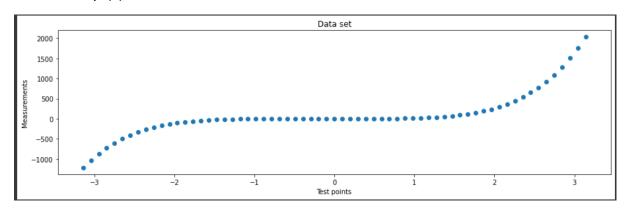
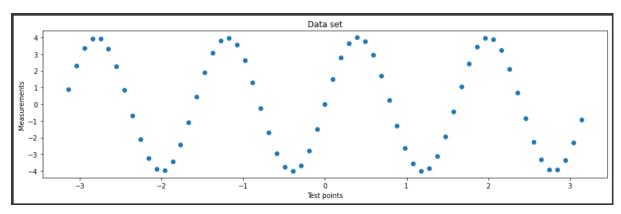
CE310 Assignment Part 2

Data set for $p_1(x)$



Data set for $p_2(x)$



Experiments

In this section Max Fitness and Min Size are my control variables.

Experiment 1

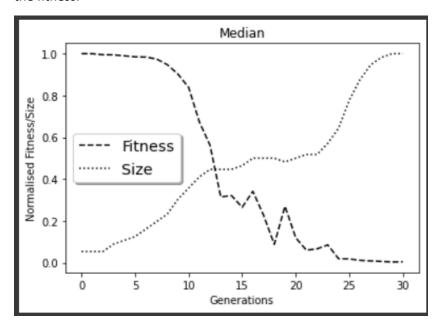
Problem = $p_1(x)$

Parameters

- Population = 500
- Tournaments = 5

Test Data:

| Tests | Min Fitness | Max Fitness | Min Size | Max Size | Evaluations |
|-------|-------------|-------------|----------|----------|-------------|
| 1 | 1894.552 | 307677.047 | 3.0 | 65.0 | 12349 |
| 2 | 3342.965 | 307580.481 | 3.0 | 67.0 | 12284 |
| 3 | 680.033 | 307677.047 | 3.0 | 74.0 | 12275 |
| 4 | 17874.904 | 307580.481 | 3.0 | 65.0 | 12304 |
| 5 | 4001.345 | 307677.047 | 3.0 | 83.0 | 12411 |
| 6 | 634.147 | 307677.047 | 3.0 | 51.0 | 12418 |
| 7 | 10133.197 | 307580.481 | 3.0 | 46.0 | 12362 |
| 8 | 154.565 | 307580.481 | 3.0 | 67.0 | 12422 |
| 9 | 453.671 | 307580.481 | 3.0 | 90.0 | 12322 |
| 10 | 10446.573 | 307585.098 | 3.0 | 48.0 | 12352 |



