004005124 * 60
U <- -1.98079 + 0.08283488 * 60
p(L)
#> [1] 0.1492517
p(U)
#> [1] 0.9520885
```

$$0.1492517 \leq p_{60k} \leq 0.9520885$$