



Machine Learning

ITAM



Outline

- Unsupervised learning
- Clustering: Grouping and data segmentation
- Similarity measures
 - Transformation of ordinal, nominal and categorical variables
- Techniques
 - Partition methods
 - EM: k-medias
 - Density methods
 - Hierarchical methods



Objective

- Group data into categories or clusters such that instances that are more closely related belong to the same group
- Sometimes we also want a hierarchy that orders data according to their relatedness
 - E.g. A taxonomy



Unsupervised learning

- Clustering algorithms are unsupervised learning algorithms
 - There are no labeled examples from which the model is created
- Uses:
 - When labeling is expensive
 - When label change with time
 - When we want to find unsuspected relationships in the data that might be useful for classification
 - When we want to better understand the data
 -



Hierarchical Methods



Clustering Algorithms

Hierarchical

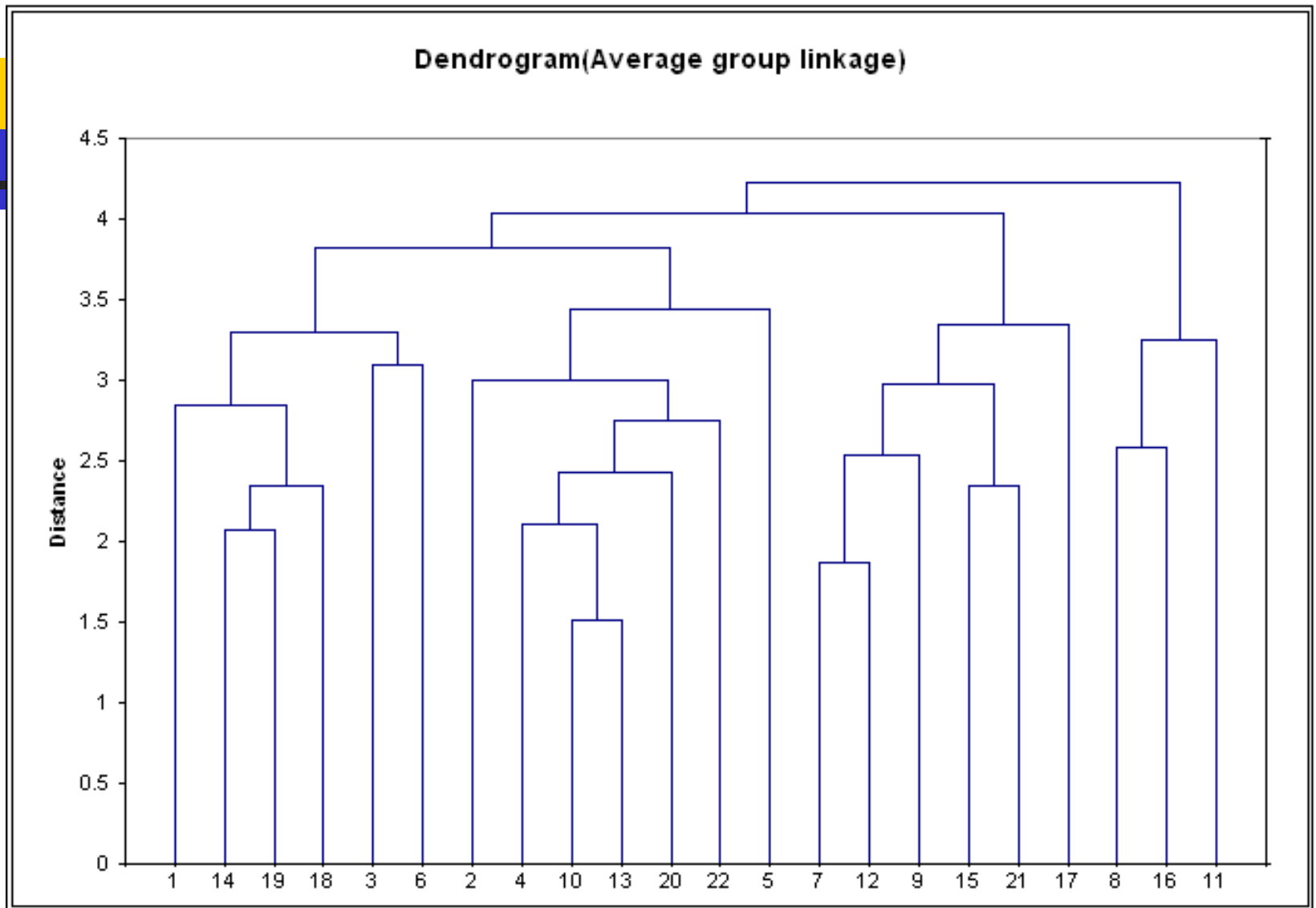
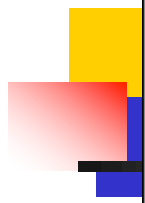
- These algorithms create a hierarchy in which each level forms groups out of groups of a lower level
 - In the lowest level is the ungrouped data i.e., each data item belongs to its own group (every group is of size 1)
 - The highest level contains one group with all the data
- The resulting structure is a tree with the root being the group with all the data and the leaves the individual data items. Inner nodes have different aggregations