Experiment 2

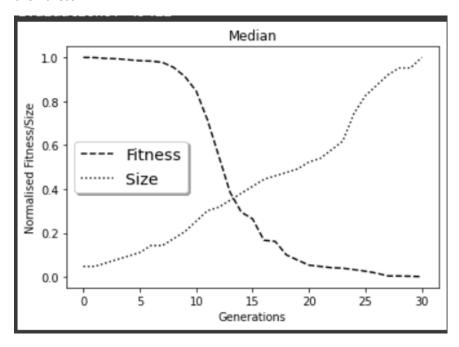
Problem = $p_1(x)$

Parameters

• Population = 2000

• Tournaments = 5

| Tests | Min Fitness | Max Fitness | Min Size | Max Size | Evaluations |
|-------|-------------|-------------|----------|----------|-------------|
| 1 | 428.376 | 307642.678 | 3.0 | 55.0 | 49498 |
| 2 | 216.009 | 307596.278 | 3.0 | 80.5 | 49399 |
| 3 | 2220.609 | 307615.570 | 3.0 | 58.0 | 49665 |
| 4 | 1168.258 | 307580.481 | 3.0 | 73.0 | 49664 |
| 5 | 2972.447 | 307580.481 | 3.0 | 54.0 | 49508 |
| 6 | 1324.364 | 307677.047 | 3.0 | 76.0 | 49503 |
| 7 | 863.569 | 307585.098 | 3.0 | 63.0 | 49469 |
| 8 | 1945.770 | 307645.281 | 3.0 | 44.0 | 49386 |
| 9 | 3477.223 | 307677.047 | 3.0 | 44.0 | 49404 |
| 10 | 1876.974 | 307580.481 | 3.0 | 48.0 | 49393 |



Experiment 3

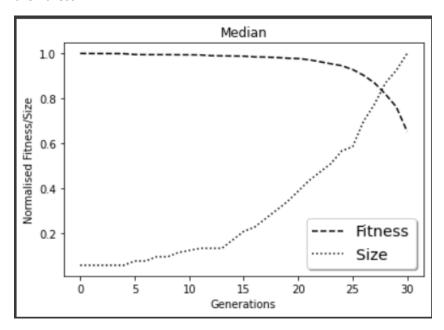
Problem = $p_1(x)$

Parameters

Population = 500

• Tournaments = 2

| Tests | Min Fitness | Max Fitness | Min Size | Max Size | Evaluations |
|-------|-------------|-------------|----------|----------|-------------|
| 1 | 145908.454 | 307580.481 | 3.0 | 53.0 | 12369 |
| 2 | 208489.836 | 307636.726 | 3.0 | 49.0 | 12283 |
| 3 | 171633.027 | 307580.481 | 3.0 | 60.0 | 12301 |
| 4 | 153582.920 | 307580.481 | 3.0 | 56.0 | 12329 |
| 5 | 178128.551 | 307677.047 | 3.0 | 71.0 | 12330 |
| 6 | 235666.839 | 307677.047 | 3.0 | 42.0 | 12422 |
| 7 | 276823.119 | 307580.481 | 3.0 | 40.0 | 12389 |
| 8 | 183133.754 | 307580.481 | 3.0 | 47.0 | 12247 |
| 9 | 228647.392 | 307677.047 | 3.0 | 57.0 | 12398 |
| 10 | 189693.967 | 307630.751 | 3.0 | 43.0 | 12295 |



Experiment 4

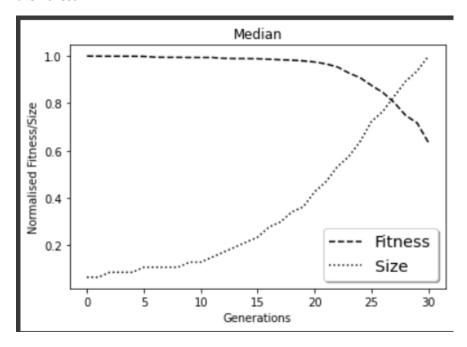
Problem = $p_1(x)$

Parameters

• Population = 2000

• Tournaments = 2

| Tests | Min Fitness | Max Fitness | Min Size | Max Size | Evaluations |
|-------|-------------|-------------|----------|----------|-------------|
| 1 | 200495.268 | 307580.481 | 3.0 | 46.0 | 49562 |
| 2 | 202074.816 | 307677.047 | 3.0 | 41.0 | 49331 |
| 3 | 214300.976 | 307587.669 | 3.0 | 46.0 | 49516 |
| 4 | 235792.731 | 307600.553 | 3.0 | 52.0 | 49387 |
| 5 | 164247.688 | 307580.481 | 3.0 | 52.0 | 49300 |
| 6 | 233530.930 | 307594.850 | 3.0 | 36.0 | 49569 |
| 7 | 208675.840 | 307677.047 | 3.0 | 44.0 | 49376 |
| 8 | 215007.990 | 307634.885 | 3.0 | 69.0 | 49522 |
| 9 | 210096.639 | 307585.098 | 3.0 | 57.0 | 49530 |
| 10 | 218506.648 | 307649.800 | 3.0 | 40.0 | 49299 |



