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///////// Computational ///////// Final //
d ///////// Physics ///////// Project //
// Richford //////////
                           Physics
                          Fall 2017
// 20171031 ///////////
// Language: Python (or C++ ?)
   Project: Distribution Unfolding
       Due: End of Fall 2017 semester
Overview: An althorithm to determine the relative contrib-
            utions of two unknown distributions that make
            up a combination distribution, using random
            distributions and checking their contributions
            to the combination distribution iteratively, until two distributions are settled upon.
   Details: We're looking for the relative yield (that is, the number of electrons created from decays) of
            two mesons, D, which has charm quarks, and B,
           which has bottom quarks. The fractions of each of these yields compared with the total yield
            indicates the number of charm and bottom quarks
            actually created during a heavy-ion collision.
            Since these two distributions are not known, we
            have to unfold (or un-convolve) their contrib-
            utions from the total yield distribution (after
            subtracting known contributions from mesons and
            hadrons composed of lighter quarks. Finally, the
            best way to approach these two mesons is from
the distributions for the distance of closest
            approach that the projected trajectories of the
            decay electrons make with the primary collision
            point, since the D-meson is far longer lived
            than the B-meson. The algorithm randomly creates
            D.C.A. distributions for the D- and B-mesons,
            checks if they fit into the combined D.C.A.
           distribution, and then calculates the fractional //
yield when good-fitting candidates are reached. //
// Figure:
  Daughter
                                   Path of decay electron,
   Hadron
                                    bent by magnetic field, //
                                    from 2ndary vertex
  Secondary Vertex
                                   Secondary Vertex (decay
                                   of charmed or bottom
                                    meson)
                                   Traced-back (projected) //
                                   path of decay electron
Solid line (|): path of
meson generated from
                  Ι
                  М
                         D
                                    primary vertex
                  S
                         C
                                   Dotted line (:):
                  0
                         Α
                                   distance of closest ap-
                  N
                                   proach from the decay-
                                    electron's traced-back
                                   path to the primary vtx
                                   Primary vertex (col-
                                    lision of two nucleons)
             Primary Vertex
```

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//
             1. Setup
//
                1.1 Dimensionality
                                                                11
                1.2 Input/Output directories
//
                1.3 Files for later use
                    1.3.1 Probability matrices
//
//
                     1.3.2 Error matrices/error-bar limits
//
                     1.3.3 Combination distribution's matrix
             2. Preliminary Work
                2.1 Exclude certain DCA bins
                2.2 Simulation for initial values, normal-
                ization, comparison with final result
2.3 Initialization for Markov chains
                                                                //
//
                                                                //
                2.4 Prior probability vector
                2.5 Modifications to individual DCA matrices
             3. Markov-Chain Monte-Carlo Sampler (emcee)
                3.1 Regularization, paramter limits, starting
                    points for random walk
                3.2 Perform a random walk, allow the matrices to evolve from the starting point
//
               (3.2+1/2 Animation ?)
//
                                                                //
//
                3.3 Get posterior probability percentiles
                3.4 Compare posterior probabilty percentiles
                    with covariance matrix
             4. Check Results
                4.1 Re-fold to check
                                                                //
                4.2 Calculate covariance from combined and
                     constituent distributions
                                                                //
//
                4.3 Get fractional contribution yield from
                     the two constituent distributions
                4.4 Calculate likelihood for the two com-
                     ponants
                    4.4.1 Likelihood of getting the expected
fractional contribution (Poisson?)
                                                                //
                     4.4.2 Likelihood from the unfolded
//
                                                                //
                           results (Monte Carlo sampling)
//
                                                                //
//
                 4.5 Plot and save results to output files
                                                                //
//
// Other Thoughts:
                                                                77
                                                                //
//
//
             1. I'm having trouble understanding the co-
                variance thing — there might be a slower, more computationally—intensive way to go
                Requires ROOT module for python — which I am having trouble installing (it should
//
                                                                //
                work with Python 3.6, but I keep getting missing-module error when I say "import
//
                                                                //
//
                                                                //
             3. Might be best to first determine the frac-
                tional yield of one particle (the B-meson) rather than two (both the B- and D-mesons)
//
                                                                //
                                                                //
//
                                                                //
```