Clustering Algorithms

Hierarchical

- The tree is drawn such that the height of each node is proportional to the dissimilarity between the subgroups that it aggregates
- The resulting figure is known as a dendrogram and provides a descriptive image of the data



For example 1=Seattle 14=San Francisco, 19=LA, 18= Phoenix



Clustering Algorithms

Hierarchical

- In contrast to k-means, the number clusters is not an intrinsic part of the algorithm
- It is the analyst's job to determine the level in the hierarchy that best represents the data's grouping
- Note:
 - These algorithms always find a hierarchy regardless of whether the data can truly be grouped
 - Different algorithms find different hierarchies
- Group formation is based on some similarity measure between groups

Dendrogram

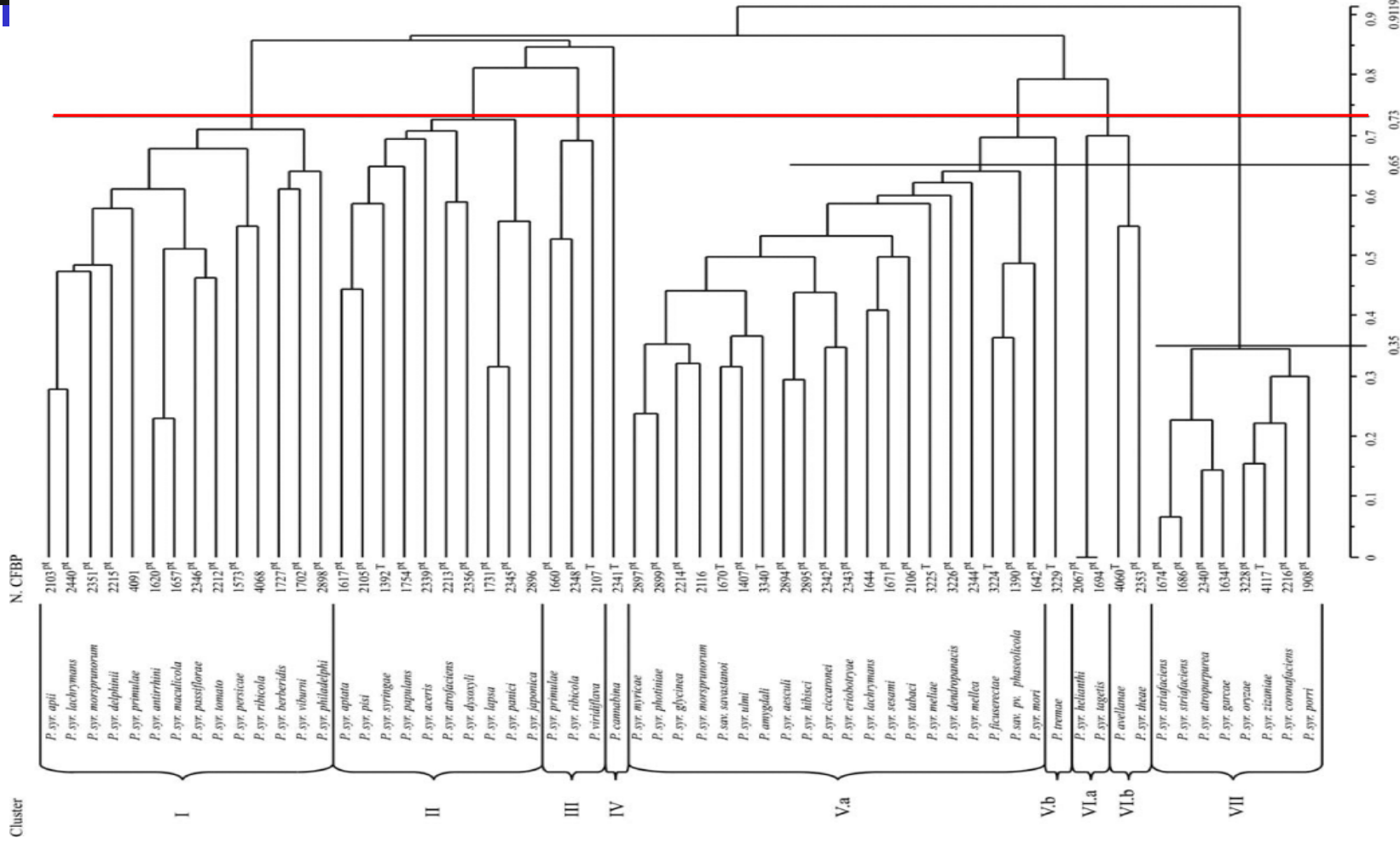


Figure 3 - Dendrogram obtained by comparison of BOX-PCR fingerprinting patterns from 61 bacterial type strains belonging to *Pseudomonas syringae* - *Pseudomonas viridiflava* large group (UPCMA analysis, Jaccard coefficient). Isolates obtained from the "Collection Française des Bactéries Phytopathogènes" (CFBP, Angers, France). [†]: species type strain, ^{ps}: pathotype strain.



Clustering Algorithms

Hierarchical

- There are two strategies to create these structures
