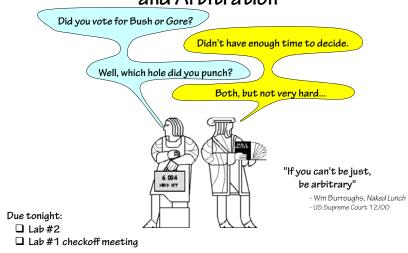
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6.004 Computation Structures Spring 2009

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Synchronization, Metastability and Arbitration



The Importance of being Discrete

We avoid possible errors by disciplines that avoid asking the tough questions - using a forbidden zone in both voltage and time dimensions:

Digital Values:

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Problem: Distinguishing voltages representing "1" from "O" Solution: Forbidden Zone: avoid using similar voltages for "1" and "O"



Digital Time:

Problem: "Which transition happened first?" questions Solution: Dynamic Discipline: avoid asking such questions in close races



LO7 - Synchronization 2

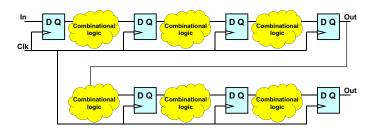
If we follow these simple rules...

2/26/09

modified 2/23/09 09:30

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Can we quarantee that our system will always work?



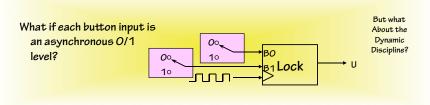
With careful design we can make sure that the dynamic discipline is obeyed everywhere*...

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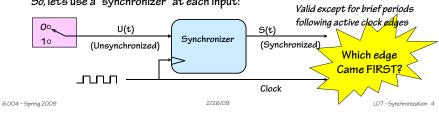
The world doesn't run on our clock!

2/26/09



To build a system with asynchronous inputs, we have to break the rules: we cannot guarantee that setup and hold time requirements are met at the inputs!

So, lets use a "synchronizer" at each input:

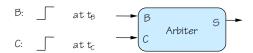


^{*} well, almost everywhere...

The Asynchronous Arbiter:

a classic problem

UNSOLVABLE



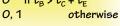
For NO finite value of t_E and t_D is this spec realizable. even with reliable components!

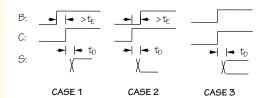
Arbiter specifications:

- · finite to (decision time)
- · finite t_F (allowable error)
- value of S at time t_c+t_p :

1 if
$$t_B < t_C - t_E$$

O if $t_B > t_C + t_E$



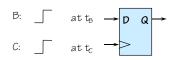


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Unsolvable?

that can't be true...

Lets just use a D Flip Flop:



We're lured by the digital abstraction into assuming that Q must be either 1 or O. But lets look at the input latch in the flip flop when B and C change at about the same time...

DECISION TIME is Tpp of flop.

ALLOWABLE ERROR is $max(t_{SETUP}, t_{HOLD})$

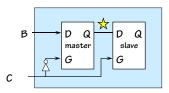
Our logic:

 T_{PD} after T_C , we'll have

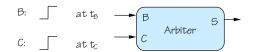
Q=O iff tB + tSETUP < tC

Q=1 iff $t_C + t_{HOLD} < t_B$

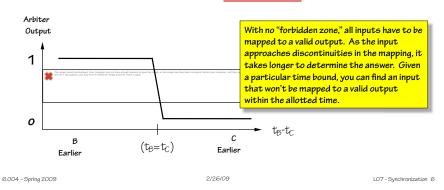
Q=0 or 1 otherwise.



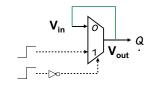
Violating the Forbidden Zone



Issue: Mapping the continuous variable $(t_B - t_C)$ onto the discrete variable S in bounded time.



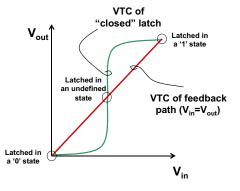
The Mysterious Metastable State



Recall that the latch output is the solution to two simultaneous constraints:

> 1. The VTC of path thru MUX; and

 $2. V_{in} = V_{out}$

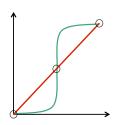


In addition to our expected stable solutions, we find an unstable equilibrium in the forbidden zone called the "Metastable State"

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Metastable State: Properties

- 1. It corresponds to an *invalid* logic level the switching threshold of the device.
- Its an unstable equilibrium; a small perturbation will cause it to accelerate toward a stable O or 1.
- 3. It will settle to a valid 0 or 1... eventually.
- 4. BUT depending on how close it is to the V_{in}=V_{out} "fixed point" of the device - it may take arbitrarily long to settle out.
- 5. EVERY bistable system exhibits at least one metastable state!



EVERY bistable system? Yep, every last one.

Coin flin??

Could land on edge.

Horse race??

Photo finish.

Presidential Election??

(Where's this twit been hiding???)