Experiment 5

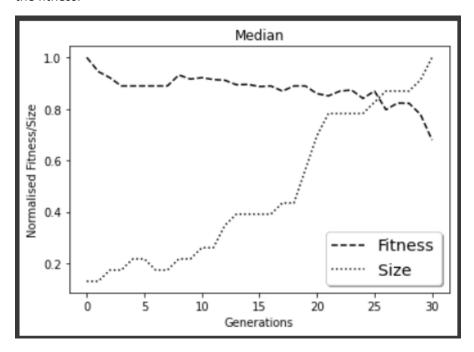
Problem = $p_2(x)$

Parameters

• Population = 500

• Tournaments = 5

| Tests | Min Fitness | Max Fitness | Min Size | Max Size | Evaluations |
|-------|-------------|-------------|----------|----------|-------------|
| 1 | 6.731 | 9.023 | 3.0 | 93.0 | 12373 |
| 2 | 6.424 | 9.023 | 3.0 | 22.0 | 12323 |
| 3 | 4.941 | 9.023 | 3.0 | 34.0 | 12356 |
| 4 | 7.292 | 9.023 | 3.0 | 18.0 | 12217 |
| 5 | 6.573 | 9.023 | 3.0 | 39.0 | 12425 |
| 6 | 5.876 | 9.023 | 3.0 | 34.0 | 12251 |
| 7 | 7.397 | 9.023 | 3.0 | 24.0 | 12376 |
| 8 | 4.490 | 9.023 | 3.0 | 87.0 | 12421 |
| 9 | 7.576 | 9.023 | 3.0 | 24.0 | 12276 |
| 10 | 7.610 | 9.023 | 3.0 | 18.0 | 12405 |



Experiment 6

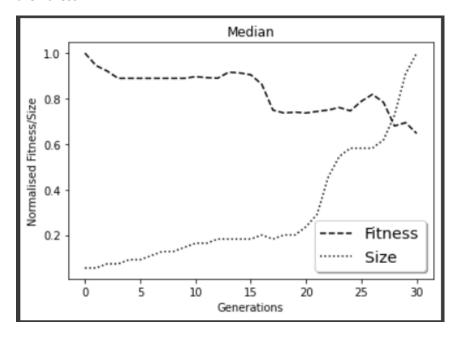
Problem = $p_2(x)$

Parameters

• Population = 2000

• Tournaments = 5

| Tests | Min Fitness | Max Fitness | Min Size | Max Size | Evaluations |
|-------|-------------|-------------|----------|----------|-------------|
| 1 | 4.356 | 9.023 | 3.0 | 29.0 | 49517 |
| 2 | 4.505 | 9.023 | 3.0 | 70.0 | 49290 |
| 3 | 4.169 | 9.023 | 3.0 | 47.0 | 49381 |
| 4 | 6.695 | 9.023 | 3.0 | 25.0 | 49307 |
| 5 | 4.464 | 9.023 | 3.0 | 24.0 | 49359 |
| 6 | 4.092 | 9.023 | 3.0 | 27.0 | 49457 |
| 7 | 6.465 | 9.023 | 3.0 | 28.0 | 49276 |
| 8 | 4.241 | 9.023 | 3.0 | 47.0 | 49538 |
| 9 | 2.807 | 9.023 | 3.0 | 47.0 | 49617 |
| 10 | 4.476 | 9.023 | 3.0 | 53.0 | 49283 |