 - Aggregation
 - Start at the lowest level (individual instances) and recursively form larger and larger groups, until you have only one
 - Disgregation
 - Start with the group with all the data and recursively divide it until there is only one item per group



Clustering Algorithms

Hierarchical

- Aggregation algorithms
 - Merge the two most similar groups
 - Repeat until there is only one
- We need a way to compute the similarity between groups



Clustering Algorithms

Hierarchical

- Single Linkage

- The distance between group A and B is the minimum distance between their individual items
- Example (using squared Euclidean distance for the distance between items):
 - $A=\{<1,2>, <3,2>\}$, $B=\{<5,6>, <5,7>, <6,6>\}$
 - $d(<1,2>, <5,6>)=32$, $d(<1,2>, <5,7>)=41$,
 $d(<1,2>, <6,6>)=41$
 - $d(<3,2>, <5,6>)=20$, $d(<3,2>, <5,7>)=29$,
 $d(<3,2>, <6,6>)=25$
 - The distance between A and B is 20



Clustering Algorithms

Hierarchical

- Complete Linkage
 - The distance or similarity between two groups is the distance between its most dissimilar items
 - From the above example
 - The distance between A and B is 41
- Group average
 - The distance between to groups is the average distance between every pair of items

$$\frac{1}{N_k N_L} \sum_{i \in C_k} \sum_{j \in C_L} d(\mathbf{x}_i, \mathbf{x}_j)$$



