

Part 2

2.1 $F = \{U V \rightarrow W X Y Z, V W \rightarrow Z, Z \rightarrow V\}$

a. Candidate keys: U, Z

b.

1st normal form **satisfied** because the relation has keys.

2nd normal form **satisfied** because it has no partial dependencies.

3rd normal form **satisfied** because for each dependency the dependency is on a superkey or the dependent is prime.

Boyce-Codd normal form **not satisfied** because in the dependency ' $V W \rightarrow Z$ ' $V W$ is not a superkey, and for the dependency ' $Z \rightarrow V$ ' Z is not a superkey.

c. Where items on the left of the pipe are primary key attributes and items on the right are not.

$[U, V \mid W, X, Y]$

$[V, W \mid Z]$

$[U, Z \mid]$

2.2 $F = \{U V \rightarrow W X Y Z, X \rightarrow W, W \rightarrow Z\}$

a. Candidate keys: U, V

b.

1st normal form **satisfied** because the relation has keys.

2nd normal form **satisfied** because it has no partial dependencies.

3rd normal form **not satisfied** because in the dependencies ' $X \rightarrow W$ ' and ' $W \rightarrow Z$ ' the left hand side of the dependencies are not superkeys and the right hand sides are not prime attributes.

Boyce-Codd normal form **not satisfied** because 3rd normal form is not satisfied.

c. Where items on the left of the pipe are primary key attributes and items on the right are not.

$[U, V \mid X, Y]$

$[X \mid W]$

$[W \mid Z]$

2.3 F={U V → W X Y Z, V → W X, X → Z, V → U}

a. Candidate key: V

b.

1st normal form **satisfied** because the relation has keys.

2nd normal form **satisfied** because it has no partial dependencies.

3rd normal form **not satisfied** because in the dependency 'X → Z' X is not a superkey and Z is not a prime attribute.

Boyce-Codd normal form **not satisfied** because 3rd normal form is not satisfied.

c. Where items on the left of the pipe are primary key attributes and items on the right are not.

[V | W, X, U, Y]

[X | Z]

2.4

a.

A, B → G

A → C

B → D E F

∴ A, B → C D E F G

b.

A B → C, D, E, F, G

∴ A, B → G