Experiment 7

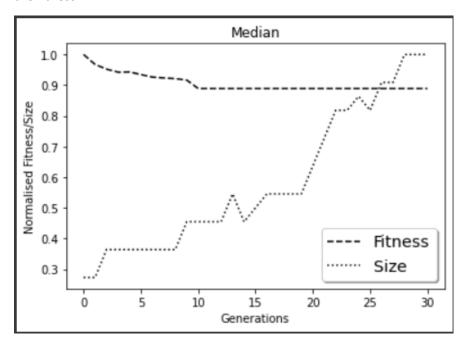
Problem = $p_2(x)$

Parameters

Population = 500

• Tournaments = 2

| Tests | Min Fitness | Max Fitness | Min Size | Max Size | Evaluations |
|-------|-------------|-------------|----------|----------|-------------|
| 1 | 8.023 | 9.023 | 3.0 | 21.0 | 12367 |
| 2 | 8.023 | 9.023 | 3.0 | 15.0 | 12269 |
| 3 | 8.023 | 9.023 | 3.0 | 9.0 | 12353 |
| 4 | 8.023 | 9.023 | 3.0 | 14.0 | 12306 |
| 5 | 8.004 | 9.023 | 3.0 | 20.0 | 12391 |
| 6 | 8.023 | 9.023 | 3.0 | 15.0 | 12405 |
| 7 | 8.023 | 9.023 | 3.0 | 15.0 | 12264 |
| 8 | 8.023 | 9.023 | 3.0 | 14.0 | 12330 |
| 9 | 8.023 | 9.023 | 3.0 | 12.0 | 12416 |
| 10 | 8.023 | 9.023 | 3.0 | 20.0 | 12271 |



Experiment 8

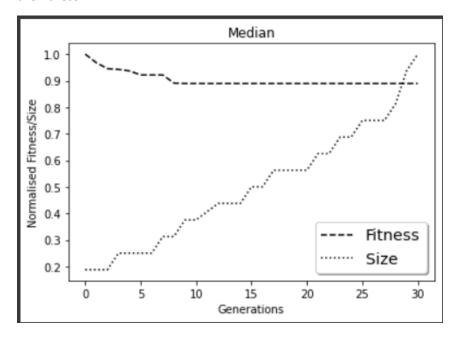
Problem = $p_2(x)$

Parameters

• Population = 2000

• Tournaments = 2

| Tests | Min Fitness | Max Fitness | Min Size | Max Size | Evaluations |
|-------|-------------|-------------|----------|----------|-------------|
| 1 | 8.023 | 9.023 | 3.0 | 15.0 | 49328 |
| 2 | 8.023 | 9.023 | 3.0 | 14.0 | 49664 |
| 3 | 8.023 | 9.023 | 3.0 | 11.0 | 49413 |
| 4 | 8.023 | 9.023 | 3.0 | 11.0 | 49330 |
| 5 | 8.023 | 9.023 | 3.0 | 22.0 | 49177 |
| 6 | 8.023 | 9.023 | 3.0 | 16.0 | 49461 |
| 7 | 7.783 | 9.023 | 3.0 | 24.0 | 49273 |
| 8 | 8.023 | 9.023 | 3.0 | 12.0 | 49561 |
| 9 | 8.023 | 9.023 | 3.0 | 18.0 | 49173 |
| 10 | 8.023 | 9.023 | 3.0 | 15.0 | 49492 |



Best Parameter Configuration

For both problems, the parameters below enabled the best outcomes.

- Population = 2000
- Tournaments = 5

So, these were the results after running another 10 tests for each problem:

Problem = p1(x)

| Tests | Min Fitness | Max Fitness | Min Size | Max Size | Evaluations |
|-------|-------------|-------------|----------|----------|-------------|
| 1 | 2220.609 | 307615.570 | 3.0 | 58.0 | 49665 |
| 2 | 216.009 | 307596.278 | 3.0 | 67.5 | 49399 |
| 3 | 1935.770 | 307645.281 | 3.0 | 45.0 | 49386 |
| 4 | 1158.258 | 307580.481 | 3.0 | 73.0 | 49664 |
| 5 | 2971.447 | 307580.481 | 3.0 | 54.0 | 49508 |
| 6 | 1223.364 | 307677.047 | 3.0 | 77.0 | 49503 |
| 7 | 428.376 | 307642.678 | 3.0 | 65.0 | 49498 |
| 8 | 1915.770 | 307645.281 | 3.0 | 42.0 | 49386 |
| 9 | 3474.223 | 307677.047 | 3.0 | 44.0 | 49404 |
| 10 | 1068.258 | 307580.481 | 3.0 | 72.0 | 49664 |