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Observed Behavior: typical metastable symptoms

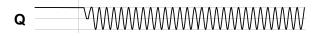
Following a clock edge on an asynchronous input:

D CLK

We may see exponentially-distributed metastable intervals:



Or periods of high-frequency oscillation (if the feedback path is long):





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Mechanical Metastability

2/26/09



Metastable State



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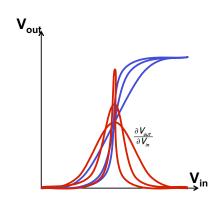
If we launch a ball up a hill we expect one of 3 possible outcomes:

- a) Goes over
- b) Rolls back
- c) Stalls at the apex

That last outcome is not stable.

- a qust of wind
- Brownian motion
- it doesn't take much

How do balls relate to digital logic?



Our hill is analogous to the derivative of the VTC (Voltage Transfer Curve)... at the metastable point, the derivative (slope) is ZERO.

Notice that the higher the gain thru the transition region, the steeper the peak of the hill... making it harder to get into a metastable state...

We can decrease the probability of getting into the metastable state, but – assuming continuous models of physics – we can't eliminate the slope=O point!

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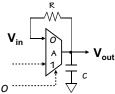
The Metastable State:

Why is it an inevitable risk of synchronization?

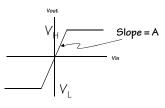
- Our active devices always have a fixed-point voltage, V_M , such that $V_{IN}=V_M$ implies $V_{OUT}=V_M$
- Violation of dynamic discipline puts our feedback loop at some voltage $\rm V_{\rm O}$ near $\rm V_{\rm M}$
- The rate at which V progresses toward a stable "O" or "1" value is proportional to $(V V_M)$
- The time to settle to a stable value depends on $(V_O V_M)$; its theoretically infinite for $V_O = V_M$
- Since there's no lower bound on $(V_O V_M)$, there's no upper bound on the settling time.
- · Noise, uncertainty complicate analysis (but don't help).

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Sketch of analysis... II.



We can model our combinational cycle as an amplifier with gain A and saturation at V_H, V_I



- For V_{out} near V_M, V_{out}(t) is an exponential whose time constant reflects RC/A:
- 3. Given interval T, we can compute a minimum value of $\varepsilon = |V_O V_M|$ that will quarantee validity after T:
- 4. Probability of metastability after T is computed by probability of a V_O yielding ϵ (T) ...

 $V_{out}(t) - V_M \cong \varepsilon e^{t(A-1)/RC}$

$$\varepsilon$$
 (T) \simeq (V_H - V_M) $e^{-T/\tau}$

$$P_{M}(T) \cong P[|V_{O}-V_{M}| < \varepsilon (T)]$$

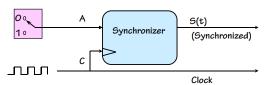
$$\cong K e^{-T/\tau}$$

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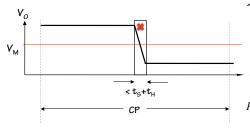
Sketch of analysis... I.

Assume asynchronous O->1 at T_A , clock period CP:

Whats the FF output voltage, V_O , immediately after T_A ?



Potential trouble comes when V_0 is near the metastable point, V_M ...



1. Whats the probability that the voltage, V_O , immediately after TA is within ϵ of V_M ?

 $P[|V_0 - V_M| \le \varepsilon] \le \frac{(ts + t_H)}{CP} * \frac{2\varepsilon}{(V_H - V_L)}$

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Failure Probabilities vs Delay

Making conservative assumptions about the distribution of $\rm V_{\rm O}$ and system time constants, and assuming a 100 MHz clock frequency, we get results like the following:

	Average time	
Delay	P(Metastable)	between failures
31 ns	3x10 ⁻¹⁶	1 year
33.2 ns	3x10 ⁻¹⁷	10 years
1 <i>00</i> ns	10 ⁻⁴⁵	10 ³⁰ years!

[For comparision:

Age of oldest hominid fossil: $5x10^6$ years Age of earth: $5x10^9$ years]

Lesson: Allowing a bit of settling time is an easy way to avoid metastable states in practice!

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The Metastable State:

a brief history

Antiquity: Early recognition Buriden's Ass, and other fables...

Denial: Early 70s Widespread disbelief. Early analyses

documenting inevitability of problem rejected by skeptical journal editors.

Folk Cures: 70s-80s

Popular pastime: Concoct a "Cure" for

the problem of "synchronization failure". Commercial synchronizer products.

Reconciliation: 80s-90s

Acceptance of the reality:

synchronization takes time. Interesting

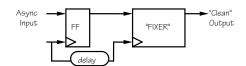
special case solutions.

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Folk Cures

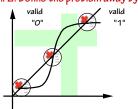
the "perpetual motion machine" of digital logic

Bad Idea # 1: Detect metastable state & Fix



Bug: detecting metastability is itself subject to metastable states, i.e., the "fixer" will fail to resolve the problem in bounded time.

Bad Idea #2: Define the problem away by making metastable point a valid output



Bug: the memory element will flip some valid "O" inputs to "1" after a while.

