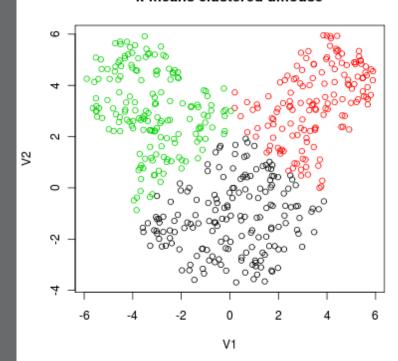
K-Means Clustering

Elliot Cohen Taryn Heilman Morning Lecture - Dec. 6, 2017



k-means clustered umouse



Learning Objectives



- Introduce unsupervised learning, compare to supervised
- Introduce clustering concept
- Enumerate clustering use-cases
- Define K-means algorithm:
 - How to code
 - Centroid initialization
 - Stopping Criteria
 - Evaluating the algorithm (metrics)
 - How to choose k

Review: Queue the Questionator



- What does supervised learning mean? Give an example
- Describe the difference between parametric and non-parametric learners, and give an example of each
- How do we measure the "success" of a supervised learning algorithm? Give examples for classification and regression
- Describe the euclidean distance metric. Name two additional distance metrics we have discussed and describe.
- What is the curse of dimensionality?

Supervised vs. Unsupervised Learning



Supervised

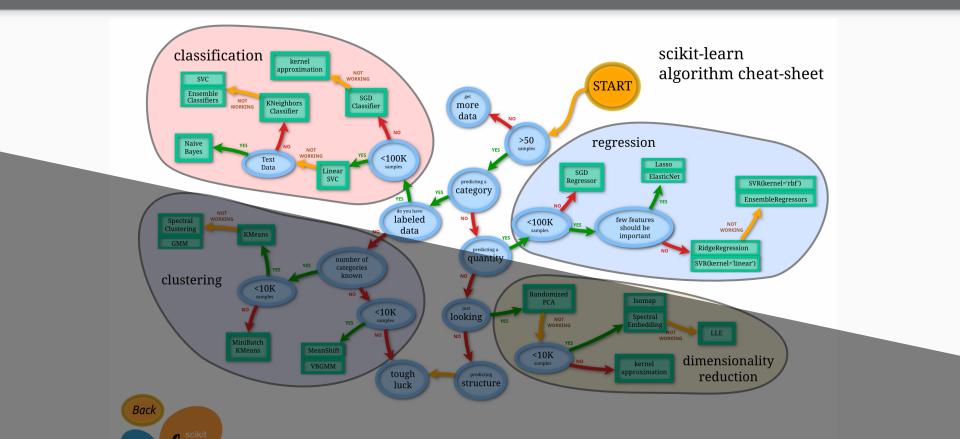
- Have a target/label that we model
- Models look like functions that take in features (X) and predict a label (y)
- Have an error metric that we can use to compare models
- Used to predict future unlabeled data

Unsupervised

- No target/label to predict
- Goal is to find underlying structure, patterns, or organization in data
- No stark error metric to compare models - determining if you have the optimal solution is very challenging. Cross validation often not applicable.

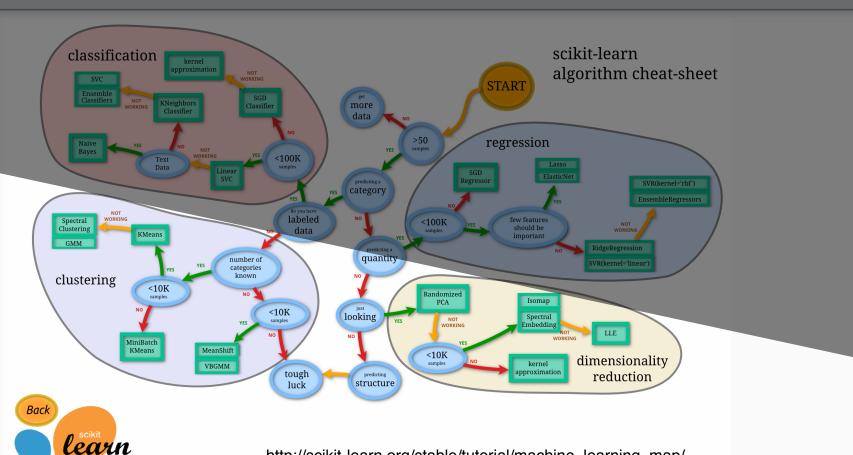
Where We've Been - Supervised Learning





Unsupervised Learning - Where We are Going!