Problem = p2(x)

| Tests | Min Fitness | Max Fitness | Min Size | Max Size | Evaluations |
|-------|-------------|-------------|----------|----------|-------------|
| 1 | 4.229 | 9.023 | 3.0 | 35.0 | 49371 |
| 2 | 4.595 | 9.023 | 3.0 | 40.0 | 49160 |
| 3 | 4.508 | 9.023 | 3.0 | 33.0 | 49356 |
| 4 | 4.608 | 9.023 | 3.0 | 50.0 | 49208 |
| 5 | 4.499 | 9.023 | 3.0 | 31.0 | 49323 |
| 6 | 7.554 | 9.023 | 3.0 | 25.0 | 49298 |
| 7 | 3.865 | 9.023 | 3.0 | 103.0 | 49329 |
| 8 | 1.545 | 9.023 | 3.0 | 85.0 | 49440 |
| 9 | 4.207 | 9.023 | 3.0 | 45.0 | 49255 |
| 10 | 5.338 | 9.023 | 3.0 | 52.0 | 49441 |

Questions

GP Behaviour

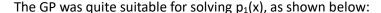
- When changing the problem, the results change completely as the have different data sets.
- When using a population size of 2000 (compared to 500), the program takes longer to complete the 30 generations but finds a better solution. This is because more evaluations have to be performed.
- When using a tournament size of 2 (compared to 5), the program finds a weaker solution. This is because tournaments are less likely to find good individuals to perform crossover and mutation on.

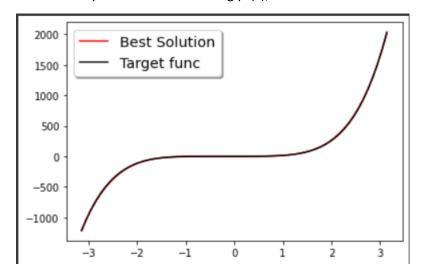
Variations

- o Through all experiments, the max size obtained seemed to variate often.
- However, for both problems, the average max fitness was the same.
- \circ Also, for $p_2(x)$ with a population of 2000 (experiments 7-8), the average min fitness was the same.

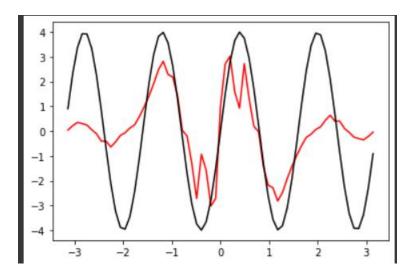
To choose the best parameter configuration, I looked at which configuration generated the lowest min fitness, which happened to be a population size of 2000 and a tournament size of 5 for both problems.

My results from the additional 10 runs seem to be consistent with the first 10 runs. However, two solutions were found with surprisingly low fitness values (see test 2 for $p_1(x)$ and test 8 for $p_2(x)$)





However, the GP was not very suitable for solving $p_2(x)$, as shown below:



The best solution line in red does seem to follow the sign curve to some extent but not nearly enough to say that the GP is suitable.

Conclusion

In this report, I have concluded that using a larger population size and a reasonable tournament size can lead to the best solutions to problems, having compiled a suitable amount of evidence to back up this claim. Also, I have discovered that this GP can be suitable for basic problems such as $p_1(x)$, but it may not be suitable for more complex problems such as $p_2(x)$.