Clustering Algorithms

Notes

- Single Linkage
 - Compact groups due to chaining
 - Produces groups with large diameter
 - The diameter is the maximum distance between any pair of items
- Complete Linkage
 - The opposite from above. Groups with small diameter
 - It is more likely that noisy data cause inadequate groupings
- Group average
 - Its a good compromise from the above two



Algorithm

1. Start with each data item in its own group
2. Find the similarity between every pair of groups
3. Merge the two most similar groups
4. Repeat from 2 until there is only one group



Clustering algorithms

- Disgregation Algorithms
 1. Start with the group of all elements
 2. Take one of the groups with more than one element and partition into two or more groups
 3. Repeat from 2 until every element is in its own group
- The group partition must seek that elements within a group are more similar than elements in different groups
- Ideas?



Clustering algorithms

- Class exercise



Density methods



Clustering algorithms

Density (DBSCAN)

- Generate groups with a certain density
- It takes two parameters: Epsilon y Min
 - The distance between a data point and its closest neighbor in the same group is at most epsilon
 - Each group has at least Min elements

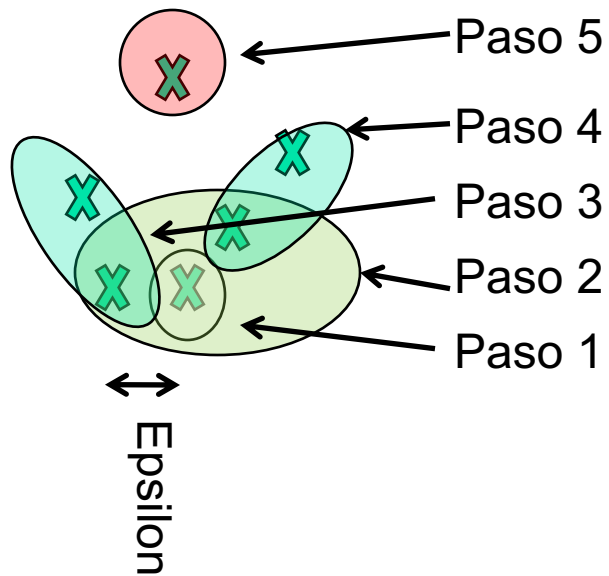


Clustering algorithms

DBSCAN

- $D \leftarrow$ All the datas, $i=0$
- While ($D \neq \{\}$)
 - Extract any p from D ($D \leftarrow D - \{p\}$)
 - $V \leftarrow \{p\}$, $C_i \leftarrow \{\}$
 - While($V \neq \{\}$)
 - Extract any d from V ($V \leftarrow V - \{d\}$)
 - $O \leftarrow$ All of the data points from D at a distance Epsilon or less to d
 - If $|O|+1 < \text{Min}$
 - if $C_i = \{\}$, d is classified as noise
 - Else
 - $V \leftarrow V \cup O$, $D \leftarrow D - V$
 - Insert V and d in C_i : $C_i \leftarrow C_i \cup V \cup \{d\}$
 - If ($C_i \neq \{\}$)
 - $i \leftarrow i+1$

DBSCAN





Clustering algorithms

Example DBSCAN

- Epsilon= 1
- Min =2

Datos
23
8
12
13
4
22
14
3



Algoritmos de Agrupamiento

Ejercicio DBSCAN

- Del que hicieron para jerárquico ahora háganlo con DBSCAN usando
 - Probar con distintas Epsilons comenzando con 0.2 (el valor de Epsilon dependerá de la medida de distancia que utilicen) Min=2



Clustering algorithms

Density

- No need to specify the number of groups
- Finds noisy data
- Groups have arbitrary shapes
- But defining epsilon is an art. Epsilon is defined once per run so it can't find groups with different densities
 - Possible solution?