

## Hierarchical Clustering

$P_1, P_2$  points

$d(P_1, P_2)$  = euclidean distance

$C_1, C_2$  clusters

$D(C_1, C_2)$  = single-link (min distance)

Distance Matrix

	A	B	C	D	min $d = d(A, B)$			
A	0	$\sqrt{2}$	3	2	* merge A & B → A & B	A & B	C	D
B	$\sqrt{2}$	0	$\sqrt{5}$	$\sqrt{10}$		0	$\sqrt{5}$	2
C	3	$\sqrt{5}$	0	$\sqrt{13}$		C	0	$\sqrt{13}$
D	2	$\sqrt{10}$	$\sqrt{13}$	0		D	2	$\sqrt{13}$

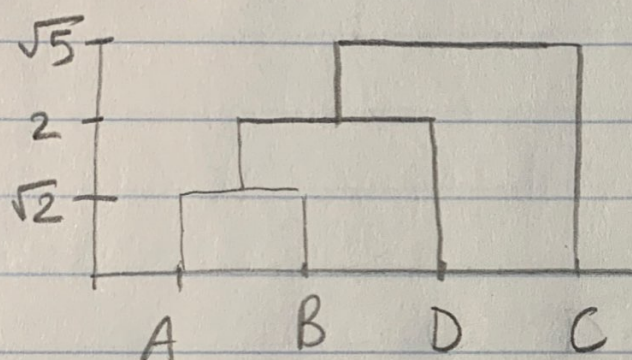


$$\min d = d(A \cup B, D)$$

\* merge A & B and D

	A & B & D	C
A & B & D	0	$\sqrt{5}$
C	$\sqrt{5}$	0

Dendrogram:



Density-Based Clustering:

- Density: if there are at least min-pts number of points in a ball of radius  $\epsilon^*$ , then this region is dense \*  $\epsilon$ -neighborhood
- Core point: if there are at least min-pts in its  $\epsilon$ -neighborhood
- Border point: is not a core point but is in the  $\epsilon$ -neighborhood of a core point
- Noise points: neither core nor border

DBSCAN Algorithm

- label all points as core, border, or noise
- eliminate noise points
- put an edge between all core points that are within  $\epsilon$ 's of each other