Many other bad ideas – involving noise injection, strange analog circuitry, ... have been proposed.

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Ancient Metastability

Metastability is the occurrence of a persistent invalid output... an unstable equilibria.

The idea of Metastability is not new:

The Paradox of Buridan's Ass

Buridan, Jean (1300-58), French Scholastic philosopher, who held a theory of determinism, contending that the will must choose the greater good. Born in Bethune, he was educated at the University of Paris, where he studied with the English Scholastic philosopher William of Ockham (whom you might recall from his razor business). After his studies were completed, he was appointed professor of philosophy, and later rector, at the same university. Buridan is traditionally, but probably incorrectly, associated with a philosophical dilemma of moral choice called "Buridan's ass."

In the problem an ass starves to death between two alluring bundles of hay because it does not have the will to decide which one to eat.

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There's no easy solution

... so, embrace the confusion.

"Metastable States":

- Inescapable consequence of bistable systems
- Eventually a metastable state will resolve itself to valid binary level.
- However, the recovery time is UNBOUNDED ... but influenced by parameters (gain, noise, etc)
- Probability of a metastable state falls off EXPONENTIALLY with time -- modest delay after state change can make it very unlikely.

Our STRATEGY; since we can't eliminate metastability, we will do the best we can to keep it from contaminating our designs

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Modern Reconciliation:

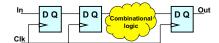
delay buys reliability

Synchronizers, extra flip flops between the asynchronous input and your logic, are the best insurance against metastable states.

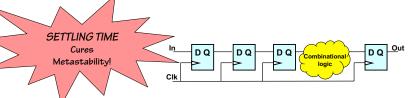
The higher the clock rate, the more synchronizers should be considered.

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A metastable state here will probably resolve itself to a valid level before it gets into my circuit.



And one here will almost certainly get resolved.



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Some things we CAN build

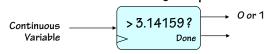
1. Unbounded-time Asynchronous Arbiter:



S valid when Done=1; unbounded time.

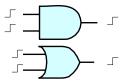
S=0 iff B edge first, 1 iff C edge first, 1 or 0 if nearly coincident

2. Unbounded-time Analog Comparator:



After arbitrary interval, decides whether input at time of last active clock edge was above/below threshold.

3. Bounded-time combinational logic:

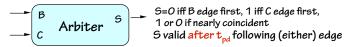


Produce an output transition within a fixed propagation delay of first (or second) transition on the input.

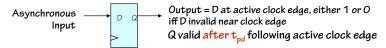
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Things we CAN'T build

1. Bounded-time Asynchronous Arbiter:



2. Bounded-time Synchronizer:

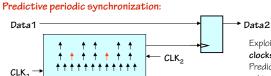


3. Bounded-time Analog Comparator:



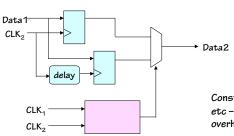
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Interesting Special Case Hacks



Exploits fact that, given 2 periodic clocks, "close calls" are predictable. Predicts, and solves in advance, arbitration problems (thus eliminating cost of delay)

Mesochronous communication:

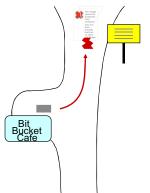


For systems with unsynchronized clocks of same nominal frequency. Data goes to two flops clocked a half period apart; one output is bound to be "clean". An observer circuit monitors the slowly-varying phase relationship between the clocks, and selects the clean output via a lenient MUX.

Constraints on clock timing – periodicity, etc – can often be used to "hide" time overhead associated with synchronization.

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Every-day Metastability - I



Ben Bitdiddle tries the famous "6.004 defense":

Ben leaves the Bit Bucket Café and approaches fork in the road. He hits the barrier in the middle of the fork, later explaining "I can't be expected to decide which fork to take in bounded time!".

Is the accident Ben's fault?

"Yes; he should have stopped until his decision was made."

Judge R. B. Trator, MIT '86

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Summary

The most difficult decisions are those that matter the least.

As a system designer...

Avoid the problem altogether, where possible

- Use single clock, obey dynamic discipline
- Avoid state. Combinational logic has no metastable states!

Delay after sampling asynchronous inputs: a fundamental cost of synchronization

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Every-day Metastability - II

GIVEN:

- · Normal traffic light:
- · GREEN, YELLOW, RED sequence
- · 55 MPH Speed Limit
- · Sufficiently long YELLOW, GREEN periods
- Analog POSITION input
- · digital RED, YELLOW, GREEN inputs
- digital GO output

Can one reliably obey....



Image by MIT OpenCourseWare

- · LAW #1: DON'T CROSS LINE while light is RED.
 - GO = GREEN
- · LAW #2: DON'T BE IN INTERSECTION while light is RED.

PLAUSIBLE STRATEGIES:

- A. Move at 55. At calculated distance D from light, sample color (using an unbounded-time synchronizer). GO ONLY WHEN stable GREEN.
- B. Stop 1 foot before intersection. On positive GREEN transition, gun it.

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