Basic K-Means Algorithm



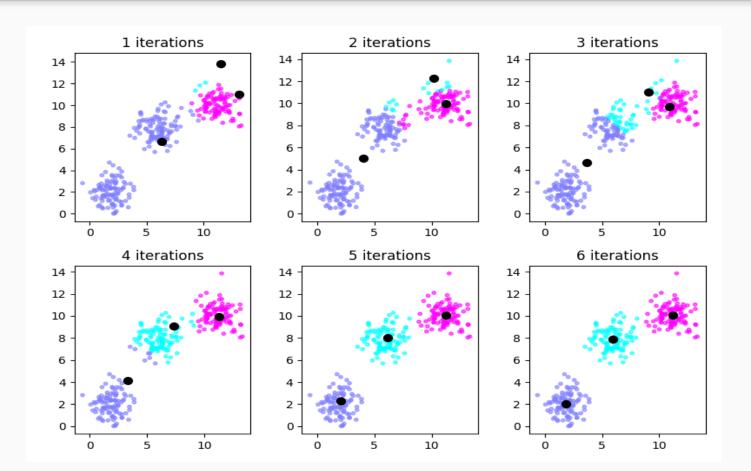
Initialize k centroids*

Until convergence**:

- assign each data point to the nearest centroid
- recompute the centroids as the mean of the data points

```
# psuedocode
initialize_centroids
while not converged:
   assign_data_to_centroids
   compute_new_centoid_means
```



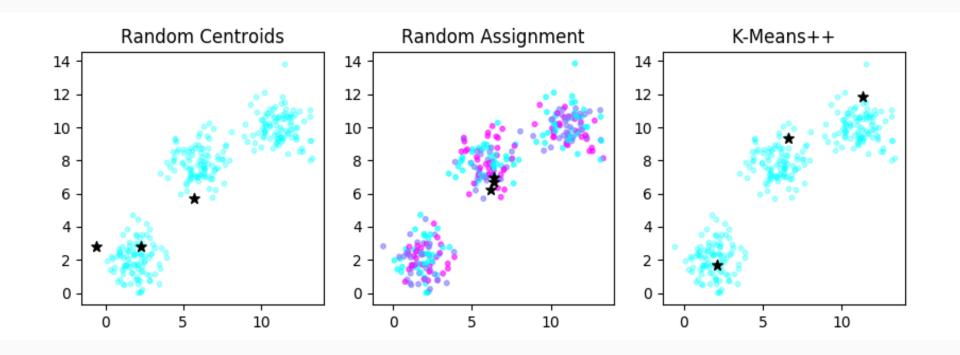


Centroid Initialization Methods



- 1) Randomly choose k points from your data and make those your initial centroids (simplest)
- 2) Randomly assign each data point to a number 1-k and initialize the kth centroid to the average of the points with the kth label (what happens as N becomes large?)
- 3) **k-means++** chooses well spread initial centroids. First centroid is chosen at random, with subsequent centroids chosen with probability proportional to the squared distance to the closest existing centroid. (default initialization in *sklearn*).





Stopping Criteria



We can update for:

- 1) A specified number of iterations (sklearn default : max_iter= 1000)
- 2) Until the centroids don't change at all
- 3) Until the centroids don't move by very much (*sklearn default : tol= .0001*)

Quick Review



Goal of unsupervised learning?

Describe the 2 steps in each k-means fitting iteration

Name 3 ways to choose centroids

Name 3 stopping criteria

Is K-Means deterministic?

Should we standardize features?

Breakout (numpy practice)

galvanize

Use these arrays:

- Use masking to grab the rows of features that correspond to the label of 1
- 2. Find the column-wise mean of that subset of features
- 3. Compute the euclidean distance from each data point in features to this mean. Try to do this in one line with broadcasting!

Breakout (numpy practice)



Use these arrays:

```
    subset = features[labels == 1]
    mean = subset.mean(axis = 0)
```

3 np.linalg.norm(features - mean, axis = 1)

Evaluating K-Means



How do we measure clustering performance / effectiveness?

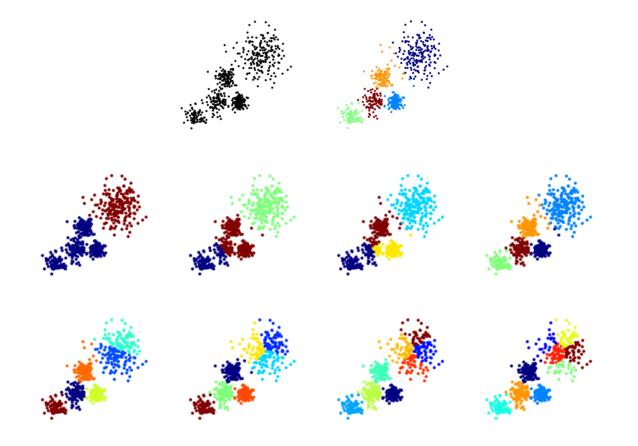
Quantify how similar items are within a cluster

