Challenge: In our particular context, there is nothing mathematically distinguishing a point from a vector. To say that we should interpret an object as a Point in an Affine Space, we would say that the object is a member of the set of Points, and vice-versa with Vectors. Amongst Affine Spaces where the set of Points is the set of Vectors, there is no way to distinguish between the two. Further, there is no such concept that I am aware of as "casting" in mathematics. A natural way to express this, I think, is stating that there is a morphism between the sets and applying it, but, again, that is not applicable here since they are the same set.

Define H,S : Coordinate Frame on \mathbb{R}^1 Define W : Coordinate Frame on \mathbb{R}^3

Let π_i denote projection

Define hardware-clock-time : \mathbb{R}^1_H Define msg : $\mathbb{R}^1_H \times (\{x \in \mathbb{R}^{3 \times 3}_W | \forall ij, x_i \cdot x_j = 0, ||x_i|| = 1\} \times R^3_W)$ Set msg := (hardware-clock-time, $\pi_2(msg)$)

Define ros-time-base : \mathbb{R}^1_S Define ros-time-base-alias:?