Minimize Intra-Cluster Variance or Within Cluster Variance (WCV)

$$\min\left\{\sum_{k=1}^K WCV(C_k)\right\}$$

Where WCV for the kth cluster is the sum of all the pairwise Euclidean distances

$$WCV(C_k) = \frac{1}{|C_k|} \sum_{i,i' \in C_k} \sum_{j=1}^p (x_{ij} - x_{i'j})^2$$
Centroid of cluster C_k



Choosing k



Choosing k requires *a-priori* information:

- business logic (e.g. identify low, medium and high propensity customers)
- domain knowledge (e.g. there are k equilibrium states resultant from the phenomena)

Or a *heuristic*:

- Elbow plot
- Silhouette score
- GAP statistic and other methods that you don't need to know today

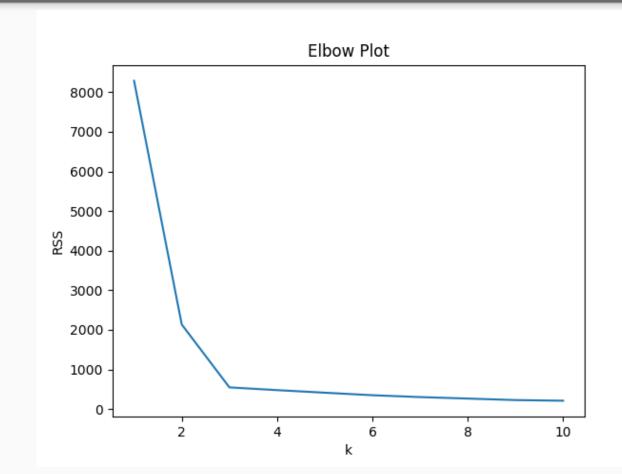
Elbow Plot



Elbow method - look for value of k that drastically reduces the residual sum of squares within the clusters

$$RSS = \sum_{k=1}^{K} \sum_{(i)=k} \left| \left| x_i - \overline{x}_k \right| \right|^2$$

Look for inflection point or value of k where improvement diminishes



Silhouette Score



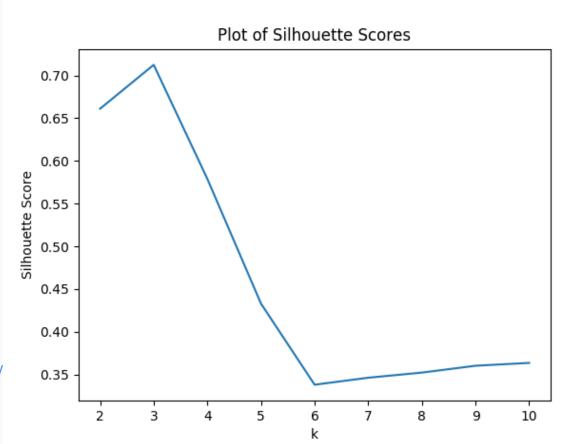
The Silhouette Coefficient is calculated using the mean intra-cluster distance (a) and the mean nearest-cluster distance (b) for each sample

$$(b - a) / max(a, b)$$

*only defined for 2 <= k < n

Values range from -1 to 1, with 1 being optimal and -1 being the worst

http://scikit-learn.org/stable/modules/generated/sklearn.metrics.silhouette_score.html#sklearn.metrics.silhouette_score

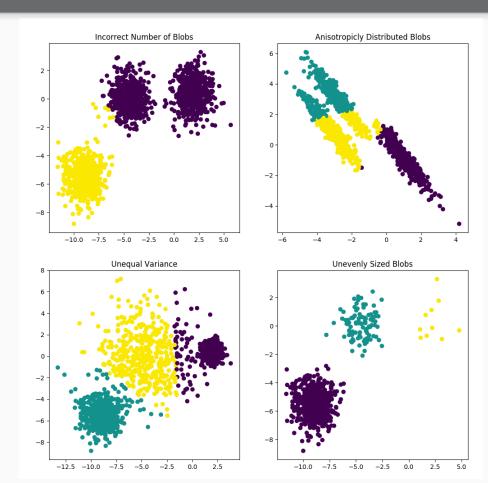


K-Means Assumptions

galvanıze

- Picked the "correct" k
- Clusters have equal variance
- Clusters are isotropic (variance spherical)
- Clusters do NOT have to contain the same number of observations

http://scikit-learn.org/stable/auto_examples/cluster/plot_kmeans_assumptions.html



Practical Considerations



- K-means is not deterministic -- falls into local minima. Remedy by reinitializing multiple times and take the version with the lowest withincluster variance (sklearn does multiple initializations by default)
- Susceptible to curse of dimensionality
- One hot encoded categorical can overwhelm look into k-modes (https://pypi.python.org/pypi/kmodes/)
- Try MiniBatchKMeans for large datasets (finds local minima, so be careful)

Real world use cases



- Customer segmentation
- Product segmentation
- Image segmentation
- Anomaly detection
- Social network analysis
- and many more...

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